TH o nepoznatoj aritmetickoj sredini osnovnog skupa:

$$H_0: ...\bar{x} = \bar{x}_0$$

$$H_1: ...\bar{x} \neq \bar{x}_0$$

Interval prihvacanja Ho:

$$\bar{x}_0 \pm z \cdot Se(\bar{x})$$

$$t^* = z^* = \frac{\hat{x} - \hat{x}_0}{Se(\bar{x})}$$

test: 
$$-t_{\frac{\alpha}{2}} < t^* < t_{\frac{\alpha}{2}} \Longrightarrow H_0$$

$$Se(\overline{x}) = \frac{\hat{\alpha}}{\sqrt{n}}, n > 30$$

$$\alpha < 0.05 => H_1$$

$$\alpha > 0.05 => H_0$$

Jednosmjerni test:

$$DG = \overline{x}_0 - z \cdot Se(\overline{x})$$

$$H_0: ... \bar{x} \ge \bar{x}_0$$

$$H_1: ...\bar{x} < \bar{x}_0$$

TH o razlici aritmetickih sredina dvaju nezavishin osnovnih skupova:

$$H_0$$
:... $\bar{x}_1 = \bar{x}_2$ 

$$H_1:...\bar{x}_1 \neq \bar{x}_2$$

Interval prihvacanja H<sub>0</sub>:

$$0 \pm z \cdot Se(\bar{x}_1 - \bar{x}_2)$$

$$t^* = z^* = \frac{|\hat{x}_1 - \hat{x}_2|}{Se(\bar{x}_1 - \bar{x}_2)}$$

$$df = \nu = n_1 + n_2 - 2$$

$$Se(\bar{x}_1 - \bar{x}_2) = \sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}$$

$$n < 30 \implies s^2 = \sigma^2 \frac{n}{n-1}$$

$$Se(\bar{x}_1 - \bar{x}_2) = \sqrt{(\frac{n_1\hat{\sigma}_1^2 + n_2\hat{\sigma}_2^2}{n_1 + n_2 - 2}) \cdot (\frac{n_1 + n_2}{n_1 n_2})}$$

uzorak mal za n<sub>1</sub>+n<sub>2</sub>≤32

Za zavisne uzorke:

$$Se = \sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}} - 2r_{1,2}Se(\bar{x}_1)Se(\bar{x}_2)$$

TH o nepoznatoj proporciji osnovnog skupa:

$$H_0: ...P = P_0$$

$$H_1:...P \neq P_0$$

Interval prihvacanja H<sub>0</sub>:

$$P_0 \pm z \cdot Se(P)$$

$$Se(P) = \sqrt{\frac{P_0 Q_0}{n}}, n > 30$$

$$Se(P) = \sqrt{\frac{P_0 Q_0}{n-1}}, n < 30$$

$$\widehat{p} = \frac{m}{n}, z^* = \frac{|\widehat{p} - p_0|}{Se(p)}$$

TH o razlici proporcija dvaju nezavisnih osnovnih skupova:

$$H_0: ...P_1 = P_2$$

$$H_1 : \dots P_1 \neq P_2$$

Interval prihvacanja H<sub>0</sub>:

$$0 \pm z \cdot Se(P_1 - P_2)$$

$$df = \nu = n_1 + n_2 - 2$$

$$Se(P_1 - P_2) = \sqrt{\hat{p} \cdot \hat{q} \cdot (\frac{1}{n_1} + \frac{1}{n_2})}$$

$$\widehat{\overline{P}} = \frac{m_1 + m_2}{n_1 + n_2}$$

$$-n_1 + n_2$$

$$z^* = \frac{\hat{p}_1 - \hat{p}_2}{Se(p_1 - p_2)}$$

TH da je koef. linearne korelacije jednak nuli

$$H_0: ... r = 0$$

Interval prihvacanja:  $0 \pm z \cdot Se(r)$ 

$$Se(r) = \sqrt{\frac{1}{n-1}}$$
 za veliki

$$Se(r) = \sqrt{\frac{1-\widehat{r}^2}{n-2}}$$
 za mali

$$\nu = n - 0$$

 $\chi^{*2}$ test:

Testiranje da distribucija ima određeni oblik:

Poisson:

$$H_0: ...X -> P(\mu)$$

$$P(X=x) = \frac{\mu}{x!}e^{-x}$$

$$H_0: ...X - > P(\mu)$$

$$H_1: ...X - / > P(\mu)$$

$$P(X = x) = \frac{\mu^x}{x!} e^{-\mu}$$

$$\chi^{*2} = \sum_{i=1}^k \frac{(f_i - f_{ii})^2}{f_{ii}}$$

$$\mu = \hat{\vec{x}}$$
  $f_{ii} = (\sum f_i) \cdot P(x_i)$   $df = \nu = k - 2$ 

Binomna:

$$H_0: ...X - > B(n; p)$$

$$P(X = x) =$$

$$H_0: ...X -> B(n; p)$$
  
 $H_1: ...X -/> B(n; p)$   $P(X = x) = \binom{n}{x} p^x q^{n-x}$   $f_{ii} = (\sum f_i) \cdot P(x_i)$ 

$$\chi^{*2} = \sum_{i=1}^{k} \frac{(f_i - f_{ii})^2}{f_{ii}}$$
  $df = \nu = k - 2$   $\mu = n \cdot p$   $p = \frac{\bar{x}}{n}$ 

$$df = \nu = k - 2$$

$$\mu = n \cdot p$$
  $p = 0$ 

$$\begin{array}{ll} H_0:...P_1=P_2=...=P \\ H_1:...\exists P_i\neq P \end{array} \qquad \begin{array}{ll} \widehat{\overline{P}}=\frac{\sum m_i}{\sum n_i} \\ e_i=n_i\cdot\widehat{\overline{P}} \end{array} \qquad \nu=k-1 \end{array}$$

$$\widehat{\widehat{P}} = \frac{\sum m_i}{\sum n}$$

$$e_i = n_i \cdot \hat{\overline{P}}$$

$$\nu = k - 1$$

$$\chi^{*2} = \sum_{i=1}^{k} \frac{(m_i - e_i)^2}{e_i}$$

TH o nezavisnosti obiljezja elemenata osnovnog skupa

$$H_0: ...P_{ij} = P_{i*} \cdot P_{*j}, \forall i \forall j$$

$$\chi^{*2} = \sum \sum \frac{(m_{ij} - e)}{e}$$

$$df = (r-1)(c-1)$$

$$H_{0}:...P_{ij} = P_{i*} \cdot P_{*j}, \forall i \forall j$$

$$H_{1}:...\exists P_{ij} \neq P_{i*} \cdot P_{*j}$$

$$\chi^{*2} = \sum_{i} \sum_{j} \frac{(m_{ij} - e_{ij})^{2}}{e_{ij}}$$

$$df = (r-1)(c-1)$$

$$e_{ij} = \frac{m_{i*} \cdot m_{*j}}{n}$$

$$\chi^{*2} > \chi^{2} \Rightarrow H_{1}$$

$$\chi^{*2} < \chi^{2} \Rightarrow H_{0}$$

Pearsonov koef. Kontingence: 
$$C = \sqrt{\frac{\chi^2}{\chi^2 + n}}$$

Analiza varijance s jednim promjenjivim faktorom

$$H_0: ... \sigma_A^{-2} = 0$$

$$H_1 : ... \sigma_A^2 \neq 0$$

$$\overline{X}_{**} = \frac{n_1 \overline{x}_{*j1} + n_2 \overline{x}_{*j2} + \dots}{n_1 + n_2 + \dots}$$

$$\overline{X}_{**} = \frac{n_1 \overline{x}_{*j1} + n_2 \overline{x}_{*j2} + \dots}{n_1 + n_2 + \dots}$$
Ukupno: 
$$\sum_{i} \sum_{j} (X_{ij} - \overline{X}_{**})^2 \quad \nu = n - 1$$

Unutar uzoraka:

$$\sum_{i} \sum_{j} (X_{ij} - \overline{X}_{*j})^{2} \qquad \nu = n - k$$

Izmedu uzoraka:

$$\sum n_j (\overline{X}_{*j} - \overline{X}_{**})^2 \quad \nu = k-1$$

$$F^* = \frac{izmedu/(k-1)}{unutar/(n-k)} \qquad F^{\alpha}_{k-1,n-k}$$

Analiza varijance sa dva promjenjiva

$$H_0: ... \sigma_A^2 = 0$$
  $H_0: ... \sigma_B^2 = 0$   
 $H_1: ... \sigma_A^2 \neq 0$   $H_1: ... \sigma_B^2 \neq 0$   
Ukupno:  $\sum_i \sum_j (X_{ij} - \overline{X}_{**})^2 \quad \nu = n-1$ 

Izmedu redaka:  

$$\sum_{i} n_{i} (\overline{X}_{i*} - \overline{X}_{**})^{2} \quad \nu = c - 1$$

Izmedu stupaca:

$$\sum_{j} n_{j} (\overline{X}_{*j} - \overline{X}_{**})^{2} \qquad \nu = k - 1$$

$$\sum_{i} \sum_{i} (X_{ij} - \overline{X}_{*j} - \overline{X}_{i*} + -\overline{X}_{**})^{2}$$

$$\nu = n - k - c + 1$$

$$F_{_A}{}^* = \frac{izmedu\_redaka/(c-1)}{ostatak/(n-k-c+1)}$$

$$F_{B}^{*} = \frac{izmedu\_stupaca/(k-1)}{ostatak/(n-k-c+1)}$$

Koeficijent korelacije

Spermanov koef. korelacije

$$r_s = 1 - \frac{6\sum_{i=1}^{n} d_i^2}{n^3 - n}$$

n-broj parova vrijednosti X

$$d_i^2 = (r_{xi} - r_{yi})^2, df = n - 2$$