

TH o nepoznatoj aritmetickoj sredini osnovnog skupa:

$$H_0 : \dots \bar{x} = \bar{x}_0$$

$$H_1 : \dots \bar{x} \neq \bar{x}_0$$

Interval prihvatanja H_0 :

$$\bar{x}_0 \pm z \cdot Se(\bar{x})$$

$$t^* = z^* = \frac{\hat{\bar{x}} - \bar{x}_0}{Se(\bar{x})}$$

$$\text{test: } -t_{\frac{\alpha}{2}} < t^* < t_{\frac{\alpha}{2}} \Rightarrow H_0$$

$$Se(\bar{x}) = \frac{\hat{\sigma}}{\sqrt{n}}, n > 30$$

$$\alpha < 0.05 \Rightarrow H_1$$

$$\alpha > 0.05 \Rightarrow H_0$$

Jednosmjerni test:

$$DG = \bar{x}_0 - z \cdot Se(\bar{x})$$

$$H_0 : \dots \bar{x} \geq \bar{x}_0$$

$$H_1 : \dots \bar{x} < \bar{x}_0$$

TH o razlici aritmetickih sredina dvaju nezavisnih osnovnih skupova:

$$H_0 : \dots \bar{x}_1 = \bar{x}_2$$

$$H_1 : \dots \bar{x}_1 \neq \bar{x}_2$$

Interval prihvatanja H_0 :

$$0 \pm z \cdot Se(\bar{x}_1 - \bar{x}_2)$$

$$t^* = z^* = \frac{|\hat{\bar{x}}_1 - \hat{\bar{x}}_2|}{Se(\bar{x}_1 - \bar{x}_2)}$$

$$df = \nu = n_1 + n_2 - 2$$

$$Se(\bar{x}_1 - \bar{x}_2) = \sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}$$

$$n < 30 \Rightarrow s^2 = \sigma^2 \frac{n}{n-1}$$

$$Se(\bar{x}_1 - \bar{x}_2) = \sqrt{\left(\frac{n_1 \hat{\sigma}_1^2 + n_2 \hat{\sigma}_2^2}{n_1 + n_2 - 2}\right) \cdot \left(\frac{n_1 + n_2}{n_1 n_2}\right)}$$

uzorak mal za $n_1 + n_2 \leq 32$

Za zavisne uzorke:

$$Se = \sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2} - 2r_{1,2} Se(\bar{x}_1) Se(\bar{x}_2)}$$

TH o nepoznatoj proporciji osnovnog skupa:

$$H_0 : \dots P = P_0$$

$$H_1 : \dots P \neq P_0$$

Interval prihvatanja H_0 :

$$P_0 \pm z \cdot Se(P)$$

$$Se(P) = \sqrt{\frac{P_0 Q_0}{n}}, n > 30$$

$$Se(P) = \sqrt{\frac{P_0 Q_0}{n-1}}, n < 30$$

$$\hat{p} = \frac{m}{n}, z^* = \frac{|\hat{p} - p_0|}{Se(p)}$$

TH o razlici proporcija dvaju nezavisnih osnovnih skupova:

$$H_0 : \dots P_1 = P_2$$

$$H_1 : \dots P_1 \neq P_2$$

Interval prihvatanja H_0 :

$$0 \pm z \cdot Se(P_1 - P_2)$$

$$df = \nu = n_1 + n_2 - 2$$

$$Se(P_1 - P_2) = \sqrt{\hat{p} \cdot \hat{q} \cdot \left(\frac{1}{n_1} + \frac{1}{n_2}\right)}$$

$$\hat{p} = \frac{m_1 + m_2}{n_1 + n_2}$$

$$z^* = \frac{\hat{p}_1 - \hat{p}_2}{Se(p_1 - p_2)}$$

χ^2 test:

Testiranje da distribucija ima određeni oblik:

Poisson:

$$H_0 : \dots X \sim P(\mu)$$

$$H_1 : \dots X \not\sim P(\mu)$$

$$\mu = \hat{\bar{x}} \quad f_{ii} = \left(\sum f_i\right) \cdot P(x_i) \quad df = \nu = k - 2$$

Binomna:

$$H_0 : \dots X \sim B(n; p)$$

$$H_1 : \dots X \not\sim B(n; p)$$

$$P(X = x) = \binom{n}{x} p^x q^{n-x} \quad f_{ii} = \left(\sum f_i\right) \cdot P(x_i)$$

Jednolika:

$$H_0 : \dots P_1 = P_2 = \dots = P$$

$$H_1 : \dots \exists P_i \neq P$$

$$\chi^2 = \sum_{i=1}^k \frac{(m_i - e_i)^2}{e_i}$$

TH o nezavisnosti obilježja elemenata osnovnog skupa

$$H_0 : \dots P_{ij} = P_{i*} \cdot P_{*j}, \forall i \forall j$$

$$H_1 : \dots \exists P_{ij} \neq P_{i*} \cdot P_{*j}$$

$$e_{ij} = \frac{m_{i*} \cdot m_{*j}}{n}$$

$$\chi^2 > \chi^2 \Rightarrow H_1$$

$$\chi^2 < \chi^2 \Rightarrow H_0$$

$$\text{Pearsonov koef. Kontingence: } C = \sqrt{\frac{\chi^2}{\chi^2 + n}}$$

$$P(X = x) = \frac{\mu^x}{x!} e^{-\mu} \quad \chi^2 = \sum_{i=1}^k \frac{(f_i - f_{ii})^2}{f_{ii}}$$

$$\mu = n \cdot p \quad p = \frac{\bar{x}}{n}$$

$$\hat{P} = \frac{\sum m_i}{\sum n_i} \quad e_i = n_i \cdot \hat{P} \quad \nu = k - 1$$

$$\chi^2 = \sum_i \sum_j \frac{(m_{ij} - e_{ij})^2}{e_{ij}} \quad df = (r-1)(c-1)$$

TH da je koef. linearne korelacije jednak nuli

$$H_0 : \dots r = 0 \quad t^* = \frac{\hat{r}}{Se(r)}$$

Interval prihvatanja:

$$0 \pm z \cdot Se(r)$$

$$Se(r) = \sqrt{\frac{1}{n-1}} \quad \text{za veliki}$$

$$Se(r) = \sqrt{\frac{1 - \hat{r}^2}{n-2}} \quad \text{za mali}$$

$$\nu = n - 2$$

Analiza varijance s jednim promjenjivim faktorom

$$H_0 : \dots \sigma_A^2 = 0$$

$$H_1 : \dots \sigma_A^2 \neq 0$$

$$\bar{X}_{**} = \frac{n_1 \bar{x}_{*j1} + n_2 \bar{x}_{*j2} + \dots}{n_1 + n_2 + \dots}$$

$$\text{Ukupno: } \sum_i \sum_j (X_{ij} - \bar{X}_{**})^2 \quad \nu = n - 1$$

Unutar uzoraka:

$$\sum_i \sum_j (X_{ij} - \bar{X}_{*j})^2 \quad \nu = n - k$$

Između uzoraka:

$$\sum_j n_j (\bar{X}_{*j} - \bar{X}_{**})^2 \quad \nu = k - 1$$

$$F^* = \frac{\text{između} / (k - 1)}{\text{unutar} / (n - k)} \quad F^{\alpha}_{k-1, n-k}$$

Analiza varijance sa dva promjenjiva faktora

$$H_0 : \dots \sigma_A^2 = 0 \quad H_0 : \dots \sigma_B^2 = 0$$

$$H_1 : \dots \sigma_A^2 \neq 0 \quad H_1 : \dots \sigma_B^2 \neq 0$$

$$\text{Ukupno: } \sum_i \sum_j (X_{ij} - \bar{X}_{**})^2 \quad \nu = n - 1$$

Između redaka:

$$\sum_i n_i (\bar{X}_{i*} - \bar{X}_{**})^2 \quad \nu = c - 1$$

Između stupaca:

$$\sum_j n_j (\bar{X}_{*j} - \bar{X}_{**})^2 \quad \nu = k - 1$$

Ostatak:

$$\sum_i \sum_j (X_{ij} - \bar{X}_{*j} - \bar{X}_{i*} + \bar{X}_{**})^2 \quad \nu = n - k - c + 1$$

$$F_A^* = \frac{\text{između_redaka} / (c - 1)}{\text{ostatak} / (n - k - c + 1)}$$

$$F_B^* = \frac{\text{između_stupaca} / (k - 1)}{\text{ostatak} / (n - k - c + 1)}$$

Koeficijent korelacije ranga

Spermanov koef. korelacije ranga:

$$r_s = 1 - \frac{6 \sum_{i=1}^n d_i^2}{n^3 - n}$$

n-broj parova vrijednosti X i Y

$$d_i^2 = (r_{xi} - r_{yi})^2, df = n - 2$$