



Bipolarni tranzistor

Elektronika – 4. predavanje

William B. Shockley (1910-1989)

- Poznat kao “otac” tranzistora



“It has today occurred to me that an amplifier using semiconductors rather than vacuum tubes is in principle possible.”

Walter Houser Brattain (1902-1987)

- Eksperimentalni fizičar koji je također radio s vakuumskim cijevima.
- Priključio se Shockleyju i Bardeenu u istraživanju poluvodiča.



John Bardeen (1908-1991)

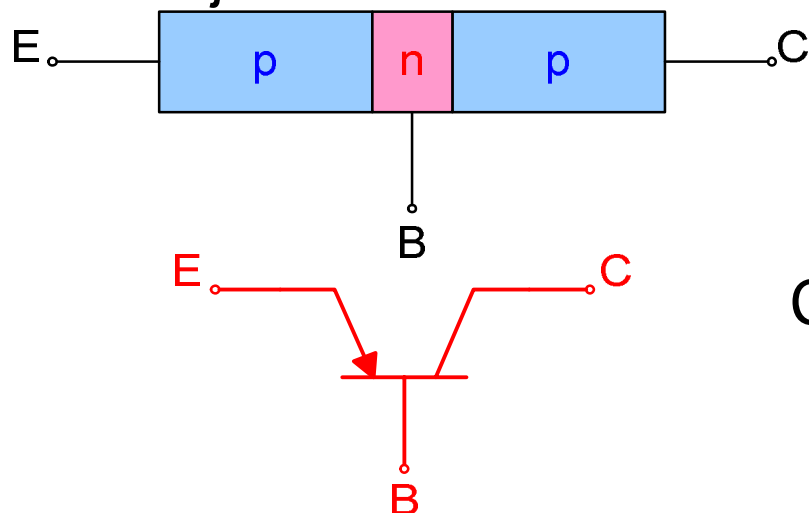
- Fizičar, Naval Ordnance Laboratory (1941-1945)
- Teorijski fizičar, Bell Telephone Laboratories (1945-1951)
- Nobelova nagrada za fiziku 1956 i 1972
 - Tranzistor 1956, supervodljivost 1972.



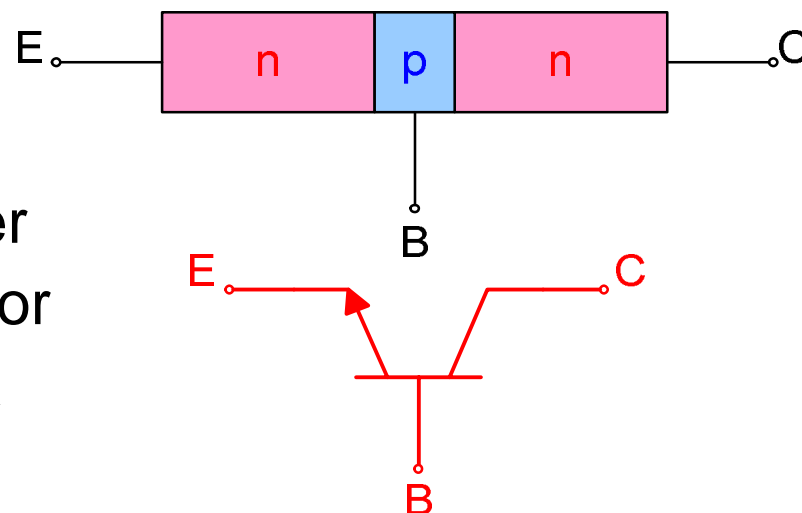
"I knew the transistor was important, but I never foresaw the revolution in electronics it would bring."

Bipolarni tranzistor

- Naziv tranzistor je nastao kao složenica od dvije engleske riječi: transfer resistor (prenijeti otpor).
- Naziv (pridjev) **bipolarni** znači da u vođenju sudjeluju oba tipa nosilaca: elektroni i šupljine.
- U stručnoj literaturi u uporabi je skraćenica **BJT** (bipolar junction transistor): bipolarni spojni tranzistor.
- Ustrojstvo i simbol:



E – emiter
C – kolektor
B - baza



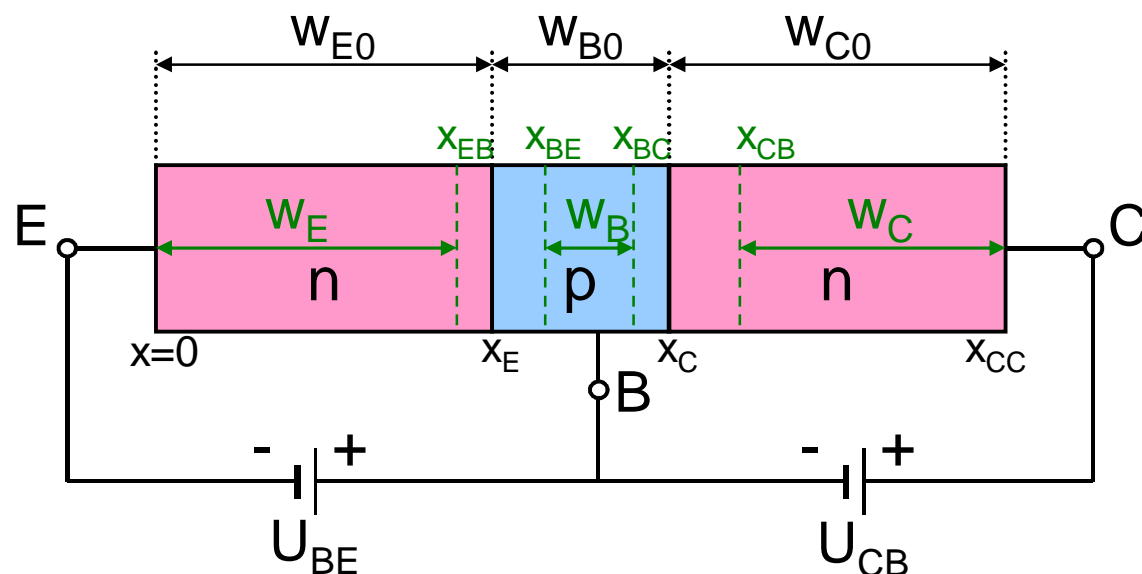
Tranzistorski efekt

- Temelji se na mehanizmu:
 - Injekcije (utiskivanja) nosilaca
 - Tranzita (prijenosa) nosilaca
 - Kolekcije (sakupljanja) nosilaca
- Polarizacija tranzistora i područja rada
 - Spoj emiter-baza je propusno polariziran, a spoj kolektor-baza nepropusno (normalno aktivno područje rada)
 - Spoj emiter-baza i kolektor-baza su propusno polarizirani (područje zasićenja)
 - Spoj emiter-baza i kolektor-baza su nepropusno polarizirani (zaporno područje)
 - Spoj emiter-baza je polariziran nepropusno, a kolektor-baza propusno (inverzno aktivno područje rada)



Normalno polarizirani npn tranzistor

- Definicija područja emitera, baze i kolektora:



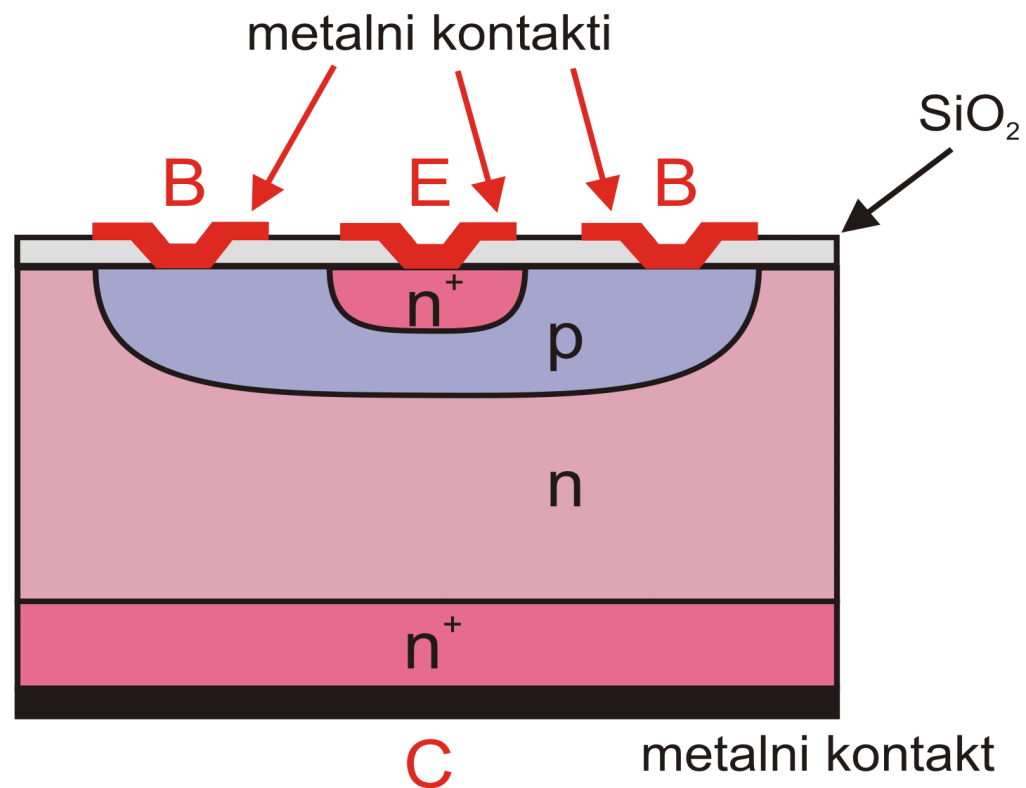
Spoj emiter-baza je
propusno polariziran

Spoj kolektor-baza je
nepropusno
polariziran

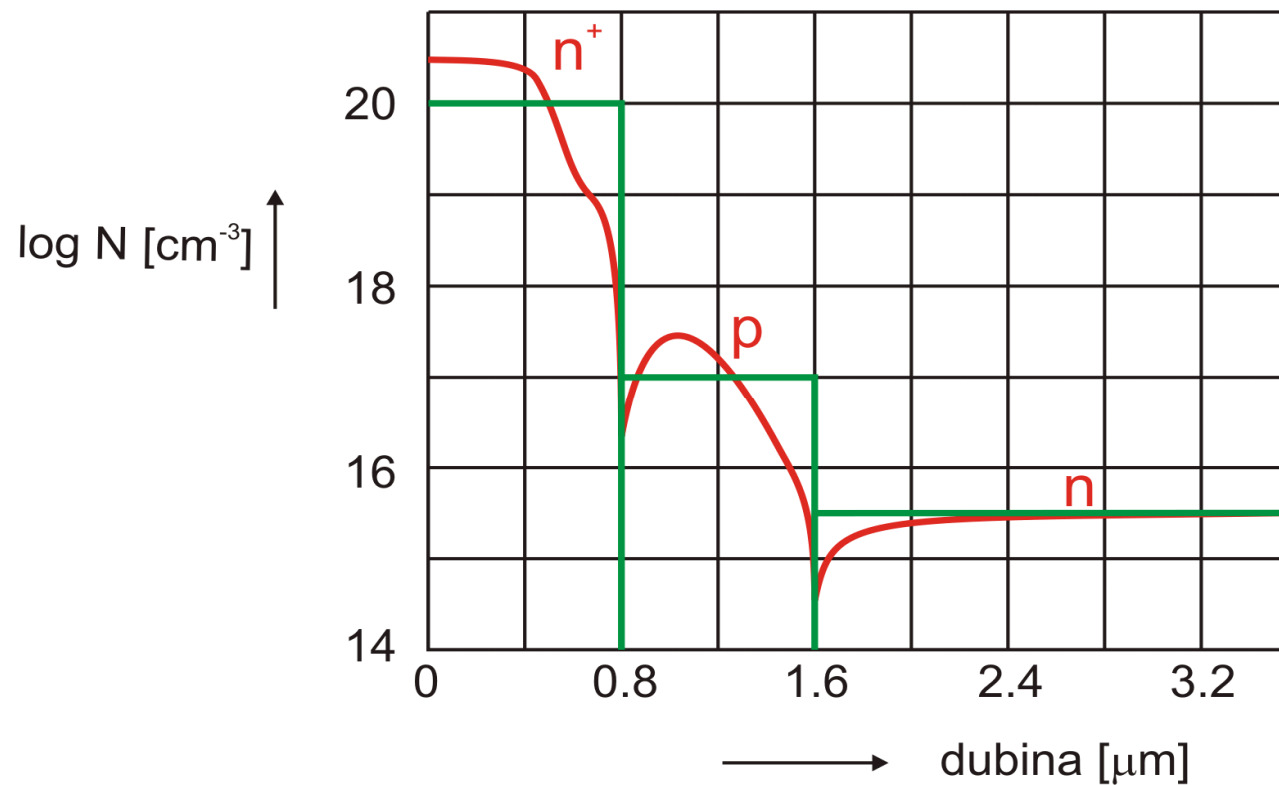
W_E – efektivna širina emitera
 W_B – efektivna širina baze
 W_C – efektivna širina kolektora
 W_{E0} – tehnološka širina emitera
 W_{B0} – tehnološka širina baze
 W_{C0} – tehnološka širina kolektora

$x_{BE} - x_{EB} \Rightarrow$ osiromašeno
područje spoja emiter-baza
 $x_{CB} - x_{BC} \Rightarrow$ osiromašeno
područje spoja kolektor-baza

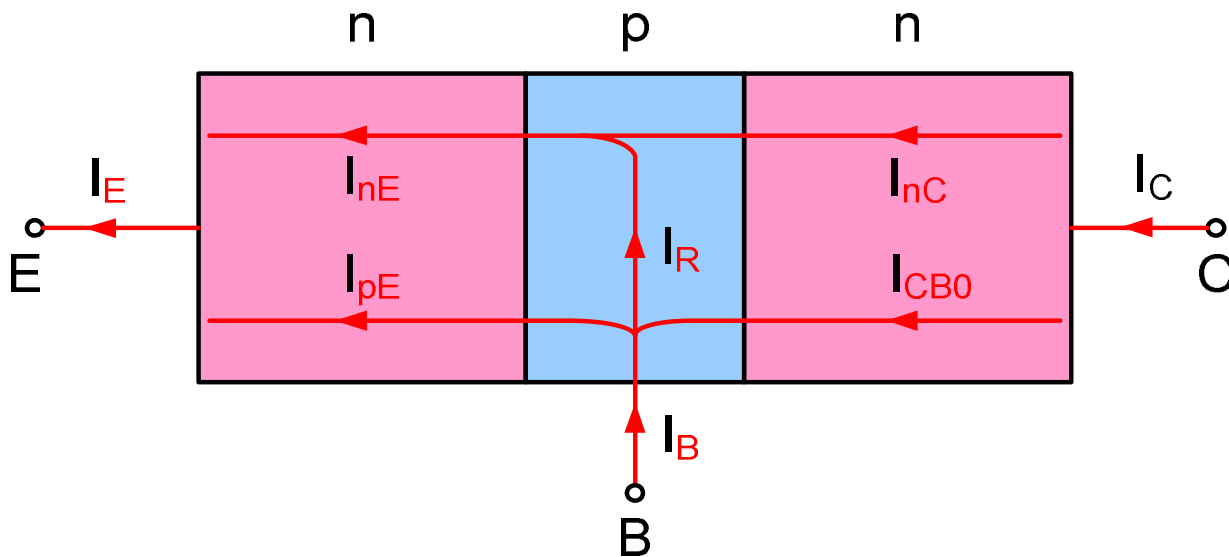
Tehnološka izvedba



- **Profil primjesa:**
 - a) Stvarna raspodjela
 - b) Idealizirana raspodjela



Struje normalno polariziranog tranzistora



$$I_E = I_{nE} + I_{pE}$$

$$I_C = I_{nC} + I_{CB0}$$

$$I_R = I_{nE} - I_{nC}$$

$$I_B = I_{pE} + I_R - I_{CB0}$$

$$I_E = I_C + I_B$$

$$I_{nE} = q \cdot S \cdot D_n \cdot \frac{dn_B}{dx}$$

Elektroni injektirani iz emitera u bazu se difuzijom prenose do kolektorskog spojišta!!!

Parametri tranzistora

- Efikasnost (djelotvornost) emitera:

$$\gamma = \frac{I_{nE}}{I_{nE} + I_{pE}} = \frac{I_{nE}}{I_E} \quad (\text{za npn tranzistor})$$

$$\gamma = \frac{I_{pE}}{I_{nE} + I_{pE}} = \frac{I_{pE}}{I_E} \quad (\text{za pnp tranzistor})$$

- Prijenosni (transportni) faktor:

$$\beta^* = \frac{I_{nC}}{I_{nE}} = 1 - \frac{I_R}{I_{nE}} \quad (\text{za npn tranzistor})$$

$$\beta^* = \frac{I_{pC}}{I_{pE}} = 1 - \frac{I_R}{I_{pE}} \quad (\text{za pnp tranzistor})$$



■ Strujno pojačanje:

$$\alpha = \frac{I_{nC}}{I_E} = \frac{I_{nC}}{I_{nE}} \cdot \frac{I_{nE}}{I_E} = \beta^* \cdot \gamma \quad (\text{za npn tranzistor})$$

$$\alpha = \frac{I_{pC}}{I_E} = \frac{I_{pC}}{I_{pE}} \cdot \frac{I_{pE}}{I_E} = \beta^* \cdot \gamma \quad (\text{za pnp tranzistor})$$

$$I_C = I_{nC} + I_{CB0} = \alpha \cdot I_E + I_{CB0} \quad I_C = f(I_E)$$

Uvrštavanjem relacije $I_E = I_C + I_B$:

$$I_C = \underbrace{\frac{\alpha}{1 - \alpha}}_{\beta} \cdot I_B + \frac{I_{CB0}}{1 - \alpha} = \beta \cdot I_B + (1 + \beta) \cdot I_{CB0}$$

Djelotvornost emitera

$$\gamma = \frac{I_{nE}}{I_E} = \frac{I_{nE}}{I_{nE} + I_{pE}} = \frac{1}{1 + \frac{I_{pE}}{I_{nE}}} \quad (\text{npn})$$

Shockleyjeva jednađba za struju emitera glasi:

$$I_E = I_{SE} \left[\exp\left(\frac{q \cdot U_{BE}}{k \cdot T}\right) - 1 \right]$$

I_{SE} – struja manjinskih nosilaca spoja emiter-baza

$$I_{SE} = q \cdot n_i^2 \cdot S \cdot \left[\frac{D_{nB}}{N_{AB} \cdot L_{nB} \cdot th(w_B / L_{nB})} + \frac{D_{pE}}{N_{DE} \cdot L_{pE} \cdot th(w_E / L_{pE})} \right]$$



Budući da je $I_E = I_{pE} + I_{nE}$:

$$\gamma = \left[1 + \frac{D_{pE} \cdot N_{AB} \cdot L_{nB} \cdot \text{th}(w_B / L_{nB})}{D_{nB} \cdot N_{DE} \cdot L_{pE} \cdot \text{th}(w_E / L_{pE})} \right]^{-1}$$

Uz aproksimacije: $w_E / L_{pE} \gg 1$ i $w_B / L_{nB} \ll 1$; $\text{th}(w_E / L_{pE}) \approx 1$ i $\text{th}(w_B / L_{nB}) \approx w_B / L_{nB}$:

$$\gamma = \left[1 + \frac{D_{pE} \cdot N_{AB} \cdot w_B}{D_{nB} \cdot N_{DE} \cdot L_{pE}} \right]^{-1}$$



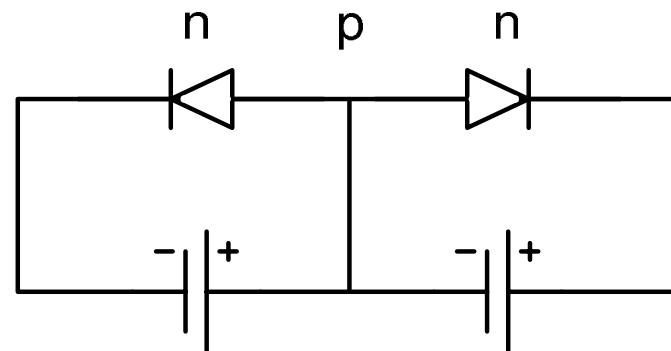
Prijenosni faktor baze tranzistora

$$\beta^* = \frac{I_{nC}}{I_{nE}}$$

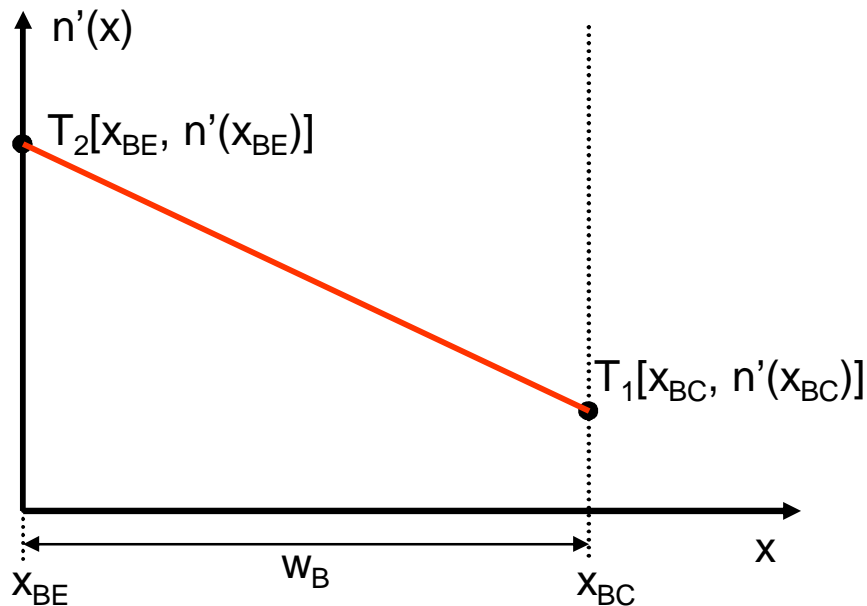
$$\beta^* = \frac{1}{1 + \frac{w_B^2}{2 \cdot L_{nB}^2}} \approx 1 - \frac{1}{2} \left(\frac{w_B}{L_{nB}} \right)^2$$

$w_B \ll L_{nB}$ (**baza je usko područje**)

Uz uvjet $w_B \gg L_{nB}$, $\beta^* \rightarrow 0$, tranzistorski efekt prestaje, a tranzistor se može prikazati s dvije diode:



Vrijeme proleta nosilaca kroz bazu



Linearna raspodjela nosilaca kroz bazu!!!

Jednadžba pravca kroz točke T_1 i T_2 :

$$n'(x) - n'(x_{BC}) = \frac{n'(x_{BE}) - n'(x_{BC})}{x_{BE} - x_{BC}} (x - x_{BC})$$

Gustoća difuzijske struje elektrona u bazi:

$$J_{nB} = q \cdot D_{nB} \cdot \frac{dn'(x)}{dx} \approx -q \cdot D_{nB} \frac{n'(x_{BE})}{w_B} = -q \cdot n'(x) \cdot v(x)$$

$v(x) \Rightarrow$ brzina nosilaca kroz bazu

U skladu s definicijom $v(x)=dx/dt$, vrijeme proleta nosilaca je:

$$t_{pr} = \int_{x_{BE}}^{x_{BC}} \frac{dx}{v(x)}$$

$$v(x) = -\frac{D_{nB}}{w_B} \cdot \frac{n'(x_{BE})}{n'(x)}$$

Uz aproksimaciju $n'(x_{BE}) \gg n'(x_{BC}) \approx 0$:

$$n'(x) = \frac{n'(x_{BE})}{-w_B} \cdot (x - x_{BC})$$



Stoga je:

$$v(x) = -\frac{D_{nB}}{x - x_{BC}}$$

$$t_{pr} = -\int_{x_{BE}}^{x_{BC}} \frac{x - x_{BC}}{D_{nB}} dx = \frac{w_B^2}{2D_{nB}}$$

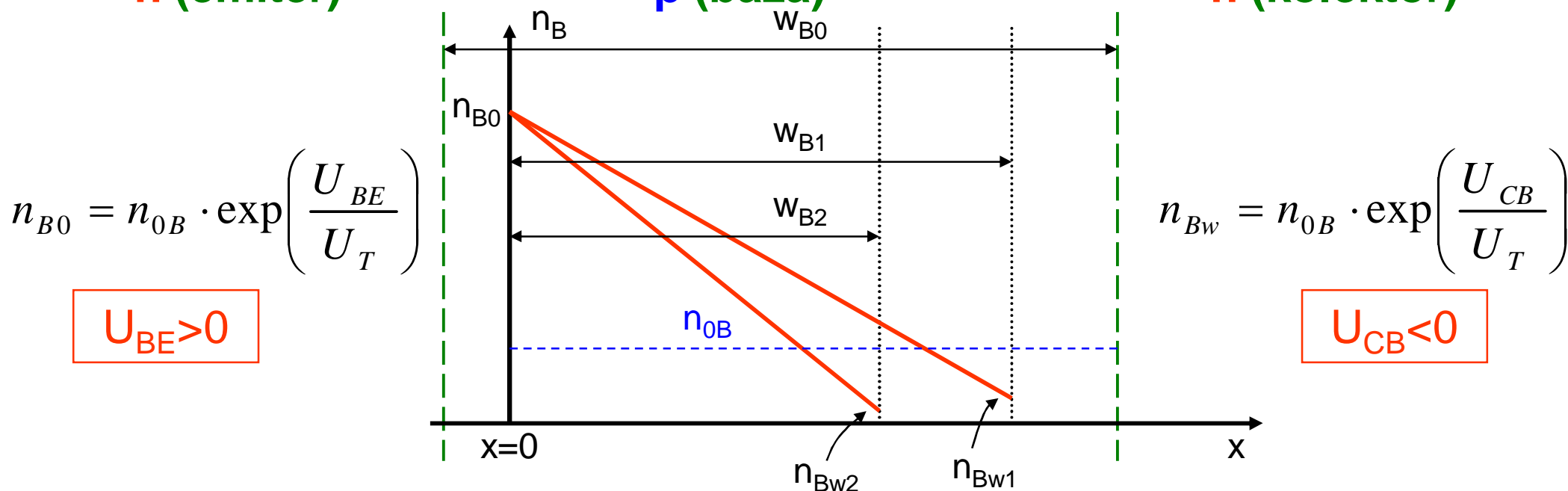
Izraz za vrijeme proleta nosilaca kroz bazu identičan je izrazu izvedenom za usku n stranu pn spoja.

Earlyjev efekt

n (emiter)

p (baza)

n (kolektor)



- Povećanjem napona nepropusne polarizacije spoja kolektor-baza, smanjuje se efektivna širina baze (Earlyjev efekt).
- Može nastupiti i naponski proboj (engl. punch-through) pri većim iznosima napona nepropusne polarizacije spoja kolektor-baza.



Ebers-Mollove jednadžbe i model tranzistora

$$I_E = a_{11} \left[\exp\left(\frac{U_{BE}}{U_T}\right) - 1 \right] + a_{12} \left[\exp\left(\frac{U_{BC}}{U_T}\right) - 1 \right]$$
$$I_C = a_{21} \left[\exp\left(\frac{U_{BE}}{U_T}\right) - 1 \right] + a_{22} \left[\exp\left(\frac{U_{BC}}{U_T}\right) - 1 \right]$$

$$a_{11} = S \cdot q \cdot \left(\frac{D_{nB} \cdot n_{0B}}{w_B} + \frac{D_{pE} \cdot p_{0E}}{L_{pE}} \right)$$

$$a_{22} = S \cdot q \cdot \left(\frac{D_{nB} \cdot n_{0B}}{w_B} + \frac{D_{pC} \cdot p_{0C}}{L_{pC}} \right)$$

$$a_{12} = a_{21} = -S \cdot q \cdot D_{nB} \cdot \frac{n_{0B}}{w_B}$$

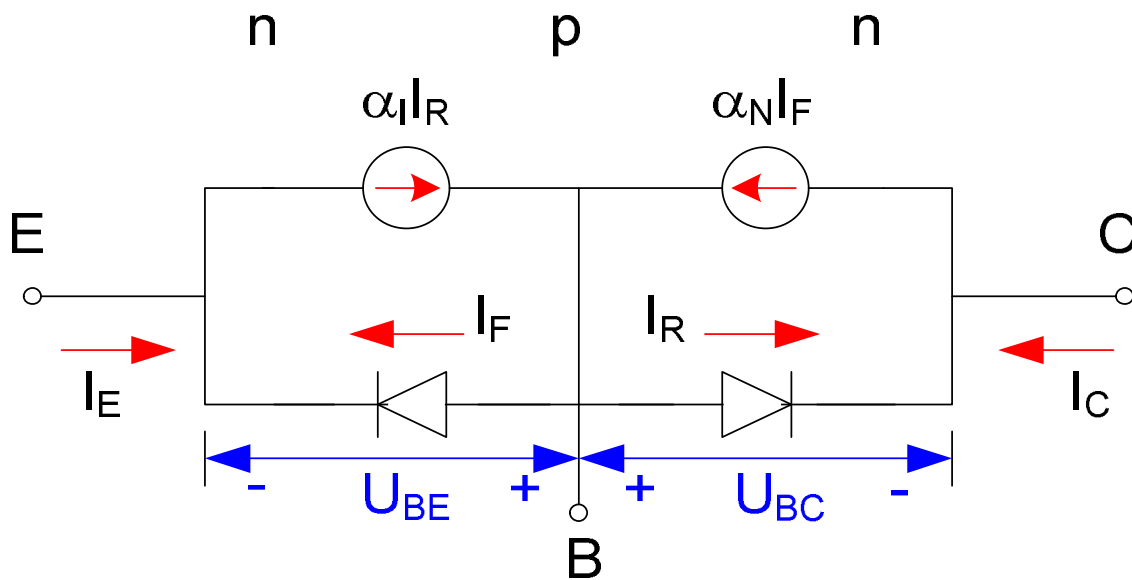
(svojstvo recipročnosti!)

a_{11} jest struja $I_E = I_{ES}$ pri $U_{BC}=0$ i $U_{BE}<0$

a_{22} jest struja $I_C = I_{CS}$ pri $U_{BE}=0$ i $U_{BC}<0$



Injekcijski Ebers-Mollov model



$$I_E - \alpha_I I_R + I_F = 0 \quad (1)$$

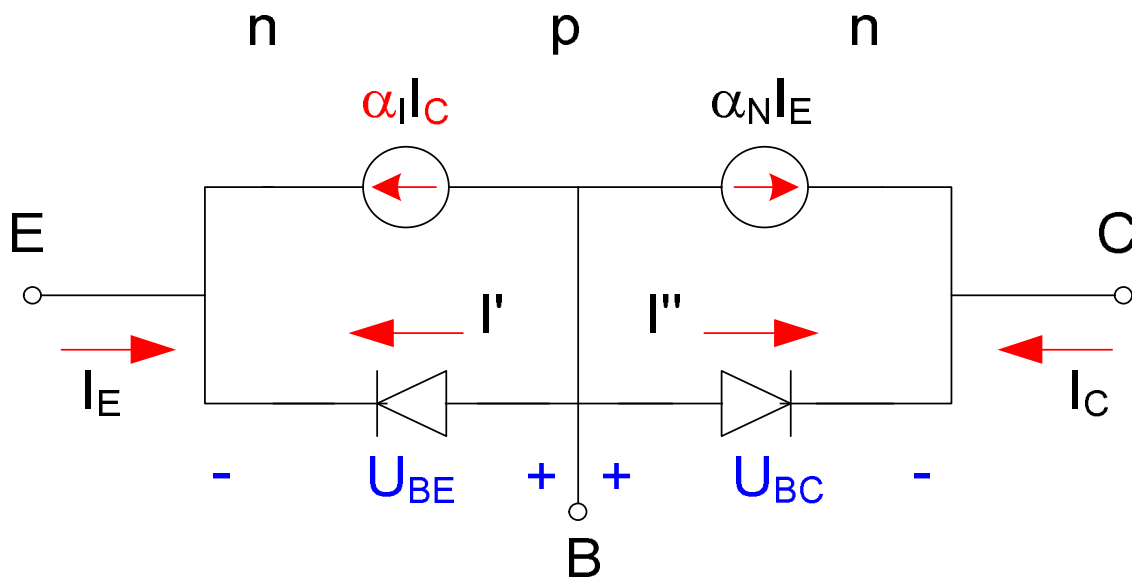
$$I_C - \alpha_N I_F + I_R = 0 \quad (2)$$

$$I_F = I_{ES} \left[\exp\left(\frac{U_{BE}}{U_T}\right) - 1 \right] \quad (3)$$

$$I_R = I_{CS} \left[\exp\left(\frac{U_{BC}}{U_T}\right) - 1 \right] \quad (4)$$

$$I_E = -I_{ES} \left[\exp\left(\frac{U_{BE}}{U_T}\right) - 1 \right] + \alpha_I I_{CS} \left[\exp\left(\frac{U_{BC}}{U_T}\right) - 1 \right]$$

$$I_C = \alpha_N I_{ES} \left[\exp\left(\frac{U_{BE}}{U_T}\right) - 1 \right] - I_{CS} \left[\exp\left(\frac{U_{BC}}{U_T}\right) - 1 \right]$$



$$I_E + \alpha_I I_C + I' = 0$$

$$I_C + \alpha_N I_E + I'' = 0$$

$$I' = I_{EB0} \left[\exp\left(\frac{U_{BE}}{U_T}\right) - 1 \right]$$

$$I'' = I_{CB0} \left[\exp\left(\frac{U_{BC}}{U_T}\right) - 1 \right]$$

$$I_E = -\frac{I_{EB0}}{1 - \alpha_I \alpha_N} \left[\exp\left(\frac{U_{BE}}{U_T}\right) - 1 \right] + \frac{\alpha_I I_{CB0}}{1 - \alpha_I \alpha_N} \left[\exp\left(\frac{U_{BC}}{U_T}\right) - 1 \right]$$

$$I_C = \frac{\alpha_N I_{EB0}}{1 - \alpha_I \alpha_N} \left[\exp\left(\frac{U_{BE}}{U_T}\right) - 1 \right] - \frac{I_{CB0}}{1 - \alpha_I \alpha_N} \left[\exp\left(\frac{U_{BC}}{U_T}\right) - 1 \right]$$

$$I_{ES} = \frac{I_{EB0}}{1 - \alpha_I \alpha_N}$$

$$I_{CS} = \frac{I_{CB0}}{1 - \alpha_I \alpha_N}$$

$$I_C = \alpha_N I_E + I_{CB0}$$

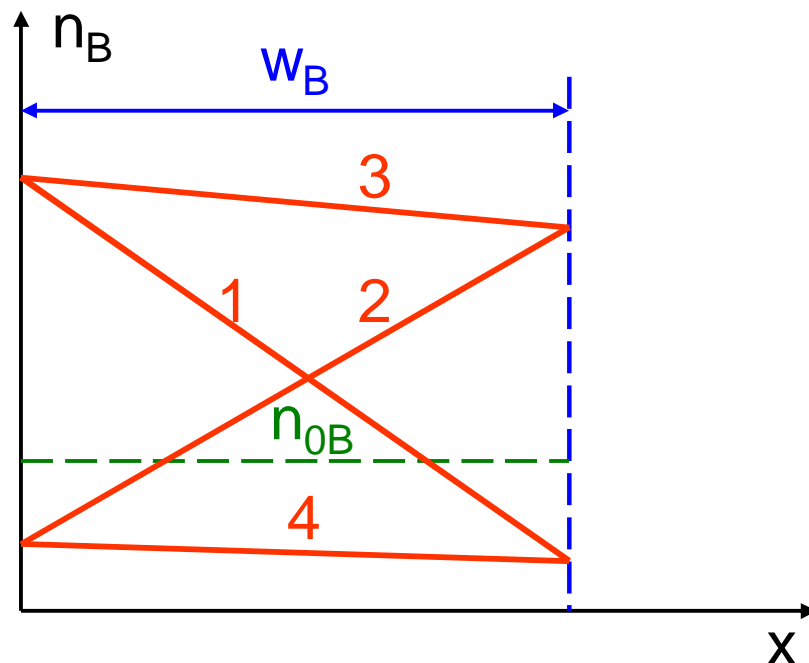
$$I_E = \alpha_I I_C + I_{EB0}$$

$$I_{CB0} = I_C \quad (\text{uz } I_E = 0)$$

$$I_{EB0} = I_E \quad (\text{uz } I_C = 0)$$



Područja rada tranzistora



- 1 – normalno aktivno područje
- 2 – inverzno aktivno područje
- 3 – područje zasićenja
- 4 – zaporno područje

■ Normalno aktivno područje

$$U_{BE} \gg U_T, U_{BC} < 0$$

$$I_E = -I_{ES} \left[\exp\left(\frac{U_{BE}}{U_T}\right) - 1 \right] - \alpha_I I_{CS} \quad (1)$$

$$I_C = \alpha_N I_{ES} \left[\exp\left(\frac{U_{BE}}{U_T}\right) - 1 \right] + I_{CS} \quad (2)$$

Iz (1) i (2) slijedi funkcija $I_C = f(I_E)$:

$$I_C = -\alpha_N I_E + \underbrace{I_{CS} (1 - \alpha_N \alpha_I)}_{I_{CB0}}$$

$$I_C = -\alpha_N I_E + I_{CB0}$$

■ Inverzno aktivno područje

$$U_{BE} < 0, U_{BC} > 0$$

$$I_E = I_{ES} + \alpha_I I_{CS} \left[\exp\left(\frac{U_{BC}}{U_T}\right) - 1 \right] \quad (1)$$

$$I_C = \alpha_N I_{ES} - I_{CS} \left[\exp\left(\frac{U_{BC}}{U_T}\right) - 1 \right] \quad (2)$$

Iz (1) i (2) slijedi funkcija $I_E = f(I_C)$:

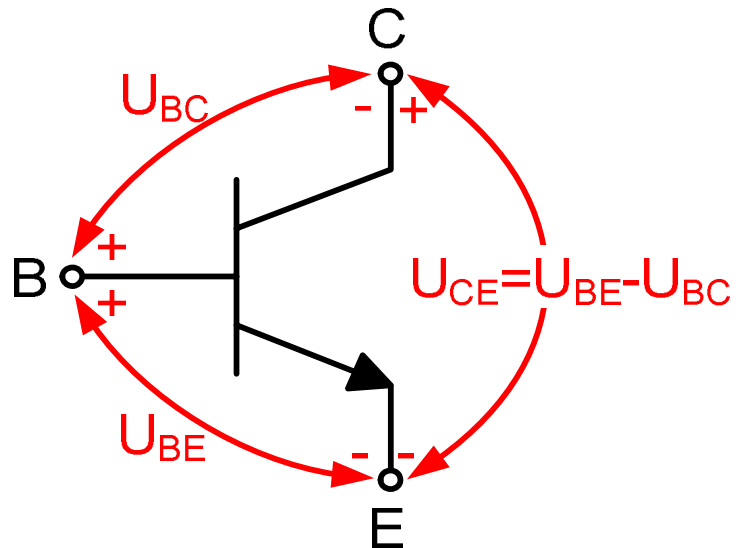
$$I_E = -\alpha_I I_C + I_{EB0}$$

■ Područje zasićenja

$$U_{BE} > 0, U_{BC} > 0$$

$$U_{BE} = U_T \cdot \ln \frac{I_E + \alpha_I I_C - I_{EB0}}{-I_{EB0}}$$

$$U_{BC} = U_T \cdot \ln \frac{I_C + \alpha_N I_E - I_{CB0}}{-I_{CB0}}$$



$$U_{CE} = U_T \cdot \ln \frac{(I_E + \alpha_I I_C - I_{EB0}) \cdot \alpha_N}{(I_C + \alpha_N I_E - I_{CB0}) \cdot \alpha_I}$$

■ Zaporno područje

$$U_{BE} < 0, U_{BC} < 0$$

$$I_E = \frac{I_{EB0}}{1 - \alpha_N \alpha_I} (1 - \alpha_N)$$

$$I_C = \frac{I_{CB0}}{1 - \alpha_N \alpha_I} (1 - \alpha_I)$$

Unatoč nepropusnoj polarizaciji kroz oba spojišta teku male struje emitera i kolektora.

Stoga se zaporno područje definira uvjetom: $I_E = 0$; $U_{BC} < 0$ te je $I_C = I_{CB0}$

Uz ove uvjete iz Ebers-Mollovih jednadžbi dobiva se odgovarajući napon U_{BE} :

$$U_{BE} = U_T \cdot \ln(1 - \alpha_N)$$

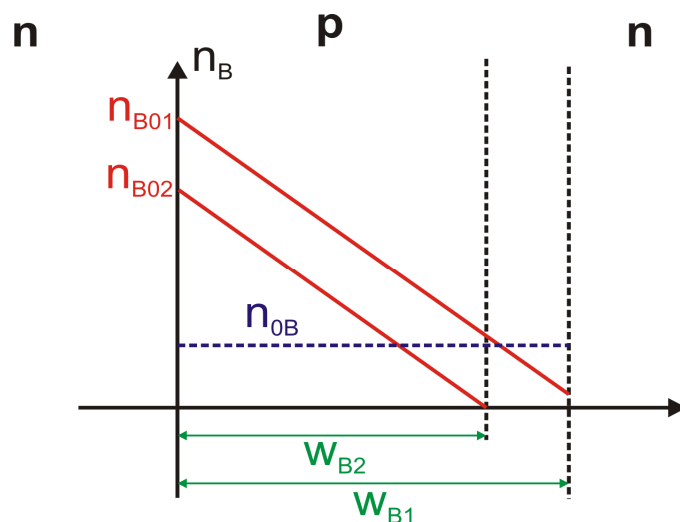
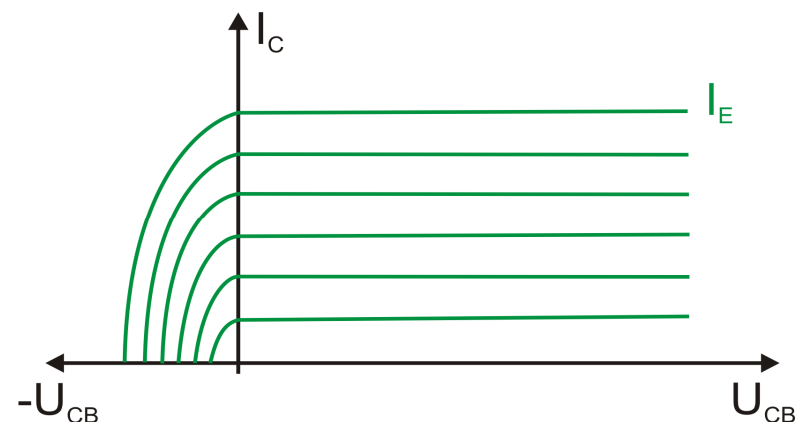
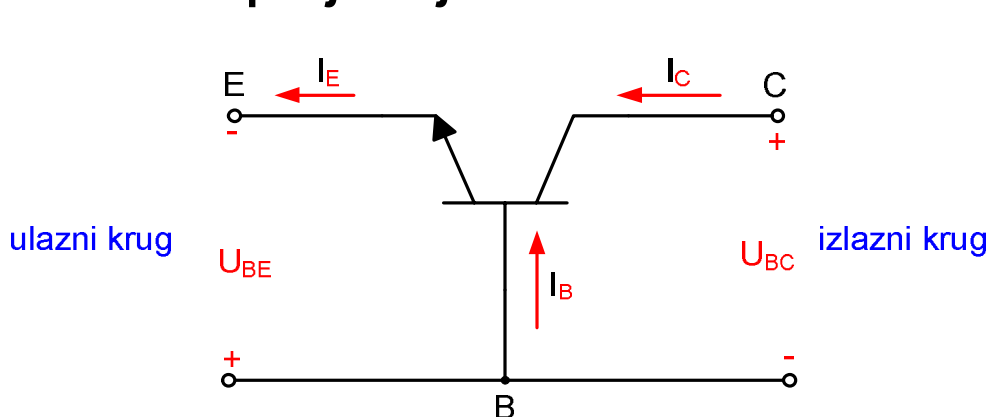
Npr. za $\alpha = 0,9$ pri $T = 300 \text{ K}$

$$U_{BE} = -59,5 \text{ mV}$$



Izlazne karakteristike tranzistora

■ Spoj zajedničke baze



$$n_{B0} = n_{0B} \cdot \exp\left(\frac{U_{BE}}{U_T}\right)$$

$$n_{Bw} = n_{0B} \cdot \exp\left(\frac{U_{BC}}{U_T}\right)$$

■ Spoj zajedničkog emitera

