

	$S_1$	$S_2$
$S_1$	0.8	0.2
$S_2$	0.3	0.7

	A	C	G	T
$S_1$	0.3	0.2	0.3	0.2
$S_2$	0.1	0.4	0.1	0.4

V-Matrix

	C	G	T	C	A
$S_1$	0.1	0.024	0.00384	0.000614	0.000147
$S_2$	0.2	0.014	0.00392	0.001098	0.00077

$$\begin{aligned}
 V_1(S_1) &= P(S_1 | *) \cdot P(C | S_1) \\
 &= 0.5 \cdot 0.2 = 0.1
 \end{aligned}$$

$$\begin{aligned}
 V_1(S_2) &= P(S_2 | *) \cdot P(C | S_2) \\
 &= 0.5 \cdot 0.4 = 0.2
 \end{aligned}$$

$$V_2(S_1) = \max \begin{cases} V_1(S_1) \cdot P(S_1 | S_1) \cdot P(G | S_1) = 0.024 \\ V_1(S_2) \cdot P(S_1 | S_2) \cdot P(G | S_1) = 0.018 \end{cases}$$

$$V_2(S_2) = \max \begin{cases} V_1(S_1) \cdot P(S_2 | S_1) \cdot P(G | S_2) = 0.002 \\ V_1(S_2) \cdot P(S_2 | S_2) \cdot P(G | S_2) = 0.014 \end{cases}$$

$$V_3(S_1) = \max \begin{cases} V_2(S_1) \cdot P(S_1|S_1) \cdot P(T|S_1) = 0.00384 \\ V_2(S_2) \cdot P(S_1|S_2) \cdot P(T|S_1) = 0.00084 \end{cases}$$

$$V_3(S_2) = \max \begin{cases} V_2(S_1) \cdot P(S_2|S_1) \cdot P(T|S_2) = 0.00192 \\ V_2(S_2) \cdot P(S_2|S_2) \cdot P(T|S_2) = 0.00392 \end{cases}$$

$$V_4(S_1) = \max \begin{cases} V_3(S_1) \cdot P(C|S_1) = 0.000614 \\ V_3(S_2) \cdot P(C|S_2) = 0.000235 \end{cases}$$

$$V_4(S_2) = \max \begin{cases} V_3(S_1) \cdot P(C|S_1) = 0.000307 \\ V_3(S_2) \cdot P(C|S_2) = 0.001098 \end{cases}$$

$$V_5(S_1) = \max \begin{cases} V_4(S_1) \cdot P(A|S_1) = 0.000147 \\ V_4(S_2) \cdot P(A|S_1) = 0.000099 \end{cases}$$

$$V_5(S_2) = \max \begin{cases} V_4(S_1) \cdot P(A|S_2) = 0.000012 \\ V_4(S_2) \cdot P(A|S_2) = 0.000077 \end{cases}$$

Based on the V matrix above,

$s_1$	*	$s_1$	$s_1$	$s_1$	$s_1$
$s_2$	*	$s_2$	$s_2$	$s_2$	$s_2$

The backtracking will be

$*$ ,  $s_1$ ,  $s_1$ ,  $s_1$ ,  $s_1$ ,  $s_1$

#### Question 2.2

Number of Files: Positive: 594  
Negative: 578

Total vocabulary: 15357

F1-score: 0.9948311785447164

The first step of this homework is to use spaCy to extract words from files. The code for this step can be found in `extractFile.py`. The stopwords, punctuations are removed during this process. Then using the `sentiment_reader.py` to generate train and test dataset from the result of previous step. Then using `multinomial_naive_bayes.py` to make prediction. The runtime for file extraction is 68s and the runtime for multinomial naive bayes is 0.21s.