SOUTH CHINA UNIVERSITY OF TECHNOLOGY

SCUT_gugugu

TEMPLATE



0 error(s), 0 warning(s)

CONTENTS 1

Contents

1	Gra	ph Theory
	1.1	Shortest Path
		1.1.1 Dijkstra
		1.1.2 SPFA
	1.2	Network Flow
		1.2.1 ISAP
		1.2.2 HLPP
		1.2.3 Dinic
		1.2.4 MCMF
	1.3	Tree Related
		1.3.1 Kruskal
		1.3.2 Prim
		1.3.3 Tree Divide and Conquer
	1.4	LCA
		1.4.1 Tree Decomposition LCA
		1.4.2 Tarjan LCA
	1.5	Tarjan
		1.5.1 SCC
		1.5.2 BCC
	1.6	Cactus
		1.6.1 Circle-Square Tree
2	Dot	a Structures 19
_	2.1	Basic Structures
	2.1	2.1.1 RMQ
		2.1.2 Divide Blocks
	2.2	Tree Structures
	2.2	2.2.1 Tree Decomposition
		•
	0.2	
	2.3	Sequence Structures
		2.3.1 Segment Tree
	0.4	2.3.2 Splay Tree
	2.4	Persistent Data Structures
		2.4.1 Chairman Tree
		2.4.2 Persistent Trie
3	Stri	ng 29
	3.1	Basics
		3.1.1 Hash
		3.1.2 KMP && exKMP
		3.1.3 AC Automaton

CONTENTS 2

		3.1.4 N	Minimum String	2
	3.2	Suffix Re	elated	2
		3.2.1 S	uffix Array	2
		3.2.2 S	uffix Automaton	3
	3.3	Palindro	me Related	ó
		3.3.1 N	Manacher	ó
		3.3.2 F	Palindromic Automaton	3
4	Mat		37	
	4.1	0	37	
			FT	
			TTT	
			WT	
			inear Basis	
	4.2		neory	
			nverse	
			ucas)
			CRT && exCRT	
			3SGS	
			Miller-Rabin && PollardRho42	
		•	$\phi(n)$	
			Culer Sieve 45	3
		4.2.8 I	OuJiao Sieve	
		4.2.9 N	Iöbius Inversion 45	5
5	Coo	\mathbf{metry}	47	7
J	5.1		aly Definition and Functions	
	5.1		Const and Functions	
			Point Definition	
			ine Definition	
			Get Area	
		0.1.1	Get Circumference	
			anticlockwise Sort	
			Hull	
	0.2		Get Convex Hull	
			Point in Convex Hull	
	5.3		ski Sum	
	5.4		Calipers	
	9.4		The Diameter of Convex Hull	
			The Min Distance Bewteen two Convex Hull	
	5.5		ne Intersection	
	5.6		cle Cover	
	5.7		nion Area	
	-		Integrate 52	

CONTENTS 3

6	Oth	ers 5	55
	6.1	Sample	55
		6.1.1 vimrc	55
		6.1.2 Check	55
		6.1.3 FastIO	55
		6.1.4 Java BigNum	56
	6.2	Offline Algorithm	58
		6.2.1 CDQ Divide and Conquer	58
		6.2.2 Mo's Algorithm	58
		6.2.3 Mo's Algorithm On Tree	59
	6.3	Randomized Algorithm	31
		6.3.1 Simulated Annealing	31
	6.4	Other Method	32
		6.4.1 Enumerate Subset	32
		6.4.2 Enumerate $\lfloor \frac{n}{d} \rfloor \lfloor \frac{m}{d} \rfloor$	32
	6.5	Formula	32
		6.5.1 Euler's Theorem	32
		6.5.2 Möbius Inversion Formula	32
		6.5.3 Math Theory Tips	32
		6.5.4 Sieve Ting	33

1 Graph Theory

1.1 Shortest Path

1.1.1 Dijkstra

```
typedef pair<int, int> P;
2
   struct Edge {
        int to, nxt;
3
4
        LL w;
5
   }e[MAXM];
   int head[MAXN], ecnt;
   LL d[MAXN];
7
   priority_queue<P, vector<P>, greater<P> > q;
8
   inline void addEdge(int x, int y, LL w) {
9
       e[++ecnt] = (Edge) \{y, head[x], w\}; head[x] = ecnt;
10
11
12
   void dijkstra(int st) {
13
       memset(d, 0x3f, sizeof(d));
14
        d[st] = 0;
15
        q.push(make_pair(0, st));
16
       while(!q.empty()) {
17
            P x = q.top(); q.pop();
18
            int u = x.second;
            for(int i = head[u], v; i; i = e[i].nxt) {
19
                v = e[i].to;
20
                if(d[v] > d[u] + e[i].w) {
21
                    d[v] = d[u] + e[i].w;
22
23
                    q.push(make_pair(d[v], v));
24
                }
25
            }
26
       }
27
   }
```

1.1.2 SPFA

```
struct Edge {
1
2
       int to, nxt;
3
       LL w;
   }e[MAXE];
4
5
   int head[MAXN], ecnt;
6 LL d[MAXN];
7
   bool exist[MAXN];
   queue<int> q;
8
9
   inline void addEdge(int x, int y, LL w) {
       e[++ecnt] = (Edge) \{y, head[x], w\}; head[x] = ecnt;
10
11
   void SPFA(int st) {
12
       memset(d,0x3f,sizeof(d));
13
        d[st] = 0;
14
        q.push(st);
15
        exist[st] = 1;
16
17
       while(!q.empty()) {
18
            int u = q.front(); q.pop();
19
            exist[u] = 0;
            for(int i = head[u], v; i; i = e[i].nxt) {
20
21
                v = e[i].to;
                if(d[v] > d[u] + e[i].w) {
22
```

```
d[v] = d[u] + e[i].w;
23
24
                      //pre[v] = u;
25
                      if(!exist[v]) {
26
                          q.push(v);
                          exist[v] = 1;
27
                      }
28
29
                 }
            }
30
        }
31
   }
32
```

1.2 Network Flow

1.2.1 ISAP

```
namespace NWF {
1
2
          struct Edge{
3
               int to, nxt;LL f;
          e[MAXM << 1];
 4
 5
          int S, T, tot;
          int ecnt, head[MAXN], cur[MAXN], pre[MAXN], num[MAXN], dis[MAXN];
 6
 7
          queue<int> q;
         void init(int _S, int _T, int _tot){
   ecnt = 1; S = _S; T = _T; tot = _tot;
   memset(num, 0, (tot + 1) * sizeof(int));
   memset(head, 0, (tot + 1) * sizeof(int));
 8
 9
10
11
12
          inline void addEdge(int u, int v, LL f) {
13
               e[++ecnt] = (Edge) \{v, head[u], f\}; head[u] = ecnt; e[++ecnt] = (Edge) \{u, head[v], 0\}; head[v] = ecnt;
14
15
16
          void bfs() {
17
               memset(dis, 0, (tot + 1) * sizeof(int));
18
19
               q.push(T);
20
               dis[T] = 1;
21
               while(!q.empty()) {
22
                    int u = q.front(), v; q.pop();
23
                    num[dis[u]]++;
                    for(int i = cur[u] = head[u]; i; i = e[i].nxt) {
24
                         if(!dis[v = e[i].to]) {
25
                              dis[v] = dis[u] + 1;
26
27
                               q.push(v);
28
                         }
29
                    }
               }
30
31
          LL augment() {
32
               LL flow = INF;
33
               for(int i = S; i != T; i = e[cur[i]].to)
34
               flow = min(flow, e[cur[i]].f);
for(int i = S; i != T; i = e[cur[i]].to) {
35
36
                    e[cur[i]].f -= flow;
37
                    e[cur[i] ^ 1].f += flow;
38
39
40
               return flow;
41
          LL isap() {
42
43
               bfs();
               int u = S, v;
44
```

```
LL flow = 0;
45
            while(dis[S] <= tot) {</pre>
46
47
                 if(u == T) {
                     flow += augment();
48
                     u = S;
49
50
                 bool fg = 0;
51
                 for(int i = cur[u]; i; i = e[i].nxt) {
52
                     if(e[i].f && dis[u] > dis[v = e[i].to]) {
53
                          pre[v] = u;
54
                          cur[u] = i;
55
                          u = v;
56
                          fg = 1;
57
                          break;
58
59
                     }
60
                 if(fg) continue;
61
                 if(!--num[dis[u]]) break;
62
                 int maxDis = tot;
63
                 for(int i = head[u]; i; i = e[i].nxt) {
64
                     if(e[i].f \&\& maxDis > dis[v = e[i].to]) {
65
                          maxDis = dis[v];
66
                          cur[u] = i;
67
                     }
68
69
70
                 num[dis[u] = maxDis + 1]++;
71
                 if(u != S) u = pre[u];
72
73
            return flow;
        }
74
   }
75
```

1.2.2 HLPP

```
namespace NWF{
1
2
         struct Edge{
              int to,nxt;LL f;
3
         e[MAXM << 1];
4
5
         int S, T, tot;
         int ecnt, head[MAXN], dis[MAXN], num[MAXN];
6
7
         LL sumf[MAXN];
8
         queue<int> q;
9
         list<int> dep[MAXN];
         void init(int _S,int _T,int _tot){
10
              ecnt = 1;S = _S;T = _T;tot = _tot;
memset(num, 0, (tot + 1) * sizeof(int));
memset(head, 0, (tot + 1) * sizeof(int));
11
12
13
              memset(sumf, 0, (tot + 1) * sizeof(LL));
14
15
         void addEdge(int u,int v,LL f){
16
              e[++ecnt] = (Edge) \{v, head[u], f\}; head[u] = ecnt; e[++ecnt] = (Edge) \{u, head[v], 0\}; head[v] = ecnt;
17
18
19
         void bfs(){
20
              memset(dis, 0, (tot + 1) * sizeof(int));
21
              q.push(T); dis[T] = 1;
22
23
              while(!q.empty()){
24
                    int u=q.front(), v; q.pop();
25
                    for(int i = head[u]; i; i = e[i].nxt)
26
                    if(!dis[v = e[i].to]){
```

```
dis[v] = dis[u] + 1;
27
28
                     q.push(v);
29
                 }
            }
30
31
        LL hlpp(){
32
            bfs();
33
34
            dis[S] = tot + 1;
            for(int i = 1;i <= tot; ++i)num[dis[i]]++;</pre>
35
            for(int i = tot + 1; ~i; --i)dep[i].clear();
36
            int_maxd = dis[S];LL f;
37
            dep[maxd].push_back(S);sumf[S] = INF;
38
39
            for(;;){
                 while(maxd && dep[maxd].empty())maxd--;
40
41
                 if(!maxd)break;
                 int u = dep[maxd].back(), v;dep[maxd].pop_back();
42
                 int minDis = tot + 1;
43
                 for(int i = head[u]; i;i = e[i].nxt)
44
45
                 if(e[i].f){
                     if(dis[u] > dis[v = e[i].to]){
46
                         f = min(sumf[u], e[i].f);
47
                         e[i].f -= f; e[i^1].f += f;
48
                         if(sumf[u] != INF) sumf[u] -= f;
49
50
                         if(sumf[v] != INF) sumf[v] += f;
                         if(v!=S \&\& v!=T \&\& sumf[v] == f){
51
                              maxd = max(maxd, dis[v]);
52
53
                              dep[dis[v]].push_back(v);
54
                         if(!sumf[u])break;
55
                     }else minDis=min(minDis, dis[v] + 1);
56
57
                 if(sumf[u]){
58
                     if(!--num[dis[u]]){
59
                         for(int i = dis[u];i <= maxd;++i){</pre>
60
                              while(!dep[i].empty()){
61
                                  --num[i];
62
                                  dis[dep[i].back()] = tot + 1;
63
                                  dep[i].pop_back();
64
                              }
65
66
                         }
67
                         maxd = dis[u] - 1; dis[u] = tot + 1;
                     }else{
68
                         dis[u] = minDis;
69
                         if(minDis > tot)continue;
70
                         num[minDis]++;
71
                         maxd = max(maxd, minDis);
72
73
                         dep[minDis].push_back(u);
                     }
74
75
                 }
76
            return sumf[T];
77
78
    }
79
```

1.2.3 Dinic

```
namespace NWF {
struct Edge {
    int to, nxt;LL f;
} e[MAXM << 1];</pre>
```

```
5
         int S, T, tot;
         int ecnt, head[MAXN], cur[MAXN], dis[MAXN];
 6
         queue<int> q;
 7
         void init(int _S, int _T, int _tot){
    ecnt = 1; S = _S; T = _T; tot = _tot;
    memset(head, 0, (tot + 1) * sizeof(int));
 8
 9
10
11
         void addEdge(int u, int v, LL f) {
    e[++ecnt] = (Edge) {v, head[u], f}; head[u] = ecnt;
    e[++ecnt] = (Edge) {u, head[v], 0}; head[v] = ecnt;
12
13
14
15
         bool bfs() {
16
              memset(dis, 0, (tot + 1) * sizeof(int));
17
              q.push(S); dis[S] = 1;
18
19
              while (!q.empty()) {
                   int u = q.front(), v; q.pop();
20
                   for (int i = cur[u] = head[u]; i ; i = e[i].nxt) {
21
22
                        if (e[i].f && !dis[v = e[i].to]) {
23
                              q.push(v);
                              dis[v] = dis[u] + 1;
24
                        }
25
                   }
26
27
              }
28
              return dis[T];
29
30
         LL dfs(int u, LL maxf) {
31
              if (u == T) return maxf;
              LL sumf = maxf;
32
              for (int &i = cur[u]; i; i = e[i].nxt) {
33
                   if (e[i].f && dis[e[i].to] > dis[u]) {
34
                        LL tmpf = dfs(e[i].to, min(sumf, e[i].f));
35
                        e[i].f -= tmpf; e[i ^ 1].f += tmpf;
36
                        sumf -= tmpf;
37
                        if (!sumf) return maxf;
38
39
                   }
              }
40
              return maxf - sumf;
41
42
43
         LL dinic() {
44
              LL ret = 0;
45
              while (bfs()) ret += dfs(S, INF);
46
              return ret;
47
         }
48
```

1.2.4 MCMF

```
1
    namespace NWF{
2
        struct Edge {
3
            int to, nxt;LL f, c;
4
        } e[MAXM << 1];</pre>
        int S, T, tot;
int ecnt, head[MAXN], cur[MAXN];LL dis[MAXN];
5
6
7
        bool exist[MAXN];
        queue<int> q;
8
        void init(int _S, int _T, int _tot){
9
            ecnt = 1; S = _S; T = _T; tot = _tot;
10
11
            memset(head, 0, (tot + 1) * sizeof(int));
12
13
        void addEdge(int u, int v, LL f, LL c) {
```

```
e[++ecnt] = (Edge) \{v, head[u], f, c\}; head[u] = ecnt;
14
              e[++ecnt] = (Edge) \{u, head[v], 0, -c\}; head[v] = ecnt;
15
16
         bool spfa() {
17
              for(int i = 0;i <= tot; ++i){</pre>
18
                   dis[i] = INF; exist[i] = cur[i] = 0;
19
20
              q.push(S);dis[S] = 0;exist[S] = 1;
21
              while(!q.empty()) {
22
                   int u = q.front(), v; q.pop();exist[u] = 0;
23
                   for(int i = head[u]; i; i = e[i].nxt) {
    if(e[i].f && dis[v = e[i].to] > dis[u] + e[i].c) {
24
25
26
                            dis[v] = dis[u] + e[i].c;
                             cur[v] = i;
27
                             if(!exist[v]) {
28
                                  q.push(v);
29
                                  exist[v] = 1;
30
31
                            }
32
                        }
                   }
33
              }
34
              return dis[T] != INF;
35
36
         LL mcmf() {
37
              LL cost = 0;
38
              while(spfa()) {
39
40
                   LL flow = INF;
41
                   for(int i = T; i != S; i = e[cur[i] ^ 1].to)
                   flow = min(flow, e[cur[i]].f);
for(int i = T; i != S; i = e[cur[i] ^ 1].to) {
    e[cur[i]].f -= flow;
42
43
44
                        e[cur[i] \land 1].f += flow;
45
46
                   cost += flow * dis[T];
47
              }
48
              return cost;
49
50
         }
51
    }
```

1.3 Tree Related

1.3.1 Kruskal

```
namespace MST{
1
2
        struct Edge{
3
            int u,v; LL w;
            bool operator < (const Edge& x) const { return w < x.w; }</pre>
4
        }e[MAXM];
5
        int ecnt, fa[MAXN];
6
        void addEdge(int u, int v, LL w) {
7
            e[++ecnt] = (Edge)\{v, u, w\}; headp[u] = ecnt;
8
9
        int Find(int x) { return x == fa[x] ? x : fa[x] = Find(fa[x]); }
10
        LL kruskal(int n) {
11
12
            sort(e + 1, e + ecnt + 1);
            for(int i = 1; i <= n; i++) fa[i] = i;
13
            LL sum = 0;
14
            for (int i = 1; i <= ecnt; i++){
15
                int fu = Find(e[i].u), fv = Find(e[i].v);
16
```

```
if(fu != fv){
    fa[fu] = fv;
    sum += e[i].w;

return sum;
}
```

1.3.2 Prim

```
namespace MST {
1
2
        struct Edge{
3
             int to,nxt; LL w;
        }e[MAXM];
4
5
        int ecnt, head[MAXN], vis[MAXN]; // pre[MAXN];
        LL dis[MAXN];
6
        void addEdge(int u, int v, LL w){
7
8
             e[++ecnt] = (Edge)\{v, head[u], w\}; head[u] = ecnt;
9
             e[++ecnt] = (Edge)\{u, head[v], w\}; head[v] = ecnt;
10
        LL Prim(int n){
11
             for (int i = 1; i <= n; i++){</pre>
12
13
                  //pre[i] = 0;
                 vis[i] = 0;
14
                 dis[i] = INF;
15
16
             vis[1] = 1;
17
             LL sum = 0;
18
             for (int i = head[1]; i; i = e[i].nxt)
19
20
                 dis[e[i].to] = min(dis[e[i].to],e[i].w);
             for (int j = 1; j < n; j++){
   int u; LL minDis = INF;</pre>
21
22
                 for (int i = 1; i <= n; ++i)</pre>
23
                      if (!vis[i] && dis[i] < minDis){</pre>
24
25
                          minDis = dis[i];
26
                          u = i;
27
                 if (minDis == INF) return -1;
28
                 vis[u] = 1;
29
30
                 sum += minDis;
                 for (int i = head[u], v; i; i = e[i].nxt)
31
                 if (!vis[v = e[i].to] && e[i].w < dis[v]){</pre>
32
                      //pre[u] = v;
33
                      dis[v] = e[i].w;
34
35
36
             return sum;
37
38
        }
39
   }
```

1.3.3 Tree Divide and Conquer

```
struct Edge {
    int to, nxt, w;
}e[MAXM];
int head[MAXN], ecnt;
int sz[MAXN];
```

```
int d[MAXN], t[5], ans;
7
    bool vis[MAXN];
   inline void add_edge(int u, int v, int w) {
   e[++ecnt] = (Edge) {v, head[u], w}; head[u] = ecnt;
8
9
        e[++ecnt] = (Edge) \{u, head[v], w\}; head[v] = ecnt;
10
11
12
    int getsz(int x, int fa) {
        sz[x] = 1;
13
        for(int i = head[x]; i; i = e[i].nxt) {
14
15
             int y = e[i].to;
            if(vis[y] || y == fa) continue;
16
17
            sz[x] += getsz(y, x);
        }
18
19
        return sz[x];
20
21
    int getrt(int x) {
        int tot = getsz(x, 0) >> 1;
22
23
        while(1) {
24
             int u = -1;
             for(int i = head[x]; i; i = e[i].nxt) {
25
26
                 int y = e[i].to;
                 if(vis[y] || sz[y] > sz[x]) continue;
27
                 if(u == -1 \mid | sz[y] > sz[u]) u = y;
28
29
30
            if(\sim u \&\& sz[u] > tot) x = u;
31
            else break;
32
        }
33
        return x;
34
    void getdep(int x, int fa) {
35
36
        t[d[x]]++;
        for(int i = head[x]; i; i = e[i].nxt) {
37
             int y = e[i].to;
38
            if(vis[y] || y == fa) continue;
39
            d[y] = (d[x] + e[i].w) % 3;
40
            getdep(y, x);
41
        }
42
   }
43
    int cal(int x, int v) {
44
45
        t[0] = t[1] = t[2] = 0;
46
        d[x] = v \% 3;
47
        getdep(x, 0);
        return t[0] * t[0] + t[1] * t[2] * 2;
48
49
   void solve(int x) {
50
        vis[x] = 1;
51
52
        ans += cal(x, 0);
        for(int i = head[x]; i; i = e[i].nxt) {
53
             int y = e[i].to;
54
55
             if(vis[y]) continue;
            ans -= cal(y, e[i].w);
56
             solve(getrt(y));
57
        }
58
59
   int main() {
60
        solve(getrt(1));
61
62
   }
```

1.4 LCA

1.4.1 Tree Decomposition LCA

```
int sz[MAXN], dep[MAXN], top[MAXN], fa[MAXN], son[MAXN], num[MAXN], totw;
   struct Edge {
        int to, nxt;
   }e[MAXN << 1];
   int head[MAXN], ecnt;
   inline void add_edge(int x, int y) {
6
        e[++ecnt] = (Edge) \{y, head[x]\}; head[x] = ecnt;
7
8
9
   void dfs1(int x) {
10
        sz[x] = 1; son[x] = 0;
11
        for(int i = head[x]; i; i = e[i].nxt) {
12
            int v = e[i].to;
13
            if(v == fa[x]) continue;
14
            fa[v] = x;
            dep[v] = dep[x] + 1;
15
16
            dfs1(v);
            sz[x] += sz[v];
17
            if(sz[v] > sz[son[x]]) son[x] = v;
18
       }
19
   }
20
   void dfs2(int x) {
21
        B[num[x]] = A[x];
22
        if(son[x]) {
23
24
            top[son[x]] = top[x];
25
            num[son[x]] = ++totw;
26
            dfs2(son[x]);
27
        for(int i = head[x]; i; i = e[i].nxt) {
28
            int v = e[i].to;
29
            if(v == fa[x] | | v == son[x]) continue;
30
            top[v] = v;
31
32
            num[v] = ++totw;
33
            dfs2(v);
34
       }
35
36
   int lca(int u, int v) {
        if(u == v) return u;
37
       while(top[u] != top[v]) {
38
            if(dep[top[u]] > dep[top[v]]) swap(u, v);
39
            v = fa[top[v]];
40
41
       if(dep[u] > dep[v]) swap(u, v);
42
        return u;
43
44
   inline void init() {
45
       memset(head, 0, sizeof(head)); ecnt = 0;
46
        fa[1] = 0; dep[1] = 1; top[1] = 1; num[1] = 1; totw = 1;
47
48
   inline void pre() {
49
50
        dfs1(1); dfs2(1);
51
   }
```

1.4.2 Tarjan LCA

```
vector< pair<int,int> > G[MAXN],ask[MAXN];
```

```
int fa[MAXN], ans[MAXN], vis[MAXN] ,dis[MAXN];
2
3
   int Find(int x){
        return x == fa[x] ? x : fa[x] = Find(fa[x]);
4
5
   void init(int n){
6
        memset(ans, 0,sizeof ans);
7
8
        memset(vis, 0,sizeof vis);
        for(int i = 0; i \le n; i++){
9
            G[i].clear();
10
            ask[i].clear();
11
        }
12
   }
13
    void LCA(int u){
14
15
        int v;
        fa[u] = u;
16
        vis[u] = true;
17
        for(auto it : ask[u])
18
19
            if(vis[v = it.first])
                ans[it.second] = dis[u] + dis[v] - 2 * dis[Find(it.first)];
20
        for(auto it : G[u])
21
        if(!vis[v = it.first]){
22
            dis[v] = dis[u] + it.second;
23
            LCA(v);
24
25
            fa[v] = u;
26
        }
27
   }
```

1.5 Tarjan

1.5.1 SCC

```
namespace SCC{
1
2
        vector<int> G[MAXN];
3
        int dfs_clock, scc_cn, dfn[MAXN], low[MAXN], sccno[MAXN];
        stack<int> S;
4
5
        void addEdge(int u, int v) {
6
            G[u].push_back(v);
7
        void tarjan(int u) {
8
            dfn[u] = low[u] = ++dfs\_clock;
9
            S.push(u);
10
            for(auto v : G[u]) {
11
                 if(!dfn[v]) {
12
                    tarjan(v);
13
                     low[u] = min(low[u], low[v]);
14
                }else if(!sccno[v]) {
15
16
                     low[u] = min(low[u], dfn[v]);
17
18
            if(dfn[u] == low[u]) {
19
20
                scc_cnt++;
21
                for(;;) {
                     int v = S.top(); S.pop();
22
                     sccno[v] = scc_cnt;
23
                     if(v == u) break;
24
25
                }
26
            }
27
        void findSCC(int n) {
28
```

```
for(int i = 1; i <= n; i++)</pre>
29
30
                  if(!dfn[i]) tarjan(i);
31
        void init(int n){
32
             dfs_clock = scc_cnt = 0;
33
             for(int i = 0;i <= n;++i){</pre>
34
35
                  dfn[i] = low[i] = sccno[i] = 0;
36
                  G[i].clear();
             }
37
        }
38
    }
39
```

1.5.2 BCC

```
namespace BCC{
 1
 2
         struct Edge {
              int to, nxt;
 3
         e[MAXM << 1];
 4
 5
         int ecnt, head[MAXN];
 6
         int dfs_clock, dfn[MAXN], low[MAXN];
 7
         int is_vertex[MAXN], vbcc_cnt, vbccno[MAXN];
 8
 9
         vector<int> vbcc[MAXN];
10
         stack<int> vS;
11
         int ebcc_cnt, ebccno[MAXN];
12
13
         stack<int> eS;
14
         inline void addEdge(int u, int v) {
    e[++ecnt] = (Edge) {v, head[u]}; head[u] = ecnt;
    e[++ecnt] = (Edge) {u, head[v]}; head[v] = ecnt;
15
16
17
18
         inline void init(int n) {
19
              ecnt = 1;
20
21
              dfs\_clock = 0;
22
              vbcc\_cnt = 0;
23
              ebcc\_cnt = 0;
              for(int i = 1; i <= n; ++i){</pre>
24
                  head[i] = dfn[i] = low[i] = 0;
25
26
                   is_vertex[i] = 0;
27
                  vbccno[i] = 0;
28
                  ebccno[i] = 0;
29
              while(!vS.empty()) vS.pop();
30
         }
31
32
         //root 's edge = -1;
33
         void tarjan(int u, int edge) {
              dfn[u] = low[u] = ++dfs\_clock;
34
35
              int ch = 0;
36
              vS.push(u);
37
              eS.push(u);
              for(int i = head[u], v; i; i = e[i].nxt) {
    if(!dfn[v = e[i].to]) {
38
39
                       tarjan(v, i ^ 1)
40
                       low[u] = min(low[u], low[v]);
41
                       if(low[v] >= dfn[u]) {
42
                            ++ch;
43
                            if(edge > 0 || ch > 1) is_vertex[u] = 1;
44
45
                            vbcc[++vbcc_cnt].clear();
46
                            vbcc[vbcc_cnt].push_back(u);
```

```
for(int x;;){
47
                               x = vS.top();vS.pop();
48
                               vbcc[vbcc_cnt].push_back(x);
49
50
                               vbccno[x] = vbcc_cnt;
51
                               if(x == v)break;
52
53
                      if(low[v] > dfn[u]) {
// i && i ^ 1 is bridge
}
54
55
56
57
                 else if(dfn[v] < dfn[u] && i != edge)</pre>
58
                      low[u] = min(low[u], dfn[v]);
59
60
             if(dfn[u] == low[u]) {
61
                 ebcc_cnt++;
62
                 for(int v;;) {
63
                      v = eS.top(); eS.pop();
64
65
                      ebccno[v] = ebcc_cnt;
                      if(v == u) break;
66
                 }
67
             }
68
69
        void findBCC(int n){
70
71
             for(int i = 1; i <= n; i++)
72
                 if(!dfn[i]) tarjan(i, -1);
73
74
             //findBridge
             for(int u = 1; u <= n; u++) {
75
                  for(int i = head[u], v; i; i = e[i].nxt)
76
                 if(ebccno[u] != ebccno[v = e[i].to]) {
77
78
                      //is bridge
79
            }
80
        }
81
   }
82
```

1.6 Cactus

1.6.1 Circle-Square Tree

```
#include <bits/stdc++.h>
1
2
   using namespace std;
3
   typedef pair<int, int> P;
   const int MAXN = 2e4 + 5;
4
   const int S = 15;
5
6
   namespace Tree {
7
        struct Edge {
8
            int to, nxt, w;
        }e[MAXN << 1];
9
        int ecnt, head[MAXN];
10
        int rt, isrt[MAXN], fa[MAXN][S + 3];
11
        int sz[MAXN];
12
        inline void addEdge(int u, int v, int w) {
13
            e[++ecnt] = (Edge) \{v, head[u], w\}; head[u] = ecnt;
14
            fa[v][0] = u;
15
       }
16
17
   int n, m, Q;
```

```
namespace BCC {
19
20
        struct Edge {
21
            int to, nxt, w;
        }e[MAXN << 1];</pre>
22
        int ecnt, head[MAXN];
23
        int dfs_clock, dfn[MAXN], low[MAXN];
24
25
        int is_vertex[MAXN], vbcc_cnt, vbccno[MAXN];
26
        vector<P> vbcc[MAXN];
        stack<P> vs;
27
        int tag[MAXN];
28
        inline void addEdge(int u, int v, int w) {
29
            e[++ecnt] = (Edge) \{v, head[u], w\}; head[u] = ecnt;
30
            e[++ecnt] = (Edge) \{u, head[v], w\}; head[v] = ecnt;
31
32
33
        inline void init(int n) {
34
            ecnt = 1;
            dfs\_clock = 0;
35
            vbcc\_cnt = 0;
36
            for(int i = 0; i <= 2 * n; i++){</pre>
37
38
                 head[i] = dfn[i] = low[i] = 0;
                 vbccno[i] = 0;
39
                 tag[i] = 0;
40
41
            while(!vs.empty()) vs.pop();
42
        }
43
44
        //root 's edge = -1;
45
        void tarjan(int u, int edge) {
46
            dfn[u] = low[u] = ++dfs\_clock;
47
            vs.push(P(u, e[edge ^ 1].w));
            for(int i = head[u], v; i; i = e[i].nxt) {
   if(!dfn[v = e[i].to]) {
48
49
                     tarjan(v, i ^ 1)
50
                     low[u] = min(low[u], low[v]);
51
                     if(low[v] >= dfn[u]) {
52
                          if(vs.top().first == v) {
53
                              Tree::addEdge(u, v, vs.top().second);
54
                              vs.pop();
55
                              continue;
56
57
58
                          vbcc[++vbcc_cnt].clear();
59
                          vbcc[vbcc_cnt].push_back(P(u, 0));
                          Tree::isrt[u] = 1;
60
                          int &sz = Tree::sz[n + vbcc_cnt];
61
                          tag[vs.top().first] = n + vbcc_cnt;
62
63
                          //Tree::addEdge(u, rt, 0);
                          for(P x;;) {
64
65
                              x = vs.top(); vs.pop();
66
                              sz += x.second;
67
                              //Tree::addEdge(rt, x.first, sz);
                              vbcc[vbcc_cnt].push_back(x);
68
                              vbccno[x.first] = vbcc_cnt;
69
                              if(x.first == v) break;
70
71
                          }
                     }
72
73
                 else if(dfn[v] < dfn[u] && i != edge)</pre>
74
75
                     low[u] = min(low[u], dfn[v]);
76
            for(int i = head[u], v; i; i = e[i].nxt) {
77
                 if(tag[v = e[i].to]) {
78
79
                     int r = tag[v]; Tree::sz[r] += e[i].w;
```

```
tag[v] = 0;
80
                 }
81
82
             }
83
         void findBCC(int n) {
84
             for(int i = 1; i <= n; i++)
85
                 if(!dfn[i]) tarjan(i, -1);
86
87
        }
88
    namespace Tree {
89
         int dis[MAXN], dep[MAXN], len[MAXN];
90
         inline void init(int n) {
91
             BCC::init(n);
92
93
             rt = n;
94
             ecnt = 1;
             for(int i = 0; i <= 2 * n; i++) {
95
                 head[i] = 0;
96
                 fa[i][0] = isrt[i] = dis[i] = dep[i] = len[i] = 0;
97
98
             }
99
         void dfs(int x) {
100
             for(int i = head[x], y; i; i = e[i].nxt) {
101
                 if(!dep[y = e[i].to]) {
102
                      dep[y] = dep[x] + 1;
103
                      dis[y] = dis[x] + e[i].w;
104
105
                      dfs(y);
106
                 }
             }
107
108
         void pre() {
109
             for(int k = 1; k <= BCC::vbcc_cnt; k++) {</pre>
110
111
                  rt++;
                 vector<P> &E = BCC::vbcc[k];
112
                 addEdge(E[0].first, rt, 0);
113
                 int cnt = 0;
114
                 for(int i = E.size() - 1; i >= 1; i--) {
115
                      cnt += E[i].second;
116
                      len[E[i].first] = cnt;
117
                      addEdge(rt, E[i].first, min(cnt, sz[rt] - cnt));
118
119
                 }
120
             for(int k = 1; k <= S; k++) {</pre>
121
                 for(int i = 1; i <= rt; i++) {</pre>
122
                      fa[i][k] = fa[fa[i][k - 1]][k - 1];
123
124
125
             dep[1] = 1;
126
             dfs(1);
127
128
         int up(int x, int d) {
129
             for(int i = S; i >= 0; i--) {
130
                  if(dep[fa[x][i]] >= d) x = fa[x][i];
131
132
             return x;
133
134
         int lca(int u, int v) {
135
             if(dep[u] > dep[v]) swap(u, v);
136
             v = up(v, dep[u]);
137
             if(u == v) return u;
138
             for(int i = S; i >= 0; i--) {
139
                 if(fa[u][i] != fa[v][i]) {
140
```

```
u = fa[u][i], v = fa[v][i];
141
142
               }
143
               return fa[u][0];
144
145
          int query(int u, int v) {
146
               int l = lca(u, v);
if(l <= n) return dis[u] + dis[v] - 2 * dis[l];</pre>
147
148
               int x = up(u, dep[l] + 1), y = up(v, dep[l] + 1);
int res = dis[u] - dis[x] + dis[v] - dis[y];
149
150
               int tmp = abs(len[x] - len[y]);
return res + min(tmp, sz[l] - tmp);
151
152
153
          }
     }
154
155
     int main() {
156
          ios::sync_with_stdio(0); cin.tie(0); cout.precision(6); cout << fixed;</pre>
157
158
          using namespace Tree;
159
          cin >> n >> m >> 0;
          init(n);
160
          for(int i = 1, u, v, w; i <= m; i++) {
161
               cin >> u >> v >> w;
162
               BCC::addEdge(u, v, w);
163
164
165
          BCC::findBCC(n);
          pre();
166
          int u, v;
167
168
          while(Q--) {
169
               cin >> u >> v;
               cout << query(u, v) << endl;</pre>
170
171
172
          return 0;
     }
173
```

2 Data Structures

2.1 Basic Structures

2.1.1 RMQ

```
struct RMQ {
1
        int d[MAXN][S + 2];
2
        inline void init(int *a, int n) {
3
            for(int i = 0; i < n; i++) d[i][0] = a[i];
4
5
            for(int k = 1; (1 << k) < n; k++)
6
                 for(int i = 0; i + (1 << k) - 1 < n; i++)
                     d[i][k] = min(d[i][k - 1], d[i + (1 << (k - 1))][k - 1]);
7
8
9
        inline int query(int 1, int r) {
            if(l > r) swap(l, r);
10
            int k = 0;
11
12
            while((1 << (k + 1)) <= r - l + 1) k++;
            return min(d[l][k], d[r - (1 << k) + 1][k]);</pre>
13
14
   }rmq;
15
    struct RMQ {
16
        LL a[MAXN];
17
        LL d[MAXM][S + 2];
LL pre[MAXM][S + 2], aft[MAXM][S + 2];
18
19
        inline void init(int n) {
20
            for(int i = 1; i <= sz; i++) {</pre>
21
                 pre[i][0] = aft[i][S + 1] = INF;
22
23
            for(int i = 1; i <= n; i++) {</pre>
24
                 pre[belong(i)][pos(i)] = min(pre[belong(i)][pos(i) - 1], a[i]);
25
26
27
            for(int i = n; i >= 1; i--) {
                 aft[belong(i)][pos(i)] = min(aft[belong(i)][pos(i) + 1], a[i]);
28
29
30
            for(int i = 1; i <= sz; i++) {
                 d[i][0] = aft[i][1];
31
32
33
            for(int k = 1; k <= S; k++)</pre>
                 for(int i = 1; i + (1 << k) <= SZ; i++)
34
                     d[i][k] = min(d[i][k - 1], d[i + (1 << (k - 1))][k - 1]);
35
36
        inline LL ask(int l, int r) {
37
            assert(l <= r);</pre>
38
39
            LL res = INF;
            if(belong(l) == belong(r)) {
40
                 for(int i = l; i <= r; i++) res = min(res, a[i]);</pre>
41
42
                 return res;
43
            res = min(aft[belong(l)][pos(l)], pre[belong(r)][pos(r)]);
44
            int k = Log[belong(r) - belong(l) - 1];
45
            if(~k) {
46
                 res = min(res, d[belong(l) + 1][k]);
47
                 res = min(res, d[belong(r) - (1 << k)][k]);
48
49
            return res;
50
51
52
   }rmq;
```

2.1.2 Divide Blocks

```
int belong[MAXN], l[MAXN], r[MAXN];
1
   int sz, num;
3
   void build(int n) {
4
        sz = sqrt(n);
       num = n / sz; if(n % sz) num++;
5
        for(int i = 1; i <= num; i++) {</pre>
6
            l[i] = (i - 1) * sz + 1;
7
            r[i] = i * sz;
8
9
10
        r[num] = n;
        for(int i = 1; i <= n; i++) {
11
            belong[i] = (i - 1) / sz + 1;
12
13
14
```

2.2 Tree Structures

2.2.1 Tree Decomposition

```
int sz[MAXN], dep[MAXN], top[MAXN], fa[MAXN], son[MAXN], num[MAXN], totw;
1
2
   struct Edge {
3
        int to, nxt;
   e[MAXN << 1];
4
   int head[MAXN], ecnt;
5
6
   int n, m, Q;
   #define Ls(x) (x << 1)
7
   #define Rs(x) (x << 1 | 1)
   struct Tree {
9
        int l, r, lazy;
10
        LL sum, mx;
11
12
   }tree[MAXN << 2];</pre>
   int A[MAXN], B[MAXN];
14
   void push_up(int x) {
       tree[x].sum = tree[Ls(x)].sum + tree[Rs(x)].sum;
15
16
       tree[x].mx = max(tree[Ls(x)].mx, tree[Rs(x)].mx);
17
   void push_down(int x) {
18
       if(tree[x].lazy) {
19
20
            tree[Ls(x)].sum += tree[x].lazy * (tree[Ls(x)].r - tree[Ls(x)].l + 1);
21
            tree[Rs(x)].sum += tree[x].lazy * (tree[Rs(x)].r - tree[Rs(x)].l + 1);
22
            tree[Ls(x)].mx += tree[x].lazy;
23
            tree[Rs(x)].mx += tree[x].lazy;
24
            tree[Ls(x)].lazy += tree[x].lazy;
25
            tree[Rs(x)].lazy += tree[x].lazy;
26
            tree[x].lazy = 0;
       }
27
28
   void build(int x, int L, int R) {
29
30
        tree[x].lazy = 0;
        tree[x].l = L; tree[x].r = R;
31
32
        if(L == R) {
33
            tree[x].sum = B[L];
34
            tree[x].mx = B[L];
35
            return;
36
        int mid = (L + R) \gg 1;
37
       build(Ls(x), L, mid);
38
```

```
build(Rs(x), mid + 1, R);
39
40
        push_up(x);
41
   void update(int x, int L, int R, LL val) {
   if(tree[x].l >= L && tree[x].r <= R) {</pre>
42
43
             tree[x].lazy += val;
44
            tree[x].sum += val * (tree[x].r - tree[x].l + 1);
45
            tree[x].mx += val;
46
47
             return;
48
        push_down(x);
49
        int mid = (tree[x].l + tree[x].r) >> 1;
50
        if(L \leftarrow mid) update(Ls(x), L, R, val);
51
        if(R > mid) update(Rs(x), L, R, val);
52
53
        push_up(x);
54
   LL query(int x, int L, int R) {
55
        if(tree[x].1 >= L && tree[x].r <= R)
56
             return tree[x].sum;
57
58
        push_down(x);
        int mid = (tree[x].l + tree[x].r) >> 1;
59
        LL res = 0;
60
        if(L <= mid) res += query(Ls(x), L, R);</pre>
61
62
        if(R > mid) res += query(Rs(x), L, R);
        return res;
63
64
65
   LL query2(int x, int L, int R) {
66
        if(tree[x].l >= L \&\& tree[x].r <= R)
67
             return tree[x].mx;
68
        push_down(x);
        int mid = (tree[x].l + tree[x].r) >> 1;
69
        LL res = -INF;
70
        if(L \le mid) res = max(res, query2(Ls(x), L, R));
71
        if(R > mid) res = max(res, query2(Rs(x), L, R));
72
        return res;
73
   }
74
   inline void add_edge(int x, int y) {
75
        e[++ecnt] = (Edge) \{y, head[x]\}; head[x] = ecnt;
76
77
   void dfs1(int x) {
78
79
        sz[x] = 1; son[x] = 0;
80
        for(int i = head[x]; i; i = e[i].nxt) {
81
             int v = e[i].to;
82
             if(v == fa[x]) continue;
             fa[v] = x;
83
            dep[v] = dep[x] + 1;
84
            dfs1(v);
85
86
             sz[x] += sz[v];
            if(sz[v] > sz[son[x]]) son[x] = v;
87
        }
88
89
    void dfs2(int x) {
90
91
        B[num[x]] = A[x];
        if(son[x]) {
92
             top[son[x]] = top[x];
93
            num[son[x]] = ++totw;
94
95
            dfs2(son[x]);
96
        for(int i = head[x]; i; i = e[i].nxt) {
97
             int v = e[i].to;
98
             if(v == fa[x] || v == son[x]) continue;
99
```

```
top[v] = v;
100
             num[v] = ++totw;
101
             dfs2(v);
102
103
        }
104
    void up(int a, int b, int c) {
105
         int f1 = top[a], f2 = top[b];
106
        while(f1 != f2) {
107
             if(dep[f1] < dep[f2]) { swap(a, b); swap(f1, f2); }
108
109
             update(1, num[f1], num[a], c);
             a = fa[f1];
110
             f1 = top[a];
111
112
         if(dep[a] > dep[b]) swap(a, b);
113
114
        update(1, num[a], num[b], c);
115
    int qsum(int a, int b) {
116
         if(a == b) return query(1, num[a], num[a]);
117
         int f1 = top[a], f2 = top[b];
118
119
         int res = 0;
        while(f1 != f2) {
120
             if(dep[f1] < dep[f2]) { swap(a, b); swap(f1, f2); }</pre>
121
             res += query(1, num[f1], num[a]);
122
             a = fa[f1];
123
             f1 = top[a];
124
125
126
        if(dep[a] > dep[b]) swap(a, b);
127
         res += query(1, num[a], num[b]);
128
         return res;
129
    int qmax(int a, int b) {
130
         if(a == b) return query2(1, num[a], num[a]);
131
         int f1 = top[a], f2 = top[b];
132
         int res = -10000000000;
133
        while(f1 != f2) {
134
             if(dep[f1] < dep[f2]) { swap(a, b); swap(f1, f2); }</pre>
135
136
             res = max(res, query2(1, num[f1], num[a]));
             a = fa[f1];
137
138
             f1 = top[a];
139
         if(dep[a] > dep[b]) swap(a, b);
140
141
         res = max(res, query2(1, num[a], num[b]));
         return res;
142
143
    }
    inline void init() {
144
        memset(head, 0, sizeof(head)); ecnt = 0;
145
146
         fa[1] = 0; dep[1] = 1; top[1] = 1; num[1] = 1; totw = 1;
147
    inline void pre() {
148
149
         dfs1(1); dfs2(1); build(1, 1, totw);
150
```

2.2.2 Link-Cut Tree

```
namespace LCT {
   int fa[MAXN], rev[MAXN], tr[MAXN][2];
   int s[MAXN], val[MAXN];
   void push_up(int x) {
      int l = tr[x][0], r = tr[x][1];
      s[x] = s[l] + s[r] + val[x];
   }
}
```

```
7
        void Rev(int x) {
8
9
            rev[x] = 1; swap(tr[x][0], tr[x][1]);
10
        void push_down(int x) {
11
            if(!rev[x]) return;
12
            int l = tr[x][0], r = tr[x][1];
13
            rev[x] = 0;
14
            if(l) Rev(l); if(r) Rev(r);
15
16
        bool isroot(int x) {
17
            return tr[fa[x]][0] != x && tr[fa[x]][1] != x;
18
19
20
        void pre(int x) {
            if(!isroot(x)) pre(fa[x]);
21
22
            push_down(x);
23
24
        void rotate(int x) {
25
            int y = fa[x]; int z = fa[y];
            int l = tr[y][1] == x;
26
            int r = 1 \wedge 1;
27
            if(!isroot(y)) tr[z][tr[z][1] == y] = x;
28
29
            fa[x] = z; fa[y] = x; fa[tr[x][r]] = y;
            tr[y][l] = tr[x][r]; tr[x][r] = y;
30
31
            push_up(y);
32
33
        void splay(int x) {
            pre(x);
34
            int y, z;
35
            while(!isroot(x)) {
36
                y = fa[x]; z = fa[y];
37
                if(!isroot(y)) {
38
                     if((tr[z][0] == y) == (tr[y][0] == x))rotate(y);
39
                     else rotate(x);
40
41
                rotate(x);
42
43
            }
            push_up(x);
44
45
46
        void access(int x) {
47
            int y = 0;
            while(x) {
48
49
                splay(x); tr[x][1] = y;
                push_up(x);
50
51
                y = x; x = fa[x];
52
53
        void makeroot(int x) {
54
            access(x); splay(x); Rev(x);
55
56
        void lnk(int x, int y) {
57
            makeroot(x); fa[x] = y;
58
59
        void cut(int x, int y) {
60
            makeroot(x); access(y); splay(y);
61
            tr[y][0] = fa[x] = 0; push_up(y);
62
63
        void update(int x, int y) {
64
            makeroot(x); val[x] = y; push_up(x);
65
66
        int query(int x, int y) {
```

```
makeroot(x); access(y); splay(y);
68
69
            return s[y];
70
71
       bool check(int x, int y) {
            int tmp = y;
72
            makeroot(x); access(y); splay(x);
73
            while(!isroot(y)) y = fa[y];
74
            splay(tmp);
75
76
            return x == y;
77
   }
78
```

2.3 Sequence Structures

2.3.1 Segment Tree

```
#define Ls(x) (x << 1)
1
2
   #define Rs(x) (x << 1 | 1)
3
   struct Tree {
        int l, r, lazy;
4
5
        LL sum, mx;
   }tree[MAXN << 2];</pre>
6
7
   int A[MAXN];
8
   void push_up(int x) {
        tree[x].sum = tree[Ls(x)].sum + tree[Rs(x)].sum;
9
10
        tree[x].mx = max(tree[Ls(x)].mx, tree[Rs(x)].mx);
11
   void push_down(int x) {
12
        if(tree[x].lazy) {
13
            tree[Ls(x)].sum += tree[x].lazy * (tree[Ls(x)].r - tree[Ls(x)].l + 1);
14
            tree[Rs(x)].sum += tree[x].lazy * (tree[Rs(x)].r - tree[Rs(x)].l + 1);
15
            tree[Ls(x)].mx += tree[x].lazy;
16
            tree[Rs(x)].mx += tree[x].lazy;
17
            tree[Ls(x)].lazy += tree[x].lazy;
18
            tree[Rs(x)].lazy += tree[x].lazy;
19
20
            tree[x].lazy = 0;
21
        }
22
   }
23
   void build(int x, int L, int R) {
24
        tree[x].lazy = 0;
        tree[x].l = L; tree[x].r = R;
25
26
        if(L == R) {
27
            tree[x].sum = A[L];
28
            tree[x].mx = A[L];
            return;
29
30
31
        int mid = (L + R) \gg 1;
        build(Ls(x), L, mid);
build(Rs(x), mid + 1, R);
32
33
34
        push_up(x);
35
36
   void update(int x, int L, int R, LL val) {
        if(tree[x].l >= L && tree[x].r <= R) {</pre>
37
            tree[x].lazy += val;
38
            tree[x].sum += val * (tree[x].r - tree[x].l + 1);
39
            tree[x].mx += val;
40
41
            return;
42
        push_down(x);
```

```
int mid = (tree[x].l + tree[x].r) >> 1;
44
        if(L \leftarrow mid) update(Ls(x), L, R, val);
45
46
        if(R > mid) update(Rs(x), L, R, val);
47
        push_up(x);
48
49
   LL query(int x, int L, int R) {
        if(tree[x].l >= L && tree[x].r <= R)
50
            return tree[x].sum;
51
52
        push_down(x);
        int mid = (tree[x].l + tree[x].r) >> 1;
53
        LL res = 0;
54
        if(L <= mid) res += query(Ls(x), L, R);</pre>
55
        if(R > mid) res += query(Rs(x), L, R);
56
57
        return res;
58
   LL query2(int x, int L, int R) {
59
        if(tree[x].l >= L && tree[x].r <= R)
60
            return tree[x].mx;
61
        push_down(x);
62
        int mid = (tree[x].l + tree[x].r) >> 1;
63
        LL res = -INF;
64
        if(L \le mid) res = max(res, query2(Ls(x), L, R));
65
        if(R > mid) res = max(res, query2(Rs(x), L, R));
66
67
        return res;
   }
68
```

2.3.2 Splay Tree

```
namespace splay{
2
        int n, m, sz, rt;
        int val[MAXN], id[MAXN];
int tr[MAXN][2], size[MAXN], fa[MAXN], rev[MAXN], s[MAXN], lazy[MAXN];
3
4
5
        void push_up(int x) {
            int l = tr[x][0], r = tr[x][1];
6
7
            s[x] = max(val[x], max(s[l], s[r]));
8
             size[x] = size[l] + size[r] + 1;
9
        void push_down(int x) {
10
             int l = tr[x][0], r = tr[x][1];
11
             if(lazy[x]) {
12
13
                 if(1) {
                     lazy[l] += lazy[x];
14
                     s[l] += lazy[x];
15
                     val[l] += lazy[x];
16
17
                 if(r) {
18
                     lazy[r] += lazy[x];
19
20
                     s[r] += lazy[x];
                     val[r] += lazy[x];
21
22
                 lazy[x] = 0;
23
24
            if(rev[x]) {
25
                 rev[x] = 0;
26
                 rev[l] ^= 1; rev[r] ^= 1;
27
                 swap(tr[x][0], tr[x][1]);
28
29
            }
30
31
        void rotate(int x, int &k) {
32
            int y = fa[x];
```

```
33
            int z = fa[y];
34
            int l, r;
            if(tr[y][0] == x) l = 0;
35
            else l = 1;
36
            r = l \wedge 1;
37
            if(y == k) k = x;
38
            else {
39
                 if(tr[z][0] == y) tr[z][0] = x;
40
41
                 else tr[z][1] = x;
42
            fa[x] = z; fa[y] = x; fa[tr[x][r]] = y;
43
            tr[y][l] = tr[x][r]; tr[x][r] = y;
44
            push_up(y); push_up(x);
45
46
47
        void splay(int x, int &k) {
            int y, z;
48
            while(x != k) {
49
                y = fa[x];
50
                 z = fa[y];
51
52
                 if(y != k) {
                     if((tr[y][0] == x) \land (tr[z][0] == y)) rotate(x, k);
53
54
                     else rotate(y, k);
55
                 rotate(x, k);
56
            }
57
58
59
        int find(int x, int rank) {
            push_down(x);
60
            int l = tr[x][0], r = tr[x][1];
61
62
            if(size[l] + 1 == rank) return x;
            else if(size[l] >= rank) return find(l, rank);
63
            else return find(r, rank - size[l] - 1);
64
65
        void update(int l, int r, int v) {
66
            int x = find(rt, 1), y = find(rt, r + 2);
67
            splay(x, rt); splay(y, tr[x][1]);
68
69
            int z = tr[y][0];
            lazy[z] += v;
70
71
            val[z] += v;
72
            S[z] += V;
73
        void reverse(int 1, int r) {
74
            int x = find(rt, l), y = find(rt, r + 2);
75
76
            splay(x, rt); splay(y, tr[x][1]);
77
            int z = tr[y][0];
            rev[z] ^= 1;
78
79
        void query(int 1, int r) {
80
            int x = find(rt, 1), y = find(rt, r + 2);
81
            splay(x, rt); splay(y, tr[x][1]);
int z = tr[y][0];
82
83
            printf("%d\n", s[z]);
84
85
        void build(int l, int r, int f) {
86
            if(l > r) return;
87
            int now = id[l], last = id[f];
88
            if(l == r) {
89
                 fa[now] = last; size[now] = 1;
90
                 if(1 < f) tr[last][0] = now;
91
                 else tr[last][1] = now;
92
93
                 return;
```

```
94
             int mid = (l + r) \gg 1; now = id[mid];
95
             build(l, mid - 1, mid); build(mid + 1, r, mid);
96
97
             fa[now] = last;
             push_up(now);
98
             if(mid < f) tr[last][0] = now;</pre>
99
100
             else tr[last][1] = now;
101
         void init() {
102
             s[0] = -INF;
103
             scanf("%d%d", &n, &m);
104
             for(int i = 1; i <= n + 2; i++) id[i] = ++sz;
105
106
             build(1, n + 2, 0); rt = (n + 3) >> 1;
107
         }
108
    }
```

2.4 Persistent Data Structures

2.4.1 Chairman Tree

```
struct Node {
1
2
       int l, r;
3
        LL sum;
4
   }t[MAXN * 40];
5
   int cnt, n;
6
   int rt[MAXN];
   void update(int pre, int &x, int l, int r, int v) {
7
       x = ++cnt; t[x] = t[pre]; t[x].sum++;
8
        if(l == r) return;
9
        int mid = (l + r) \gg 1;
10
        if(v \le mid) update(t[pre].l, t[x].l, l, mid, v);
11
        else update(t[pre].r, t[x].r, mid + 1, r, v);
12
   }
13
   int query(int x, int y, int l, int r, int v) {
14
        if(l == r) return l;
15
16
        int mid = (l + r) >> 1;
17
        int sum = t[t[y].l].sum - t[t[x].l].sum;
        if(sum >= v) return query(t[x].1, t[y].1, 1, mid, v);
18
19
        else return query(t[x].r, t[y].r, mid + 1, r, v - sum);
20
```

2.4.2 Persistent Trie

```
//区间异或最值查询
1
2
   const int N=5e4+10;
3
   int t[N];
   int ch[N*32][2],val[N*32];
4
5
   int cnt;
6
   void init(){
7
       mem(ch,0)
8
       mem(val,0);
9
       cnt=1;
   }
10
   int add(int root,int x){
11
        int newroot=cnt++,ret=newroot;
12
13
        for(int i=30;i>=0;i--){
14
            ch[newroot][0]=ch[root][0];
15
            ch[newroot][1]=ch[root][1];
```

```
int now=(x>>i)&1;
16
            root=ch[root][now];
17
18
            ch[newroot][now]=cnt++;
19
            newroot=ch[newroot][now];
20
            val[newroot]=val[root]+1;
        }
21
22
        return ret;
   }
int query(int lt,int rt,int x){
23
24
25
        int ans=0;
        for(int i=30;i>=0;i--){
26
            int now=(x>>i)&1;
27
            if(val[ch[rt][now^1]]-val[ch[lt][now^1]]){
28
29
                ans l = (1 << i);
                 rt=ch[rt][now^1];
30
                lt=ch[lt][now^1];
31
32
                } else{
                rt=ch[rt][now];
33
                lt=ch[lt][now];
34
            }
35
36
37
        return ans;
38
```

3 String

3.1 Basics

3.1.1 Hash

```
const LL p1 = 201, p2 = 301, mod1 = 12000000319, mod2 = 2147483647;
   struct Hash {
2
3
        LL a, b;
        void append(Hash pre, int v) {
4
5
            a = (pre.a * p1 + v) \% mod1;
            b = (pre.b * p2 + v) \% mod2;
6
7
        void init(string S) {
8
9
            a = b = 0;
            for(int i = 0; i < S.size(); i++) append(*this, S[i]);</pre>
10
11
12
        bool operator == (const Hash &x) const {
13
            return a == x.a \&\& b == x.b;
14
15
        bool operator < (const Hash &x) const {</pre>
16
            return a < x.a | | (a == x.a \& b < x.b);
17
        }
18
   };
```

3.1.2 KMP && exKMP

```
namespace KMP {
1
        int fa[MAXN];
2
3
        void get_fail(char* t, int tn) {
4
            fa[0] = -1;
5
            int i = 0, j = -1;
6
            while(i < tn) {</pre>
7
                 if (j == -1 || t[i] == t[j]) {
8
                     ++i; ++j;
9
                     fa[i] = t[i] != t[j] ? j : fa[j];
                 }else{
10
                     j = fa[j];
11
12
                 }
            }
13
14
15
        void kmp(char* s, int sn, char* t, int tn) {
16
            int i = 0, j = 0;
            while(i < sn) {</pre>
17
18
                 if (j == -1 || s[i] == t[j]) {
19
                     i++;j++;
20
                     if(j == tn) {
21
22
                 }else j = fa[j];
23
            }
        }
24
25
   }
26
   namespace exKMP {
27
        int nxt[MAXN], ext[MAXN];
28
        void get_nxt(char* t, int tn) {
29
            int j = 0, mx = 0;
            nxt[0] = tn;
30
            for(int i = 1; i < tn; i++) {</pre>
31
```

```
if(i \ge mx \mid | i + nxt[i - j] \ge mx) {
32
33
                     if(i > mx) mx = i;
34
                     while(mx < tn && t[mx] == t[mx - i]) mx++;
                     nxt[i] = mx - i;
35
                     j = i;
36
                 }else nxt[i] = nxt[i - j];
37
            }
38
39
        void exkmp(char *s, int sn, char *t, int tn) {
40
            int j = 0, mx = 0;
41
            for(int i = 0; i < sn; i++) {</pre>
42
                 if(i >= mx || i + nxt[i - j] >= mx) {
43
                     if(i > mx) mx = i;
44
                     while(mx < sn && mx - i < tn && s[mx] == t[mx - i]) mx++;
45
46
                     ext[i] = mx - i;
47
                     j = i;
                 }else ext[i] = nxt[i - j];
48
49
            }
        }
50
51
   }
```

3.1.3 AC Automaton

```
namespace AC {
1
        int ch[MAXN][sigma_size], last[MAXN];
2
3
        int val[MAXN], f[MAXN], sz;
        inline void init() { sz = 1; memset(ch[0], 0, sizeof(ch[0])); }
4
        inline int idx(char c) { return c - 'a'; }
5
6
        void insert(string s, int v) {
7
            int u = 0;
            for(int i = 0; i < s.size(); i++) {</pre>
8
                 int c = idx(s[i]);
9
10
                 if(!ch[u][c]) {
                     memset(ch[sz], 0, sizeof(ch[sz]));
11
                     val[sz] = 0;
12
                     ch[u][c] = sz++;
13
14
                u = ch[u][c];
15
16
17
            val[u] = v;
18
        void get_fail() {
19
            queue<int> q;
20
            f[0] = 0;
21
            for(int c = 0; c < sigma_size; c++) {</pre>
22
23
                 int u = ch[0][c];
24
                 if(u) { f[u] = 0; q.push(u); last[u] = 0; }
25
            while(!q.empty()) {
26
27
                 int r = q.front(); q.pop();
28
                 for(int c = 0; c < sigma_size; c++) {</pre>
29
                     int u = ch[r][c]
                     if(!u) { ch[r][c] = ch[f[r]][c]; continue; }
30
31
                     q.push(u);
                     int v = f[r];
32
                     while(v && !ch[v][c]) v = f[v];
33
                     f[u] = ch[v][c]
34
35
                     last[u] = val[f[u]] ? f[u] : last[f[u]];
36
                }
37
```

```
38
39
        inline void solve(int j) {
40
            if(j) {
                 ans += val[j];
41
42
                 solve(last[j]);
43
44
        void find(string T) {
45
46
             int j = 0;
             for(int i = 0; i < T.size(); i++) {</pre>
47
                 int c = idx(T[i]);
48
                 j = ch[j][c];
49
                 if(val[j]) solve(j);
50
                 else if(last[j]) solve(last[j]);
51
52
            }
53
        }
   }
54
55
    namespace AC {
56
        int root, tcnt;
        int ch[MAXN][sigma_size], fa[MAXN];
57
58
        inline int newnode() {
            fa[++tcnt] = 0;
59
             for(int i = 0; i < sigma_size; ++i) ch[tcnt][i] = 0;
60
            return tcnt;
61
62
        inline void init() {
63
64
            tcnt = -1;
65
            root = newnode();
66
        inline int idx(char c) { return c - 'a'; }
67
        void extend(char *s, int sn) {
68
69
            int cur = root;
            for(int i = 0, c; i < sn; i++) {</pre>
70
                 if(!ch[cur][c = idx(s[i])])
71
                     ch[cur][c] = newnode();
72
                 cur = ch[cur][c];
73
            }
74
        }
75
76
        int q[MAXN], qh, qt;
77
        void get_fail() {
78
            qh = 1; qt = 0;
79
            fa[root] = 0;
80
             for(int c = 0, now; c < sigma_size; c++)</pre>
                 if((now = ch[root][c]) != 0)
81
                     q[++qt] = now;
82
            while(qh <= qt) {</pre>
83
84
                 int cur = q[qh++];
                 for(int c = 0, now; c < sigma_size; c++)</pre>
85
                     if((now = ch[cur][c]) != 0) {
86
                          fa[now] = ch[fa[cur]][c];
87
88
                          q[++qt] = now;
                     }else
89
                          ch[cur][c] = ch[fa[cur]][c];
90
            }
91
92
    //统计模板串出现次数,每个模板串只计算一次
93
94
            int \ cur = root, \ ans = 0;
             for(int i = 0; i < sn; ++i) {
95
                 cur = ch[cur][idx(s[i])];
96
97
                 for(int \ j = cur; \ j \ \&\& \ cnt[j] \ != -1; \ j = fa[j]) \ \{
98
                     ans \neq = cnt/j/;
```

3.1.4 Minimum String

```
namespace minstring{
          int getmin(char *s, int sn) {
   int i = 0, j = 1, k = 0, t;
   while(i < sn && j < sn && k < sn) {</pre>
2
3
4
                     t = s[(i + k) % sn] - s[(j + k) % sn];
5
6
                     if(!t) k++;
7
                     else {
                           if(t > 0) i += k + 1; else j += k + 1;
8
9
                          if(i == j) j++;
                           k = 0;
10
11
12
               }
13
               return i < j ? i : j;</pre>
14
15
```

3.2 Suffix Related

3.2.1 Suffix Array

```
namespace SA {
2
        char s[MAXN];
3
        int sa[MAXN], rank[MAXN], height[MAXN];
        int t[MAXN], t2[MAXN], c[MAXN], n;
4
       void clear() { n = 0; memset(sa, 0, sizeof(sa)); }
5
6
        void build(int m) {
            int *x = t, *y = t2;
7
            for(int i = 0; i < m; i++) c[i] = 0;
8
9
            for(int i = 0; i < n; i++) c[x[i] = s[i]]++;
10
            for(int i = 1; i < m; i++) c[i] += c[i - 1];
            for(int i = n - 1; i \ge 0; i--) sa[--c[x[i]]] = i;
11
            for(int k = 1; k <= n; k <<= 1) {</pre>
12
                int p = 0;
13
                for(int i = n - k; i < n; i++) y[p++] = i;
14
                for(int i = 0; i < n; i++) if(sa[i] >= k) y[p++] = sa[i] - k;
15
16
                for(int i = 0; i < m; i++) c[i] = 0;
17
                for(int i = 0; i < n; i++) c[x[y[i]]]++;
18
                for(int i = 1; i < m; i++) c[i] += c[i - 1];
                for(int i = n - 1; i \ge 0; i--) sa[--c[x[y[i]]]] = y[i];
19
                swap(x, y);
20
                p = 1; x[sa[0]] = 0;
21
                for(int i = 1; i < n; i++)</pre>
22
                    x[sa[i]] = y[sa[i - 1]] == y[sa[i]] && y[sa[i - 1] + k] == y[sa[i] + k]
23
       ? p - 1 : p++;
                if(p >= n) break;
24
25
                m = p;
26
            }
27
28
        void buildHeight() {
29
            int k = 0;
```

```
for(int i = 0; i < n; i++) rank[sa[i]] = i;</pre>
30
             for(int i = 0; i < n; i++) {</pre>
31
32
                  if(k) k--;
                 int j = sa[rank[i] - 1];
33
                 while(s[i + k] == s[j + k]) k++;
34
                 height[rank[i]] = k;
35
             }
36
37
        void init() {
38
             n = strlen(s) + 1;
39
             build(z' + 1);
40
             buildHeight();
41
        }
42
43
    }
```

3.2.2 Suffix Automaton

```
namespace SAM{
1
2
        int scnt, root, last;
        int fa[MAXN<<1], len[MAXN<<1], ch[MAXN<<1][26];</pre>
3
4
        int sc[MAXN<<1], tmpl[MAXN<<1], minl[MAXN<<1];</pre>
5
6
        int newnode(int _len, int q = 0) {
            fa[++scnt] = fa[q]; len[scnt] = _len;
7
8
            sc[scnt] = 0;tmpl[scnt] = 0; minl[scnt] = INF;
9
            for(int i = 0; i < 26; i++) ch[scnt][i] = ch[q][i];
10
            return scnt;
11
12
        void init() {
13
            scnt = 0;
14
            root = last = newnode(0);
15
        void extend(int c) {
16
            int p = last, np = newnode(len[p] + 1);
17
            for(;p \&\& ch[p][c] == 0; p = fa[p]) ch[p][c] = np;
18
            if(!p) fa[np] = root;
19
20
            else{
                 int q = ch[p][c];
21
                 if(len[p] + 1 == len[q]) fa[np] = q;
22
23
24
                     int nq = newnode(len[p] + 1, q);
25
                     fa[np] = fa[q] = nq;
                     for(; p && ch[p][c] == q; p = fa[p]) ch[p][c] = nq;
26
                 }
27
28
29
            last = np;
30
        int c[MAXN], rs[MAXN << 1];</pre>
31
32
        void radix_sort(int n){
33
            for(int i = 0; i <= n; i++) c[i] = 0;
            for(int i = 1; i <= scnt; i++) c[len[i]]++;</pre>
34
            for(int i = 1; i <= n; i++) c[i] += c[i-1];</pre>
35
            for(int i = scnt; i >= 1; i--) rs[c[len[i]]--] = i;
36
37
        void go(){
38
            scanf("%s",s);
39
            int n = strlen(s);
40
41
            for(int i = 0; i < n; ++i)</pre>
42
                 extend(s[i] - 'a');
43
            radix_sort(n);
```

```
//以下sc集合意义不同
44
            {//每个节点对应的位置之后有多少个不同子串
45
46
                for(int i = scnt; i >= 1; i--) {
                    int S = 0;
47
                    for(int j = 0; j < 26; j++)
48
                        S += sc[ch[rs[i]][j]];
49
                    sc[rs[i]] = S + 1;
50
                }
51
52
            {//right集合大小
53
                int cur = root;
54
                for(int i = 0; i < n; ++i) {</pre>
55
                    cur = ch[cur][s[i] - 'a'];
56
57
                    sc[cur]++;
58
                for(int i = scnt; i >= 1; --i) {
59
                    sc[ fa[rs[i]] ] += sc[rs[i]];
60
61
62
63
            //公共子串
64
            //tmpl,当前字符串:在状态cur,与模板串的最长公共后缀
            //minl, 多个字符串:在状态cur,与模板串的最长公共后缀
65
            //注意:在状态cur匹配成功时,cur的祖先状态与字符串的最长公共后缀
66
            for(; ~scanf("%s",s);) {
67
                int cur = root, Blen = 0;
68
69
                for(int i = 0; i <= scnt; i++)</pre>
70
                    tmpl[i] = 0;
                n = strlen(s);
71
72
                for(int i = 0, x; i < n; i++) {
                    x = s[i] - a';
73
                    if(ch[cur][x]) {
74
75
                        ++Blen;
                        cur = ch[cur][x];
76
                    }else{
77
                        for(; cur \&\& ch[cur][x] == 0; cur = fa[cur]);
78
79
                        if(cur) {
                            Blen = len[cur] + 1;
80
                            cur = ch[cur][x];
81
82
                        }else{
83
                            cur = root; Blen = 0;
84
85
                    tmpl[cur] = max(tmpl[cur], Blen);
86
87
                for(int i = scnt; i ; --i) {
88
                    if( tmpl[ fa[rs[i]] ] < tmpl[ rs[i] ])</pre>
89
90
                        tmpl[ fa[rs[i]] ] = len[ fa[rs[i]] ];
                    minl[ rs[i] ] = min(minl[ rs[i] ], tmpl[ rs[i] ]);
91
92
                }
93
            }
94
95
    namespace exSAM{
96
97
        int scnt, root;
        int fa[MAXN<<1], len[MAXN<<1], ch[MAXN<<1][26];</pre>
98
        int sc[MAXN<<1], tmpl[MAXN<<1];</pre>
99
100
        int newnode(int _len, int q = 0) {
101
            fa[++scnt] = fa[q]; len[scnt] = _len;
102
            sc[scnt] = 0;tmpl[scnt] = 0; minl[scnt] = INF;
103
104
            for(int i = 0; i < 26; i++) ch[scnt][i] = ch[q][i];
```

```
105
            return scnt;
106
         void init() {
107
108
             scnt = 0;
             root = newnode(0);
109
110
         int work(int p,int c){
111
112
             int q = ch[p][c];
             int nq = newnode(len[p] + 1, q);
113
             fa[q] = nq;
114
             for(; p \& ch[p][c] == q; p = fa[p]) ch[p][c] = nq;
115
             return nq;
116
117
         int extend(int p, int c) {
118
119
             if (ch[p][c]){
120
                  int q = ch[p][c];
                  if (len[p] + 1 == len[q]) return q;
121
122
                  return work(p, c);
123
             }
             int np = newnode(len[p] + 1);
124
             for(;p \&\& ch[p][c] == 0; p = fa[p]) ch[p][c] = np;
125
             if (!p) fa[np] = root;
126
             else{
127
                  int q = ch[p][c];
128
129
                  if (len[p] + 1 == len[q]) fa[np] = q;
130
                  else fa[np] = work(p, c);
             }
131
132
             return np;
133
         void solve() {
134
             int n; scanf("%d",&n);
135
             for(int i = 1; i <= n; i++) {
    scanf("%s", s);</pre>
136
137
                  int sn = strlen(s);
138
                  int last = root;
139
                  for(int j = 0; j < sn; ++j)
140
                      last = extend(last, s[j] - 'a');
141
142
             }
143
         }
144
```

3.3 Palindrome Related

3.3.1 Manacher

```
namespace Manachar {
 1
 2
            char S[MAXN << 1];</pre>
3
            int scnt, ans;
           int p[MAXN << 1]; //p[i] - 1
void init(char *s0, int sn0) {
    S[0] = '$'; S[1] = '#';
    for(int i = 0; i < sn0; i++) {</pre>
 4
 5
 6
 7
                         S[2 * i + 2] = s0[i];
 8
                        S[2 * i + 3] = '\#';
9
10
                  scnt = sn0 * 2 + 2;
11
                  S[scnt] = \frac{1}{2};
12
13
           void manachar() {
14
```

STRING 36

```
int id = 0, mx = 0;
15
16
            for(int i = 1; i < scnt; i++) {</pre>
                 p[i] = mx > i ? min(p[2 * id - i], mx - i) : 1;
17
18
                 while(S[i + p[i]] == S[i - p[i]]) p[i]++;
19
                 if(i + p[i] > mx) {
20
                     mx = i + p[i];
21
                     id = i;
                 }
22
            }
23
        }
24
   }
25
```

3.3.2 Palindromic Automaton

```
namespace PAM {
1
       int scnt, S[MAXN];
2
3
       int pcnt, last, len[MAXN], fail[MAXN], ch[MAXN][26];
       int cnt[MAXN]; //节点i表示的本质不同的串的个数(调用count())
4
5
       int\ num[MAXN];\ //以节点i表示的最长回文串的最右端点为回文串结尾的回文串个数
6
       int newnode(int _len) {
7
           len[pcnt] = _len;
8
           cnt[pcnt] = num[pcnt] = 0;
           for(int i = 0; i < 26; i++) ch[pcnt][i] = 0;
9
10
           return pcnt++;
11
       inline void init() {
12
           S[scnt = 0] = -1;
13
           pcnt = 0;newnode(0);newnode(-1);
14
           fail[0] = 1; last = 0;
15
16
       int getfail(int x) {
17
           while(S[scnt - len[x] - 1] != S[scnt]) x = fail[x];
18
19
           return x;
20
21
       void extend(int c) {
22
           S[++scnt] = c;
23
           int cur = getfail(last);
           if(!ch[cur][c]) {
24
               int now = newnode(len[cur] + 2);
25
               fail[now] = ch[getfail(fail[cur])][c];
26
27
               ch[cur][c] = now;
28
               num[now] = num[fail[now]] + 1;
29
           last = ch[cur][c];
30
           cnt[last]++;
31
32
33
       void count() {
           for(int i = pcnt - 1; i >= 0; i--) cnt[fail[i]] += cnt[i];
34
35
       }
36
   };
```

4 Math

4.1 Algebra

4.1.1 FFT

```
const double pi = acos(-1.0);
   const int MAXN = 300003;
   struct comp {
4
        double x, y;
        comp operator + (const comp a) const { return (comp) \{x + a.x, y + a.y\}; }
5
6
        comp operator - (const comp a) const { return (comp) {x - a.x, y - a.y}; }
        comp operator * (const comp a) const { return (comp) \{x * a.x - y * a.y, x * a.y + y\}
7
        * a.x}; }
8
   };
   int rev[MAXN], T;
9
   comp tmp;
10
   void fft(comp *a, int r) {
11
12
        if(r == -1) for(int i = 0; i < T; i++) a[i] = a[i] * a[i];
        for(int i = 0; i < T; i++) if(rev[i] > i) swap(a[rev[i]], a[i]);
13
14
        for(int i = 2, mid = 1; i <= T; mid = i, i <<= 1) {
            comp step = (comp) \{\cos(pi / mid), r * \sin(pi / mid)\};
15
            for(int j = 0; j < T; j += i) {
16
                 comp cur = (comp) \{1, 0\};
17
                 for(int k = j; k < j + mid; k++, cur = cur * step) {
    tmp = a[k + mid] * cur;</pre>
18
19
                     a[k + mid] = a[k] - tmp;
20
                     a[k] = a[k] + tmp;
21
                }
22
            }
23
24
25
        if(r == -1) for(int i = 0; i < T; i++) a[i].y = (int)(a[i].y / T / 2 + 0.5);
26
   }
27
   int n, m;
   comp A[MAXN];
28
29
   void init() {
        for(T = 1; T \le n + m; T \le 1);
30
31
        for(int i = 1; i < T; i++) {</pre>
32
            if(i & 1) rev[i] = (rev[i >> 1] >> 1) ^ (T >> 1);
33
            else rev[i] = rev[i >> 1] >> 1;
34
        }
35
   }
```

4.1.2 NTT

```
const int MAXN = 300005, G = 3, mod = 998244353; //or (479LL << 21) + 1
   int rev[MAXN], T;
   LL qpow(LL x, LL y) {
3
       LL res = 1;
4
       while(y) {
5
           if(y \& 1) res = res * x % mod;
6
7
           x = x * x % mod;
8
           y >>= 1;
9
       }
10
       return res;
11
   }
   void ntt(LL *a, int r) {
   if(r == -1) for(int i = 0; i < T; i++) A[i] = A[i] * B[i] % mod;
```

```
for(int i = 0; i < T; i++) if(rev[i] > i) swap(a[rev[i]], a[i]);
14
        for(int i = 2, mid = 1; i <= T; mid = i, i <<= 1) {
15
             LL gn = qpow(G, (mod - 1) / i);
16
17
             if(r == -1) gn = qpow(gn, mod - 2);
             for(int j = 0; j < T; j += i) {
18
                 LL cur = 1, tmp;
19
                 for(int k = j; k < j + mid; k++, cur = cur * gn % mod) {
    tmp = a[k + mid] * cur % mod;</pre>
20
21
                      a[k + mid] = ((a[k] - tmp) \% mod + mod) \% mod;
22
                      a[k] = (a[k] + tmp) \% mod;
23
                 }
24
            }
25
26
        if(r == -1) {
27
             LL inv = qpow(T, mod - 2);
28
             for(int i = 0; i < T; i++) a[i] = a[i] * inv % mod;
29
30
        }
   }
31
   int n, m;
32
  LL A[MAXN], B[MAXN];
33
   void init() {
34
        for(T = 1; T \le n + m; T \le 1);
35
        for(int i = 0; i < T; i++) {</pre>
36
            if(i & 1) rev[i] = (rev[i >> 1] >> 1) ^ (T >> 1);
37
38
            else rev[i] = rev[i >> 1] >> 1;
39
        }
40
   }
```

4.1.3 FWT

```
void FWT(LL *a,int n) {
        for(int i = 2;i <= n; i <<= 1) {
2
             for(int j = 0; j < n; j += i) {
   for(int d = 0, w = i >> 1; d < w; d++){</pre>
3
4
                     LL u = a[j + d], v = a[j + d + w];
5
6
                     //xor: a[j + d] = u + v, a[j + d + w] = u - v;
                     //and: a[j + d] = u + v;
7
8
                     //or : a[j + d + w] = u + v;
9
                 }
            }
10
        }
11
12
   void UFWT(LL *a, int n) {
13
        for(int i = 2; i <= n; i <<= 1) {</pre>
14
             for(int j = 0; j < n; j += i) {
15
                 for(int d = 0, w = i >> 1; d < w; d++) {
16
                     LL u = a[j + d], v = a[j + d + w];
17
                     //xor: a[j+d] = (u+v) / 2, a[j+d+w] = (u-v) / 2;
18
19
                     //and: a[j + d] = u - v;
                     //or : a[j + d + w] = v - u;
20
21
                 }
22
            }
        }
23
24
   void solve(int n) {
25
        FWT(a, n); FWT(b, n);
26
        for(int i = 0; i < n; i++) a[i] = a[i] * b[i];
27
        UFWT(a, n);
28
29
   }
```

4.1.4 Linear Basis

```
//dynamic
1
   const int D = 60;
3
   struct Basis {
4
        vector<int> ind;
5
        vector<LL> base;
6
        Basis() {
            ind.resize(D, -1);
7
8
            base.resize(D);
9
10
        bool update(LL x, int id) {
            for(int i = 0; i < D; i++) if(~ind[i] && x >> i & 1) {
11
12
                x \sim base[i];
13
            if(!x) return 1;
14
            int pos = __builtin_ctzll(x);
15
            ind[pos] = id;
16
17
            base[pos] = x;
            return 0;
18
19
        }
20
   };
   //array
21
22
   int Gauss(int n, int m) {
        int num = 1;
23
        for(int x = 1; x <= n && x <= m; x++) {
24
25
            int t = 0;
            for(int j = x; j \le m; j++) if(g[j][x]) { t = j; break; }
26
27
            if(t) {
                swap(g[x], g[t]);
28
29
                for(int i = x + 1; i \le n; i++) {
                     if(g[i][x]) {
30
                         for(int k = 1; k \le m; k++) g[i][k] ^= g[x][k];
31
32
33
                }
34
                num++;
35
            }
36
        return --num;
37
   }
38
39
    //long long
   int Gauss() {
40
        int num = 1;
41
42
        for(int k = 61; k >= 0; k--) {
43
            int t = 0;
44
            for(int j = num; j \le cnt; j++) if((A[j] >> k) & 1) { t = j; break; }
45
            if(t) {
46
                swap(A[t], A[num]);
                for(int j = num + 1; j <= cnt; j++) if((A[j] >> k) & 1) A[j] ^- A[num];
47
48
                num++;
49
            }
        }
50
51
        return --num;
52
   }
```

4.2 Math Theory

4.2.1 Inverse

```
1
   //O(logn)求n的逆元
   const int mod = 1e6 + 3;
2
   int exgcd(int a, int b, int &x, int &y) {
3
        int d = a;
4
        if(b != 0) {
5
6
            d = exgcd(b, a \% b, y, x);
7
            y -= (a / b) * x;
8
9
        else {
            x = 1; y = 0;
10
11
12
        return d;
13
   int inverse(int a) {
14
15
        int x, y;
        exgcd(a, mod, x, y);
16
        return (x % mod + mod) % mod;
17
18
19
   int inverse(int a) { return qpow(a, mod - 2); }
20
   //O(n) 求1~n的 逆元
   int inv[MAXN];
21
   void init() {
22
23
        inv[0] = inv[1] = 1;
        for(int i = 2; i < MAXN; i++) inv[i] = (long long)(mod - mod / i) * inv[mod % i] %</pre>
24
       mod;
25
   }
```

4.2.2 Lucas

```
//mod很小可以预处理逆元的情况
2
   void init() {
3
        fac[0] = 1;
        for(int i = 1; i < mod; i++) fac[i] = (long long)fac[i - 1] * i % mod;
4
        inv[0] = inv[1] = 1;
5
        for(int i = 2; i < mod; i++) inv[i] = (long long)(mod - mod / i) * <math>inv[mod \% i] \%
6
       mod;
        for(int i = 1; i < mod; i++) inv[i] = (long long)inv[i] * <math>inv[i - 1] % mod;
7
   }
8
9
   int C(int a, int b) {
10
        if(b > a) return 0;
        if(a < mod) return (long long)fac[a] * inv[b] % mod * inv[a - b] % mod;</pre>
11
        return (long long)C(a / mod, b / mod) * C(a % mod, b % mod) % mod;
12
13
    //mod过大不能预处理逆元的情况
14
   LL qpow(LL x, LL y) {
15
16
        LL res = 1;
17
       while(y) {
18
           if(y \& 1) res = res * x % mod;
            x = x * x % mod;
19
20
            y >>= 1;
       }
21
22
        return res;
23
   LL C(LL a, LL b) {
24
25
        if(b > a) return 0;
        if(b > a - b) b = a - b;
26
27
        LL s1 = 1, s2 = 1;
28
        for(LL i = 0; i < b; i++) {</pre>
            s1 = s1 * (a - i) % mod;
29
            s2 = s2 * (i + 1) % mod;
30
```

```
31    }
32    return s1 * qpow(s2, mod - 2) % mod;
33  }
34  LL lucas(LL a, LL b) {
35    if(a < mod) return C(a, b);
36    return lucas(a / mod, b / mod) * C(a % mod, b % mod);
37  }</pre>
```

4.2.3 CRT && exCRT

```
namespace CRT {
1
        LL m[MAXN], a[MAXN]; //x_i = a[i] \pmod{m[i]} LL exgcd(LL _a, LL _b, LL &x, LL &y) {
2
3
             if(!_b) {
4
                 x = 1; y = 0;
5
6
                 return _a;
7
             LL d = exgcd(_b, _a % _b, y, x);
8
9
             y = (_a / _b) * x;
10
             return d;
11
        LL crt(int n) {
12
13
             LL M = 1, tmp, res = 0, x, y;
             for(int i = 1; i <= n; i++) M *= m[i];</pre>
14
             for(int i = 1; i <= n; i++) {</pre>
15
                 tmp = M / m[i];
16
                 exgcd(tmp, m[i], x, y);
17
                 x = (x + m[i]) % m[i];
18
                 res = (a[i] * x % M * tmp % M + res) % M;
19
20
             }
21
             return res;
22
        }
23
    namespace EXCRT {
24
        LL m[MAXN], a[MAXN];
25
        LL exgcd(LL _a, LL _b, LL &x, LL &y) {
26
27
             if(!_b) {
                 x = 1; y = 0;
28
29
                 return _a;
30
31
             LL d = exgcd(_b, _a % _b, y, x);
             y = (_a / _b) * x;
32
33
             return d;
34
        LL excrt(int n) {
35
             LL M = m[1], A = a[1], x, y, d, tmp;
36
             for(int i = 2; i <= n; i++) {</pre>
37
                 d = exgcd(M, m[i], x, y);
38
                 if((A - a[i]) % d) return -1; //No solution
39
                 tmp = M / d; M *= m[i] / d;
40
41
                 y = (A - a[i]) / d % M * y % M;
42
                 y = (y + tmp) \% tmp;
                 A = (m[i] \% M * y \% M + a[i]) \% M;
43
                 A = (A + M) \% M;
44
             }
45
             return A;
46
        }
47
   }
48
```

4.2.4 BSGS

```
const int MOD = 76543;
1
   int hs[MOD + 5], head[MOD + 5], nxt[MOD + 5], id[MOD + 5], ecnt;
   void insert(int x, int y) {
        int k = x \% MOD;
 4
        hs[ecnt] = x, id[ecnt] = y, nxt[ecnt] = head[k], head[k] = ecnt++;
5
   }
6
   int find(int x) {
7
        int k = x \% MOD;
8
        for(int i = head[k]; i; i = nxt[i])
9
10
            if(hs[i] == x)
                return id[i];
11
        return -1;
12
13
   }
   int BSGS(int a, int b, int c){
14
15
        memset(head, 0, sizeof head); ecnt = 1;
        if(b == 1) return 0;
16
        int m = sqrt(c * 1.0), j;
17
        LL x = 1, p = 1;
18
        for(int i = 0; i < m; i++, p = p * a % c)
19
            insert(p * b % c, i);
20
21
        for(LL i = m; ; i += m){
            if((j = find(x = x * p % c)) != -1) return i - j;
22
23
            if(i > c) break;
24
        }
25
        return -1;
   }
26
```

4.2.5 Miller-Rabin && PollardRho

```
LL ksc(LL a, LL n, LL mod){
1
        LL ret=0;
2
3
        for(;n;n>>=1){
             if(n&1){ret+=a;if(ret>=mod)ret-=mod;}
4
5
            a \le 1; if(a \ge mod)a = mod;
        }
6
7
        return ret;
8
   }
9
   LL ksm(LL a, LL n, LL mod){
10
        LL ret = 1;
11
        for(;n;n>>=1){
12
             if(n&1)ret=ksc(ret,a,mod);
13
            a=ksc(a,a,mod);
14
15
        return ret;
16
    int millerRabin(LL n){
17
        if(n<2 || (n!=2 && !(n&1)))return 0;
18
        LL d=n-1; for(;!(d%1); d>>=1);
19
        for(int i=0;i<20;++i){</pre>
20
             LL a=rand()%(n-1)+1;
21
            LL t=d, m=ksm(a,d,n);
22
            for(;t!=n-1 && m!=1 && m!=n-1;m=ksc(m,m,n),t<<=1);</pre>
23
24
             if(m!=n-1 && !(t&1)) return 0;
        }
25
26
        return 1;
27
   LL cnt, fact[100];
```

```
LL gcd(LL a, LL b) {return !b?a:gcd(b,a%b);}
29
   LL pollardRho(LL n, int a){
30
31
        LL x=rand()%n, y=x, d=1, k=0, i=1;
32
        while(d==1){
            ++k;
33
34
            x=ksc(x,x,n)+a;if(x>=n)x-=n;
            d=gcd(x>y?x-y:y-x,n);
35
36
            if(k==i){y=x;i<<=1;}
37
        if(d==n)return pollardRho(n,a+1);
38
        return d;
39
40
    void findfac(LL n){
41
        if(millerRabin(n)){fact[++cnt]=n; return;}
42
43
        LL p=pollardRho(n,rand()%(n-1)+1);
        findfac(p);
44
        findfac(n/p);
45
46
   }
```

4.2.6 $\varphi(n)$

```
1
   int phi(int x) {
2
        int res = x;
3
        for(int i = 2; i * i <= x; i++) {
4
            if(x \% i == 0) {
                res = res / i * (i - 1);
5
6
                while(x % i == 0) x /= i;
7
            }
8
9
        if(x > 1) res = res / x * (x - 1);
10
        return res;
11
```

4.2.7 Euler Sieve

```
int prime[MAXN], cnt, phi[MAXN], mu[MAXN];
1
   bool isp[MAXN];
2
3
   int min_pow[MAXN];
                         //最小质因子最高次幂
4
   int min_sum[MAXN];
                         //1+p+p^2+\ldots+p^k
5
   int div_sum[MAXN];
                         //约数和
6
7
   int min_index[MAXN]; //最小质因子的指数
8
9
   int div_num[MAXN];
                         //约数个数
10
   void Euler(int n) {
       mu[1] = phi[1] = div_num[1] = div_sum[1] = 1;
11
12
        for(int i = 2; i <= n; i++) {
            if(!isp[i]) {
13
                prime[++cnt] = min_pow[i] = i;
14
15
                phi[i] = i - 1;
                mu[i] = -1;
16
                min_index[i] = 1; div_num[i] = 2;
17
                div_sum[i] = min_sum[i] = i + 1;
18
19
            for(int j = 1; j <= cnt && i * prime[j] <= n; j++) {</pre>
20
                isp[i * prime[j]] = 1;
21
                if(i % prime[j] == 0) {
22
                    phi[i * prime[j]] = phi[i] * prime[j];
23
```

```
mu[i * prime[j]] = 0;
24
25
26
                        min_index[i * prime[j]] = min_index[i] + 1;
                        div_num[i * prime[j]] = div_num[i] / (min_index[i] + 1) * (min_index[i *
27
          prime[j]] + 1);
28
                        min_sum[i * prime[j]] = min_sum[i] + min_pow[i] * prime[j];
div_sum[i * prime[j]] = div_sum[i] / min_sum[i] * min_sum[i * prime[j]];
min_pow[i * prime[j]] = min_pow[i] * prime[j];
29
30
31
32
                        break;
33
                   phi[i * prime[j]] = phi[i] * (prime[j] - 1);
34
35
                   mu[i * prime[j]] = -mu[i];
36
                   div_num[i * prime[j]] = div_num[i] << 1;</pre>
37
                   min_index[i * prime[j]] = 1;
38
39
                   div_sum[i * prime[j]] = div_sum[i] * (prime[j] + 1);
40
                   min_pow[i * prime[j]] = prime[j];
41
                   min_sum[i * prime[j]] = prime[j] + 1;
42
              }
43
         }
44
45
    }
```

4.2.8 DuJiao Sieve

$$\sum_{i=1}^{n} \phi(i)$$

```
vector<int> prime;
   int phi[MAXN], P[MAXN];
   bool isp[MAXN];
   unordered_map<LL, int> mp;
   void Euler(int n) {
5
        phi[1] = 1;
6
        for(int i = 2; i <= n; i++) {</pre>
7
            if(!isp[i]) {
8
9
                prime.push_back(i);
10
                 phi[i] = i - 1;
11
            for(auto x : prime) {
12
                 if(i * x > n) break;
13
                 isp[i * x] = 1;
14
                 if(i % x == 0) {
15
                     phi[i * x] = phi[i] * x;
16
17
                     break;
18
                phi[i * x] = phi[i] * (x - 1);
19
            }
20
21
        for(int i = 1; i <= n; i++) P[i] = (P[i - 1] + phi[i]) % mod;
22
23
   LL cal(LL n) {
24
        if(n < MAXN) return P[n];</pre>
25
26
        if(mp.count(n)) return mp[n];
27
        LL res = 0;
        for(LL i = 2, last; i <= n; i = last + 1) {</pre>
28
            last = n / (n / i);
29
```

```
30     res += (last - i + 1) % mod * cal(n / i) % mod;
31     res %= mod;
32     }
33     mp[n] = ((__int128)n * (n + 1) / 2 % mod + mod - res) % mod;
34     return mp[n];
35 }
```

 $\sum_{i=1}^{n} \mu(i)$

```
LL cal(LL n) {
1
        if(n < MAXN) return M[n];</pre>
2
        if(mp.count(n)) return mp[n];
3
        LL res = 0;
4
        for(LL i = 2, last; i <= n; i = last + 1) {</pre>
5
            last = n / (n / i);
6
7
             res += (last - i + 1) * cal(n / i);
8
        }
9
        mp[n] = 1 - res;
10
        return 1 - res;
11
```

4.2.9 Möbius Inversion

$$\sum_{i}^{n} \sum_{j}^{m} lcm(i, j) (mod \ p)$$

```
int mu[MAXN], prime[MAXN], sum[MAXN], cnt;
2
    bool isp[MAXN];
    void getmu(int n) {
3
        mu[1] = 1;
4
        for(int i = 2; i <= n; i++) {</pre>
5
             if(!isp[i]) {
6
7
                 mu[i] = -1;
8
                 prime[++cnt] = i;
9
             for(int j = 1; j <= cnt && i * prime[j] <= n; j++) {</pre>
10
                 isp[i * prime[j]] = 1;
11
                 if(i % prime[j] == 0) {
12
                      mu[i * prime[j]] = 0;
13
                      break;
14
15
                 mu[i * prime[j]] = -mu[i];
16
17
             }
        }
18
19
20
   ll n, m, ans;
   ll query(ll x, ll y) { return (x * (x + 1) / 2 % mod) * (y * (y + 1) / 2 % mod) % mod; }
21
22
   ll F(ll x, ll y) {
23
        ll res = 0, last;
        for(ll i = 1; i \le min(x, y); i = last + 1) {
24
             last = min(x / (x / i), y / (y / i));
res = (res + (sum[last] - sum[i - 1]) * query(x / i, y / i) % mod) % mod;
25
26
        }
27
28
        return res;
29
   }
30
   int main() {
        cin>>n>>m;
```

```
getmu(min(n, m));
32
          for(ll\ i=1;\ i' \leftarrow min(n,\ m);\ i++)\ sum[i] = (sum[i-1]+(i*i*mu[i]) \% mod) \%
33
          mod;
ll last;
34
          for(ll d = 1; d <= min(n, m); d = last + 1) {
    last = min(n / (n / d), m / (m / d));
    ans = (ans + (last - d + 1) * (d + last) / 2 % mod * F(n / d, m / d) % mod) %</pre>
35
36
37
          mod;
38
          ans = (ans + mod) \% mod;
39
          cout<<ans<<endl;</pre>
40
41
           return 0;
     }
42
```

5 Geometry

5.1 Commonly Definition and Functions

5.1.1 Const and Functions

```
namespace CG{
1
        #define Point Vector
2
3
        const double pi=acos(-1.0);
        const double inf=1e100;
4
5
        const double eps=1e-9;
        template <typename T> inline T Abs(T x){return x>0?x:-x;}
6
        template <typename T> inline bool operator == (T x, T y){return Abs(x-y)<eps;}
7
8
        int sqn(double x){
9
            if (Abs(x)<eps) return 0;</pre>
            if (x>0) return 1;
10
            else return -1;
11
12
        }
13
   }
```

5.1.2 Point Definition

```
1
   namespace CG{
2
       struct Point{
3
            double x,y;
4
           Point(double x=0, double y=0):x(x),y(y){}
5
6
       Vector operator + (const Vector a,const Vector b){return Vector(a.x+b.x,a.y+b.y);}
       Vector operator - (const Vector a,const Vector b){return Vector(a.x-b.x,a.y-b.y);}
7
       Vector operator * (const Vector a,const double k){return Vector(a.x*k,a.y*k);}
8
       Vector operator / (const Vector a,const double k){return Vector(a.x/k,a.y/k);}
9
10
       bool operator < (const Vector a,const Vector b) {return a.x==b.x?a.y<b.y:a.x<b.x;}</pre>
11
       bool operator == (const Vector a,const Vector b) {return a.x==b.x && a.y==b.y;}
12
       double Dot(const Vector a,const Vector b){return a.x*b.x+a.y*b.y;}
       double Cross(const Vector a,const Vector b){return a.x*b.y-a.y*b.x;}
13
       double mult_Cross(const Vector a,const Vector b,const Vector c){return (a.x-c.x)*(b.
14
       y-c.y)-(b.x-c.x)*(a.y-c.y);}
       double mult_Dot(const Vector a,const Vector b,const Vector c){return (a.x-c.x)*(b.x-
15
       c.x)+(a.y-c.y)*(b.y-c.y);}
       double Norm(const Vector a){return sqrt(Dot(a,a));}
16
       double Angle(const Vector a,const Vector b){return acos(Dot(a,b)/Norm(a)/Norm(b));}
17
18
       Vector Rotate(const Vector a, const double theta){return Vector(a.x*cos(theta)-a.y*
       sin(theta),a.x*sin(theta)+a.y*cos(theta));}
       bool ToLeftTest(const Vector a,const Vector b){return Cross(a,b)<0;}</pre>
19
       double DisPP(const Vector a,const Vector b){return sqrt((a.x-b.x)*(a.x-b.x)+(a.y-b.y
20
       )*(a.y-b.y));}
21
   }
```

5.1.3 Line Definition

```
namespace CG{
struct Line{
    point p0,v,p1;
    double t,theta;
    Line(Point _p0=0,Point _v=0,double _t=1):p0(_p0),v(_v),t(_t){p1=p0+v*t; theta=
    atan2(v.y,v.x);}
```

```
6
            // Line(Point \_p0=0, Point \_v=0, double \_t=1): p0(\_p0), p1(\_v)\{v=(p1-p0)/t; theta=1\}
       atan2(v.y,v.x);
7
       };
8
       bool operator < (const Line n,const Line m) {return n.theta<m.theta;}</pre>
       Point GetIntersection(const Line n,const Line m){return n.p0+n.v*Cross(m.v,(n.p0-m.
9
       p0))/Cross(n.v,m.v);}
       bool OnLine(const Vector a, const Line 1){return Cross(1.p0-a,1.p1-a)==0;}
10
       bool OnSegment(const Point a,const Line 1){return sgn(Cross(l.p0-a,l.p1-a))==0 &&
11
       sgn(Dot(l.p0-a,l.p1-a))<0;}
       double DisPL(const Point a,const Line 1){return Abs(Cross(1.p1-1.p0,a-1.p0)/Norm(1.
12
       p1-l.p0));}
       double DisPS(const Point a,const Line 1){
13
            if (l.p0==l.p1) return Norm(a-l.p0);
14
            Vector v1=l.p1-l.p0,v2=a-l.p0,v3=a-l.p1;
15
            if (sgn(Dot(v1,v2))<0) return Norm(v2);</pre>
16
            if (sgn(Dot(v1,v3))>0) return Norm(v3);
17
            return DisPL(a,1);
18
19
20
        Point GetProjection(const Point a, const Line 1){
21
            Vector v=l.p1-l.p0;
            return 1.p0+v*(Dot(v,a-1.p0)/Dot(v,v));
22
23
        bool SegmentIntersection(const Line n,const Line m,bool p){
24
            double c1=Cross(n.p1-n.p0,m.p1-m.p0);
25
            double c2=Cross(n.p1-n.p0,m.p1-n.p0);
26
27
            double c3=Cross(m.p1-m.p0,n.p0-m.p0);
28
            double c4=Cross(m.p1-m.p0,n.p1-m.p0);
            if (p){
29
                if (!sgn(c1) || !sgn(c2) || !sgn(c3) || !sgn(c4)){
30
                     return OnSegment(n.p0,m) | OnSegment(n.p1,m) | OnSegment(m.p0,n) |
31
       OnSegment(m.p0,m);
32
                }
33
            }
34
35
            return (sgn(c1)*sgn(c2)<0 && sgn(c3)*sgn(c4)<0);</pre>
36
       }
37
   }
```

5.1.4 Get Area

```
namespace CG{
    double GetArea(Point *p,int n){
        double area=Cross(p[n],p[1]);
        for (int i=2;i<=n;i++) area+=0.5*Cross(p[i-1],p[i]);
        return Abs(area);
    }
}</pre>
```

5.1.5 Get Circumference

5.1.6 Anticlockwise Sort

```
1
   namespace CG{
2
        void clockwise_sort(Point *p,int n){
3
             for(int i=0;i<n-2;i++){</pre>
4
                 double tmp = mult_Cross(p[i+1],p[i+2],p[i]);
5
                 if(tmp>0) return;
6
                 else if(tmp<0){</pre>
7
8
                      reverse(p,p+n);
9
                      return;
10
                 }
11
            }
12
        }
13
   }
```

5.2 Convex Hull

5.2.1 Get Convex Hull

```
namespace CG{
1
2
        Point p[MAXN],s[MAXN];
        int ConvexHull(Point *p,int n,Point *s){
3
4
            sort(p,p+n,cmp); //x从小到大,y从小到大;
5
            int m=0;
            for (int i=0;i<n;i++){</pre>
6
                 for (;m>=2 && Cross(s[m-1]-s[m-2],p[i]-s[m-1])<=0;m--);</pre>
7
8
                s[++m]=p[i];
            }
9
            int k=m;
10
            for (int i=n-2;i;i--){
11
                 for (;m>=k+1 && Cross(s[m-1]-s[m-2],p[i]-s[m-1])<=0;m--);</pre>
12
                s[++m]=p[i];
13
14
15
            return m-1;
16
        }
17
   }
```

5.2.2 Point in Convex Hull

```
namespace CG{
1
2
        bool PointInConvexHull(Point A){
            int l=1,r=tot-2,mid;
3
            while(l<=r){</pre>
4
5
                 mid=(l+r)>>1;
                 double a1=Cross(p[mid]-p[0],A-p[0]);
6
7
                 double a2=Cross(p[mid+1]-p[0],A-p[0]);
                 if(a1>=0 \&\& a2<=0){
8
                     if(Cross(p[mid+1]-p[mid],A-p[mid])>=0) return true;
9
10
                     return false;
11
                 else if(a1<0) r=mid-1;</pre>
12
13
                 else l=mid+1;
14
            return false;
15
16
        }
17
   }
```

5.3 Minkowski Sum

```
1
    namespace CG{
2
        void Minkowski(Point *C1,int n,Point *C2,int m){
            for(int i=1;i<=n;i++) s1[i]=C1[i]-C1[i-1];</pre>
3
            for(int i=1;i<=m;i++) s2[i]=C2[i]-C2[i-1];</pre>
4
5
            A[tot=1]=C1[1]+C2[1];
6
            int p1=1,p2=1;
            while (p1<=n && p2<=m) ++tot,A[tot]=A[tot-1]+(s1[p1]*s2[p2]>=0?s1[p1++]:s2[p2
7
        ++]);
8
            while (p1<=n) ++tot,A[tot]=A[tot-1]+s1[p1++];</pre>
9
            while (p2<=m) ++tot,A[tot]=A[tot-1]+s2[p2++];</pre>
10
            tot=ConvexHull(A,tot);
11
        }
12
    }
```

5.4 Rotating Calipers

5.4.1 The Diameter of Convex Hull

```
namespace CG{
1
2
        double RotatingCalipers(Point *p,int n){
3
            double dis=0;
4
            for(int i=0, j=2; i<n;++i){</pre>
                 while (abs(Cross(p[i+1]-p[i],p[j]-p[i]))<abs(Cross(p[i+1]-p[i],p[j+1]-p[i]))</pre>
5
        ) j=(j+1)%n;
                 dis=max(dis,max(DisPP(p[j],p[i]),DisPP(p[j],p[i+1])));
6
7
8
            return dis;
9
        }
10
   }
```

5.4.2 The Min Distance Bewteen two Convex Hull

```
1
   namespace CG{
2
       ///点c到线段ab的最短距离
      double GetDist(Point a,Point b,Point c){
3
          if(dis(a,b) < esp) return dis(b,c); ///a,b是同一个点
4
          if(mult_Dot(b,c,a)<-esp) return dis(a,c); ///投影
5
6
          if(mult_Dot(a,c,b)<-esp) return dis(b,c);</pre>
7
          return fabs(mult_Cross(b,c,a)/dis(a,b));
8
      }
9
       ///求一条线段ab的两端点到另外一条线段bc的距离,反过来一样,共4种情况
10
      double MinDist(Point a, Point b, Point c, Point d){
11
12
          return min(min(GetDist(a,b,c),GetDist(a,b,d)),min(GetDist(c,d,a),GetDist(c,d,b))
      );
      }
13
      double RotatingCalipers(Point *p,int n,Point *q,int m){
14
          int yminP = 0,ymaxQ=0;
15
          for(int i=1;i< n;i++){ ///找到点集p组成的凸包的左下角
16
             17
18
19
          for(int i=1;i<m;i++){ ///找到点集q组成的凸包的右上角
             if(q[i].y>q[ymaxQ].y||(q[i].y==q[ymaxQ].y)&&(q[i].x>q[ymaxQ].x))              ymaxQ = i;
20
21
          double ans = DisPP(p[yminP],q[ymaxQ]); ///距离(yminP,ymaxQ)维护为当前最小值。
22
```

```
for(int i=0;i<n;i++){</pre>
23
                 double tmp;
24
                 while(tmp=(mult_Cross(q[ymaxQ+1],p[yminP],p[yminP+1])-mult_Cross(q[ymaxQ],p[
25
       yminP],p[yminP+1]))>esp)
26
                     ymaxQ = (ymaxQ+1)%m;
                 if(tmp<-esp) ans = min(ans,GetDist(p[yminP],p[yminP+1],q[ymax0]));</pre>
27
                 else ans=min(ans,MinDist(p[yminP],p[yminP+1],q[ymaxQ],q[ymaxQ+1]));
28
29
                yminP = (yminP+1)%n;
30
31
            return ans;
        }
32
   }
33
```

5.5 Half Plane Intersection

```
1
   namespace CG{
        void HalfPlaneIntersection(Line 1[],int n){
2
3
            deque <Point> p;
4
            sort(l+1,l+1+n);
            deque <Line> q;
5
            q.push_back(l[1]);
6
            for (int i=2;i<=n;i++){</pre>
7
                for (;!p.empty() && !ToLeftTest(p.back()-l[i].p0,l[i].v);q.pop_back(),p.
8
       pop_back());
                for (;!p.empty() && !ToLeftTest(p.front()-l[i].p0,l[i].v);q.pop_front(),p.
9
       pop_front());
                if (sqn(Cross(l[i].v,q.back().v))==0)
10
                    if (ToLeftTest(l[i].p0-q.back().p0),q.back().v){
11
12
                        q.pop_back();
13
                        if (!p.empty()) p.pop_back();
14
                if (!q.empty()) p.push_back(GetIntersection(q.back(),l[i]));
15
                q.push_back(l[i]);
16
17
            for (;!p.empty() && !ToLeftTest(p.back()-q.front().p0,q.front().v);q.pop_back(),
18
       p.pop_back());
            p.push_back(GetIntersection(q.back(),q.front()));
19
            double area=0.5*Cross(p.back(),p.front()); Point last=p.front();
20
21
            for (p.pop_front();!p.empty();last=p.front(),p.pop_front()) area+=0.5*Cross(last
        ,p.front());
            printf("%.1f",Abs(area));
22
23
24
   }
```

5.6 Min Circle Cover

```
namespace CG{
1
       Point GetCircleCenter(const Point a, const Point b, const Point c){
2
3
           Point p=(a+b)/2.0, q=(a+c)/2.0;
           Vector v=Rotate(b-a,pi/2.0),w=Rotate(c-a,pi/2.0);
4
           if (sgn(Norm(Cross(v,w)))==0){
5
                if (sgn(Norm(a-b)+Norm(b-c)-Norm(a-c))==0) return (a+c)/2;
6
                if (sgn(Norm(b-a)+Norm(a-c)-Norm(b-c))==0) return (b+c)/2;
7
                if (sgn(Norm(a-c)+Norm(c-b)-Norm(a-b))==0) return (a+c)/2;
8
9
           }
10
            return GetIntersection(Line(p,v),Line(q,w));
       }
11
       void MinCircleCover(Point p[],int n){
```

```
13
             random_shuffle(p+1,p+1+n);
             Point c=p[1];
14
             double r=0;
15
             for (int i=2;i<=n;i++)</pre>
16
                  if (sgn(Norm(c-p[i])-r)>0){
17
                      c=p[i],r=0;
18
                      for (int j=1;j<i;j++)</pre>
19
20
                           if (sgn(Norm(c-p[j])-r)>0){
                               c=(p[i]+p[j])/2.0;
21
22
                               r=Norm(c-p[i]);
                               for (int k=1;k<j;k++)</pre>
23
                                    if (sgn(Norm(c-p[k])-r)>0){
24
                                        c=GetCircleCenter(p[i],p[j],p[k]);
25
                                        r=Norm(c-p[i]);
26
27
                                    }
28
                          }
29
             printf("%.10f\n%.10f %.10f",r,c.x,c.y);
30
31
        }
32
   }
```

5.7 Circle Union Area

```
1
   //k次覆盖
2
    //圆并去重后s[0]
3 typedef pair<double, int> P;
   const double pi = acos(-1.0);
   const int MAXN = 10003;
6 P arc[MAXN << 1];</pre>
7
   int acnt, cnt;
   double s[1003];
8
   bool del[1003];
10
   void add(double st, double en) {
11
        if(st < -pi) {
12
            add(st + 2 * pi, pi);
13
            add(-pi, en);
            return;
14
15
        if(en > pi) {
16
            add(st, pi);
17
            add(-pi, en - 2 * pi);
18
19
            return;
20
        arc[++acnt] = P(st, 1);
21
       arc[++acnt] = P(en, -1);
22
23
24
   double F(double x) {
        return (x - \sin(x)) / 2;
25
   }
26
27
   struct Node {
28
        int x, y, r;
       Node(int _x = 0, int _y = 0, int _r = 0):x(_x), y(_y), r(_r) {}
29
       bool operator == (const Node& t) {
30
31
            return x == t.x & y == t.y & r == t.r;
32
        inline void read() {
33
            scanf("%d%d%d", &x, &y, &r);
34
35
   }a[1003];
36
```

```
int main() {
37
38
        int n;
        scanf("%d", &n);
39
40
        for(int i = 1; i <= n; i++) a[i].read();</pre>
41
        //去重
42
43
        int nn = 0;
        for(int \ i = 1; \ i \ll n; \ i++)
44
45
            bool\ same = 0;
46
            for(int \ j = 1; \ j < i; \ j++)  {
                 if(a/i) == a/j) {
47
                     same = 1; break;
48
49
50
51
            if(!same) \ a[++nn] = a[i];
52
53
        n = nn;
        //去包含
54
        for(int \ i = 1; \ i <= n; \ i++) 
55
56
            for(int \ j = 1; \ j \le n; \ j++) \ if(i != j) 
                 if(hypot(a[i].x - a[j].x, a[i].y - a[j].y) < (double)(a[i].r - a[j].r)) del[i]
57
        j / = 1;
58
59
        nn = 0;
60
61
        for(int \ i = 1; \ i \le n; \ i++) \ if(!del[i])  {
62
            a/++nn/ = a/i/;
63
64
        n = nn;
65
        for(int i = 1; i <= n; i++) {
66
            acnt = 0;
67
            for(int j = 1; j <= n; j++) if(i != j) {
68
                 int dis = (a[i].x - a[j].x) * (a[i].x - a[j].x) + (a[i].y - a[j].y) * (a[i].
69
       y - a[j].y);
                if(a[j].r > a[i].r \& dis <= (a[j].r - a[i].r) * (a[j].r - a[i].r)) add(-pi,
70
        pi);
                else if(dis > (a[i].r - a[j].r) * (a[i].r - a[j].r) & dis < (a[i].r + a[j].
71
        r) * (a[i].r + a[j].r)){
72
                     double c = sqrt(dis);
                     double angle = a\cos((a[i].r * a[i].r + c * c - a[j].r * a[j].r) / (2 * a
73
        [i].r * c));
                     double k = atan2(a[j].y - a[i].y, a[j].x - a[i].x);
74
                     add(k - angle, k + angle);
75
76
77
            }
            arc[++acnt] = P(pi, -1);
78
            sort(arc + 1, arc + acnt + 1);
79
80
            cnt = 0;
            double last = -pi;
81
            for(int j = 1; j <= acnt; j++) {</pre>
82
                 s[cnt] += F(arc[j].first - last) * a[i].r * a[i].r; //扇形 - 三角形
83
                double xa = a[i].x + a[i].r * cos(last);
84
                double ya = a[i].y + a[i].r * sin(last);
85
                last = arc[j].first;
86
                double xb = a[i].x + a[i].r * cos(last);
87
                double yb = a[i].y + a[i].r * sin(last);
88
                s[cnt] += (xa * yb - xb * ya) / 2; //到圆心的三角形面积
89
                cnt += arc[j].second;
90
            }
91
92
```

5.8 Simpson Integrate

```
1
   double Simpson(double 1,double r){
2
        return (r-1)*(F(1)+4*F((1+r)/2)+F(r))/6;
3
   double Integrate(double l,double r,double S){
4
       double mid=(l+r)/2;
5
       double A=Simpson(l,mid);
6
7
       double B=Simpson(mid,r);
8
       if(A+B-S<eps)return S;</pre>
9
       return Integrate(l,mid,A)+Integrate(mid,r,B);
10
   }
```

6 Others

6.1 Sample

6.1.1 vimrc

```
1  set cindent
2  set number
3  set mouse=a
4  set tabstop=4
5  set shiftwidth=4
6  syntax on
7  inoremap { {}<left>
8  map <F9> :w<CR> :! g++ % -o %< -Wall --std=c++14 -g && ./%< <CR>
```

6.1.2 Check

```
while true; do
./data > in
./tmp < in > out
./std < in > ans
diff out ans
if [ $? -ne 0 ]; then exit; fi
echo Passed
done
```

6.1.3 FastIO

```
namespace IO {
1
        const int MB = 1048576;
2
        const int RMAX = 16 * MB;
3
        const int WMAX = 16 * MB;
4
        #define getchar() *(rp++)
5
        #define putchar(x) (*(wp++) = (x))
6
7
        char rb[RMAX], *rp = rb, wb[WMAX], *wp = wb;
8
        inline void init() {
9
             fread(rb, sizeof(char), RMAX, stdin);
10
        template <class _T> inline void read(_T &_a) {
11
            _a = 0; register bool _f = 0; register int _c = getchar(); while (_c < '0' \mid | _c > '9') _f \mid = _c = '-', _c = getchar();
12
13
             while (_c >= '0' \& _c <= '9') _a = _a * 10 + (_c ^ '0'), _c = getchar();
14
             _a = _f ? -_a : _a;
15
16
        template <class _T> inline void write(_T _a) {
17
             static char buf[20], *top = buf;
18
19
             if (_a) {
20
                 while (_a) {
                      register _T tm = _a / 10;
21
                      *(++top) = char(_a - tm * 10) | '0';
22
23
                      _a = tm;
24
                 while (top != buf) putchar(*(top--));
25
26
             else putchar('0');
27
28
```

```
void output() {
    fwrite(wb, sizeof(char), wp - wb, stdout);
}
```

6.1.4 Java BigNum

```
import java.math.*;
   import java.util.*;
3
   import java.lang.*;
   public class Main{
5
       public static void main(String []args){}
6
7
   }
    //IO
8
9
   Scanner in = new Scanner(System.in);
10 while(in.hasNext()){} //EOF
   //fast-IO
11
   public static void main(String argv[]) throws IOException{}
13 StreamTokenizer cin = new StreamTokenizer(new BufferedReader(new InputStreamReader(
       System.in)));
14 PrintWriter cout = new PrintWriter(new OutputStreamWriter(System.out));
while(cin.nextToken() != StreamTokenizer.TT_EOF);//EOF
16 cin.nextToken();int n = (int)cin.nval;String s = cin.sval;
   cout.println( Type );cout.flush();
17
   cin.ordinaryChar('/');
18
19
   BufferedReader br = new BufferedReader(new InputStreamReader(System.in));
20
   br.ready()//EOF
21
22
   while ((valueString=bf.readLine())!=null);
23
   br.close();
24
   //true\ fast-IO
25
   static class InputReader {
       public BufferedReader reader;
26
       public StringTokenizer tokenizer;
27
28
29
       public InputReader(InputStream stream) {
            reader = new BufferedReader(new InputStreamReader(stream), 32768);
30
            tokenizer = null;
31
       }
32
33
       public String next() {
34
           while (tokenizer == null || !tokenizer.hasMoreTokens()) {
35
36
                try {
                    tokenizer = new StringTokenizer(reader.readLine());
37
38
                } catch (IOException e) {
39
                    throw new RuntimeException(e);
40
           }
41
            return tokenizer.nextToken();
42
43
44
       public int nextInt() {
45
            return Integer.parseInt(next());
46
47
48
   }
49
   //类 Number
50
51
   //double Value ()
   //intValue()
```

```
//long Value()
53
54
    //shortValue()
55
   //类 BigDecimal
   //ROUND_CEILING 接近正无穷大的舍入模式。
56
57
    //ROUND_FLOOR 接近负无穷大的舍入模式。
58
    //ROUND_DOWN 接近零的舍入模式
    //ROUND_HALF_UP 四舍五入 >=0.5向上舍入
59
    //ROUND_HALF_DOWN 四舍五入 >0.5向上舍入
60
61
    //BigDecimal(BigInteger\ val)
62
    //BigDecimal(BigInteger\ unscaledVal,\ int\ scale)
    //BigDecimal(char[] in, int offset, int len, MathContext mc)
63
    //BigDecimal(double val, MathContext mc)不建议
64
    //BigDecimal(int val, MathContext mc)
65
66
    //BigDecimal(long val, MathContext mc)
67
    //BigDecimal(String val, MathContext mc)
68
    //abs()
    //add(BigDecimal augend, MathContext mc)
69
70 //compareTo(BigDecimal val)
   //divide (BigDecimal divisor, MathContext mc)
71
72
   //divideToIntegralValue(BigDecimal divisor, MathContext mc)
73 //max(BigDecimal\ val)
74
   //min(BigDecimal\ val)
    //multiply (BigDecimal\ multiplicand\ ,\ MathContext\ mc)
75
76
    //negate() 其值为 (-this), 其标度为 this.scale()
    //pow(int n)
77
    //remainder(BigDecimal divisor) 返回其值为 (this % divisor) 的 BigDecimal
78
79
    //round(Math Context mc) 返回根据 Math Context 设置进行舍入后的 Big Decimal。
80
    //caleByPowerOfTen(int n) 返回其数值等于 (this * 10^n) 的 BigDecimal。
    //subtract(BigDecimal\ subtrahend\ ,\ MathContext\ mc)
81
82
    //setScale(int\ newScale, RoundingMode\ roundingMode)
83
    //toString()
    //ulp()返回此 BigDecimal 的 ulp (最后一位的单位) 的大小
84
    //String s = b.stripTrailingZeros().toPlainString();让bigdecimal不用科学计数法显示
85
    //类 BigInteger
86
    //parseInt
87
88
    //BigInteger\ zero = BigInteger.valueOf(0);
    //BigInteger\ a = in.nextBigInteger();
89
90
   //abs()
   //and(BigInteger val) 返回其值为 (this & val)
91
92
   //or(BigInteger val) 返回其值为 (this | val)
93
   //andNot(BigInteger val) 返回其值为 (this & ~val)
94
   //compareTo(BigInteger\ val)
95
   //add(BigInteger\ val)
96
    //divide(BigInteger\ val)
    //BigInteger[] divideAndRemainder(BigInteger val) 返回包含 (this / val) 后跟 (this %
97
        val) 的两个 BigInteger 的数组。
    //equals(Object x)
98
99
    //gcd(BigInteger\ val)
100
    //isProbablePrime(int certainty) e.g. a.isProbablePrime(4)
    //max(BigInteger val) min(BigInteger val)
101
102
    //mod(BigInteger m)
    //modInverse(BigInteger m) 返回其值为 (this ~-1 mod m)
103
104
    //modPow(BigInteger exponent, BigInteger m) 返回其值为 (this exponent mod m)
    //multiply(BigInteger val)
105
106
    //not() 返回其值为 (~this)
    //shiftLeft(int n) 返回其值为 (this << n)
107
    //shiftRight(int n) 返回其值为 (this >> n)
108
    //toString()
109
110
    //valueOf(long val)
    //xor(BigInteger val) 返回其值为 (this ^ val)
111
112
    //other
```

113 //Arrays.sort(array);

6.2 Offline Algorithm

6.2.1 CDQ Divide and Conquer

```
1
    struct Node {
2
        int x, y, z, ans;
3
        Node() {}
        Node(int _x, int _y, int _z):x(_x), y(_y), z(_z) {}
4
        bool operator < (const Node &b) const {</pre>
5
6
             if(y == b.y) {
7
                 if(z == b.z) return x < b.x;
                 return z < b.z;</pre>
8
9
10
             return y < b.y;</pre>
11
   }A[MAXN], B[MAXN], C[MAXN];
12
   int bit[MAXN];
13
   void add(int k, int v) {
15
        for(; k <= m; k += k & -k) bit[k] = max(bit[k], v);</pre>
16
   }
   void clear(int k) {
17
        for(; k <= m; k += k & -k) bit[k] = 0;</pre>
18
19
20
   int sum(int k) {
        int res = 0;
21
22
        for(; k; k \rightarrow k - k) res = max(res, bit[k]);
23
        return res;
24
   }
25
    void solve(int l, int r) {
26
        if(l == r) {
27
             B[l] = A[l];
28
             return;
29
        int mid = (l + r) >> 1;
30
31
        solve(l, mid);
        for(int i = mid + 1; i <= r; i++) B[i] = A[i];</pre>
32
        //sort(B + l, B + mid + 1);
33
        sort(B + mid + 1, B + r + 1);
34
35
        int L = 1;
        for(int R = mid + 1; R <= r; R++) {</pre>
36
             while(L \leftarrow mid && B[L].y \leftarrow B[R].y) add(B[L].z, B[L].ans), L++;
37
             A[B[R].x].ans = max(A[B[R].x].ans, sum(B[R].z - 1) + 1);
38
             B[R].ans = A[B[R].x].ans;
39
40
41
        for(int i = 1; i <= L; i++) clear(B[i].z);</pre>
42
        solve(mid + 1, r);
43
        L = 1;
        int p = 1, q = mid + 1;
44
        while(p \ll mid \mid | q \ll r) {
45
             if(q > r | | (p \le mid \&\& B[p].y \le B[q].y)) C[L++] = B[p++];
46
             else C[L++] = B[q++];
47
48
        for(int i = 1; i <= r; i++) B[i] = C[i];</pre>
49
50
```

```
1
   struct Node{
2
        int 1, r, t, id;
3
        bool operator < (const Node& a) const {</pre>
4
             if(l /sz == a.l / sz) {
                 if(r == a.r) return t < a.t;</pre>
5
6
                 return r < a.r;</pre>
7
8
             return l / sz < a.l / sz;</pre>
9
    }q[MAXN];
10
    void solve() {
11
        while (t < q[i].t) addTime(t++, 1);</pre>
12
        while (t > q[i].t) addTime(--t, -1);
13
14
        while(L < q[i].l) add(L++, -1);
        while(L > q[i].l) add(--L, 1);
15
        while(R < q[i].r) add(++R, 1);
16
        while(R > q[i].r) add(R--, -1);
17
18
```

6.2.3 Mo's Algorithm On Tree

```
struct Edge {
1
       int to, nxt;
2
   }e[MAXN << 1];
3
   int head[MAXN], ecnt;
4
   int stack[MAXN], top, belong[MAXN], cnt, sz;
5
   struct Node {
6
7
        int l, r, id, ti;
8
        bool operator < (const Node &x) const {</pre>
            return belong[1] < belong[x.1] || (belong[1] == belong[x.1] && belong[r] <</pre>
9
       belong[x.r]) || (belong[l] == belong[x.l] && belong[r] == belong[x.r] && ti < x.ti);
10
   }q[MAXN];
11
   struct Node2 {
12
       int l, r, ti;
13
   }qq[MAXN];
14
   int n, m, Q, Q0, Q1;
15
   int V[MAXN], W[MAXN], C[MAXN];
16
   int fa[MAXN][S + 3], dep[MAXN];
17
   long long ans[MAXN], tans;
19
   int vis[MAXN], cur[MAXN];
20 long long sum[MAXN];
21
   int l, r, tm;
22
   inline int read() {
23
        int x = 0; char ch = getchar(); bool fg = 0;
       while(ch < '0' || ch > '9') { if(ch == '-') fg = 1; ch = getchar(); }
24
       while(ch >= 0, && ch <= 9) { x = x * 10 + ch - 0; ch = getchar(); }
25
       return fg ? -x : x;
26
27
   inline void add_edge(int u, int v) {
28
        e[++ecnt] = (Edge) \{v, head[u]\}; head[u] = ecnt;
29
        e[++ecnt] = (Edge) \{u, head[v]\}; head[v] = ecnt;
30
31
   void dfs(int u, int f) {
32
        fa[u][0] = f;
33
        dep[u] = dep[f] + 1;
34
        int bot = top;
35
36
        for(int i = head[u]; i; i = e[i].nxt) {
37
            int v = e[i].to;
            if(v == f) continue;
```

```
39
            dfs(v, u);
            if(top - bot >= sz) {
40
41
                while(top != bot) belong[stack[top--]] = cnt;
42
43
44
        stack[++top] = u;
45
46
    void G(int &u, int step) {
47
        for(int i = 0; i < S; i++) if((1 << i) & step) u = fa[u][i];
48
49
   int lca(int u, int v) {
50
        if(dep[u] > dep[v]) swap(u, v);
51
        G(v, dep[v] - dep[u]);
52
        if(u == v) return u;
53
        for(int i = S; i >= 0; i--) if(fa[u][i] != fa[v][i]) {
54
            u = fa[u][i]; v = fa[v][i];
55
56
        return fa[u][0];
57
58
   inline void modify(int u) {
59
        tans -= V[C[u]] * sum[cur[C[u]]];
60
        cur[C[u]] += vis[u];
61
        vis[u] = -vis[u];
62
        tans += V[C[u]] * sum[cur[C[u]]];
63
64
65
    inline void update(int u, int v) {
66
        if(u == v) return;
67
        if(dep[u] > dep[v]) swap(u, v);
        while(dep[v] > dep[u]) {
68
69
            modify(v);
            v = fa[v][0];
70
71
        while(u != v) {
72
            modify(u); modify(v);
73
            u = fa[u][0]; v = fa[v][0];
74
        }
75
   }
76
   inline void upd(int t) {
77
78
        if(vis[qq[t].l] == -1) {
79
            modify(qq[t].1);
80
            swap(C[qq[t].1], qq[t].r);
81
            modify(qq[t].l);
82
        else swap(C[qq[t].1], qq[t].r);
83
84
    inline void moveto(int u, int v) {
85
        update(l, u); update(r, v);
86
        l = u; r = v;
87
88
89
    int main() {
        n = read(); m = read(); Q = read();
90
        sz = (int)pow(n, 2.0 / 3.0);
91
        for(int i = 1; i <= m; i++) V[i] = read();</pre>
92
        for(int i = 1; i \le n; i++) W[i] = read();
93
        for(int i = 1, u, v; i < n; i++) {
94
            u = read(); v = read();
95
96
            add_edge(u, v);
97
        for(int i = 1; i <= n; i++) {
98
99
            C[i] = read();
```

```
100
             vis[i] = 1;
             sum[i] = sum[i - 1] + W[i];
101
102
103
         for(int i = 1, tp; i <= Q; i++) {
             tp = read();
104
             if(tp) {
105
                  ++01
106
107
                 q[Q1].l = read(); q[Q1].r = read();
108
                 q[Q1].id = Q1;
                 q[Q1].ti = i;
109
110
             else {
111
                 ++00:
112
                 qq[Q0].l = read(); qq[Q0].r = read();
113
114
                 qq[Q0].ti = i;
115
             }
116
         dfs(1, 0);
117
         while(top) belong[stack[top--]] = cnt;
118
119
         sort(q + 1, q + Q1 + 1);
         for(int k = 1; k \le S; k++) {
120
             for(int i = 1; i <= n; i++) {</pre>
121
                  fa[i][k] = fa[fa[i][k - 1]][k - 1];
122
123
124
125
         for(int i = 1; i <= Q1; i++) {
126
             if(belong[q[i].l] > belong[q[i].r]) swap(q[i].l, q[i].r);
127
             moveto(q[i].l, q[i].r);
128
             int lc = lca(l, r);
             modify(lc);
129
             while(qq[tm + 1].ti < q[i].ti && tm < Q0) upd(++tm);</pre>
130
             while(qq[tm].ti > q[i].ti) upd(tm--);
131
             ans[q[i].id] = tans;
132
             modify(lc);
133
134
135
         for(int i = 1; i <= Q1; i++) printf("%lld\n", ans[i]);</pre>
136
         return 0;
137
    }
```

6.3 Randomized Algorithm

6.3.1 Simulated Annealing

```
void solve() {
1
2
        while(T > eps) {
             double alpha = ((rand() % 30001) / 15000.0) * pi;
double theta = ((rand() % 10001) / 10000.0) * pi;
3
4
             tmp.x = cur.x + T * sin(theta) * cos(alpha);
5
             tmp.y = cur.y + T * sin(theta) * sin(alpha);
6
             tmp.z = cur.z + T * cos(theta);
7
             tmp.dis = cal(tmp);
8
             if(tmp.dis < cur.dis || (tmp.dis * 0.999 < cur.dis && (rand() & 7) == 7)) cur =
9
        tmp;
10
             //if(exp((cur.d - tmp.d) / T) > ((double)rand() / RAND_MAX)) cur = tmp;
11
             T *= 0.999;
12
13
        }
14
   }
```

6.4 Other Method

6.4.1 Enumerate Subset

```
for(int i = 0; i < (1 << k); i++) {
  for(int j = i; ; --j &= i) {
      // work();
      if(j == 0) break;
    }
}</pre>
```

6.4.2 Enumerate $\lfloor \frac{n}{d} \rfloor \lfloor \frac{m}{d} \rfloor$

```
int cal(int n, int m) {
   if(n > m) swap(n, m);
   int res = 0, last;
   for(int i = 1; i <= n; i = last + 1) {
        last = min(n / (n / i), m / (m / i));
        res += (n / i) * (m / i) * (sum(last) - sum(i - 1));
   }
   return res;
}</pre>
```

6.5 Formula

6.5.1 Euler's Theorem

$$a^b \equiv \begin{cases} a^{b\%\varphi(p)} & \gcd(a,p) = 1 \\ a^b & \gcd(a,p) \neq 1, b < \varphi(p) \\ a^{b\%\varphi(p) + \varphi(p)} & \gcd(a,p) \neq 1, b \geq \varphi(p) \end{cases} \end{cases} (mod \ p)$$

6.5.2 Möbius Inversion Formula

Dirichlet Convolution is $(f\times g)(N)=\sum_{d\mid N}f(d)*g(\frac{N}{d})$ Theorem:

$$\begin{cases} f = g \times 1 \\ g = f \times \mu \end{cases}$$

6.5.3 Math Theory Tips

$$\begin{cases} id(n) = \sum_{d|n} \varphi(d) \\ e(n) = \sum_{d|n} \mu(d) \end{cases}$$
 (1)

$$\begin{cases}
\sum_{i}^{n} \sum_{j}^{m} gcd(i,j) = \sum_{d}^{\max(n,m)} \varphi(d) * \lfloor \frac{n}{d} \rfloor \lfloor \frac{m}{d} \rfloor \\
\sum_{i}^{n} \sum_{j}^{m} e(gcd(i,j)) = \sum_{d}^{\min(n,m)} \mu(d) * \lfloor \frac{n}{d} \rfloor \lfloor \frac{m}{d} \rfloor \\
\sum_{i=1}^{n} |\mu(i)| = \sum_{i=1}^{\lfloor \sqrt{n} \rfloor} \mu(i) * \lfloor \frac{n}{i * i} \rfloor
\end{cases} \tag{2}$$

$$\begin{cases} sum(x,y) = \sum_{i}^{x} \sum_{j}^{y} i * j = \frac{x * (x+1)}{2} * \frac{y * (y+1)}{2} \\ F(x,y) = \sum_{i=1}^{\min(x,y)} i^{2} * \mu(i) * sum(\lfloor \frac{x}{i} \rfloor, \lfloor \frac{y}{i} \rfloor) \\ \sum_{i}^{n} \sum_{j}^{m} lcm(i,j) = \sum_{i=1}^{\min(n,m)} d * F(\lfloor \frac{n}{i} \rfloor, \lfloor \frac{y}{i} \rfloor) \end{cases}$$

$$(3)$$

6.5.4 Sieve Tips

$$\varphi(n) = \sum_{i=1}^{n} [(n,i) = 1] \cdot i = \frac{n * \varphi(n) + [n=1]}{2}$$
(4)

$$\begin{cases}
id = \varphi \times 1 \\
\frac{n \cdot (n+1)}{2} = \sum_{i=1}^{n} i = \sum_{i=1}^{n} \sum_{d|i} \cdot \varphi(d) = \sum_{\frac{i}{d}=1}^{n} \sum_{d=1}^{\lfloor \frac{n}{d} \rfloor} \varphi(d) = \sum_{i=1}^{n} \phi(\lfloor \frac{n}{i} \rfloor)
\end{cases}$$
(5)

$$\begin{cases} e = \mu \times 1 \\ 1 = \sum_{i=1}^{n} [i = 1] = \sum_{i=1}^{n} \sum_{d \mid i} \mu(d) = \sum_{i=1}^{n} \sum_{d=1}^{\lfloor \frac{n}{i} \rfloor} \mu(d) = \sum_{i=1}^{n} M(\lfloor \frac{n}{i} \rfloor) \end{cases}$$
(6)

$$\begin{cases}
id^{2} = (id \cdot \varphi) \times id \\
\phi'(n) = \sum_{i=1}^{n} i \cdot \varphi(i) \\
\frac{n \cdot (n+1) \cdot (2n+1)}{6} = \sum_{i=1}^{n} i^{2} = \sum_{i=1}^{n} \sum_{d \mid i} d \cdot \varphi(d) \cdot \frac{i}{d} = \sum_{\frac{i}{d}=1}^{\lfloor \frac{n}{i} \rfloor} d \cdot \varphi(d) = \sum_{i=1}^{n} i \cdot \phi'(\lfloor \frac{n}{i} \rfloor)
\end{cases}$$
(7)