

Introduction to Transformers

Transformers

LLMs are built out of transformers

Transformer: a specific kind of network architecture, like a fancier feedforward network, but based on attention

Attention Is All You Need

Ashish Vaswani*

Google Brain

avaswani@google.com

Noam Shazeer*

Google Brain

noam@google.com

Niki Parmar*

Google Research

nikip@google.com

Jakob Uszkoreit*

Google Research

usz@google.com

Llion Jones*

Google Research

llion@google.com

Aidan N. Gomez* †

University of Toronto

aidan@cs.toronto.edu

Łukasz Kaiser*

Google Brain

lukaszkaiser@google.com

Illia Polosukhin* ‡

illia.polosukhin@gmail.com

A very approximate timeline

1990 Static Word Embeddings

2003 Neural Language Model

2008 Multi-Task Learning

2015 Attention

2017 Transformer

2018 Contextual Word Embeddings and Pretraining

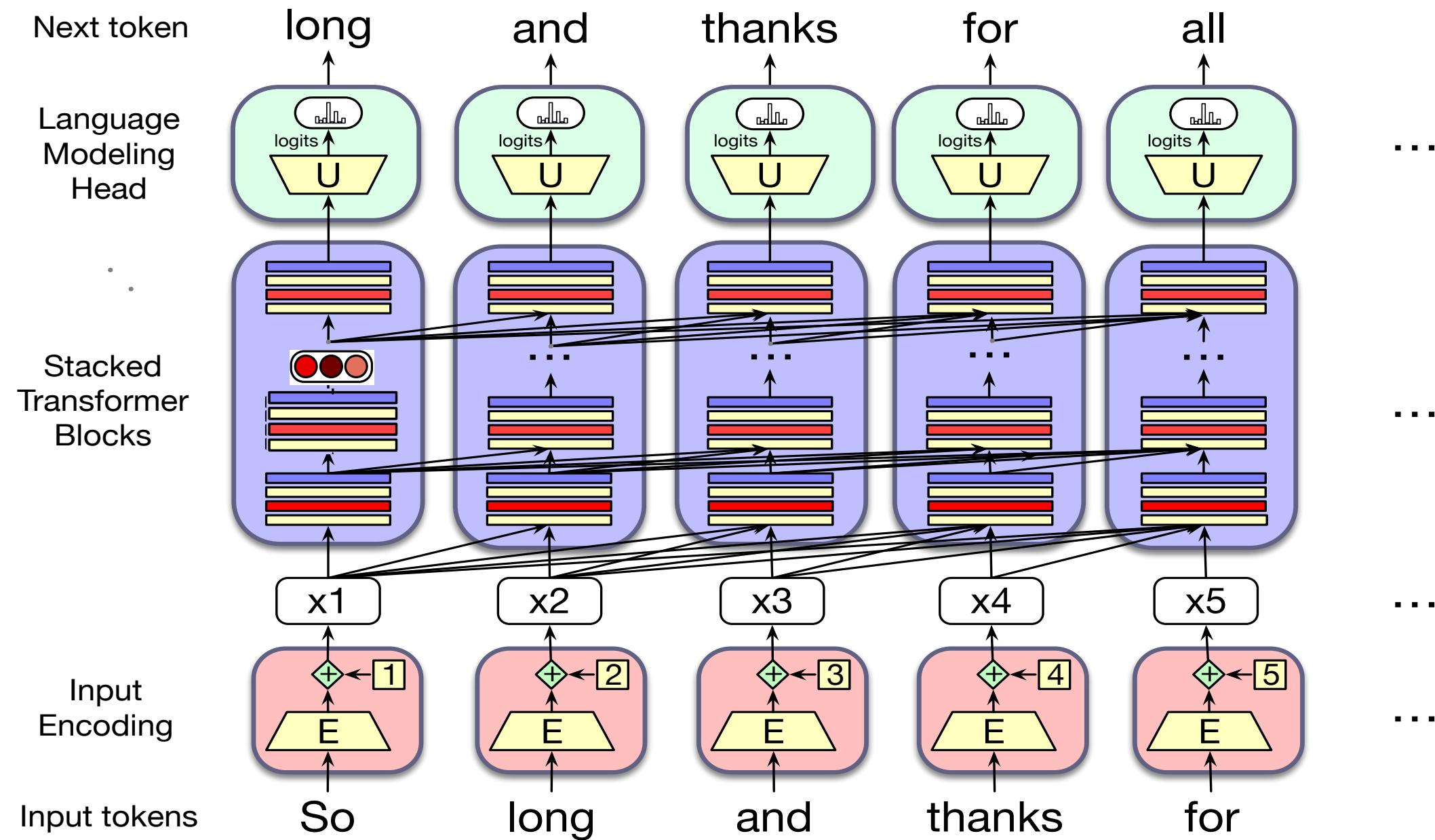
2019 Prompting

Attention

Transformers

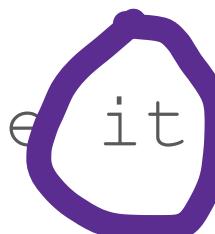
Instead of starting with the big picture

Let's consider the embeddings for an individual word from a particular layer



Problem with static embeddings (word2vec)

They are static! The embedding for a word doesn't reflect how its meaning changes in context.

The chicken didn't cross the road because  it was too tired

What is the meaning represented in the static embedding for "it"?

Contextual Embeddings

- Intuition: a representation of meaning of a word should be different in different contexts!
- **Contextual Embedding:** each word has a different vector that expresses different meanings depending on the surrounding words
- How to compute contextual embeddings?
 - **Attention**

Contextual Embeddings

The chicken didn't cross the road because it

What should be the properties of "it"?

The chicken didn't cross the road because it was too **tired**

The chicken didn't cross the road because it was too **wide**

At this point in the sentence, it's probably referring to either the chicken or the street

Intuition of attention

Build up the contextual embedding from a word by selectively integrating information from all the neighboring words

We say that a word "attends to" some neighboring words more than others

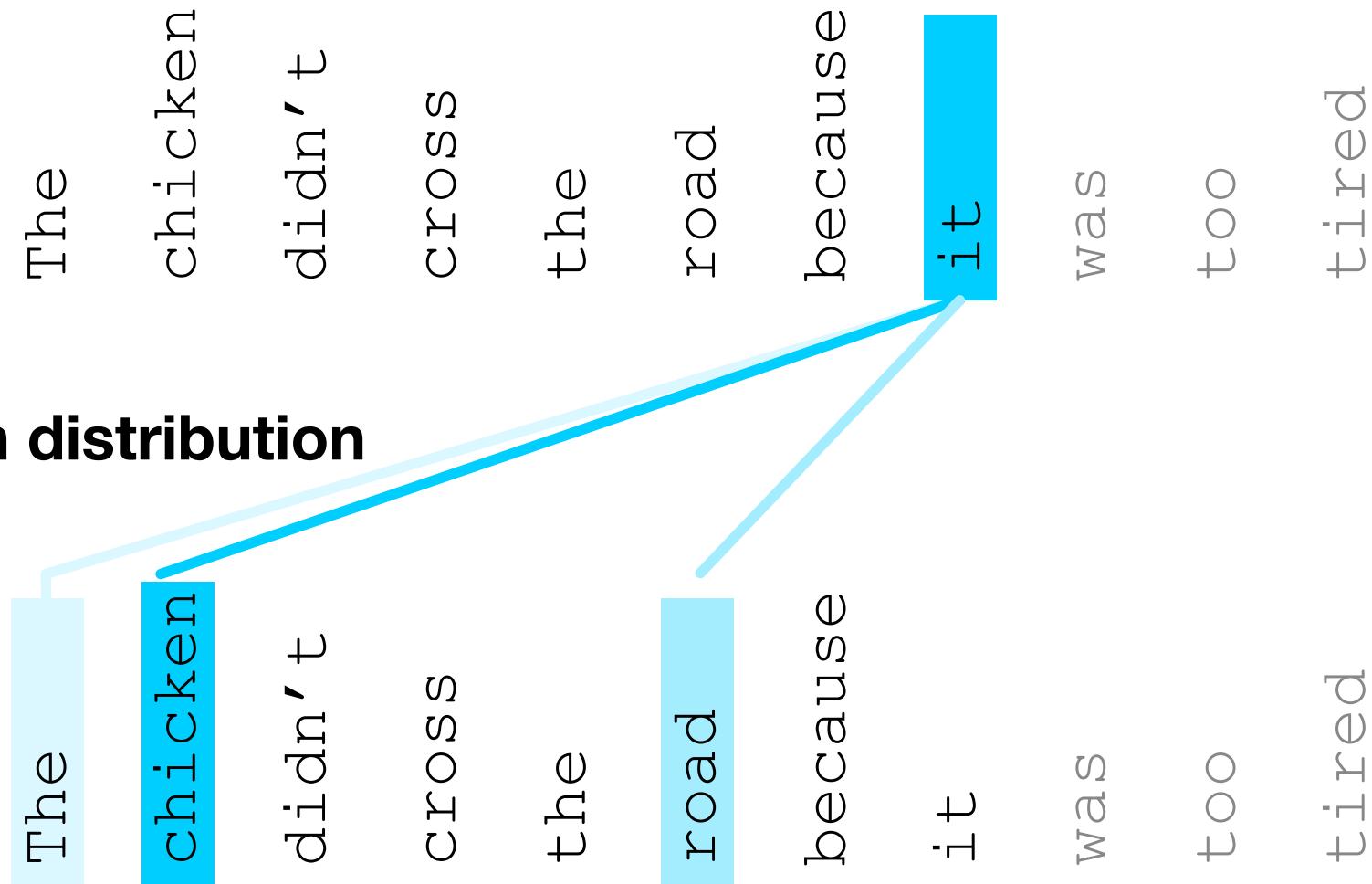
Intuition of attention:

columns corresponding to input tokens

Layer $k+1$

self-attention distribution

Layer k

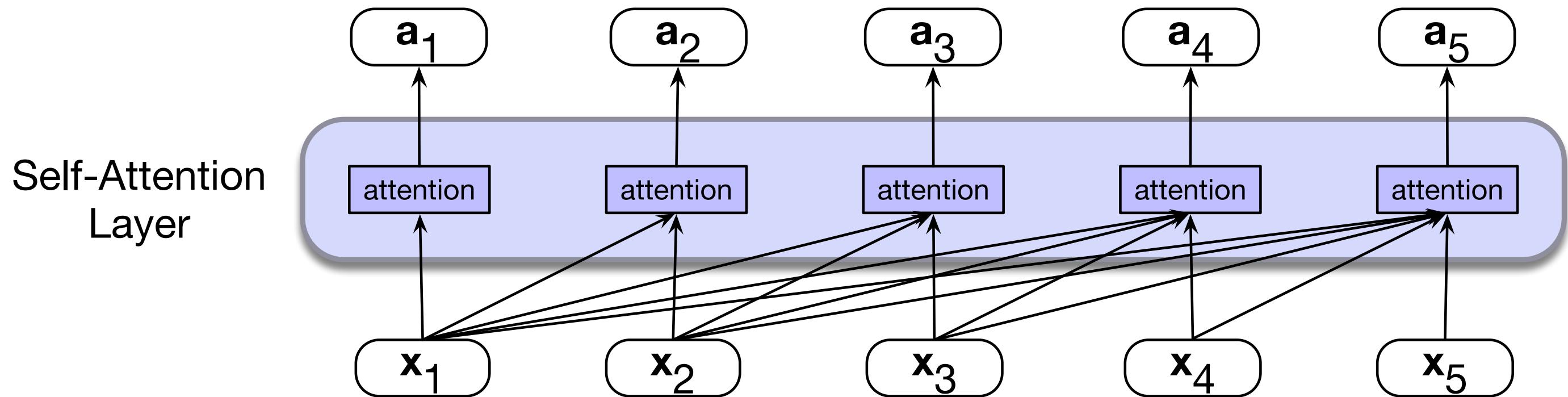


Attention definition

A mechanism for helping compute the embedding for a token by selectively attending to and integrating information from surrounding tokens (at the previous layer).

More formally: a method for doing a weighted sum of vectors.

Attention is left-to-right



Simplified version of attention: a sum of prior words weighted by their similarity with the current word

Given a sequence of token embeddings:

$$\mathbf{x}_1 \quad \mathbf{x}_2 \quad \mathbf{x}_3 \quad \mathbf{x}_4 \quad \mathbf{x}_5 \quad \mathbf{x}_6 \quad \mathbf{x}_7 \quad \mathbf{x}_i$$

Produce: $\mathbf{a}_i =$ a weighted sum of \mathbf{x}_1 through \mathbf{x}_7 (and \mathbf{x}_i)
Weighted by their similarity to \mathbf{x}_i

$$\text{score}(\mathbf{x}_i, \mathbf{x}_j) = \mathbf{x}_i \cdot \mathbf{x}_j$$

$$\alpha_{ij} = \text{softmax}(\text{score}(\mathbf{x}_i, \mathbf{x}_j)) \quad \forall j \leq i$$

$$\mathbf{a}_i = \sum_{j \leq i} \alpha_{ij} \mathbf{x}_j$$

Intuition of attention:

columns corresponding to input tokens

Layer $k+1$

The chicken didn't cross the road because it was too tired

self-attention distribution

Layer k

The

chicken

didn't

cross

the

road

because

it

was

too

tired

$x_1 \ x_2 \ x_3 \ x_4 \ x_5 \ x_6 \ x_7 \ x_i$

An Actual Attention Head: slightly more complicated

High-level idea: instead of using vectors (like x_i and x_4) directly, we'll represent 3 separate roles each vector x_i plays:

- **query**: As *the current element* being compared to the preceding inputs.
- **key**: as *a preceding input* that is being compared to the current element to determine a similarity
- **value**: a value of a preceding element that gets weighted and summed

Attention intuition

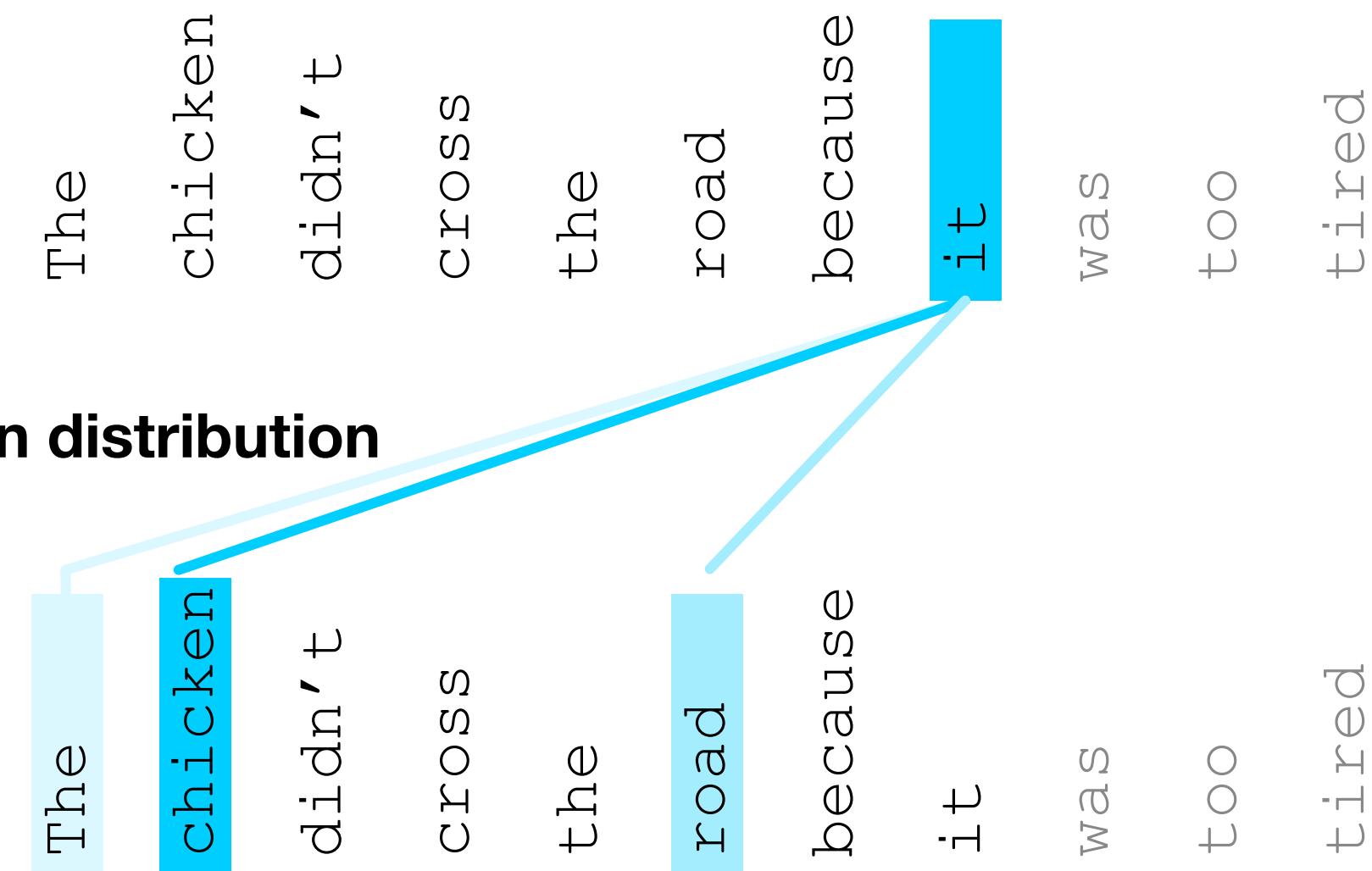
Layer $k+1$

self-attention distribution

Layer k

$x_1 \ x_2 \ x_3 \ x_4 \ x_5 \ x_6 \ x_7 \ x_i$

values



query

Intuition of attention:

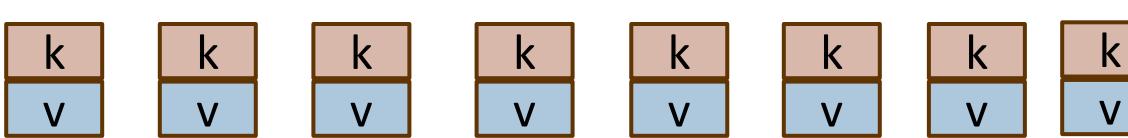
Layer $k+1$

The chicken didn't cross the road because it was too tired

query

self-attention distribution

Layer k



*keys
values*

$x_1 \quad x_2 \quad x_3 \quad x_4 \quad x_5 \quad x_6 \quad x_7 \quad x_i$

An Actual Attention Head: slightly more complicated

We'll use matrices to project each vector \mathbf{x}_i into a representation of its role as query, key, value:

- **query: \mathbf{W}^Q**
- **key: \mathbf{W}^K**
- **value: \mathbf{W}^V**

$$\mathbf{q}_i = \mathbf{x}_i \mathbf{W}^Q; \quad \mathbf{k}_i = \mathbf{x}_i \mathbf{W}^K; \quad \mathbf{v}_i = \mathbf{x}_i \mathbf{W}^V$$

An Actual Attention Head: slightly more complicated

Given these 3 representation of \mathbf{x}_i

$$\mathbf{q}_i = \mathbf{x}_i \mathbf{W}^Q; \quad \mathbf{k}_i = \mathbf{x}_i \mathbf{W}^K; \quad \mathbf{v}_i = \mathbf{x}_i \mathbf{W}^V$$

To compute similarity of current element \mathbf{x}_i with some prior element \mathbf{x}_j

We'll use dot product between \mathbf{q}_i and \mathbf{k}_j .

And instead of summing up \mathbf{x}_j , we'll sum up \mathbf{v}_j

Final equations for one attention head

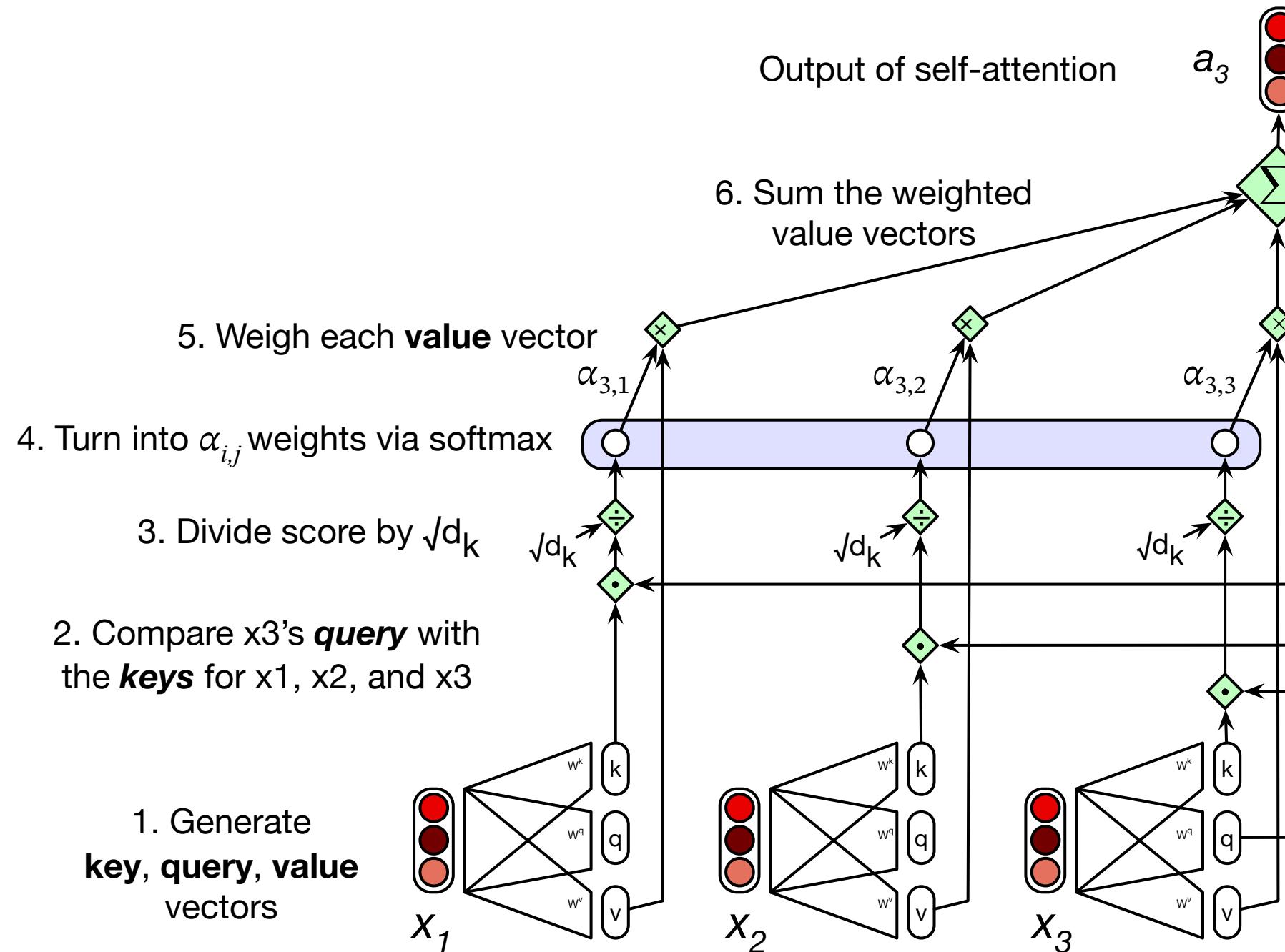
$$\mathbf{q}_i = \mathbf{x}_i \mathbf{W}^Q; \quad \mathbf{k}_j = \mathbf{x}_j \mathbf{W}^K; \quad \mathbf{v}_j = \mathbf{x}_j \mathbf{W}^V$$

$$\text{score}(\mathbf{x}_i, \mathbf{x}_j) = \frac{\mathbf{q}_i \cdot \mathbf{k}_j}{\sqrt{d_k}}$$

$$\alpha_{ij} = \text{softmax}(\text{score}(\mathbf{x}_i, \mathbf{x}_j)) \quad \forall j \leq i$$

$$\mathbf{a}_i = \sum_{j \leq i} \alpha_{ij} \mathbf{v}_j$$

Calculating the value of a_3



Actual Attention: slightly more complicated

- Instead of one attention head, we'll have lots of them!
- Intuition: each head might be attending to the context for different purposes
 - Different linguistic relationships or patterns in the context

$$\mathbf{q}_i^c = \mathbf{x}_i \mathbf{W}^{Qc}; \quad \mathbf{k}_j^c = \mathbf{x}_j \mathbf{W}^{Kc}; \quad \mathbf{v}_j^c = \mathbf{x}_j \mathbf{W}^{Vc}; \quad \forall c \quad 1 \leq c \leq h$$

$$\text{score}^c(\mathbf{x}_i, \mathbf{x}_j) = \frac{\mathbf{q}_i^c \cdot \mathbf{k}_j^c}{\sqrt{d_k}}$$

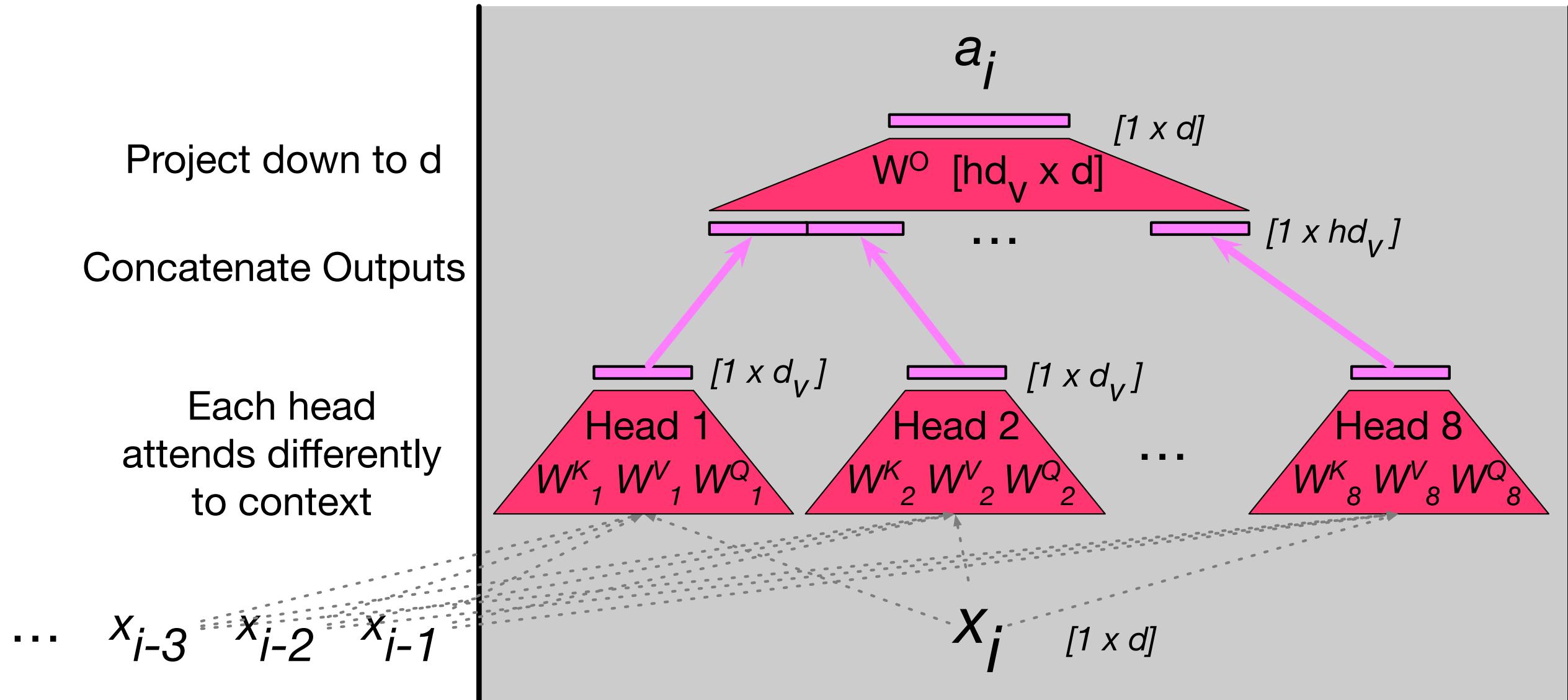
$$\alpha_{ij}^c = \text{softmax}(\text{score}^c(\mathbf{x}_i, \mathbf{x}_j)) \quad \forall j \leq i$$

$$\mathbf{head}_i^c = \sum_{j \leq i} \alpha_{ij}^c \mathbf{v}_j^c$$

$$\mathbf{a}_i = (\mathbf{head}^1 \oplus \mathbf{head}^2 \dots \oplus \mathbf{head}^h) \mathbf{W}^O$$

$$\text{MultiHeadAttention}(\mathbf{x}_i, [\mathbf{x}_1, \dots, \mathbf{x}_N]) = \mathbf{a}_i$$

Multi-head attention



Summary

Attention is a method for enriching the representation of a token by incorporating contextual information

The result: the embedding for each word will be different in different contexts!

Contextual embeddings: a representation of word meaning in its context.

We'll see in the next lecture that attention can also be viewed as a way to move information from one token to another.

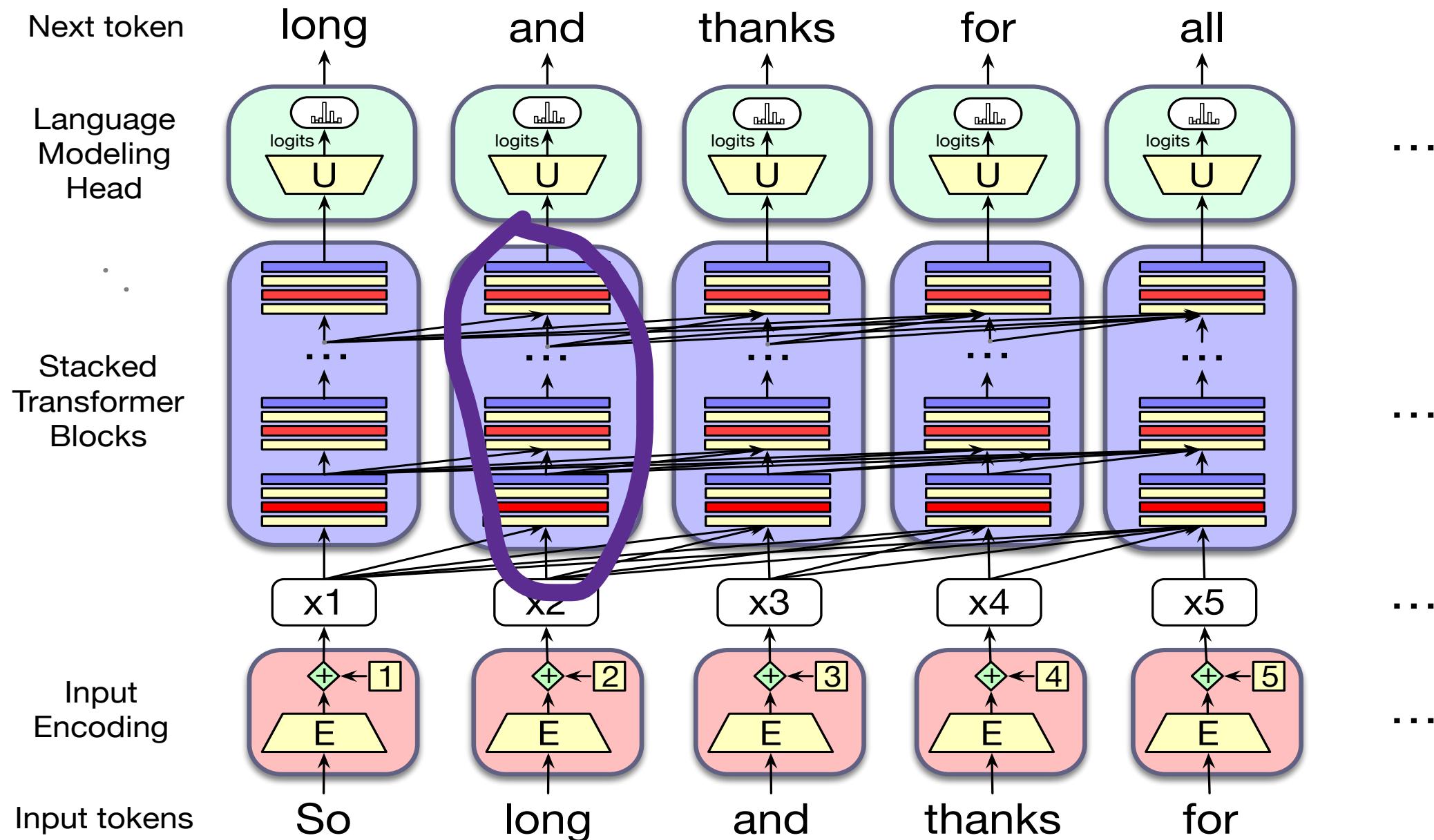
Attention

Transformers

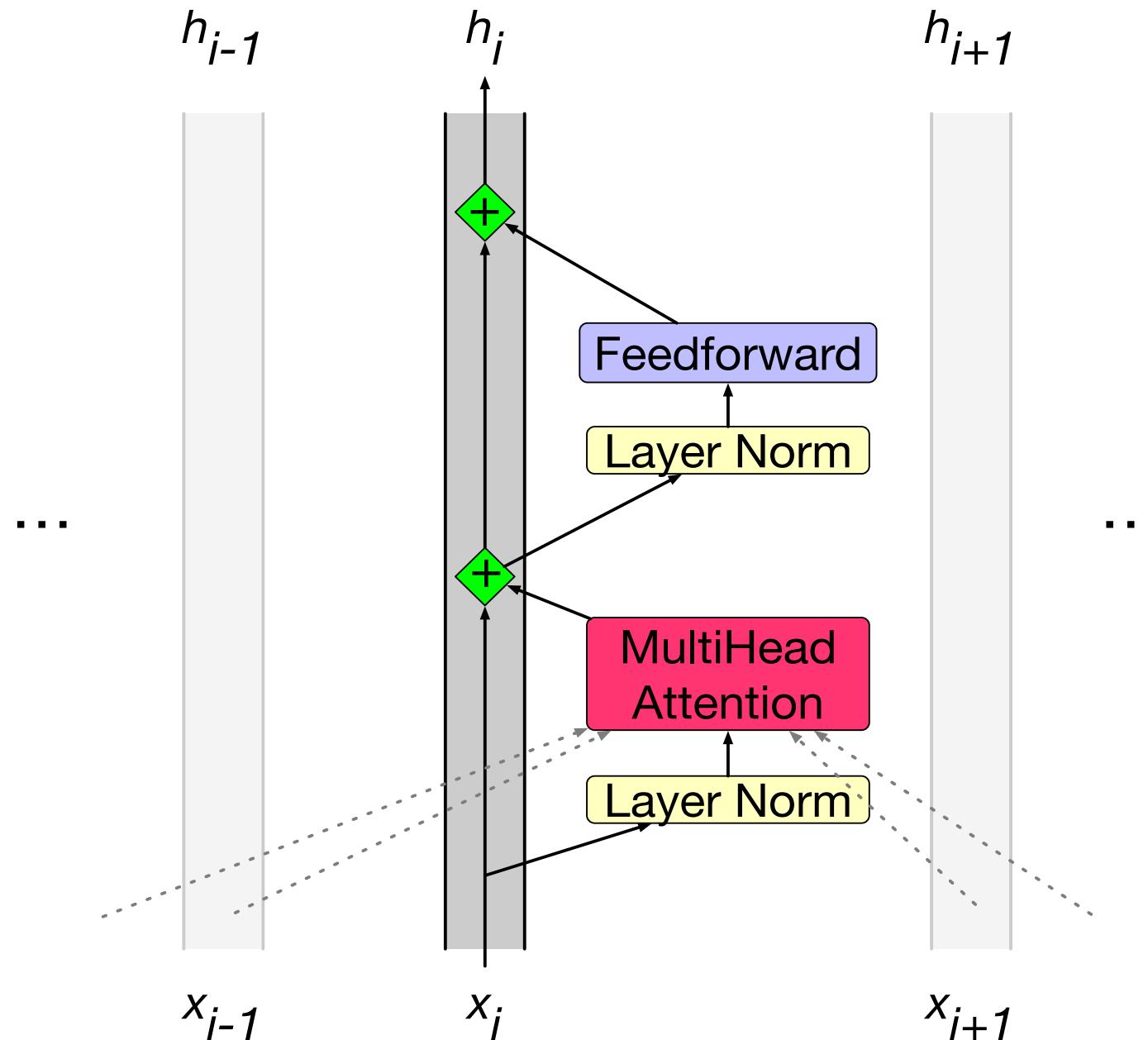
The Transformer Block

Transformers

Reminder: transformer language model

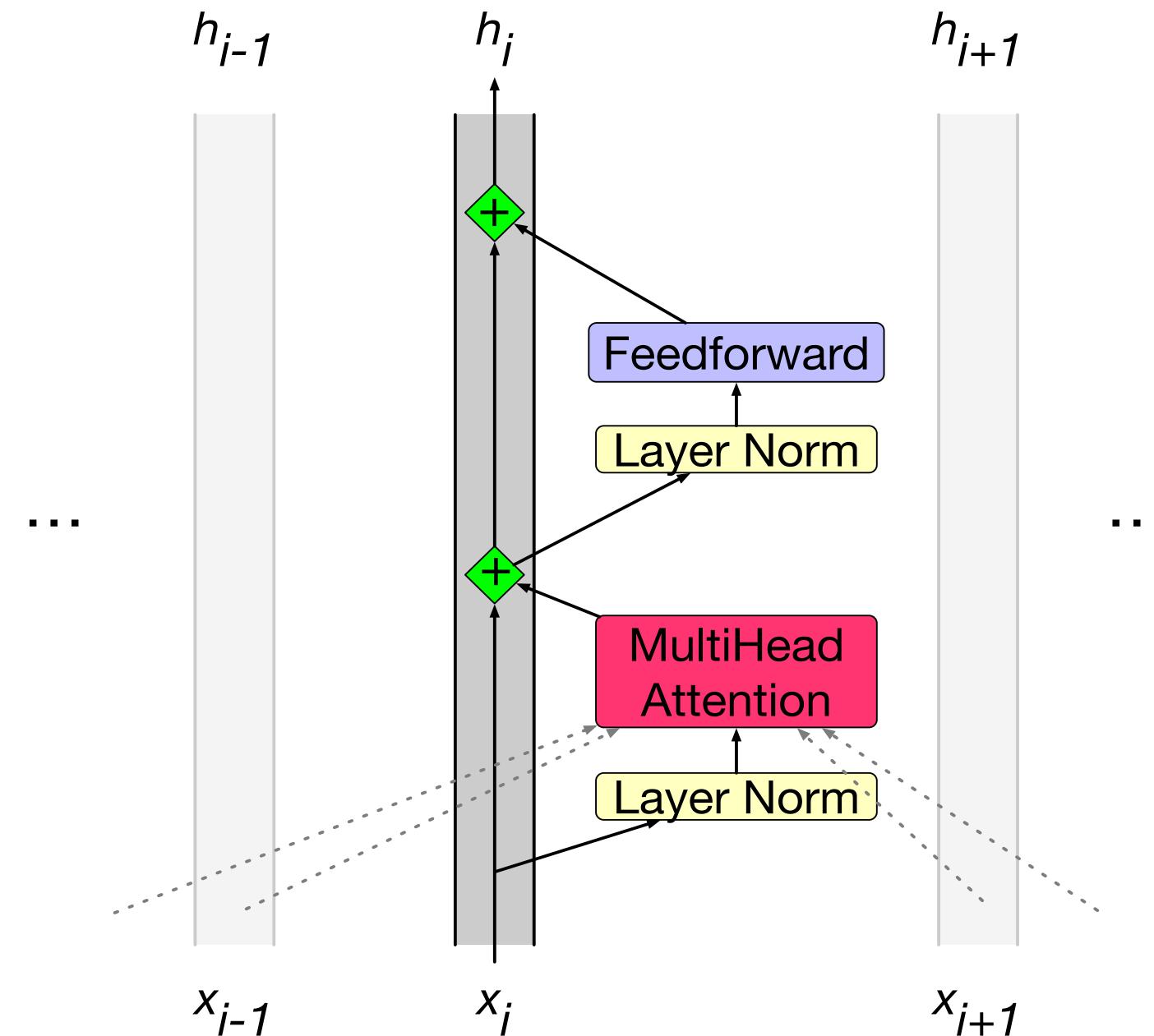


The residual stream: each token gets passed up and modified

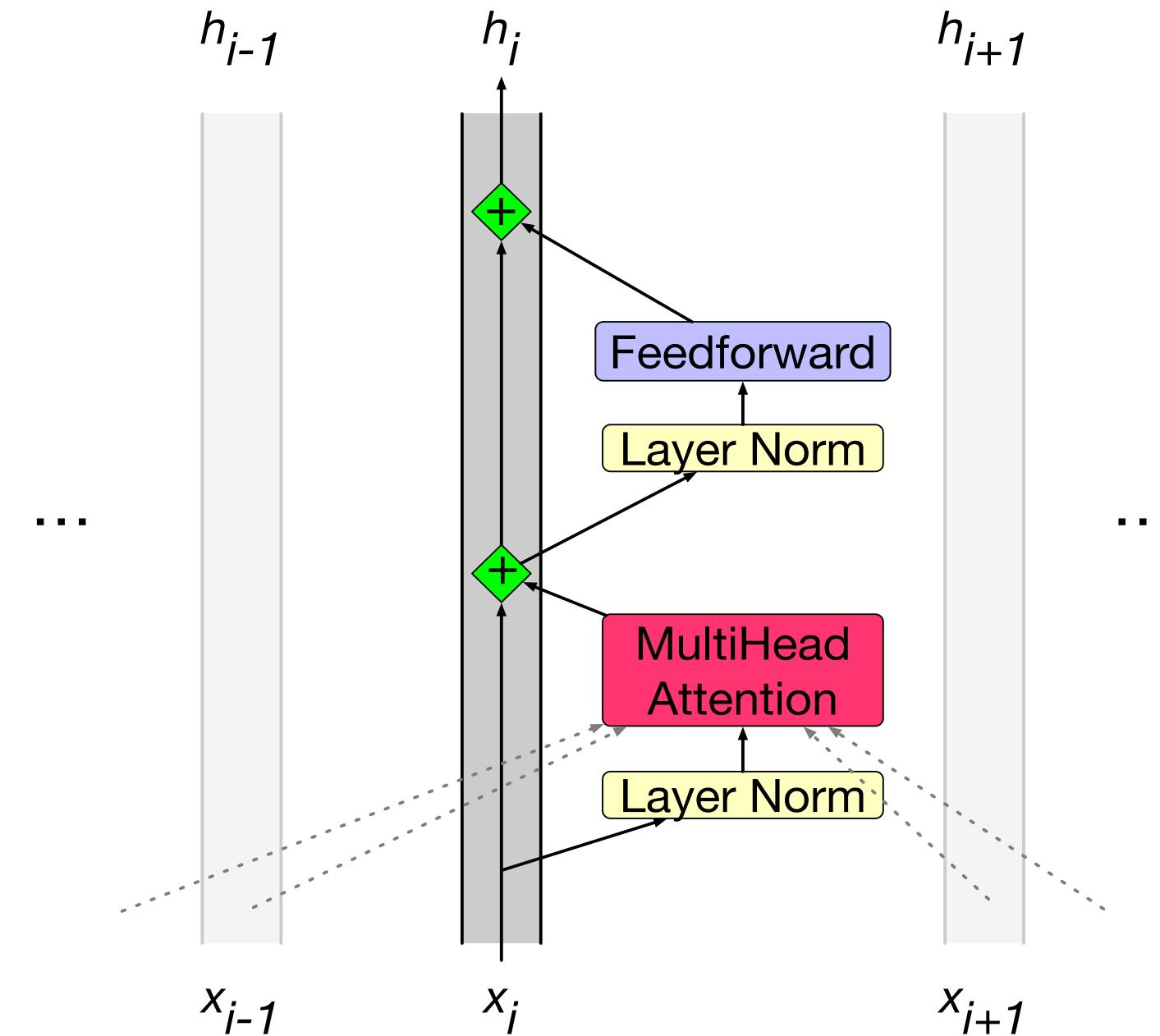


We'll need nonlinearities, so a feedforward layer

$$\text{FFN}(\mathbf{x}_i) = \text{ReLU}(\mathbf{x}_i \mathbf{W}_1 + b_1) \mathbf{W}_2 + b_2$$



Layer norm: the vector x_i is normalized twice



Layer Norm

Layer norm is a variation of the z-score from statistics, applied to a single vector in a hidden layer

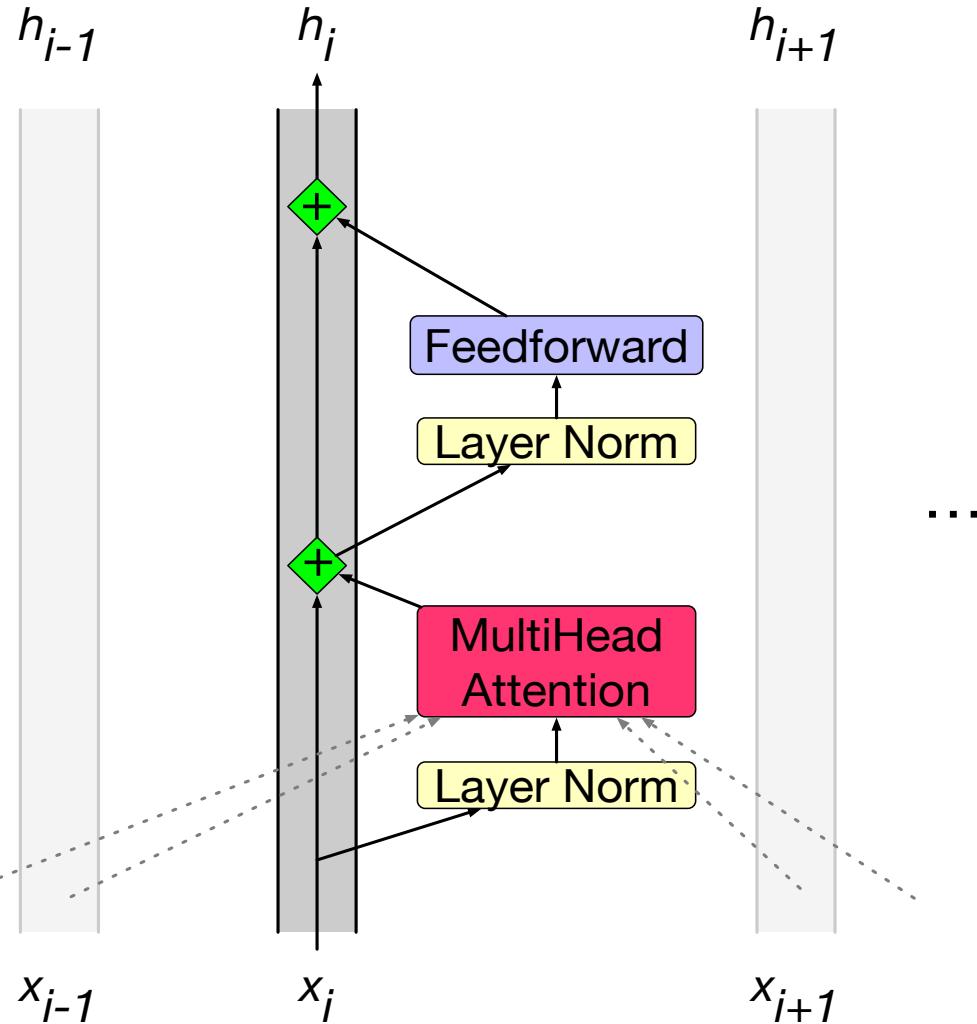
$$\mu = \frac{1}{d} \sum_{i=1}^d x_i$$

$$\sigma = \sqrt{\frac{1}{d} \sum_{i=1}^d (x_i - \mu)^2}$$

$$\hat{\mathbf{x}} = \frac{(\mathbf{x} - \mu)}{\sigma}$$

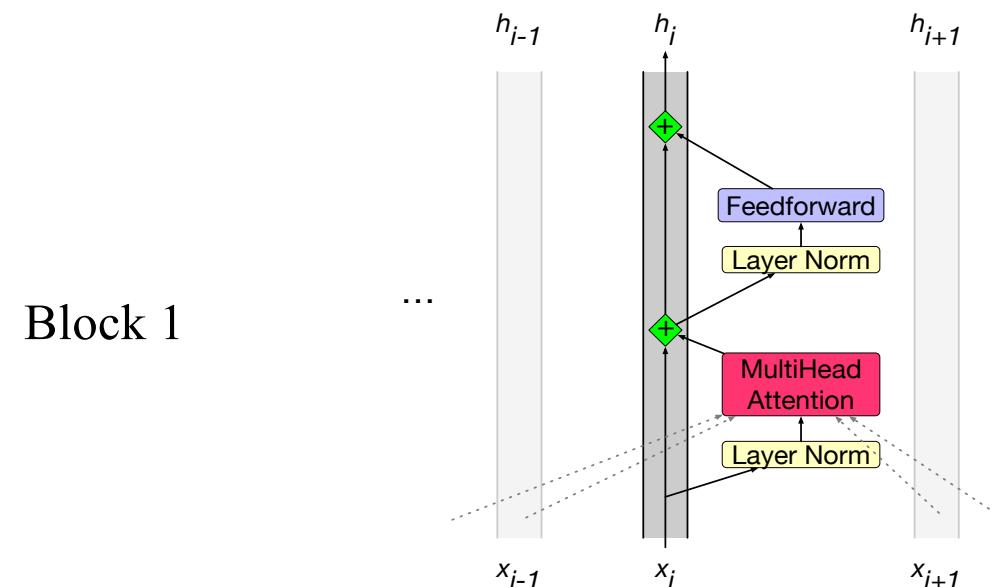
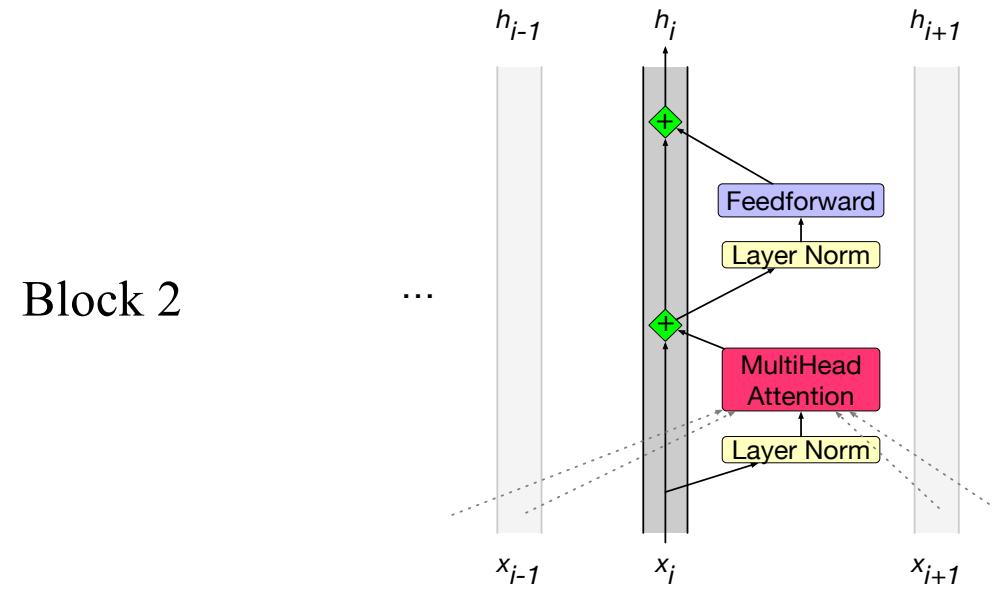
$$\text{LayerNorm}(\mathbf{x}) = \gamma \frac{(\mathbf{x} - \mu)}{\sigma} + \beta$$

Putting together a single transformer block



$$\begin{aligned}\mathbf{t}_i^1 &= \text{LayerNorm}(\mathbf{x}_i) \\ \mathbf{t}_i^2 &= \text{MultiHeadAttention}(\mathbf{t}_i^1, [\mathbf{x}_1^1, \dots, \mathbf{x}_N^1]) \\ \mathbf{t}_i^3 &= \mathbf{t}_i^2 + \mathbf{x}_i \\ \mathbf{t}_i^4 &= \text{LayerNorm}(\mathbf{t}_i^3) \\ \mathbf{t}_i^5 &= \text{FFN}(\mathbf{t}_i^4) \\ \mathbf{h}_i &= \mathbf{t}_i^5 + \mathbf{t}_i^3\end{aligned}$$

A transformer is a stack of these blocks
so all the vectors are of the same dimensionality d

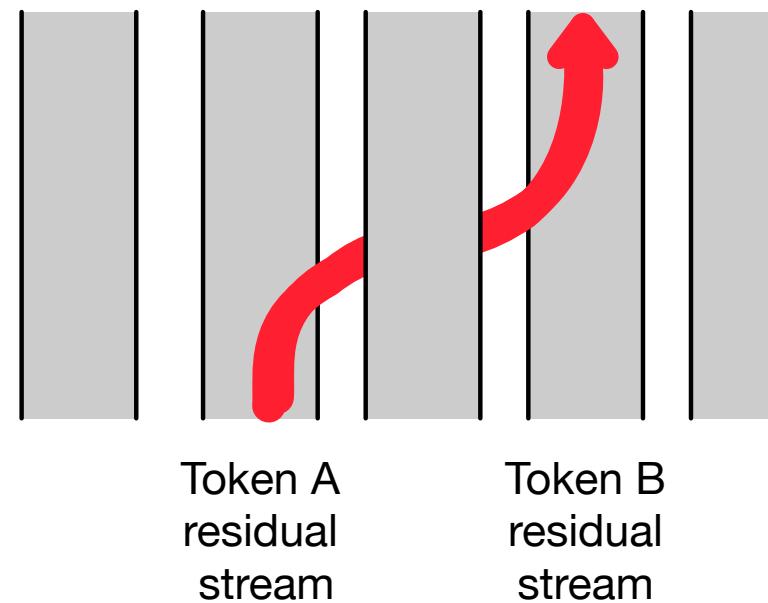


Residual streams and attention

Notice that all parts of the transformer block apply to 1 residual stream (1 token).

Except attention, which takes information from other tokens

[Elhage et al. \(2021\)](#) show that we can view attention heads as literally moving information from the residual stream of a neighboring token into the current stream .



The Transformer Block

Transformers

Parallelizing Attention Computation

Transformers

Parallelizing computation using \mathbf{X}

For attention/transformer block we've been computing a **single** output at a **single** time step i in a **single** residual stream.

But we can pack the N tokens of the input sequence into a single matrix \mathbf{X} of size $[N \times d]$.

Each row of \mathbf{X} is the embedding of one token of the input.

\mathbf{X} can have 1K-32K rows, each of the dimensionality of the embedding d (the **model dimension**)

$$\mathbf{Q} = \mathbf{X}\mathbf{W}^Q; \quad \mathbf{K} = \mathbf{X}\mathbf{W}^K; \quad \mathbf{V} = \mathbf{X}\mathbf{W}^V$$

$$QK^T$$

Now can do a single matrix multiply to combine Q and K^T

$q_1 \cdot k_1$	$q_1 \cdot k_2$	$q_1 \cdot k_3$	$q_1 \cdot k_4$
$q_2 \cdot k_1$	$q_2 \cdot k_2$	$q_2 \cdot k_3$	$q_2 \cdot k_4$
$q_3 \cdot k_1$	$q_3 \cdot k_2$	$q_3 \cdot k_3$	$q_3 \cdot k_4$
$q_4 \cdot k_1$	$q_4 \cdot k_2$	$q_4 \cdot k_3$	$q_4 \cdot k_4$

Parallelizing attention

- Scale the scores, take the softmax, and then multiply the result by V resulting in a matrix of shape $N \times d$
 - An attention vector for each input token

$$\mathbf{A} = \text{softmax} \left(\text{mask} \left(\frac{\mathbf{Q}\mathbf{K}^T}{\sqrt{d_k}} \right) \right) \mathbf{V}$$

Masking out the future

$$\mathbf{A} = \text{softmax} \left(\text{mask} \left(\frac{\mathbf{Q}\mathbf{K}^T}{\sqrt{d_k}} \right) \right) \mathbf{V}$$

- What is this mask function?
 $\mathbf{Q}\mathbf{K}^T$ has a score for each query dot every key,
including those that follow the query.
- Guessing the next word is pretty simple if you already know it!

Masking out the future

$$\mathbf{A} = \text{softmax} \left(\text{mask} \left(\frac{\mathbf{Q}\mathbf{K}^T}{\sqrt{d_k}} \right) \right) \mathbf{V}$$

Add $-\infty$ to cells in upper triangle

The softmax will turn it to 0

$q_1 \cdot k_1$	$-\infty$	$-\infty$	$-\infty$
$q_2 \cdot k_1$	$q_2 \cdot k_2$	$-\infty$	$-\infty$
$q_3 \cdot k_1$	$q_3 \cdot k_2$	$q_3 \cdot k_3$	$-\infty$
$q_4 \cdot k_1$	$q_4 \cdot k_2$	$q_4 \cdot k_3$	$q_4 \cdot k_4$

N

N

Another point: Attention is quadratic in length

$$\mathbf{A} = \text{softmax} \left(\text{mask} \left(\frac{\mathbf{Q}\mathbf{K}^T}{\sqrt{d_k}} \right) \right) \mathbf{V}$$

$q_1 \cdot k_1$	$-\infty$	$-\infty$	$-\infty$
$q_2 \cdot k_1$	$q_2 \cdot k_2$	$-\infty$	$-\infty$
$q_3 \cdot k_1$	$q_3 \cdot k_2$	$q_3 \cdot k_3$	$-\infty$
$q_4 \cdot k_1$	$q_4 \cdot k_2$	$q_4 \cdot k_3$	$q_4 \cdot k_4$

N

N

Attention again

$$\begin{array}{c}
 X \\
 \left[\begin{array}{c} \text{Input Token 1} \\ \text{Input Token 2} \\ \text{Input Token 3} \\ \text{Input Token 4} \end{array} \right]_{N \times d} \times W^Q = Q \\
 \left[\begin{array}{c} \text{Query Token 1} \\ \text{Query Token 2} \\ \text{Query Token 3} \\ \text{Query Token 4} \end{array} \right]_{N \times d_k} \\
 d \times d_k
 \end{array}
 \quad
 \begin{array}{c}
 X \\
 \left[\begin{array}{c} \text{Input Token 1} \\ \text{Input Token 2} \\ \text{Input Token 3} \\ \text{Input Token 4} \end{array} \right]_{N \times d} \times W^K = K \\
 \left[\begin{array}{c} \text{Key Token 1} \\ \text{Key Token 2} \\ \text{Key Token 3} \\ \text{Key Token 4} \end{array} \right]_{N \times d_k} \\
 d \times d_k
 \end{array}
 \quad
 \begin{array}{c}
 X \\
 \left[\begin{array}{c} \text{Input Token 1} \\ \text{Input Token 2} \\ \text{Input Token 3} \\ \text{Input Token 4} \end{array} \right]_{N \times d} \times W^V = V \\
 \left[\begin{array}{c} \text{Value Token 1} \\ \text{Value Token 2} \\ \text{Value Token 3} \\ \text{Value Token 4} \end{array} \right]_{N \times d_v} \\
 d \times d_v
 \end{array}$$

$$\begin{array}{c}
 Q \\
 \left[\begin{array}{c} q1 \\ q2 \\ q3 \\ q4 \end{array} \right]_{N \times d_k} \times K^T \\
 \left[\begin{array}{c} \kappa \\ \kappa \\ \kappa \\ \kappa \end{array} \right]_{d_k \times N} = QK^T \\
 \left[\begin{array}{cccc} q1 \cdot k1 & q1 \cdot k2 & q1 \cdot k3 & q1 \cdot k4 \\ q2 \cdot k1 & q2 \cdot k2 & q2 \cdot k3 & q2 \cdot k4 \\ q3 \cdot k1 & q3 \cdot k2 & q3 \cdot k3 & q3 \cdot k4 \\ q4 \cdot k1 & q4 \cdot k2 & q4 \cdot k3 & q4 \cdot k4 \end{array} \right]_{N \times N} \\
 N \times N
 \end{array}
 \quad
 \begin{array}{c}
 V \\
 \left[\begin{array}{c} v1 \\ v2 \\ v3 \\ v4 \end{array} \right]_{N \times d_v} \times A \\
 \left[\begin{array}{c} a1 \\ a2 \\ a3 \\ a4 \end{array} \right]_{N \times d_v} = A
 \end{array}$$

Parallelizing Multi-head Attention

$$\mathbf{Q}^i = \mathbf{X}\mathbf{W}^{Qi}; \quad \mathbf{K}^i = \mathbf{X}\mathbf{W}^{Ki}; \quad \mathbf{V}^i = \mathbf{X}\mathbf{W}^{Vi}$$

$$\mathbf{head}_i = \text{SelfAttention}(\mathbf{Q}^i, \mathbf{K}^i, \mathbf{V}^i) = \text{softmax}\left(\frac{\mathbf{Q}^i \mathbf{K}^{iT}}{\sqrt{d_k}}\right) \mathbf{V}^i$$

$$\text{MultiHeadAttention}(\mathbf{X}) = (\mathbf{head}_1 \oplus \mathbf{head}_2 \dots \oplus \mathbf{head}_h) \mathbf{W}^O$$

Parallelizing Multi-head Attention

$$\mathbf{O} = \text{LayerNorm}(\mathbf{X} + \text{MultiHeadAttention}(\mathbf{X}))$$

$$\mathbf{H} = \text{LayerNorm}(\mathbf{O} + \text{FFN}(\mathbf{O}))$$

or

$$\mathbf{T}^1 = \text{MultiHeadAttention}(\mathbf{X})$$

$$\mathbf{T}^2 = \mathbf{X} + \mathbf{T}^1$$

$$\mathbf{T}^3 = \text{LayerNorm}(\mathbf{T}^2)$$

$$\mathbf{T}^4 = \text{FFN}(\mathbf{T}^3)$$

$$\mathbf{T}^5 = \mathbf{T}^4 + \mathbf{T}^3$$

$$\mathbf{H} = \text{LayerNorm}(\mathbf{T}^5)$$

Parallelizing Attention Computation

Transformers

Input and output: Position embeddings and the Language Model Head

Transformers

Token and Position Embeddings

The matrix X (of shape $[N \times d]$) has an embedding for each word in the context.

This embedding is created by adding two distinct embedding for each input

- token embedding
- positional embedding

Token Embeddings

Embedding matrix E has shape $[|V| \times d]$.

- One row for each of the $|V|$ tokens in the vocabulary.
- Each word is a row vector of d dimensions

Given: string "*Thanks for all the*"

1. Tokenize with BPE and convert into vocab indices

$w = [5, 4000, 10532, 2224]$

2. Select the corresponding rows from E , each row an embedding

- (row 5, row 4000, row 10532, row 2224).

Position Embeddings

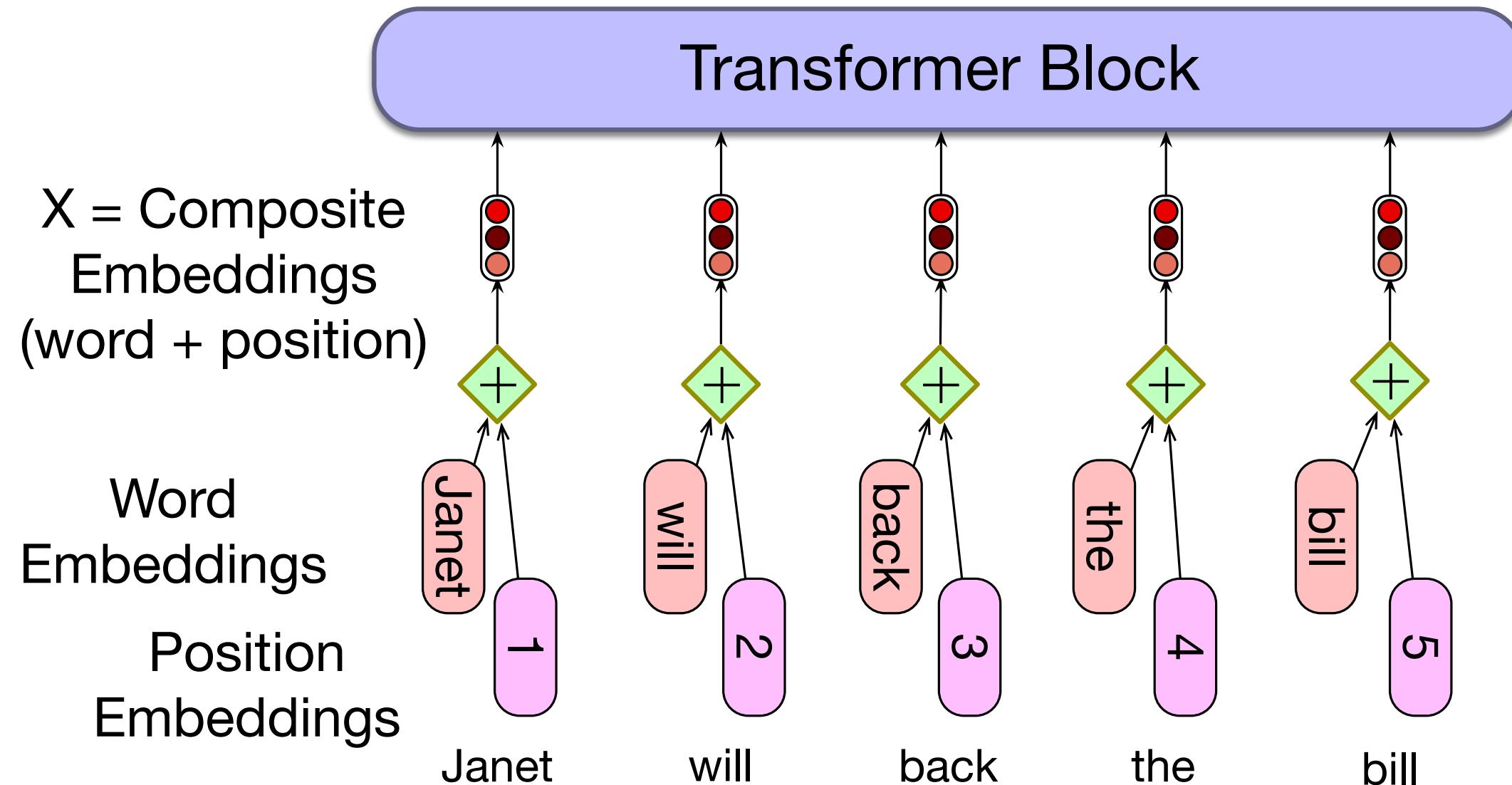
There are many methods, but we'll just describe the simplest: absolute position.

Goal: learn a position embedding matrix E_{pos} of shape $[1 \times N]$.

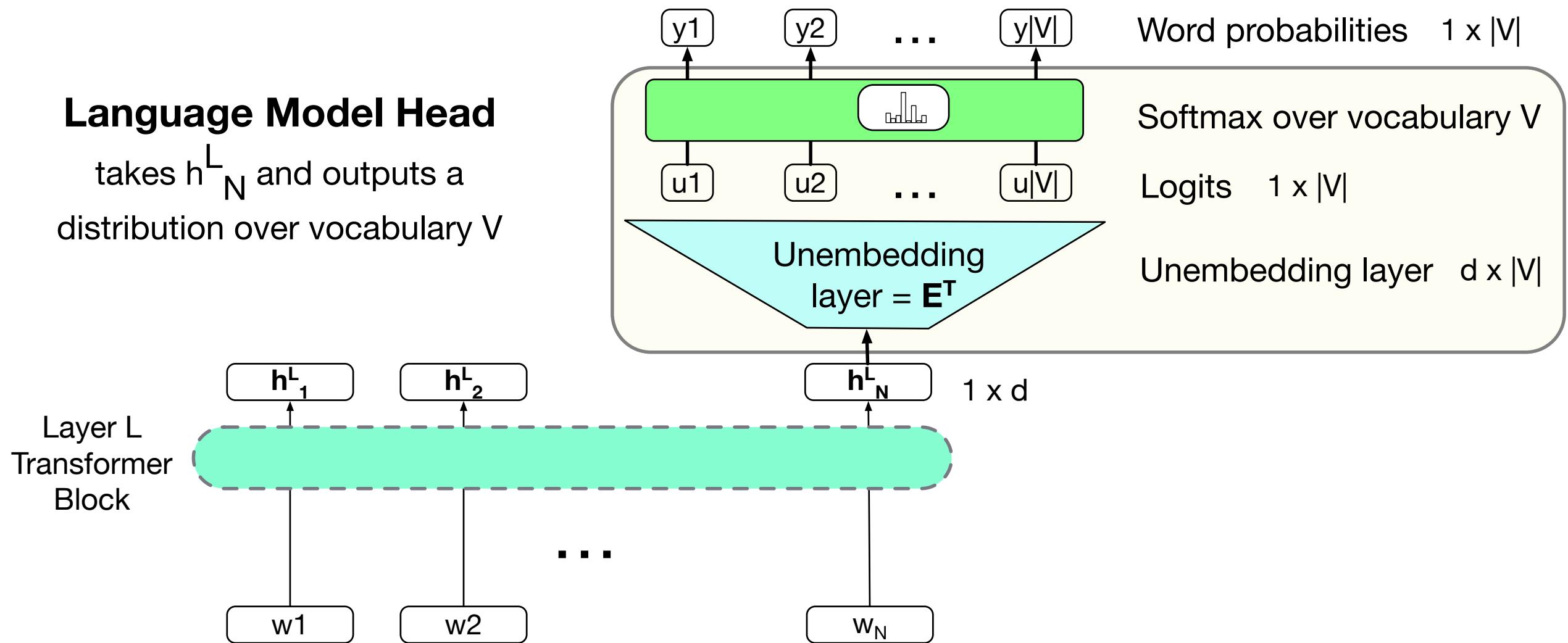
Start with randomly initialized embeddings

- one for each integer up to some maximum length.
- i.e., just as we have an embedding for token *fish*, we'll have an embedding for position 3 and position 17.
- As with word embeddings, these position embeddings are learned along with other parameters during training.

Each x is just the sum of word and position embeddings

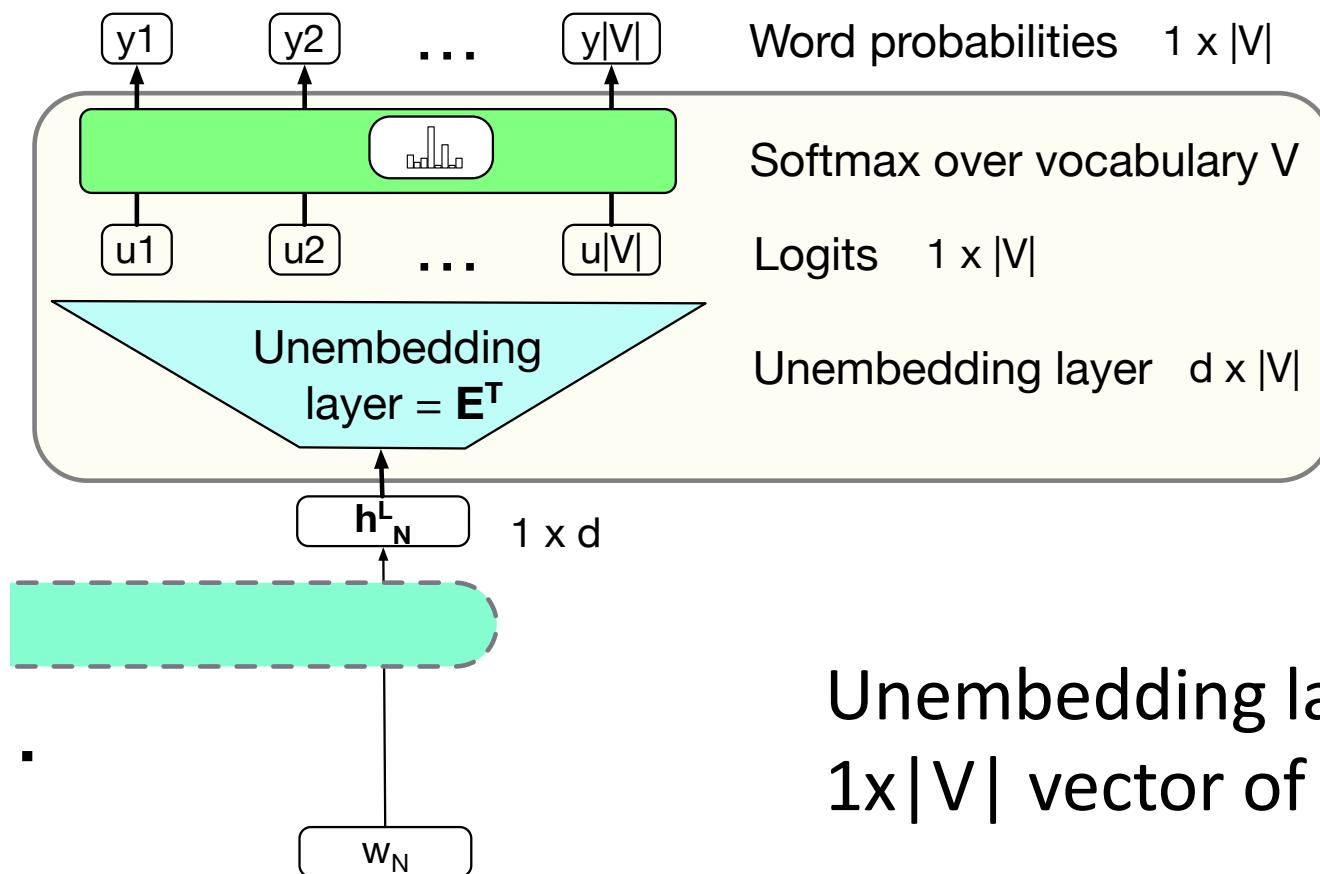


Language modeling head



Language modeling head

Unembedding layer: linear layer projects from h_N^L (shape $[1 \times d]$) to logit vector



Why "unembedding"? **Tied to E^T**

Weight tying, we use the same weights for two different matrices

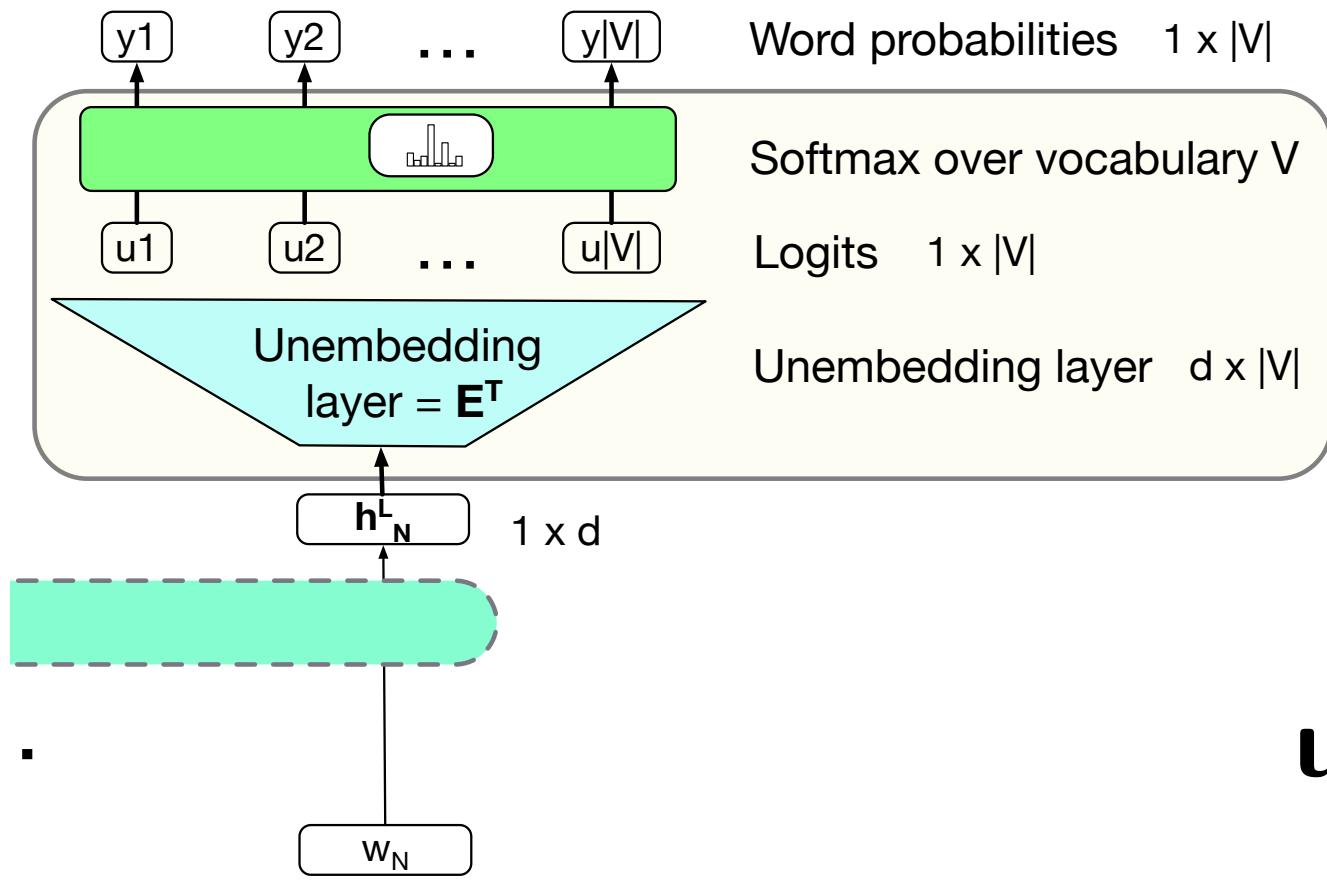
Unembedding layer maps from an embedding to a $1 \times |V|$ vector of logits

Language modeling head

Logits, the score vector u

One score for each of the $|V|$ possible words in the vocabulary V .
Shape $1 \times |V|$.

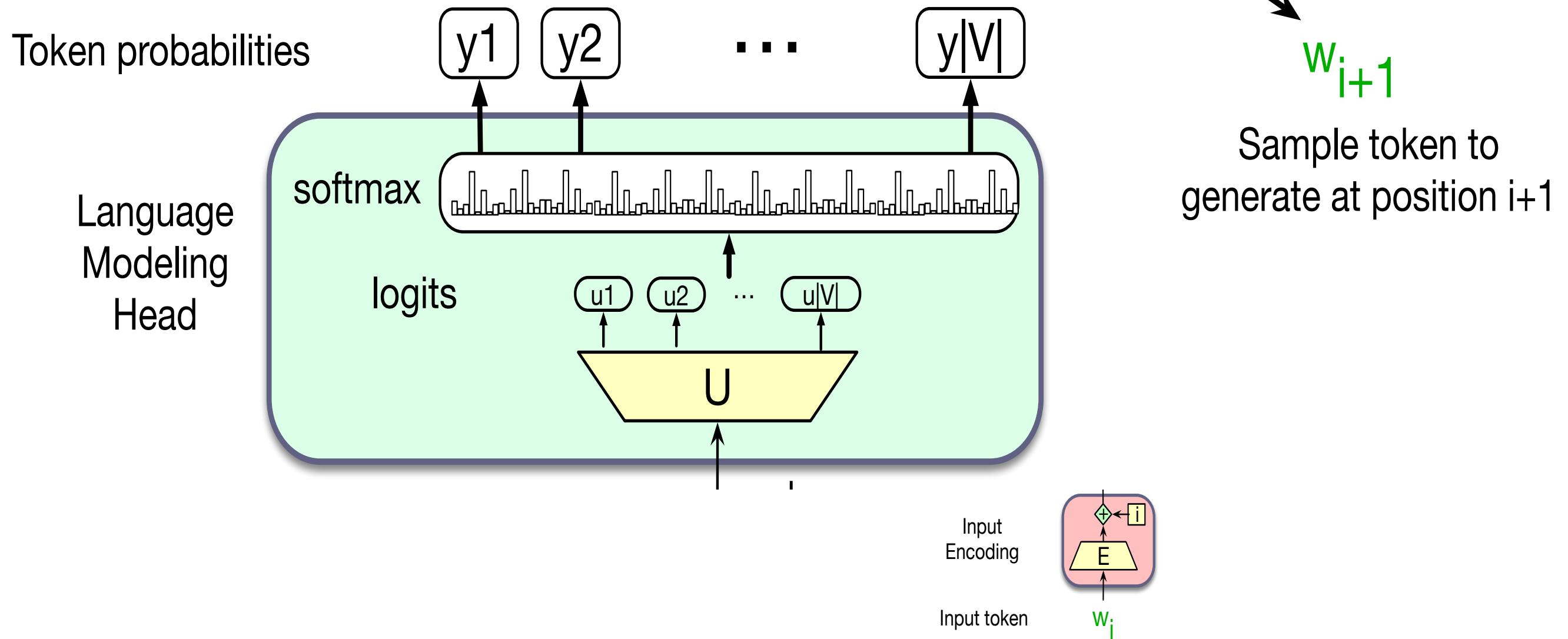
Softmax turns the logits into probabilities over vocabulary.
Shape $1 \times |V|$.



$$u = h_N^L E^T$$

$$y = \text{softmax}(u)$$

The final transformer model



Input and output: Position embeddings and the Language Model Head

Transformers

Large
Language
Models

Dealing with Scale

Scaling Laws

LLM performance depends on

- Model size: the number of parameters not counting embeddings
- Dataset size: the amount of training data
- Compute: Amount of compute (in FLOPS or etc)

Can improve a model by adding parameters (more layers, wider contexts), more data, or training for more iterations

The performance of a large language model (the loss) scales as a power-law with each of these three

Scaling Laws

Loss L as a function of # parameters N , dataset size D , compute budget C (if other two are held constant)

$$L(N) = \left(\frac{N_c}{N} \right)^{\alpha_N}$$

$$L(D) = \left(\frac{D_c}{D} \right)^{\alpha_D}$$

$$L(C) = \left(\frac{C_c}{C} \right)^{\alpha_C}$$

Scaling laws can be used early in training to predict what the loss would be if we were to add more data or increase model size.

Number of non-embedding parameters N

$$\begin{aligned} N &\approx 2d n_{\text{layer}}(2d_{\text{attn}} + d_{\text{ff}}) \\ &\approx 12n_{\text{layer}}d^2 \\ &\quad (\text{assuming } d_{\text{attn}} = d_{\text{ff}}/4 = d) \end{aligned}$$

Thus GPT-3, with $n = 96$ layers and dimensionality $d = 12288$, has $12 \times 96 \times 122882 \approx 175$ billion parameters.

KV Cache

In training, we can compute attention very efficiently in parallel:

$$\mathbf{A} = \text{softmax} \left(\frac{\mathbf{Q}\mathbf{K}^T}{\sqrt{d_k}} \right) \mathbf{V}$$

But not at inference! We generate the next tokens **one at a time!**

For a new token x , need to multiply by \mathbf{W}^Q , \mathbf{W}^K , and \mathbf{W}^V to get query, key, values

But don't want to **recompute** the key and value vectors for all the prior tokens $x_{<i}$

Instead, store key and value vectors in memory in the KV cache, and then we can just grab them from the cache

KV Cache

$$\begin{array}{c}
 \left[\begin{array}{c} Q \\ \hline q1 \\ q2 \\ q3 \\ q4 \end{array} \right] \times \left[\begin{array}{c} K^T \\ \hline k1 | k2 | k3 | k4 \end{array} \right] = \left[\begin{array}{c} QK^T \\ \hline \begin{array}{cccc} q1 \cdot k1 & q1 \cdot k2 & q1 \cdot k3 & q1 \cdot k4 \\ q2 \cdot k1 & q2 \cdot k2 & q2 \cdot k3 & q2 \cdot k4 \\ q3 \cdot k1 & q3 \cdot k2 & q3 \cdot k3 & q3 \cdot k4 \\ q4 \cdot k1 & q4 \cdot k2 & q4 \cdot k3 & q4 \cdot k4 \end{array} \end{array} \right] \\
 N \times d_K \qquad \qquad \qquad N \times N
 \end{array}$$

$$\left[\begin{array}{c} V \\ \hline v1 \\ v2 \\ v3 \\ v4 \end{array} \right] \times \left[\begin{array}{c} A \\ \hline a1 \\ a2 \\ a3 \\ a4 \end{array} \right] = \left[\begin{array}{c} N \times d_V \\ \hline N \times d_V \end{array} \right]$$

$$\begin{array}{c}
 \left[\begin{array}{c} Q \\ \hline q4 \end{array} \right] \times \left[\begin{array}{c} K^T \\ \hline k1 | k2 | k3 | k4 \end{array} \right] = \left[\begin{array}{c} QK^T \\ \hline \begin{array}{cccc} q4 \cdot k1 & q4 \cdot k2 & q4 \cdot k3 & q4 \cdot k4 \end{array} \end{array} \right] \\
 1 \times d_K \qquad \qquad \qquad 1 \times N
 \end{array}$$

$$\left[\begin{array}{c} V \\ \hline v1 \\ v2 \\ v3 \\ v4 \end{array} \right] \times \left[\begin{array}{c} A \\ \hline a4 \end{array} \right] = \left[\begin{array}{c} N \times d_V \\ \hline 1 \times d_V \end{array} \right]$$

Parameter-Efficient Finetuning

Adapting to a new domain by continued pretraining (finetuning) is a problem with huge LLMs.

- Enormous numbers of parameters to train
- Each pass of batch gradient descent has to backpropagate through many many huge layers.
- Expensive in processing power, in memory, and in time.

Instead, **parameter-efficient fine tuning (PEFT)**

- Efficiently select a subset of parameters to update when finetuning.
- E.g., freeze some of the parameters (don't change them),
- And only update some a few parameters.

LoRA (Low-Rank Adaptation)

- Transformers have many dense matrix multiply layers
 - Like W^Q , W^K , W^V , W^O layers in attention
- Instead of updating these layers during finetuning,
 - Freeze these layers
 - Update a low-rank approximation with fewer parameters.

LoRA

- Consider a **matrix W** (shape $[N \times d]$) that needs to be updated during finetuning via gradient descent.
 - Normally updates are ΔW (shape $[N \times d]$)
- In LoRA, we freeze W and update instead a low-rank decomposition of W:
 - A of shape $[N \times r]$,
 - B of shape $[r \times d]$, r is very small (like 1 or 2)
 - That is, during finetuning we update A and B instead of W.
 - Replace $W + \Delta W$ with $W + BA$.

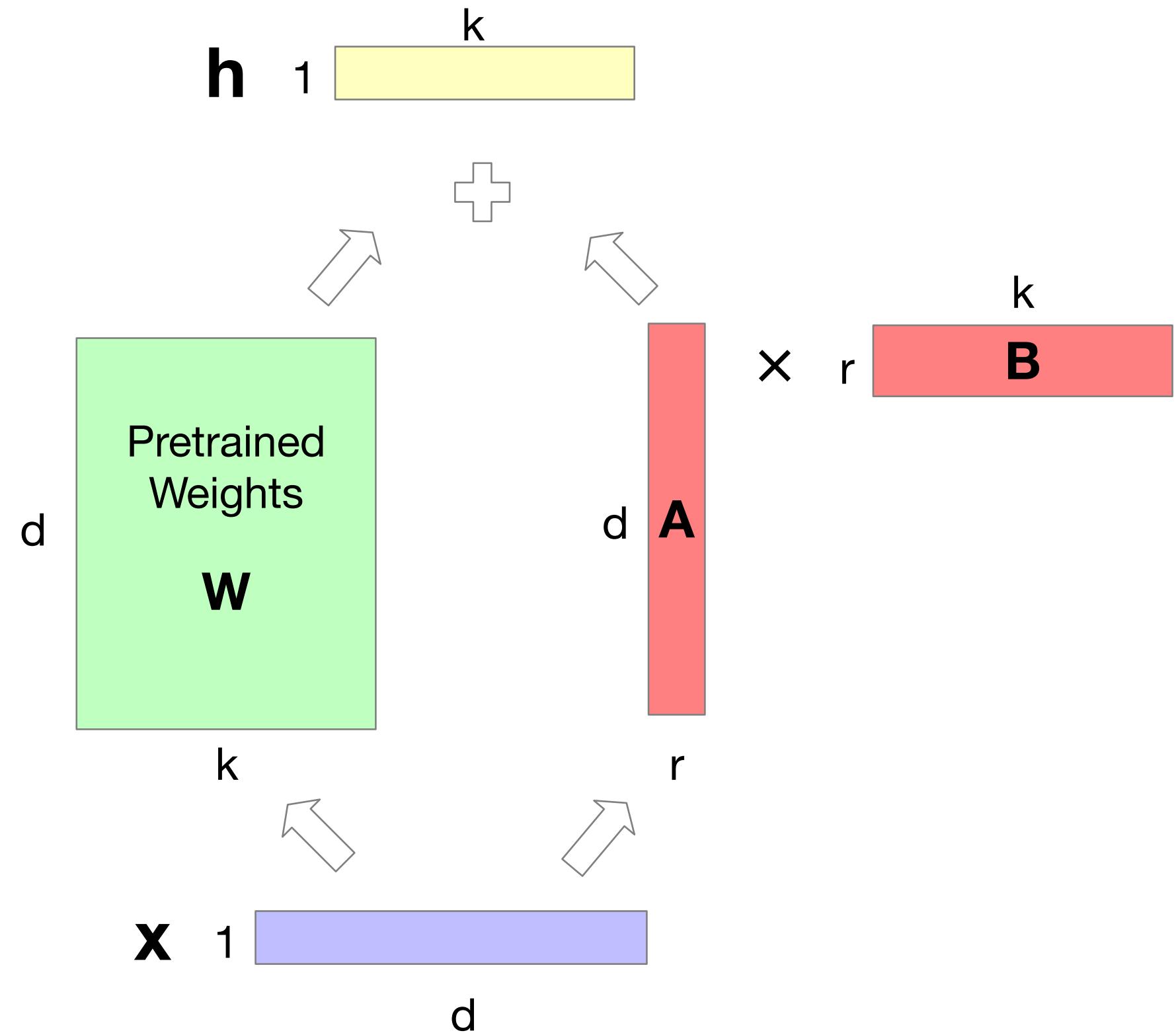
Forward pass: instead of

$$\mathbf{h} = \mathbf{xW}$$

We do

$$\mathbf{h} = \mathbf{xW} + \mathbf{xAB}$$

LoRA



Large
Language
Models

Dealing with Scale