

# Stock-recruitment and reference points

Strategic requirements for sustainable fisheries

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# Expectations

- Be kind
- Make an honest effort to learn
- Share code
  - I share my code with all of you, so please do the same
- This course lies at the intersection of many fields
  - Failure is okay and to be expected

# Disclaimers

1. Reference points are a vast and difficult topic 
2. This is not a mathematical statistics, coding, or assessment modeling course
3. Please ask questions
4. I don't know everything, but will do my best to track down answers
5. When in doubt, see points 1-4

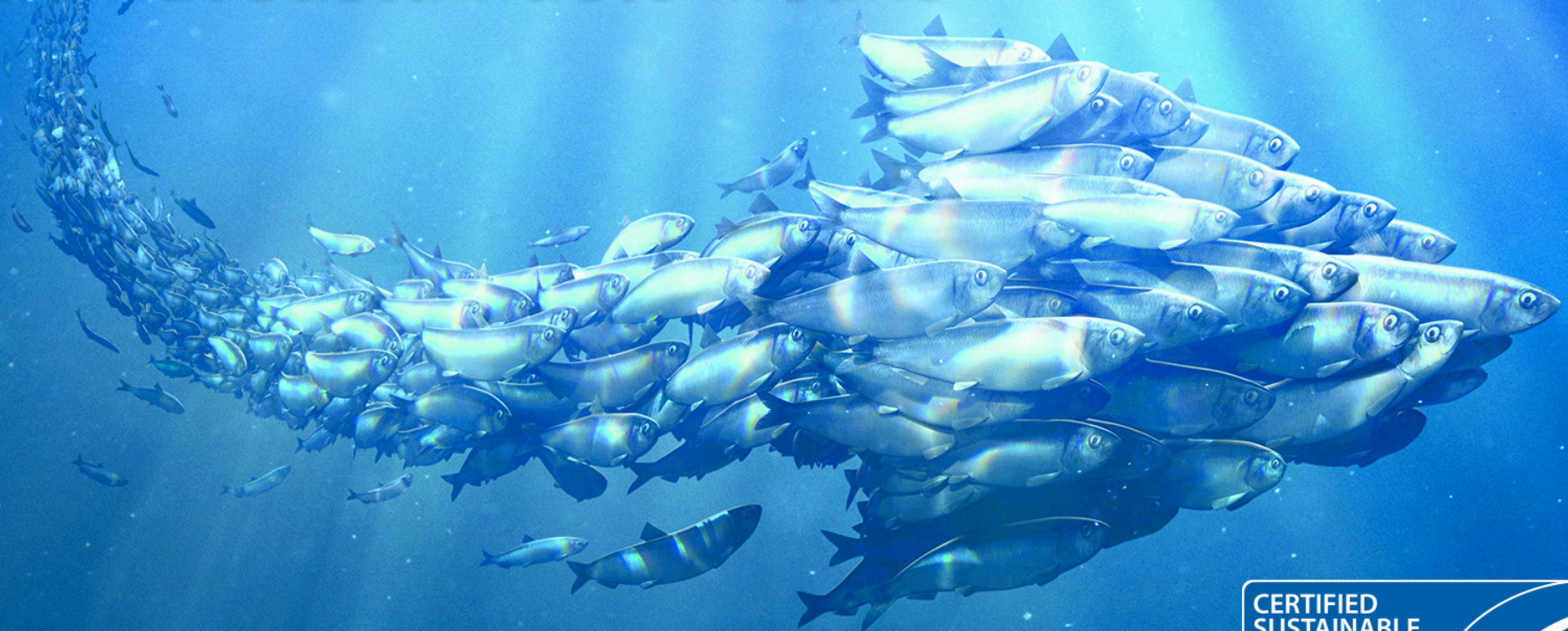
# Objectives

1. To explore how scientists have understood and measured fishing pressure over time
2. To learn the origins and meaning of reference points





Fishing like there's <sup>a</sup>~~no~~ tomorrow  
*That's what sustainable means*



*Look for this label on your seafood*



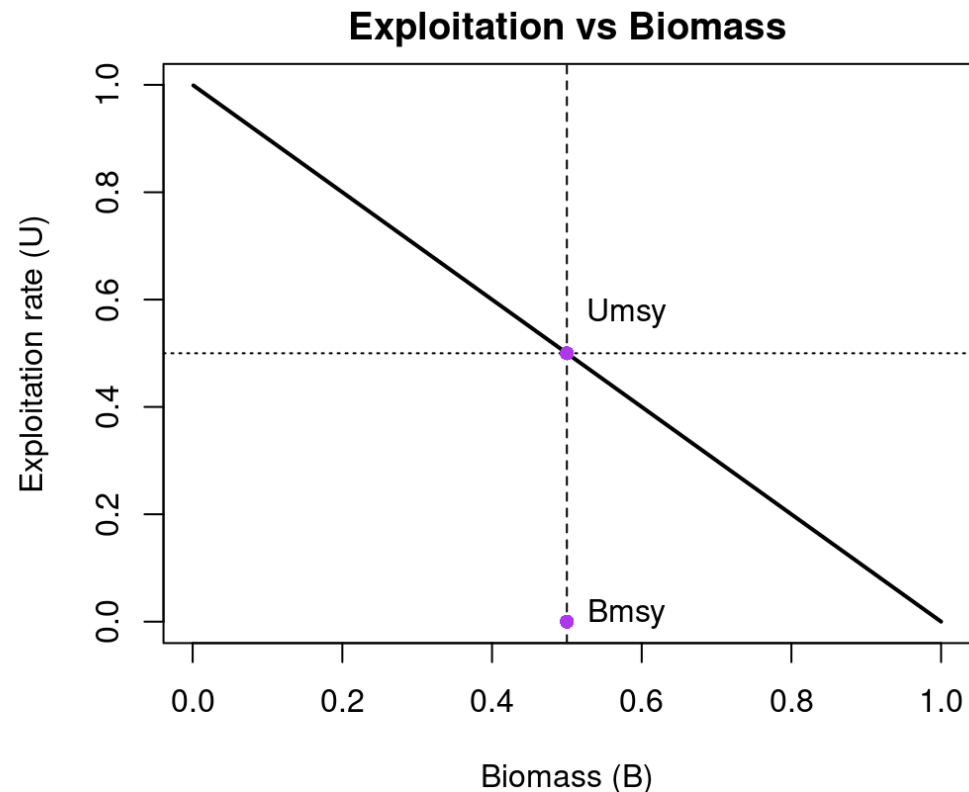
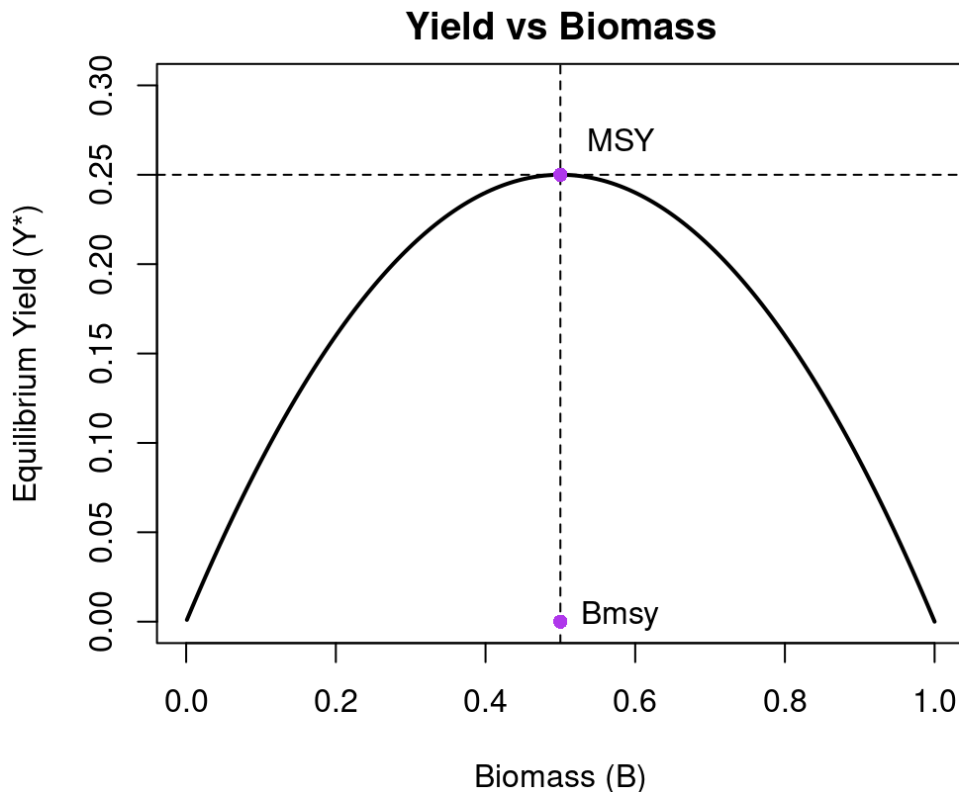


# Goals and objectives of harvest management

- Management strategies for exploited fish stocks depend on goals and objectives to be achieved
  - Few like to explicitly do this
- Conservation concern (in the sense of 'wise-use') suggests that a long-term perspective is necessary, although short term objectives often require attention because of pressure from stakeholders
- In this chunk of the class, we apply recruitment models developed in the first half of the class and extend them to age-structured setting to estimate reference points and feedback policies

# Equilibrium population concepts

- Under average conditions, a fish population produces surplus production each year which can be taken as equilibrium yield  $Y^*$  each year without changing the population's size or biomass ( $B$ )
- The relationship between  $Y^*$  and  $B$  is typically domed:



- Note  $Y^* = U \cdot B$

Schaefer 1954; Beverton and Holt 1957

# Equilibrium population concepts

- This is a Schaefer or logistic population model:

$$Y^* = rB \left( 1 - \frac{B}{K} \right)$$

-  $Y^*$  is equilibrium yield,  $r$  is the intrinsic population growth rate,  $K$  is carrying capacity,  $B$  is biomass

- Purple points represent analytical (mathematical) solutions to the Schaefer model

$$B_{\text{MSY}} = \frac{K}{2}, \quad Y_{\text{MSY}} = \frac{rK}{4}, \quad U_{\text{MSY}} = \frac{r}{2}$$

- Why the hump?
- The Good, the Bad, and the Ugly



# Historical overview of managing fishing mortality: 1950s-1960s

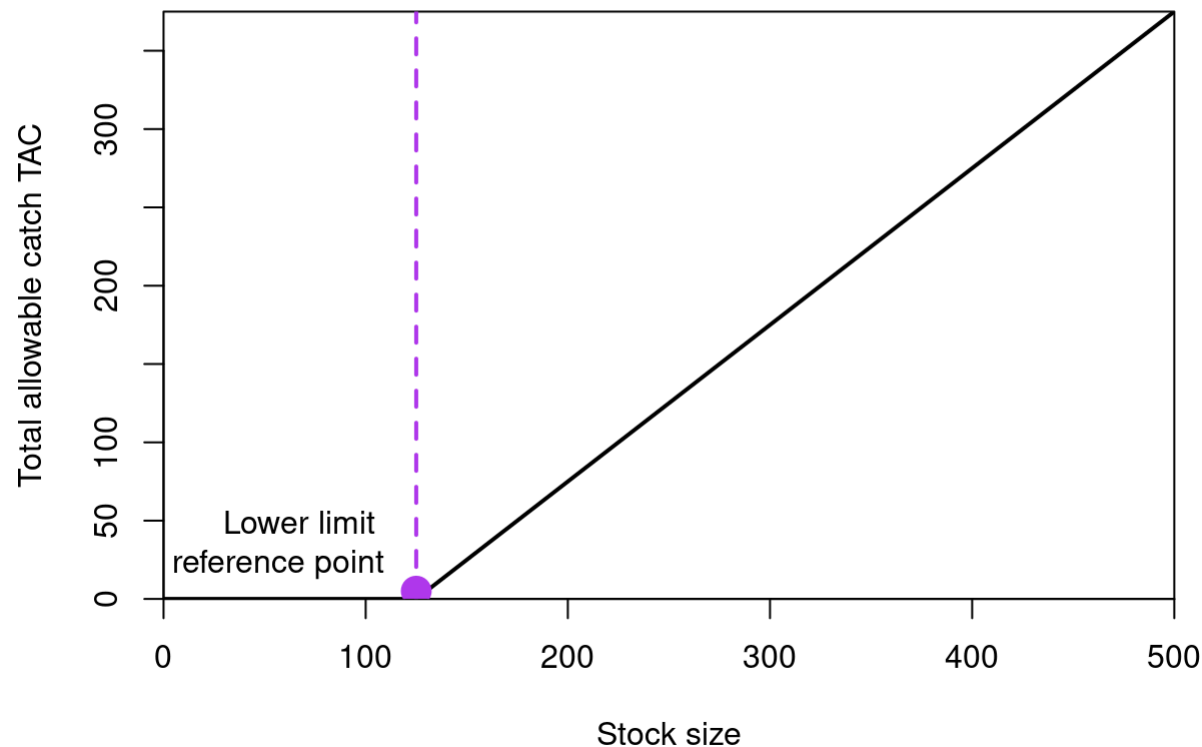
- Surplus production models and approaches to setting quotas were state of the art owing in large part to the mathematical tractability of these models
- Used as a way to reduce acrimonious debate in management meetings as it is very clear that we don't want to be to the left side of the hump on the yield vs. biomass plot (which indicates overfishing)
- A number of theoretical developments happened during this time, and it was noted that harvesting a fixed quota year after year were liable to produce catastrophic and depensatory collapses, while constant fishing rate policies were less likely to result in these issues
- It was suggested that policies might need to be dynamic, or reduce fishing as stock size declined

# Historical overview of managing fishing mortality: 1970s-1980s

- The golden era of harvesting theory, driven by widespread development and use of computers
  - Feedback policy design and the optimality of policies
  - True adaptive management (not just trial and error)
  - The role of stochasticity and recruitment variation
  - Effects of age structure
- Dynamic programming showed that for simple models, optimal management for yield was not a constant quota every year, but rather a *feedback policy* modulating mortality rate as population size changes
  - Difficult to implement, but powerful. Like analytical methods, DP provides a *solution* rather than an *approximation*
  - However, the 'big-n' problem limited applicability to many ecological settings
- Approximation in policy space and other optimization methods proved very powerful for more complicated models, but require explicit objectives
  - These methods search for good policies that achieve some a priori objectives

# Themes from the Golden Era: maximizing yield

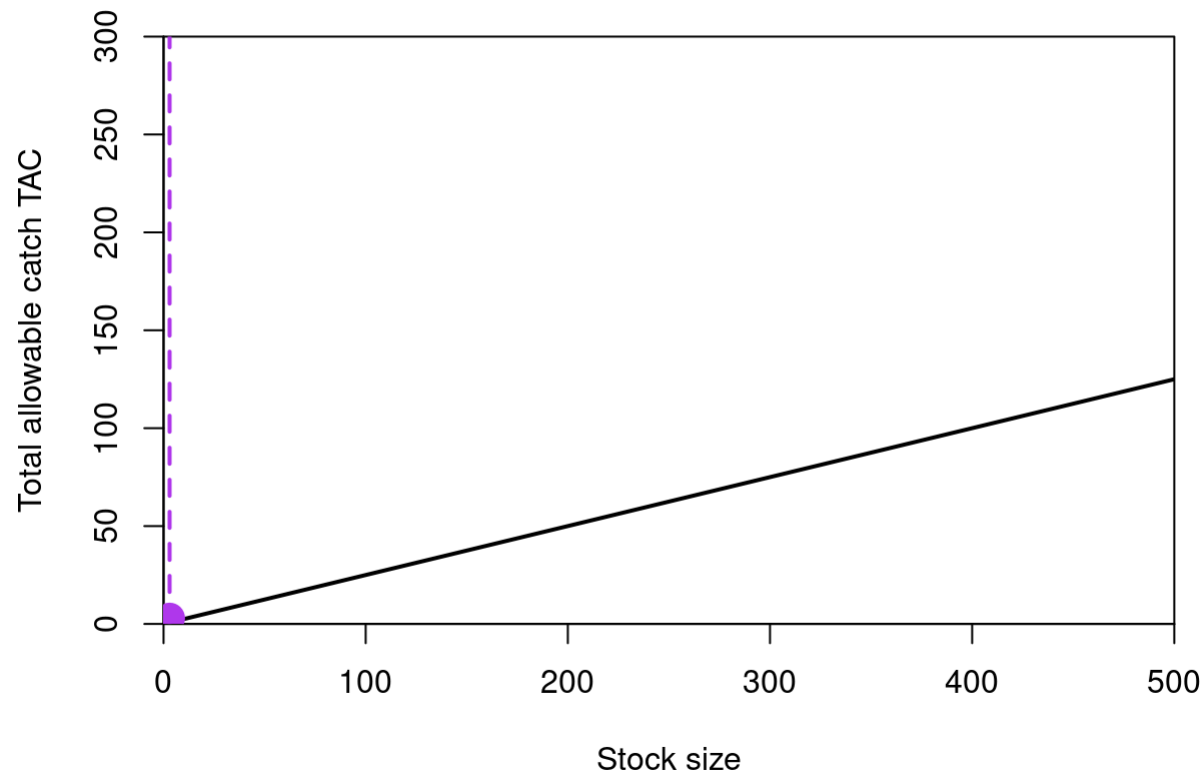
- The optimal yield policy is often a feedback policy of the following form:



This is also called a 'fixed escapement' policy; Walters 1975

# Themes from the Golden Era: risk-averse utility

- The optimal policy that maintains consistency in catch rates over time is the following:



This is a type of 'fixed' or 'constant' F policy; Walters and Parma 1996

# 1970s-1980s cont'd: developments in age-structured models

- Lou Botsford (1981; 1983) derived a mathematical solution to equilibrium recruitment calculations in standard age-structured fish population models
- Botsford incidence functions, which refer to the rate at which events (like spawner biomass or yield) occur per recruit
- Greatly simplified equilibrium and simulation-based calculations in age-structured models



# Reference points: what are they

- Benchmark values used to guide sustainable management
- In their purest form, reference points are different aspects of a model (like the analytical solutions to the surplus production model) or emergent properties of dynamic programming or other analytical or numerical solutions (i.e., lower limit reference points)
- They depend on the model (surplus production MSY is not the same as age-structured model MSY)
- They depend on method (age-structured equilibrium Fmsy is not the same as age-structured simulation based Fmsy)
- Biological reference points, which are those linked specifically to the mathematics of a model, are determinable by an analyst in an objective way (i.e., Fmsy, Bmsy)
  - All others require value judgements, risk thresholds, or policy preferences, which by definition make them subjective

# Reference points: what are they

- Modern understanding of reference points is inextricably linked to feedback or harvest control
- Equilibrium and simulation based reference points are much simpler to compute than feedback policies
- Feedback policies can maximize yield or risk-averse utility (or anything) and very powerful
  - Feedback policy remain state of the art for harvest management

# Historical overview of managing fishing mortality: 1990s-present

- A number of notable fisheries declines and collapses (e.g., Atlantic cod) led to widespread shifts in federal legislation such as updates to the Magnuson-Stevens Act (1996, 2006), Canada's Precautionary Approach, and the ICES Precautionary Approach in Europe
- This legislation often advocates the 'precautionary-approach' to fisheries management, which among other things often specifies a specific harvest control rule form (i.e., feedback policy)
- Modern variations on simple feedback policies can be quite complex relationships between fishing rate and stock size, and are used by many agencies to define targets and reference points for management
- Examples of these types of policies in Great Lakes or your specific systems?



① Limit Reference Point

② Upper Stock Reference

③ Removal Reference

④ Target Reference Point

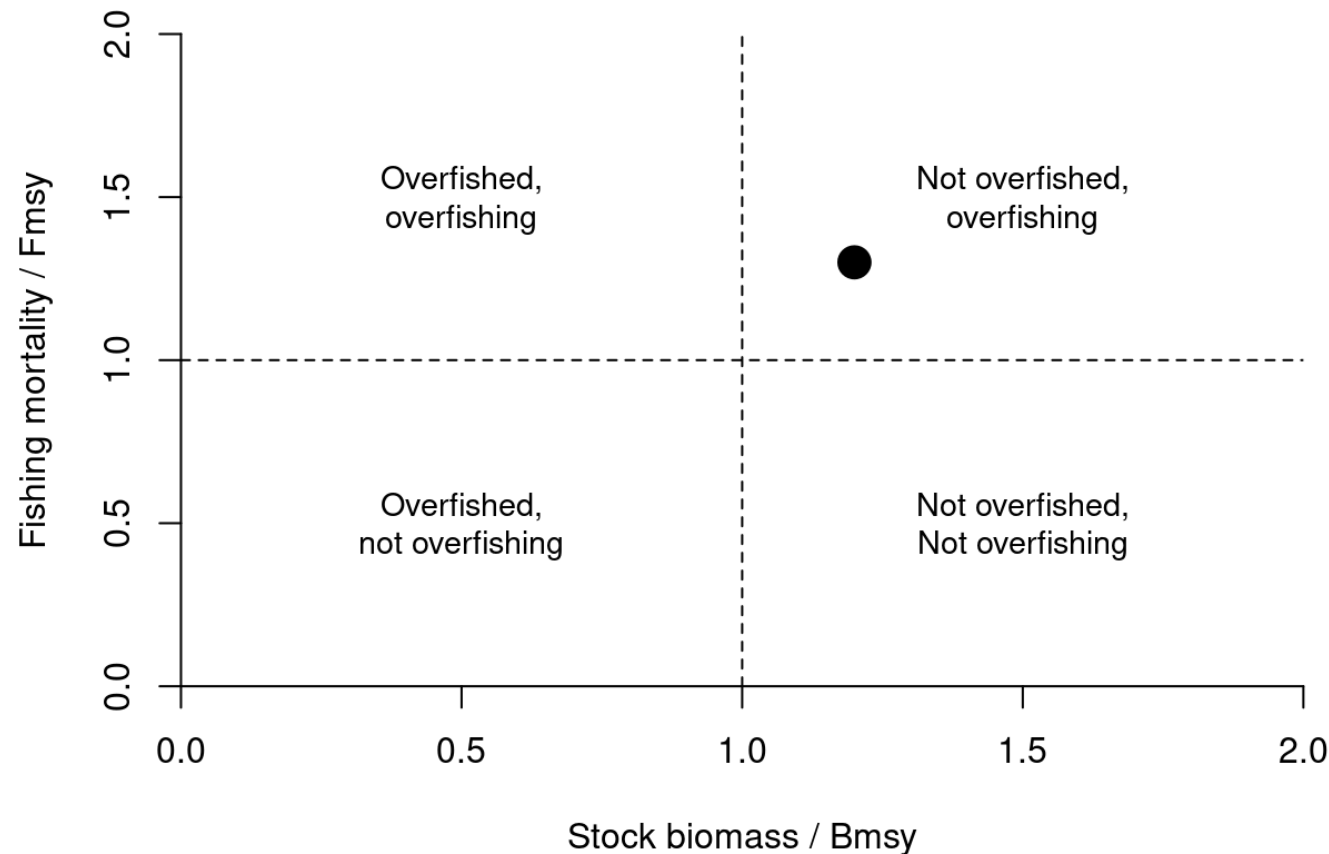
An example of a “precautionary” harvest control rule; DFO 2009

# Communicating status: Kobe plots

- First joint meeting of the tuna regional fisheries management organization, held in Kobe, Japan
- Ray Hilborn noted that stock status and assessment results could be categorized with a four quadrant plot relating current mortality rates and biomass estimates to reference points
- The point: reference points are useful for conveying stock status and are now used worldwide as a standard tool

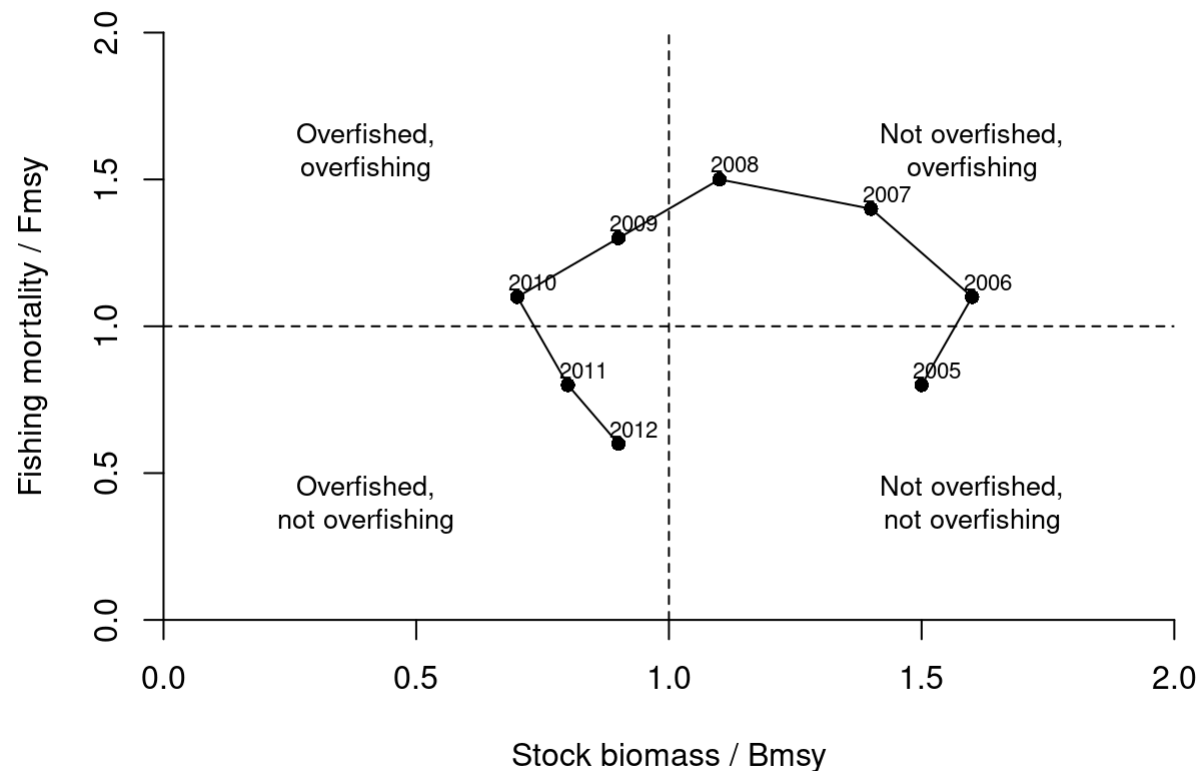


# Communicating sustainability status: Kobe plots

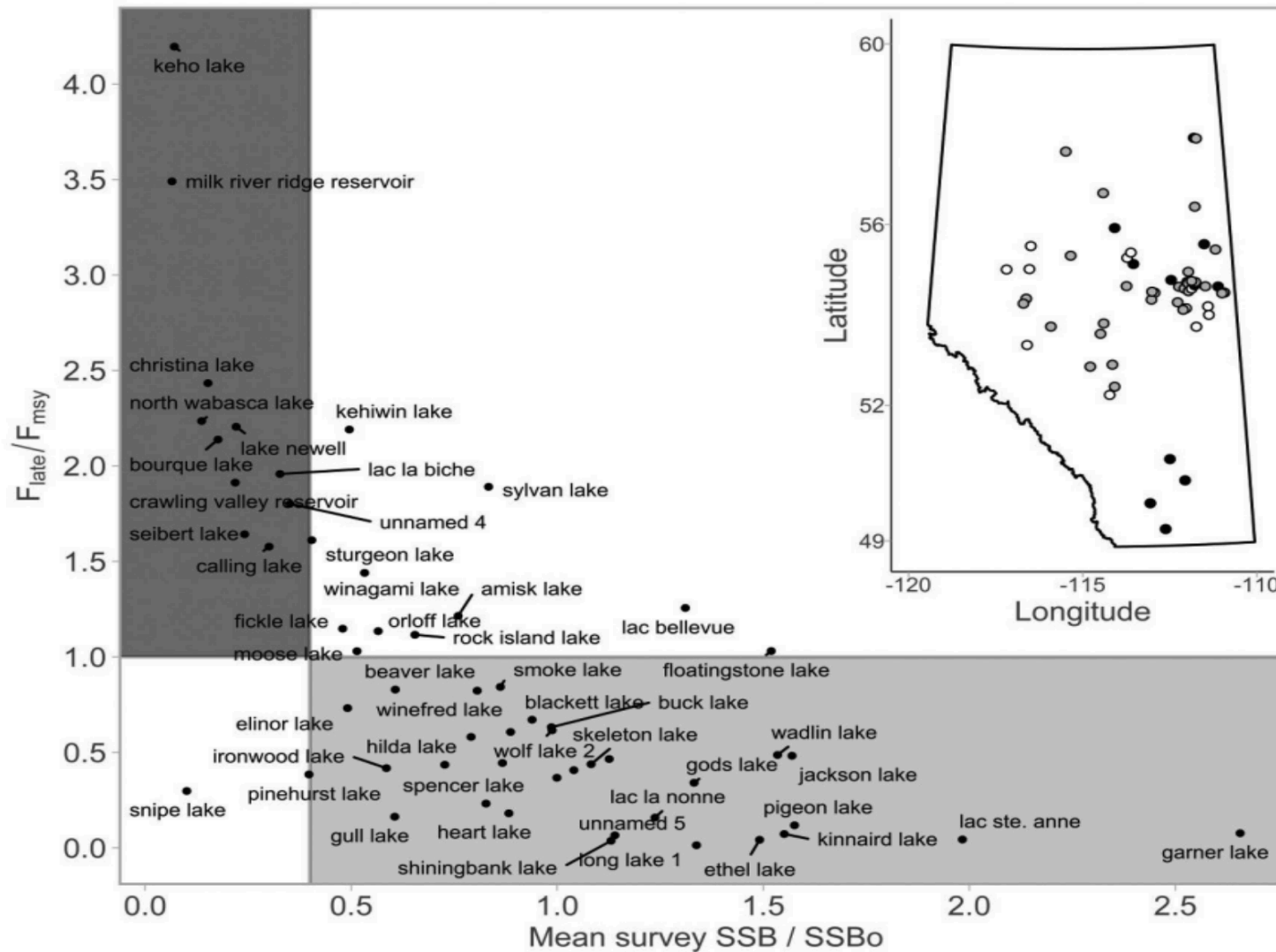


# Communicating sustainability status: Kobe plots

- Evolving status through time

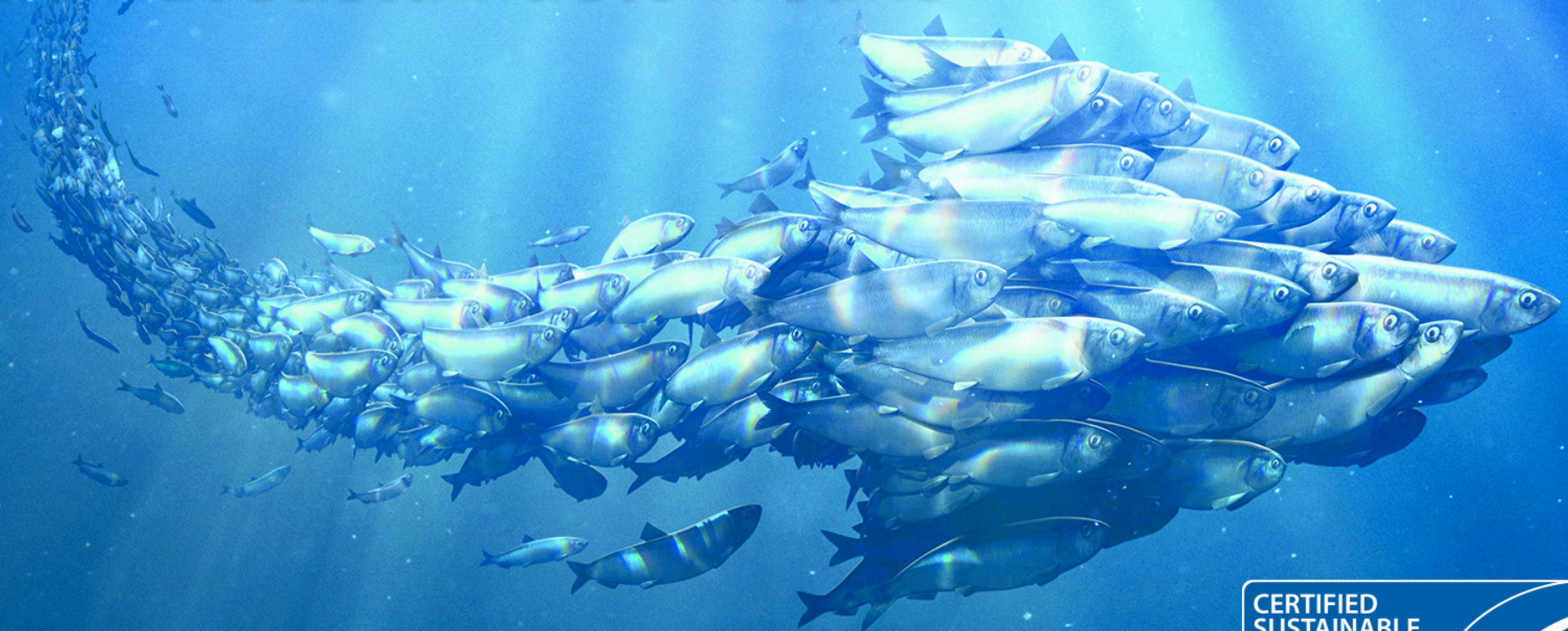


# Kobe plots in inland fisheries





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# Summary

- Sustainability assessments typically require the determination of one or more reference points
- Feedback policies difficult to compute but very powerful and provide much of the theoretical foundation for sustainable harvesting in dynamic environments
- Biological reference points are objective benchmarks derived from models, used to guide sustainable management decisions
- Many modern harvest control rules (i.e., feedback policies) such as those recommended by NOAA or DFO require these types of reference points as inputs
  - Most of the class is about calculating these types of reference points
- Group discussion about harvest management practices in the Great Lakes region



# Road map for the next few lectures

- Mathematical foundations and the ecological basis of sustainable harvesting
- Calculating equilibrium  $F_{msy}/MSY$  for an age-structured model
- Calculating simulation based  $F_{msy}/MSY$  for an age-structured model
- The omniscient fishery manager and maximizing yield vs. risk-averse utility
- Approximation of feedback in policy space

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