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9/15

lecture 6, Exercise A

1a.

2. If  $G$  Abelian, then

$$hg = gh \quad \forall g, h \in G$$

$$\text{So } Z(G) = \{g \in G \mid gh = hg \quad \forall h \in G\} \\ = G$$

$$C_G(A) = \{g \in G \mid ga = ag \quad \forall a \in A\}$$

We know every  $g \in G$  commutes  
with every  $h \in G$ , and we  
know  $A \subseteq G$ , so  $g$  commutes  
with every element of  $A$ .

$$\text{So } C_G(A) = G$$

$$N_G(A) = \{g \in G \mid gA = Ag\}$$

Note  $ga = ag \quad \forall g \in G, a \in A$

So  $gA = Ag \quad \forall g \in G$

So  $N_G(A) = G$