# SOUTH CHINA UNIVERSITY OF TECHNOLOGY

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# **TEMPLATE**



0 error(s), 0 warning(s)

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# 1 Graph Theory

#### 1.1 Shortest Path

#### 1.1.1 Dijkstra

```
typedef pair<int, int> P;
2
   struct Edge {
        int to, nxt;
3
4
        LL w;
5
   }e[MAXM];
   int head[MAXN], ecnt;
   LL d[MAXN];
7
   priority_queue<P, vector<P>, greater<P> > q;
8
   inline void addEdge(int x, int y, LL w) {
9
       e[++ecnt] = (Edge) \{y, head[x], w\}; head[x] = ecnt;
10
11
12
   void dijkstra(int st) {
13
       memset(d, 0x3f, sizeof(d));
14
        d[st] = 0;
15
        q.push(make_pair(0, st));
16
       while(!q.empty()) {
17
            P x = q.top(); q.pop();
18
            int u = x.second;
            for(int i = head[u], v; i; i = e[i].nxt) {
19
                v = e[i].to;
20
                if(d[v] > d[u] + e[i].w) {
21
                    d[v] = d[u] + e[i].w;
22
23
                    q.push(make_pair(d[v], v));
24
                }
25
            }
26
       }
27
   }
```

#### 1.1.2 SPFA

```
struct Edge {
1
2
       int to, nxt;
3
       LL w;
   }e[MAXE];
4
5
   int head[MAXN], ecnt;
6 LL d[MAXN];
7
   bool exist[MAXN];
   queue<int> q;
8
9
   inline void addEdge(int x, int y, LL w) {
       e[++ecnt] = (Edge) \{y, head[x], w\}; head[x] = ecnt;
10
11
   void SPFA(int st) {
12
       memset(d,0x3f,sizeof(d));
13
        d[st] = 0;
14
        q.push(st);
15
        exist[st] = 1;
16
17
       while(!q.empty()) {
18
            int u = q.front(); q.pop();
19
            exist[u] = 0;
            for(int i = head[u], v; i; i = e[i].nxt) {
20
21
                v = e[i].to;
                if(d[v] > d[u] + e[i].w) {
22
```

```
d[v] = d[u] + e[i].w;
23
24
                      //pre[v] = u;
25
                      if(!exist[v]) {
26
                          q.push(v);
                          exist[v] = 1;
27
                      }
28
29
                 }
            }
30
        }
31
   }
32
```

#### 1.2 Network Flow

#### 1.2.1 ISAP

```
namespace NWF {
1
2
          struct Edge{
3
               int to, nxt;LL f;
          e[MAXM << 1];
 4
 5
          int S, T, tot;
          int ecnt, head[MAXN], cur[MAXN], pre[MAXN], num[MAXN], dis[MAXN];
 6
 7
          queue<int> q;
         void init(int _S, int _T, int _tot){
   ecnt = 1; S = _S; T = _T; tot = _tot;
   memset(num, 0, (tot + 1) * sizeof(int));
   memset(head, 0, (tot + 1) * sizeof(int));
 8
 9
10
11
12
          inline void addEdge(int u, int v, LL f) {
13
               e[++ecnt] = (Edge) \{v, head[u], f\}; head[u] = ecnt; e[++ecnt] = (Edge) \{u, head[v], 0\}; head[v] = ecnt;
14
15
16
          void bfs() {
17
               memset(dis, 0, (tot + 1) * sizeof(int));
18
19
               q.push(T);
20
               dis[T] = 1;
21
               while(!q.empty()) {
22
                    int u = q.front(), v; q.pop();
23
                    num[dis[u]]++;
                    for(int i = cur[u] = head[u]; i; i = e[i].nxt) {
24
                         if(!dis[v = e[i].to]) {
25
                              dis[v] = dis[u] + 1;
26
27
                               q.push(v);
28
                         }
29
                    }
               }
30
31
          LL augment() {
32
               LL flow = INF;
33
               for(int i = S; i != T; i = e[cur[i]].to)
34
               flow = min(flow, e[cur[i]].f);
for(int i = S; i != T; i = e[cur[i]].to) {
35
36
                    e[cur[i]].f -= flow;
37
                    e[cur[i] ^ 1].f += flow;
38
39
40
               return flow;
41
          LL isap() {
42
43
               bfs();
               int u = S, v;
44
```

```
LL flow = 0;
45
            while(dis[S] <= tot) {</pre>
46
47
                 if(u == T) {
                     flow += augment();
48
                     u = S;
49
50
                 bool fg = 0;
51
                 for(int i = cur[u]; i; i = e[i].nxt) {
52
                     if(e[i].f && dis[u] > dis[v = e[i].to]) {
53
                          pre[v] = u;
54
                          cur[u] = i;
55
                          u = v;
56
                          fg = 1;
57
                          break;
58
59
                     }
60
                 if(fg) continue;
61
                 if(!--num[dis[u]]) break;
62
                 int maxDis = tot;
63
                 for(int i = head[u]; i; i = e[i].nxt) {
64
                     if(e[i].f \&\& maxDis > dis[v = e[i].to]) {
65
                          maxDis = dis[v];
66
                          cur[u] = i;
67
                     }
68
69
70
                 num[dis[u] = maxDis + 1]++;
71
                 if(u != S) u = pre[u];
72
73
            return flow;
        }
74
   }
75
```

#### 1.2.2 HLPP

```
namespace NWF{
1
2
         struct Edge{
              int to,nxt;LL f;
3
         e[MAXM << 1];
4
5
         int S, T, tot;
         int ecnt, head[MAXN], dis[MAXN], num[MAXN];
6
7
         LL sumf[MAXN];
8
         queue<int> q;
9
         list<int> dep[MAXN];
         void init(int _S,int _T,int _tot){
10
              ecnt = 1;S = _S;T = _T;tot = _tot;
memset(num, 0, (tot + 1) * sizeof(int));
memset(head, 0, (tot + 1) * sizeof(int));
11
12
13
              memset(sumf, 0, (tot + 1) * sizeof(LL));
14
15
         void addEdge(int u,int v,LL f){
16
              e[++ecnt] = (Edge) \{v, head[u], f\}; head[u] = ecnt; e[++ecnt] = (Edge) \{u, head[v], 0\}; head[v] = ecnt;
17
18
19
         void bfs(){
20
              memset(dis, 0, (tot + 1) * sizeof(int));
21
              q.push(T); dis[T] = 1;
22
23
              while(!q.empty()){
24
                    int u=q.front(), v; q.pop();
25
                    for(int i = head[u]; i; i = e[i].nxt)
26
                    if(!dis[v = e[i].to]){
```

```
dis[v] = dis[u] + 1;
27
28
                     q.push(v);
29
                 }
            }
30
31
        LL hlpp(){
32
            bfs();
33
34
            dis[S] = tot + 1;
            for(int i = 1;i <= tot; ++i)num[dis[i]]++;</pre>
35
            for(int i = tot + 1; ~i; --i)dep[i].clear();
36
            int_maxd = dis[S];LL f;
37
            dep[maxd].push_back(S);sumf[S] = INF;
38
39
            for(;;){
                 while(maxd && dep[maxd].empty())maxd--;
40
41
                 if(!maxd)break;
                 int u = dep[maxd].back(), v;dep[maxd].pop_back();
42
                 int minDis = tot + 1;
43
                 for(int i = head[u]; i;i = e[i].nxt)
44
45
                 if(e[i].f){
                     if(dis[u] > dis[v = e[i].to]){
46
                         f = min(sumf[u], e[i].f);
47
                         e[i].f -= f; e[i^1].f += f;
48
                         if(sumf[u] != INF) sumf[u] -= f;
49
50
                         if(sumf[v] != INF) sumf[v] += f;
                         if(v!=S \&\& v!=T \&\& sumf[v] == f){
51
                              maxd = max(maxd, dis[v]);
52
53
                              dep[dis[v]].push_back(v);
54
                         if(!sumf[u])break;
55
                     }else minDis=min(minDis, dis[v] + 1);
56
57
                 if(sumf[u]){
58
                     if(!--num[dis[u]]){
59
                         for(int i = dis[u];i <= maxd;++i){</pre>
60
                              while(!dep[i].empty()){
61
                                  --num[i];
62
                                  dis[dep[i].back()] = tot + 1;
63
                                  dep[i].pop_back();
64
                              }
65
66
                         }
67
                         maxd = dis[u] - 1; dis[u] = tot + 1;
                     }else{
68
                         dis[u] = minDis;
69
                         if(minDis > tot)continue;
70
                         num[minDis]++;
71
                         maxd = max(maxd, minDis);
72
73
                         dep[minDis].push_back(u);
                     }
74
75
                 }
76
            return sumf[T];
77
78
    }
79
```

# 1.2.3 Dinic

```
namespace NWF {
struct Edge {
    int to, nxt;LL f;
} e[MAXM << 1];</pre>
```

```
5
         int S, T, tot;
         int ecnt, head[MAXN], cur[MAXN], dis[MAXN];
 6
         queue<int> q;
 7
         void init(int _S, int _T, int _tot){
    ecnt = 1; S = _S; T = _T; tot = _tot;
    memset(head, 0, (tot + 1) * sizeof(int));
 8
 9
10
11
         void addEdge(int u, int v, LL f) {
    e[++ecnt] = (Edge) {v, head[u], f}; head[u] = ecnt;
    e[++ecnt] = (Edge) {u, head[v], 0}; head[v] = ecnt;
12
13
14
15
         bool bfs() {
16
              memset(dis, 0, (tot + 1) * sizeof(int));
17
              q.push(S); dis[S] = 1;
18
19
              while (!q.empty()) {
                   int u = q.front(), v; q.pop();
20
                   for (int i = cur[u] = head[u]; i ; i = e[i].nxt) {
21
22
                        if (e[i].f && !dis[v = e[i].to]) {
23
                              q.push(v);
                              dis[v] = dis[u] + 1;
24
                        }
25
                   }
26
27
              }
28
              return dis[T];
29
30
         LL dfs(int u, LL maxf) {
31
              if (u == T) return maxf;
              LL sumf = maxf;
32
              for (int &i = cur[u]; i; i = e[i].nxt) {
33
                   if (e[i].f && dis[e[i].to] > dis[u]) {
34
                        LL tmpf = dfs(e[i].to, min(sumf, e[i].f));
35
                        e[i].f -= tmpf; e[i ^ 1].f += tmpf;
36
                        sumf -= tmpf;
37
                        if (!sumf) return maxf;
38
39
                   }
              }
40
              return maxf - sumf;
41
42
43
         LL dinic() {
44
              LL ret = 0;
45
              while (bfs()) ret += dfs(S, INF);
46
              return ret;
47
         }
48
```

#### 1.2.4 MCMF

```
1
    namespace NWF{
2
        struct Edge {
3
            int to, nxt;LL f, c;
4
        } e[MAXM << 1];</pre>
        int S, T, tot;
int ecnt, head[MAXN], cur[MAXN];LL dis[MAXN];
5
6
7
        bool exist[MAXN];
        queue<int> q;
8
        void init(int _S, int _T, int _tot){
9
            ecnt = 1; S = _S; T = _T; tot = _tot;
10
11
            memset(head, 0, (tot + 1) * sizeof(int));
12
13
        void addEdge(int u, int v, LL f, LL c) {
```

```
e[++ecnt] = (Edge) \{v, head[u], f, c\}; head[u] = ecnt;
14
              e[++ecnt] = (Edge) \{u, head[v], 0, -c\}; head[v] = ecnt;
15
16
         bool spfa() {
17
              for(int i = 0;i <= tot; ++i){</pre>
18
                   dis[i] = INF; exist[i] = cur[i] = 0;
19
20
              q.push(S);dis[S] = 0;exist[S] = 1;
21
              while(!q.empty()) {
22
                   int u = q.front(), v; q.pop();exist[u] = 0;
23
                   for(int i = head[u]; i; i = e[i].nxt) {
    if(e[i].f && dis[v = e[i].to] > dis[u] + e[i].c) {
24
25
26
                            dis[v] = dis[u] + e[i].c;
                             cur[v] = i;
27
                             if(!exist[v]) {
28
                                  q.push(v);
29
                                  exist[v] = 1;
30
31
                            }
32
                        }
                   }
33
              }
34
              return dis[T] != INF;
35
36
         LL mcmf() {
37
              LL cost = 0;
38
              while(spfa()) {
39
40
                   LL flow = INF;
41
                   for(int i = T; i != S; i = e[cur[i] ^ 1].to)
                   flow = min(flow, e[cur[i]].f);
for(int i = T; i != S; i = e[cur[i] ^ 1].to) {
    e[cur[i]].f -= flow;
42
43
44
                        e[cur[i] \land 1].f += flow;
45
46
                   cost += flow * dis[T];
47
              }
48
              return cost;
49
50
         }
51
    }
```

#### 1.3 Tree Related

### 1.3.1 Kruskal

```
namespace MST{
1
2
        struct Edge{
3
            int u,v; LL w;
            bool operator < (const Edge& x) const { return w < x.w; }</pre>
4
        }e[MAXM];
5
        int ecnt, fa[MAXN];
6
        void addEdge(int u, int v, LL w) {
7
            e[++ecnt] = (Edge)\{v, u, w\}; headp[u] = ecnt;
8
9
        int Find(int x) { return x == fa[x] ? x : fa[x] = Find(fa[x]); }
10
        LL kruskal(int n) {
11
12
            sort(e + 1, e + ecnt + 1);
            for(int i = 1; i <= n; i++) fa[i] = i;
13
            LL sum = 0;
14
            for (int i = 1; i <= ecnt; i++){
15
                int fu = Find(e[i].u), fv = Find(e[i].v);
16
```

```
if(fu != fv){
    fa[fu] = fv;
    sum += e[i].w;

return sum;
}
```

#### 1.3.2 Prim

```
namespace MST {
1
2
        struct Edge{
3
             int to,nxt; LL w;
        }e[MAXM];
4
5
        int ecnt, head[MAXN], vis[MAXN]; // pre[MAXN];
        LL dis[MAXN];
6
        void addEdge(int u, int v, LL w){
7
8
             e[++ecnt] = (Edge)\{v, head[u], w\}; head[u] = ecnt;
9
             e[++ecnt] = (Edge)\{u, head[v], w\}; head[v] = ecnt;
10
        LL Prim(int n){
11
             for (int i = 1; i <= n; i++){</pre>
12
13
                  //pre[i] = 0;
                 vis[i] = 0;
14
                 dis[i] = INF;
15
16
             vis[1] = 1;
17
             LL sum = 0;
18
             for (int i = head[1]; i; i = e[i].nxt)
19
20
                 dis[e[i].to] = min(dis[e[i].to],e[i].w);
             for (int j = 1; j < n; j++){
   int u; LL minDis = INF;</pre>
21
22
                 for (int i = 1; i <= n; ++i)</pre>
23
                      if (!vis[i] && dis[i] < minDis){</pre>
24
25
                          minDis = dis[i];
26
                          u = i;
27
                 if (minDis == INF) return -1;
28
                 vis[u] = 1;
29
30
                 sum += minDis;
                 for (int i = head[u], v; i; i = e[i].nxt)
31
                 if (!vis[v = e[i].to] && e[i].w < dis[v]){</pre>
32
                      //pre[u] = v;
33
                      dis[v] = e[i].w;
34
35
36
             return sum;
37
38
        }
39
   }
```

#### 1.3.3 Tree Divide and Conquer

```
struct Edge {
    int to, nxt, w;
}e[MAXM];
int head[MAXN], ecnt;
int sz[MAXN];
```

```
int d[MAXN], t[5], ans;
7
    bool vis[MAXN];
   inline void add_edge(int u, int v, int w) {
   e[++ecnt] = (Edge) {v, head[u], w}; head[u] = ecnt;
8
9
        e[++ecnt] = (Edge) \{u, head[v], w\}; head[v] = ecnt;
10
11
12
    int getsz(int x, int fa) {
        sz[x] = 1;
13
        for(int i = head[x]; i; i = e[i].nxt) {
14
15
             int y = e[i].to;
            if(vis[y] || y == fa) continue;
16
17
            sz[x] += getsz(y, x);
        }
18
19
        return sz[x];
20
21
    int getrt(int x) {
        int tot = getsz(x, 0) >> 1;
22
23
        while(1) {
24
             int u = -1;
             for(int i = head[x]; i; i = e[i].nxt) {
25
26
                 int y = e[i].to;
                 if(vis[y] || sz[y] > sz[x]) continue;
27
                 if(u == -1 \mid | sz[y] > sz[u]) u = y;
28
29
30
            if(\sim u \&\& sz[u] > tot) x = u;
31
            else break;
32
        }
33
        return x;
34
    void getdep(int x, int fa) {
35
36
        t[d[x]]++;
        for(int i = head[x]; i; i = e[i].nxt) {
37
             int y = e[i].to;
38
            if(vis[y] || y == fa) continue;
39
            d[y] = (d[x] + e[i].w) % 3;
40
            getdep(y, x);
41
        }
42
   }
43
    int cal(int x, int v) {
44
45
        t[0] = t[1] = t[2] = 0;
46
        d[x] = v \% 3;
47
        getdep(x, 0);
        return t[0] * t[0] + t[1] * t[2] * 2;
48
49
   void solve(int x) {
50
        vis[x] = 1;
51
52
        ans += cal(x, 0);
        for(int i = head[x]; i; i = e[i].nxt) {
53
             int y = e[i].to;
54
55
             if(vis[y]) continue;
            ans -= cal(y, e[i].w);
56
             solve(getrt(y));
57
        }
58
59
   int main() {
60
        solve(getrt(1));
61
62
   }
```

#### 1.4 LCA

#### 1.4.1 Tree Decomposition LCA

```
int sz[MAXN], dep[MAXN], top[MAXN], fa[MAXN], son[MAXN], num[MAXN], totw;
   struct Edge {
        int to, nxt;
   }e[MAXN << 1];
   int head[MAXN], ecnt;
   inline void add_edge(int x, int y) {
6
        e[++ecnt] = (Edge) \{y, head[x]\}; head[x] = ecnt;
7
8
9
   void dfs1(int x) {
10
        sz[x] = 1; son[x] = 0;
11
        for(int i = head[x]; i; i = e[i].nxt) {
12
            int v = e[i].to;
13
            if(v == fa[x]) continue;
14
            fa[v] = x;
            dep[v] = dep[x] + 1;
15
16
            dfs1(v);
            sz[x] += sz[v];
17
            if(sz[v] > sz[son[x]]) son[x] = v;
18
       }
19
   }
20
   void dfs2(int x) {
21
        B[num[x]] = A[x];
22
        if(son[x]) {
23
24
            top[son[x]] = top[x];
25
            num[son[x]] = ++totw;
26
            dfs2(son[x]);
27
        for(int i = head[x]; i; i = e[i].nxt) {
28
            int v = e[i].to;
29
            if(v == fa[x] | | v == son[x]) continue;
30
            top[v] = v;
31
32
            num[v] = ++totw;
33
            dfs2(v);
34
       }
35
36
   int lca(int u, int v) {
        if(u == v) return u;
37
       while(top[u] != top[v]) {
38
            if(dep[top[u]] > dep[top[v]]) swap(u, v);
39
            v = fa[top[v]];
40
41
       if(dep[u] > dep[v]) swap(u, v);
42
        return u;
43
44
   inline void init() {
45
       memset(head, 0, sizeof(head)); ecnt = 0;
46
        fa[1] = 0; dep[1] = 1; top[1] = 1; num[1] = 1; totw = 1;
47
48
   inline void pre() {
49
50
        dfs1(1); dfs2(1);
51
   }
```

#### 1.4.2 Tarjan LCA

```
vector< pair<int,int> > G[MAXN],ask[MAXN];
```

```
int fa[MAXN], ans[MAXN], vis[MAXN] ,dis[MAXN];
2
3
   int Find(int x){
        return x == fa[x] ? x : fa[x] = Find(fa[x]);
4
5
   void init(int n){
6
        memset(ans, 0,sizeof ans);
7
8
        memset(vis, 0,sizeof vis);
        for(int i = 0; i \le n; i++){
9
            G[i].clear();
10
            ask[i].clear();
11
        }
12
   }
13
    void LCA(int u){
14
15
        int v;
        fa[u] = u;
16
        vis[u] = true;
17
        for(auto it : ask[u])
18
19
            if(vis[v = it.first])
                ans[it.second] = dis[u] + dis[v] - 2 * dis[Find(it.first)];
20
        for(auto it : G[u])
21
        if(!vis[v = it.first]){
22
            dis[v] = dis[u] + it.second;
23
            LCA(v);
24
25
            fa[v] = u;
26
        }
27
   }
```

# 1.5 Tarjan

#### 1.5.1 SCC

```
namespace SCC{
1
2
        vector<int> G[MAXN];
3
        int dfs_clock, scc_cn, dfn[MAXN], low[MAXN], sccno[MAXN];
        stack<int> S;
4
5
        void addEdge(int u, int v) {
6
            G[u].push_back(v);
7
        void tarjan(int u) {
8
            dfn[u] = low[u] = ++dfs\_clock;
9
            S.push(u);
10
            for(auto v : G[u]) {
11
                 if(!dfn[v]) {
12
                    tarjan(v);
13
                     low[u] = min(low[u], low[v]);
14
                }else if(!sccno[v]) {
15
16
                     low[u] = min(low[u], dfn[v]);
17
18
            if(dfn[u] == low[u]) {
19
20
                scc_cnt++;
21
                for(;;) {
                     int v = S.top(); S.pop();
22
                     sccno[v] = scc_cnt;
23
                     if(v == u) break;
24
25
                }
26
            }
27
        void findSCC(int n) {
28
```

```
for(int i = 1; i <= n; i++)</pre>
29
30
                  if(!dfn[i]) tarjan(i);
31
        void init(int n){
32
             dfs_clock = scc_cnt = 0;
33
             for(int i = 0;i <= n;++i){</pre>
34
35
                  dfn[i] = low[i] = sccno[i] = 0;
36
                  G[i].clear();
             }
37
        }
38
    }
39
```

#### 1.5.2 BCC

```
namespace BCC{
 1
 2
         struct Edge {
              int to, nxt;
 3
         e[MAXM << 1];
 4
 5
         int ecnt, head[MAXN];
 6
         int dfs_clock, dfn[MAXN], low[MAXN];
 7
         int is_vertex[MAXN], vbcc_cnt, vbccno[MAXN];
 8
 9
         vector<int> vbcc[MAXN];
10
         stack<int> vS;
11
         int ebcc_cnt, ebccno[MAXN];
12
13
         stack<int> eS;
14
         inline void addEdge(int u, int v) {
    e[++ecnt] = (Edge) {v, head[u]}; head[u] = ecnt;
    e[++ecnt] = (Edge) {u, head[v]}; head[v] = ecnt;
15
16
17
18
         inline void init(int n) {
19
              ecnt = 1;
20
21
              dfs\_clock = 0;
22
              vbcc\_cnt = 0;
23
              ebcc\_cnt = 0;
              for(int i = 1; i <= n; ++i){</pre>
24
                  head[i] = dfn[i] = low[i] = 0;
25
26
                   is_vertex[i] = 0;
27
                  vbccno[i] = 0;
28
                  ebccno[i] = 0;
29
              while(!vS.empty()) vS.pop();
30
         }
31
32
         //root 's edge = -1;
33
         void tarjan(int u, int edge) {
              dfn[u] = low[u] = ++dfs\_clock;
34
35
              int ch = 0;
36
              vS.push(u);
37
              eS.push(u);
              for(int i = head[u], v; i; i = e[i].nxt) {
    if(!dfn[v = e[i].to]) {
38
39
                       tarjan(v, i ^ 1)
40
                       low[u] = min(low[u], low[v]);
41
                       if(low[v] >= dfn[u]) {
42
                            ++ch;
43
                            if(edge > 0 || ch > 1) is_vertex[u] = 1;
44
45
                            vbcc[++vbcc_cnt].clear();
46
                            vbcc[vbcc_cnt].push_back(u);
```

```
for(int x;;){
47
                               x = vS.top();vS.pop();
48
                               vbcc[vbcc_cnt].push_back(x);
49
50
                               vbccno[x] = vbcc_cnt;
51
                               if(x == v)break;
52
53
                      if(low[v] > dfn[u]) {
// i && i ^ 1 is bridge
}
54
55
56
57
                 else if(dfn[v] < dfn[u] && i != edge)</pre>
58
                      low[u] = min(low[u], dfn[v]);
59
60
             if(dfn[u] == low[u]) {
61
                 ebcc_cnt++;
62
                 for(int v;;) {
63
                      v = eS.top(); eS.pop();
64
65
                      ebccno[v] = ebcc_cnt;
                      if(v == u) break;
66
                 }
67
             }
68
69
        void findBCC(int n){
70
71
             for(int i = 1; i <= n; i++)
72
                 if(!dfn[i]) tarjan(i, -1);
73
74
             //findBridge
             for(int u = 1; u <= n; u++) {
75
                  for(int i = head[u], v; i; i = e[i].nxt)
76
                 if(ebccno[u] != ebccno[v = e[i].to]) {
77
78
                      //is bridge
79
            }
80
        }
81
   }
82
```

# 1.6 Cactus

#### 1.6.1 Circle-Square Tree

```
#include <bits/stdc++.h>
1
2
   using namespace std;
3
   typedef pair<int, int> P;
   const int MAXN = 2e4 + 5;
4
   const int S = 15;
5
6
   namespace Tree {
7
        struct Edge {
8
            int to, nxt, w;
        }e[MAXN << 1];
9
        int ecnt, head[MAXN];
10
        int rt, isrt[MAXN], fa[MAXN][S + 3];
11
        int sz[MAXN];
12
        inline void addEdge(int u, int v, int w) {
13
            e[++ecnt] = (Edge) \{v, head[u], w\}; head[u] = ecnt;
14
            fa[v][0] = u;
15
       }
16
17
   int n, m, Q;
```

```
namespace BCC {
19
20
        struct Edge {
21
            int to, nxt, w;
        }e[MAXN << 1];</pre>
22
        int ecnt, head[MAXN];
23
        int dfs_clock, dfn[MAXN], low[MAXN];
24
25
        int is_vertex[MAXN], vbcc_cnt, vbccno[MAXN];
26
        vector<P> vbcc[MAXN];
        stack<P> vs;
27
        int tag[MAXN];
28
        inline void addEdge(int u, int v, int w) {
29
            e[++ecnt] = (Edge) \{v, head[u], w\}; head[u] = ecnt;
30
            e[++ecnt] = (Edge) \{u, head[v], w\}; head[v] = ecnt;
31
32
33
        inline void init(int n) {
34
            ecnt = 1;
            dfs\_clock = 0;
35
            vbcc\_cnt = 0;
36
            for(int i = 0; i <= 2 * n; i++){</pre>
37
38
                 head[i] = dfn[i] = low[i] = 0;
                 vbccno[i] = 0;
39
                 tag[i] = 0;
40
41
            while(!vs.empty()) vs.pop();
42
        }
43
44
        //root 's edge = -1;
45
        void tarjan(int u, int edge) {
46
            dfn[u] = low[u] = ++dfs\_clock;
47
            vs.push(P(u, e[edge ^ 1].w));
            for(int i = head[u], v; i; i = e[i].nxt) {
   if(!dfn[v = e[i].to]) {
48
49
                     tarjan(v, i ^ 1)
50
                     low[u] = min(low[u], low[v]);
51
                     if(low[v] >= dfn[u]) {
52
                          if(vs.top().first == v) {
53
                              Tree::addEdge(u, v, vs.top().second);
54
                              vs.pop();
55
                              continue;
56
57
58
                          vbcc[++vbcc_cnt].clear();
59
                          vbcc[vbcc_cnt].push_back(P(u, 0));
                          Tree::isrt[u] = 1;
60
                          int &sz = Tree::sz[n + vbcc_cnt];
61
                          tag[vs.top().first] = n + vbcc_cnt;
62
63
                          //Tree::addEdge(u, rt, 0);
                          for(P x;;) {
64
65
                              x = vs.top(); vs.pop();
66
                              sz += x.second;
67
                              //Tree::addEdge(rt, x.first, sz);
                              vbcc[vbcc_cnt].push_back(x);
68
                              vbccno[x.first] = vbcc_cnt;
69
                              if(x.first == v) break;
70
71
                          }
                     }
72
73
                 else if(dfn[v] < dfn[u] && i != edge)</pre>
74
75
                     low[u] = min(low[u], dfn[v]);
76
            for(int i = head[u], v; i; i = e[i].nxt) {
77
                 if(tag[v = e[i].to]) {
78
79
                     int r = tag[v]; Tree::sz[r] += e[i].w;
```

```
tag[v] = 0;
80
                 }
81
82
             }
83
         void findBCC(int n) {
84
             for(int i = 1; i <= n; i++)
85
                 if(!dfn[i]) tarjan(i, -1);
86
87
        }
88
    namespace Tree {
89
         int dis[MAXN], dep[MAXN], len[MAXN];
90
         inline void init(int n) {
91
             BCC::init(n);
92
93
             rt = n;
94
             ecnt = 1;
             for(int i = 0; i <= 2 * n; i++) {
95
                 head[i] = 0;
96
                 fa[i][0] = isrt[i] = dis[i] = dep[i] = len[i] = 0;
97
98
             }
99
         void dfs(int x) {
100
             for(int i = head[x], y; i; i = e[i].nxt) {
101
                 if(!dep[y = e[i].to]) {
102
                      dep[y] = dep[x] + 1;
103
                      dis[y] = dis[x] + e[i].w;
104
105
                      dfs(y);
106
                 }
             }
107
108
         void pre() {
109
             for(int k = 1; k <= BCC::vbcc_cnt; k++) {</pre>
110
111
                  rt++;
                 vector<P> &E = BCC::vbcc[k];
112
                 addEdge(E[0].first, rt, 0);
113
                 int cnt = 0;
114
                 for(int i = E.size() - 1; i >= 1; i--) {
115
                      cnt += E[i].second;
116
                      len[E[i].first] = cnt;
117
                      addEdge(rt, E[i].first, min(cnt, sz[rt] - cnt));
118
119
                 }
120
             for(int k = 1; k <= S; k++) {</pre>
121
                 for(int i = 1; i <= rt; i++) {</pre>
122
                      fa[i][k] = fa[fa[i][k - 1]][k - 1];
123
124
125
             dep[1] = 1;
126
             dfs(1);
127
128
         int up(int x, int d) {
129
             for(int i = S; i >= 0; i--) {
130
                  if(dep[fa[x][i]] >= d) x = fa[x][i];
131
132
             return x;
133
134
         int lca(int u, int v) {
135
             if(dep[u] > dep[v]) swap(u, v);
136
             v = up(v, dep[u]);
137
             if(u == v) return u;
138
             for(int i = S; i >= 0; i--) {
139
                 if(fa[u][i] != fa[v][i]) {
140
```

```
u = fa[u][i], v = fa[v][i];
141
142
               }
143
               return fa[u][0];
144
145
          int query(int u, int v) {
146
               int l = lca(u, v);
if(l <= n) return dis[u] + dis[v] - 2 * dis[l];</pre>
147
148
               int x = up(u, dep[l] + 1), y = up(v, dep[l] + 1);
int res = dis[u] - dis[x] + dis[v] - dis[y];
149
150
               int tmp = abs(len[x] - len[y]);
return res + min(tmp, sz[l] - tmp);
151
152
153
          }
     }
154
155
     int main() {
156
          ios::sync_with_stdio(0); cin.tie(0); cout.precision(6); cout << fixed;</pre>
157
158
          using namespace Tree;
159
          cin >> n >> m >> 0;
          init(n);
160
          for(int i = 1, u, v, w; i <= m; i++) {
161
               cin >> u >> v >> w;
162
               BCC::addEdge(u, v, w);
163
164
165
          BCC::findBCC(n);
          pre();
166
          int u, v;
167
168
          while(Q--) {
169
               cin >> u >> v;
               cout << query(u, v) << endl;</pre>
170
171
172
          return 0;
     }
173
```

# 2 Data Structures

#### 2.1 Basic Structures

#### 2.1.1 RMQ

```
struct RMQ {
1
        int d[MAXN][S + 2];
2
        inline void init(int *a, int n) {
3
            for(int i = 0; i < n; i++) d[i][0] = a[i];
4
5
            for(int k = 1; (1 << k) < n; k++)
6
                 for(int i = 0; i + (1 << k) - 1 < n; i++)
                     d[i][k] = min(d[i][k - 1], d[i + (1 << (k - 1))][k - 1]);
7
8
9
        inline int query(int 1, int r) {
            if(l > r) swap(l, r);
10
            int k = 0;
11
12
            while((1 << (k + 1)) <= r - l + 1) k++;
            return min(d[l][k], d[r - (1 << k) + 1][k]);</pre>
13
14
   }rmq;
15
    struct RMQ {
16
        LL a[MAXN];
17
        LL d[MAXM][S + 2];
LL pre[MAXM][S + 2], aft[MAXM][S + 2];
18
19
        inline void init(int n) {
20
            for(int i = 1; i <= sz; i++) {</pre>
21
                 pre[i][0] = aft[i][S + 1] = INF;
22
23
            for(int i = 1; i <= n; i++) {</pre>
24
                 pre[belong(i)][pos(i)] = min(pre[belong(i)][pos(i) - 1], a[i]);
25
26
27
            for(int i = n; i >= 1; i--) {
                 aft[belong(i)][pos(i)] = min(aft[belong(i)][pos(i) + 1], a[i]);
28
29
30
            for(int i = 1; i <= sz; i++) {
                 d[i][0] = aft[i][1];
31
32
33
            for(int k = 1; k <= S; k++)</pre>
                 for(int i = 1; i + (1 << k) <= SZ; i++)
34
                     d[i][k] = min(d[i][k - 1], d[i + (1 << (k - 1))][k - 1]);
35
36
        inline LL ask(int l, int r) {
37
            assert(l <= r);</pre>
38
39
            LL res = INF;
            if(belong(l) == belong(r)) {
40
                 for(int i = l; i <= r; i++) res = min(res, a[i]);</pre>
41
42
                 return res;
43
            res = min(aft[belong(l)][pos(l)], pre[belong(r)][pos(r)]);
44
            int k = Log[belong(r) - belong(l) - 1];
45
            if(~k) {
46
                 res = min(res, d[belong(l) + 1][k]);
47
                 res = min(res, d[belong(r) - (1 << k)][k]);
48
49
            return res;
50
51
52
   }rmq;
```

#### 2.1.2 Divide Blocks

```
int belong[MAXN], l[MAXN], r[MAXN];
1
   int sz, num;
3
   void build(int n) {
4
        sz = sqrt(n);
       num = n / sz; if(n % sz) num++;
5
        for(int i = 1; i <= num; i++) {</pre>
6
            l[i] = (i - 1) * sz + 1;
7
            r[i] = i * sz;
8
9
10
        r[num] = n;
        for(int i = 1; i <= n; i++) {
11
            belong[i] = (i - 1) / sz + 1;
12
13
14
```

#### 2.2 Tree Structures

#### 2.2.1 Tree Decomposition

```
int sz[MAXN], dep[MAXN], top[MAXN], fa[MAXN], son[MAXN], num[MAXN], totw;
1
2
   struct Edge {
3
        int to, nxt;
   e[MAXN << 1];
4
   int head[MAXN], ecnt;
5
6
   int n, m, Q;
   #define Ls(x) (x << 1)
7
   #define Rs(x) (x << 1 | 1)
   struct Tree {
9
        int l, r, lazy;
10
        LL sum, mx;
11
12
   }tree[MAXN << 2];</pre>
   int A[MAXN], B[MAXN];
14
   void push_up(int x) {
       tree[x].sum = tree[Ls(x)].sum + tree[Rs(x)].sum;
15
16
       tree[x].mx = max(tree[Ls(x)].mx, tree[Rs(x)].mx);
17
   void push_down(int x) {
18
       if(tree[x].lazy) {
19
20
            tree[Ls(x)].sum += tree[x].lazy * (tree[Ls(x)].r - tree[Ls(x)].l + 1);
21
            tree[Rs(x)].sum += tree[x].lazy * (tree[Rs(x)].r - tree[Rs(x)].l + 1);
22
            tree[Ls(x)].mx += tree[x].lazy;
23
            tree[Rs(x)].mx += tree[x].lazy;
24
            tree[Ls(x)].lazy += tree[x].lazy;
25
            tree[Rs(x)].lazy += tree[x].lazy;
26
            tree[x].lazy = 0;
       }
27
28
   void build(int x, int L, int R) {
29
30
        tree[x].lazy = 0;
        tree[x].l = L; tree[x].r = R;
31
32
        if(L == R) {
33
            tree[x].sum = B[L];
34
            tree[x].mx = B[L];
35
            return;
36
        int mid = (L + R) \gg 1;
37
       build(Ls(x), L, mid);
38
```

```
build(Rs(x), mid + 1, R);
39
40
        push_up(x);
41
   void update(int x, int L, int R, LL val) {
   if(tree[x].l >= L && tree[x].r <= R) {</pre>
42
43
             tree[x].lazy += val;
44
            tree[x].sum += val * (tree[x].r - tree[x].l + 1);
45
            tree[x].mx += val;
46
47
             return;
48
        push_down(x);
49
        int mid = (tree[x].l + tree[x].r) >> 1;
50
        if(L \leftarrow mid) update(Ls(x), L, R, val);
51
        if(R > mid) update(Rs(x), L, R, val);
52
53
        push_up(x);
54
   LL query(int x, int L, int R) {
55
        if(tree[x].1 >= L && tree[x].r <= R)
56
             return tree[x].sum;
57
58
        push_down(x);
        int mid = (tree[x].l + tree[x].r) >> 1;
59
        LL res = 0;
60
        if(L <= mid) res += query(Ls(x), L, R);</pre>
61
62
        if(R > mid) res += query(Rs(x), L, R);
        return res;
63
64
65
   LL query2(int x, int L, int R) {
66
        if(tree[x].l >= L \&\& tree[x].r <= R)
67
             return tree[x].mx;
68
        push_down(x);
        int mid = (tree[x].l + tree[x].r) >> 1;
69
        LL res = -INF;
70
        if(L \le mid) res = max(res, query2(Ls(x), L, R));
71
        if(R > mid) res = max(res, query2(Rs(x), L, R));
72
        return res;
73
   }
74
   inline void add_edge(int x, int y) {
75
        e[++ecnt] = (Edge) \{y, head[x]\}; head[x] = ecnt;
76
77
   void dfs1(int x) {
78
79
        sz[x] = 1; son[x] = 0;
80
        for(int i = head[x]; i; i = e[i].nxt) {
81
             int v = e[i].to;
82
             if(v == fa[x]) continue;
             fa[v] = x;
83
            dep[v] = dep[x] + 1;
84
            dfs1(v);
85
86
             sz[x] += sz[v];
            if(sz[v] > sz[son[x]]) son[x] = v;
87
        }
88
89
    void dfs2(int x) {
90
91
        B[num[x]] = A[x];
        if(son[x]) {
92
             top[son[x]] = top[x];
93
            num[son[x]] = ++totw;
94
95
            dfs2(son[x]);
96
        for(int i = head[x]; i; i = e[i].nxt) {
97
             int v = e[i].to;
98
             if(v == fa[x] | | v == son[x]) continue;
99
```

```
top[v] = v;
100
             num[v] = ++totw;
101
             dfs2(v);
102
103
        }
104
    void up(int a, int b, int c) {
105
         int f1 = top[a], f2 = top[b];
106
        while(f1 != f2) {
107
             if(dep[f1] < dep[f2]) { swap(a, b); swap(f1, f2); }
108
109
             update(1, num[f1], num[a], c);
             a = fa[f1];
110
             f1 = top[a];
111
112
         if(dep[a] > dep[b]) swap(a, b);
113
114
        update(1, num[a], num[b], c);
115
    int qsum(int a, int b) {
116
         if(a == b) return query(1, num[a], num[a]);
117
         int f1 = top[a], f2 = top[b];
118
119
         int res = 0;
        while(f1 != f2) {
120
             if(dep[f1] < dep[f2]) { swap(a, b); swap(f1, f2); }</pre>
121
             res += query(1, num[f1], num[a]);
122
             a = fa[f1];
123
             f1 = top[a];
124
125
126
        if(dep[a] > dep[b]) swap(a, b);
127
         res += query(1, num[a], num[b]);
128
         return res;
129
    int qmax(int a, int b) {
130
         if(a == b) return query2(1, num[a], num[a]);
131
         int f1 = top[a], f2 = top[b];
132
         int res = -10000000000;
133
        while(f1 != f2) {
134
             if(dep[f1] < dep[f2]) { swap(a, b); swap(f1, f2); }</pre>
135
136
             res = max(res, query2(1, num[f1], num[a]));
             a = fa[f1];
137
138
             f1 = top[a];
139
         if(dep[a] > dep[b]) swap(a, b);
140
141
         res = max(res, query2(1, num[a], num[b]));
         return res;
142
143
    }
    inline void init() {
144
        memset(head, 0, sizeof(head)); ecnt = 0;
145
146
         fa[1] = 0; dep[1] = 1; top[1] = 1; num[1] = 1; totw = 1;
147
    inline void pre() {
148
149
         dfs1(1); dfs2(1); build(1, 1, totw);
150
```

#### 2.2.2 Link-Cut Tree

```
namespace LCT {
   int fa[MAXN], rev[MAXN], tr[MAXN][2];
   int s[MAXN], val[MAXN];
   void push_up(int x) {
      int l = tr[x][0], r = tr[x][1];
      s[x] = s[l] + s[r] + val[x];
   }
}
```

```
7
        void Rev(int x) {
8
9
            rev[x] = 1; swap(tr[x][0], tr[x][1]);
10
        void push_down(int x) {
11
            if(!rev[x]) return;
12
            int l = tr[x][0], r = tr[x][1];
13
            rev[x] = 0;
14
            if(l) Rev(l); if(r) Rev(r);
15
16
        bool isroot(int x) {
17
            return tr[fa[x]][0] != x && tr[fa[x]][1] != x;
18
19
20
        void pre(int x) {
            if(!isroot(x)) pre(fa[x]);
21
22
            push_down(x);
23
24
        void rotate(int x) {
25
            int y = fa[x]; int z = fa[y];
            int l = tr[y][1] == x;
26
            int r = 1 \wedge 1;
27
            if(!isroot(y)) tr[z][tr[z][1] == y] = x;
28
29
            fa[x] = z; fa[y] = x; fa[tr[x][r]] = y;
            tr[y][l] = tr[x][r]; tr[x][r] = y;
30
31
            push_up(y);
32
33
        void splay(int x) {
            pre(x);
34
            int y, z;
35
            while(!isroot(x)) {
36
                y = fa[x]; z = fa[y];
37
                if(!isroot(y)) {
38
                     if((tr[z][0] == y) == (tr[y][0] == x))rotate(y);
39
                     else rotate(x);
40
41
                rotate(x);
42
43
            }
            push_up(x);
44
45
46
        void access(int x) {
47
            int y = 0;
            while(x) {
48
49
                splay(x); tr[x][1] = y;
                push_up(x);
50
51
                y = x; x = fa[x];
52
53
        void makeroot(int x) {
54
            access(x); splay(x); Rev(x);
55
56
        void lnk(int x, int y) {
57
            makeroot(x); fa[x] = y;
58
59
        void cut(int x, int y) {
60
            makeroot(x); access(y); splay(y);
61
            tr[y][0] = fa[x] = 0; push_up(y);
62
63
        void update(int x, int y) {
64
            makeroot(x); val[x] = y; push_up(x);
65
66
        int query(int x, int y) {
```

```
makeroot(x); access(y); splay(y);
68
69
            return s[y];
70
71
       bool check(int x, int y) {
            int tmp = y;
72
            makeroot(x); access(y); splay(x);
73
            while(!isroot(y)) y = fa[y];
74
            splay(tmp);
75
76
            return x == y;
77
   }
78
```

#### 2.3 Sequence Structures

#### 2.3.1 Segment Tree

```
#define Ls(x) (x << 1)
1
2
   #define Rs(x) (x \ll 1 | 1)
3
   struct Tree {
        int l, r, lazy;
4
5
        LL sum, mx;
   }tree[MAXN << 2];</pre>
6
7
   int A[MAXN];
8
   void push_up(int x) {
        tree[x].sum = tree[Ls(x)].sum + tree[Rs(x)].sum;
9
10
        tree[x].mx = max(tree[Ls(x)].mx, tree[Rs(x)].mx);
11
   void push_down(int x) {
12
        if(tree[x].lazy) {
13
            tree[Ls(x)].sum += tree[x].lazy * (tree[Ls(x)].r - tree[Ls(x)].l + 1);
14
            tree[Rs(x)].sum += tree[x].lazy * (tree[Rs(x)].r - tree[Rs(x)].l + 1);
15
            tree[Ls(x)].mx += tree[x].lazy;
16
            tree[Rs(x)].mx += tree[x].lazy;
17
            tree[Ls(x)].lazy += tree[x].lazy;
18
            tree[Rs(x)].lazy += tree[x].lazy;
19
20
            tree[x].lazy = 0;
21
        }
22
   }
23
   void build(int x, int L, int R) {
24
        tree[x].lazy = 0;
        tree[x].l = L; tree[x].r = R;
25
26
        if(L == R) {
27
            tree[x].sum = A[L];
28
            tree[x].mx = A[L];
            return;
29
30
31
        int mid = (L + R) \gg 1;
        build(Ls(x), L, mid);
build(Rs(x), mid + 1, R);
32
33
34
        push_up(x);
35
36
   void update(int x, int L, int R, LL val) {
        if(tree[x].l >= L && tree[x].r <= R) {</pre>
37
            tree[x].lazy += val;
38
            tree[x].sum += val * (tree[x].r - tree[x].l + 1);
39
            tree[x].mx += val;
40
41
            return;
42
        push_down(x);
```

```
int mid = (tree[x].l + tree[x].r) >> 1;
44
        if(L \leftarrow mid) update(Ls(x), L, R, val);
45
46
        if(R > mid) update(Rs(x), L, R, val);
47
        push_up(x);
48
49
   LL query(int x, int L, int R) {
        if(tree[x].l >= L && tree[x].r <= R)
50
            return tree[x].sum;
51
52
        push_down(x);
        int mid = (tree[x].l + tree[x].r) >> 1;
53
        LL res = 0;
54
        if(L <= mid) res += query(Ls(x), L, R);</pre>
55
        if(R > mid) res += query(Rs(x), L, R);
56
57
        return res;
58
   LL query2(int x, int L, int R) {
59
        if(tree[x].l >= L && tree[x].r <= R)
60
            return tree[x].mx;
61
        push_down(x);
62
        int mid = (tree[x].l + tree[x].r) >> 1;
63
        LL res = -INF;
64
        if(L \le mid) res = max(res, query2(Ls(x), L, R));
65
        if(R > mid) res = max(res, query2(Rs(x), L, R));
66
67
        return res;
   }
68
```

#### 2.3.2 Splay Tree

```
namespace splay{
2
        int n, m, sz, rt;
        int val[MAXN], id[MAXN];
int tr[MAXN][2], size[MAXN], fa[MAXN], rev[MAXN], s[MAXN], lazy[MAXN];
3
4
5
        void push_up(int x) {
            int l = tr[x][0], r = tr[x][1];
6
7
            s[x] = max(val[x], max(s[l], s[r]));
8
             size[x] = size[l] + size[r] + 1;
9
        void push_down(int x) {
10
             int l = tr[x][0], r = tr[x][1];
11
             if(lazy[x]) {
12
13
                 if(1) {
                     lazy[l] += lazy[x];
14
                     s[l] += lazy[x];
15
                     val[l] += lazy[x];
16
17
                 if(r) {
18
                     lazy[r] += lazy[x];
19
20
                     s[r] += lazy[x];
                     val[r] += lazy[x];
21
22
                 lazy[x] = 0;
23
24
            if(rev[x]) {
25
                 rev[x] = 0;
26
                 rev[l] ^= 1; rev[r] ^= 1;
27
                 swap(tr[x][0], tr[x][1]);
28
29
            }
30
31
        void rotate(int x, int &k) {
32
            int y = fa[x];
```

```
33
            int z = fa[y];
34
            int l, r;
            if(tr[y][0] == x) l = 0;
35
            else l = 1;
36
            r = l \wedge 1;
37
            if(y == k) k = x;
38
            else {
39
                 if(tr[z][0] == y) tr[z][0] = x;
40
41
                 else tr[z][1] = x;
42
            fa[x] = z; fa[y] = x; fa[tr[x][r]] = y;
43
            tr[y][l] = tr[x][r]; tr[x][r] = y;
44
            push_up(y); push_up(x);
45
46
47
        void splay(int x, int &k) {
            int y, z;
48
            while(x != k) {
49
                y = fa[x];
50
                 z = fa[y];
51
52
                 if(y != k) {
                     if((tr[y][0] == x) \land (tr[z][0] == y)) rotate(x, k);
53
54
                     else rotate(y, k);
55
                 rotate(x, k);
56
            }
57
58
59
        int find(int x, int rank) {
            push_down(x);
60
            int l = tr[x][0], r = tr[x][1];
61
62
            if(size[l] + 1 == rank) return x;
            else if(size[l] >= rank) return find(l, rank);
63
            else return find(r, rank - size[l] - 1);
64
65
        void update(int l, int r, int v) {
66
            int x = find(rt, 1), y = find(rt, r + 2);
67
            splay(x, rt); splay(y, tr[x][1]);
68
69
            int z = tr[y][0];
            lazy[z] += v;
70
71
            val[z] += v;
72
            S[z] += V;
73
        void reverse(int 1, int r) {
74
            int x = find(rt, l), y = find(rt, r + 2);
75
76
            splay(x, rt); splay(y, tr[x][1]);
77
            int z = tr[y][0];
            rev[z] ^= 1;
78
79
        void query(int 1, int r) {
80
            int x = find(rt, 1), y = find(rt, r + 2);
81
            splay(x, rt); splay(y, tr[x][1]);
int z = tr[y][0];
82
83
            printf("%d\n", s[z]);
84
85
        void build(int l, int r, int f) {
86
            if(l > r) return;
87
            int now = id[l], last = id[f];
88
            if(l == r) {
89
                 fa[now] = last; size[now] = 1;
90
                 if(1 < f) tr[last][0] = now;
91
                 else tr[last][1] = now;
92
93
                 return;
```

```
94
             int mid = (l + r) \gg 1; now = id[mid];
95
             build(l, mid - 1, mid); build(mid + 1, r, mid);
96
97
             fa[now] = last;
             push_up(now);
98
             if(mid < f) tr[last][0] = now;</pre>
99
100
             else tr[last][1] = now;
101
         void init() {
102
             s[0] = -INF;
103
             scanf("%d%d", &n, &m);
104
             for(int i = 1; i <= n + 2; i++) id[i] = ++sz;
105
106
             build(1, n + 2, 0); rt = (n + 3) >> 1;
107
         }
108
    }
```

# 2.4 Persistent Data Structures

#### 2.4.1 Chairman Tree

```
struct Node {
1
2
       int l, r;
3
        LL sum;
4
   }t[MAXN * 40];
5
   int cnt, n;
6
   int rt[MAXN];
   void update(int pre, int &x, int l, int r, int v) {
7
       x = ++cnt; t[x] = t[pre]; t[x].sum++;
8
        if(l == r) return;
9
        int mid = (l + r) \gg 1;
10
        if(v \le mid) update(t[pre].l, t[x].l, l, mid, v);
11
        else update(t[pre].r, t[x].r, mid + 1, r, v);
12
   }
13
   int query(int x, int y, int l, int r, int v) {
14
        if(l == r) return l;
15
16
        int mid = (l + r) >> 1;
17
        int sum = t[t[y].l].sum - t[t[x].l].sum;
        if(sum >= v) return query(t[x].1, t[y].1, 1, mid, v);
18
19
        else return query(t[x].r, t[y].r, mid + 1, r, v - sum);
20
```

#### 2.4.2 Persistent Trie

```
//区间异或最值查询
1
2
   const int N=5e4+10;
3
   int t[N];
   int ch[N*32][2],val[N*32];
4
5
   int cnt;
6
   void init(){
7
       mem(ch,0)
8
       mem(val,0);
9
       cnt=1;
   }
10
   int add(int root,int x){
11
        int newroot=cnt++,ret=newroot;
12
13
        for(int i=30;i>=0;i--){
14
            ch[newroot][0]=ch[root][0];
15
            ch[newroot][1]=ch[root][1];
```

```
int now=(x>>i)&1;
16
            root=ch[root][now];
17
18
            ch[newroot][now]=cnt++;
19
            newroot=ch[newroot][now];
20
            val[newroot]=val[root]+1;
        }
21
22
        return ret;
   }
int query(int lt,int rt,int x){
23
24
25
        int ans=0;
        for(int i=30;i>=0;i--){
26
            int now=(x>>i)&1;
27
            if(val[ch[rt][now^1]]-val[ch[lt][now^1]]){
28
29
                ans l = (1 << i);
                 rt=ch[rt][now^1];
30
                lt=ch[lt][now^1];
31
32
                } else{
                rt=ch[rt][now];
33
                lt=ch[lt][now];
34
            }
35
36
37
        return ans;
38
```

# 3 String

#### 3.1 Basics

#### 3.1.1 Hash

```
const LL p1 = 201, p2 = 301, mod1 = 12000000319, mod2 = 2147483647;
   struct Hash {
2
3
        LL a, b;
        void append(Hash pre, int v) {
4
5
            a = (pre.a * p1 + v) \% mod1;
            b = (pre.b * p2 + v) \% mod2;
6
7
        void init(string S) {
8
9
            a = b = 0;
            for(int i = 0; i < S.size(); i++) append(*this, S[i]);</pre>
10
11
12
        bool operator == (const Hash &x) const {
13
            return a == x.a \&\& b == x.b;
14
15
        bool operator < (const Hash &x) const {</pre>
16
            return a < x.a | | (a == x.a \&\& b < x.b);
17
        }
18
   };
```

#### 3.1.2 KMP && exKMP

```
namespace KMP {
1
        int fa[MAXN];
2
3
        void get_fail(char* t, int tn) {
4
            fa[0] = -1;
5
            int i = 0, j = -1;
6
            while(i < tn) {</pre>
7
                 if (j == -1 || t[i] == t[j]) {
8
                     ++i; ++j;
9
                     fa[i] = t[i] != t[j] ? j : fa[j];
                 }else{
10
                     j = fa[j];
11
12
                 }
            }
13
14
15
        void kmp(char* s, int sn, char* t, int tn) {
16
            int i = 0, j = 0;
            while(i < sn) {</pre>
17
18
                 if (j == -1 || s[i] == t[j]) {
19
                     i++;j++;
20
                     if(j == tn) {
21
22
                 }else j = fa[j];
23
            }
        }
24
25
   }
26
   namespace exKMP {
27
        int nxt[MAXN], ext[MAXN];
28
        void get_nxt(char* t, int tn) {
29
            int j = 0, mx = 0;
            nxt[0] = tn;
30
            for(int i = 1; i < tn; i++) {</pre>
31
```

```
if(i \ge mx \mid | i + nxt[i - j] \ge mx) {
32
33
                     if(i > mx) mx = i;
34
                     while(mx < tn && t[mx] == t[mx - i]) mx++;
                     nxt[i] = mx - i;
35
                     j = i;
36
                 }else nxt[i] = nxt[i - j];
37
            }
38
39
        void exkmp(char *s, int sn, char *t, int tn) {
40
            int j = 0, mx = 0;
41
            for(int i = 0; i < sn; i++) {</pre>
42
                 if(i >= mx || i + nxt[i - j] >= mx) {
43
                     if(i > mx) mx = i;
44
                     while(mx < sn && mx - i < tn && s[mx] == t[mx - i]) mx++;
45
46
                     ext[i] = mx - i;
47
                     j = i;
                 }else ext[i] = nxt[i - j];
48
49
            }
        }
50
51
   }
```

#### 3.1.3 AC Automaton

```
namespace AC {
1
        int ch[MAXN][sigma_size], last[MAXN];
2
3
        int val[MAXN], f[MAXN], sz;
        inline void init() { sz = 1; memset(ch[0], 0, sizeof(ch[0])); }
4
        inline int idx(char c) { return c - 'a'; }
5
6
        void insert(string s, int v) {
7
            int u = 0;
            for(int i = 0; i < s.size(); i++) {</pre>
8
                 int c = idx(s[i]);
9
10
                 if(!ch[u][c]) {
                     memset(ch[sz], 0, sizeof(ch[sz]));
11
                     val[sz] = 0;
12
                     ch[u][c] = sz++;
13
14
                u = ch[u][c];
15
16
17
            val[u] = v;
18
        void get_fail() {
19
            queue<int> q;
20
            f[0] = 0;
21
            for(int c = 0; c < sigma_size; c++) {</pre>
22
23
                 int u = ch[0][c];
24
                 if(u) { f[u] = 0; q.push(u); last[u] = 0; }
25
            while(!q.empty()) {
26
27
                 int r = q.front(); q.pop();
28
                 for(int c = 0; c < sigma_size; c++) {</pre>
29
                     int u = ch[r][c]
                     if(!u) { ch[r][c] = ch[f[r]][c]; continue; }
30
31
                     q.push(u);
                     int v = f[r];
32
                     while(v && !ch[v][c]) v = f[v];
33
                     f[u] = ch[v][c]
34
35
                     last[u] = val[f[u]] ? f[u] : last[f[u]];
36
                }
37
```

```
38
39
        inline void solve(int j) {
40
            if(j) {
                 ans += val[j];
41
42
                 solve(last[j]);
43
44
        void find(string T) {
45
46
             int j = 0;
             for(int i = 0; i < T.size(); i++) {</pre>
47
                 int c = idx(T[i]);
48
                 j = ch[j][c];
49
                 if(val[j]) solve(j);
50
                 else if(last[j]) solve(last[j]);
51
52
            }
53
        }
   }
54
55
    namespace AC {
56
        int root, tcnt;
        int ch[MAXN][sigma_size], fa[MAXN];
57
58
        inline int newnode() {
            fa[++tcnt] = 0;
59
             for(int i = 0; i < sigma_size; ++i) ch[tcnt][i] = 0;
60
            return tcnt;
61
62
        inline void init() {
63
64
            tcnt = -1;
65
            root = newnode();
66
        inline int idx(char c) { return c - 'a'; }
67
        void extend(char *s, int sn) {
68
69
            int cur = root;
            for(int i = 0, c; i < sn; i++) {</pre>
70
                 if(!ch[cur][c = idx(s[i])])
71
                     ch[cur][c] = newnode();
72
                 cur = ch[cur][c];
73
            }
74
        }
75
76
        int q[MAXN], qh, qt;
77
        void get_fail() {
78
            qh = 1; qt = 0;
79
            fa[root] = 0;
80
             for(int c = 0, now; c < sigma_size; c++)</pre>
                 if((now = ch[root][c]) != 0)
81
                     q[++qt] = now;
82
            while(qh <= qt) {</pre>
83
84
                 int cur = q[qh++];
                 for(int c = 0, now; c < sigma_size; c++)</pre>
85
                     if((now = ch[cur][c]) != 0) {
86
                          fa[now] = ch[fa[cur]][c];
87
88
                          q[++qt] = now;
                     }else
89
                          ch[cur][c] = ch[fa[cur]][c];
90
            }
91
92
    //统计模板串出现次数,每个模板串只计算一次
93
94
            int \ cur = root, \ ans = 0;
             for(int i = 0; i < sn; ++i) {
95
                 cur = ch[cur][idx(s[i])];
96
97
                 for(int \ j = cur; \ j \ \&\& \ cnt[j] \ != -1; \ j = fa[j]) \ \{
98
                     ans \neq = cnt/j/;
```

#### 3.1.4 Minimum String

```
namespace minstring{
          int getmin(char *s, int sn) {
   int i = 0, j = 1, k = 0, t;
   while(i < sn && j < sn && k < sn) {</pre>
2
3
4
                     t = s[(i + k) % sn] - s[(j + k) % sn];
5
6
                     if(!t) k++;
7
                     else {
                           if(t > 0) i += k + 1; else j += k + 1;
8
9
                          if(i == j) j++;
                           k = 0;
10
11
12
               }
13
               return i < j ? i : j;</pre>
14
15
```

#### 3.2 Suffix Related

#### 3.2.1 Suffix Array

```
namespace SA {
2
        char s[MAXN];
3
        int sa[MAXN], rank[MAXN], height[MAXN];
        int t[MAXN], t2[MAXN], c[MAXN], n;
4
       void clear() { n = 0; memset(sa, 0, sizeof(sa)); }
5
6
        void build(int m) {
            int *x = t, *y = t2;
7
            for(int i = 0; i < m; i++) c[i] = 0;
8
9
            for(int i = 0; i < n; i++) c[x[i] = s[i]]++;
10
            for(int i = 1; i < m; i++) c[i] += c[i - 1];
            for(int i = n - 1; i \ge 0; i--) sa[--c[x[i]]] = i;
11
            for(int k = 1; k <= n; k <<= 1) {</pre>
12
                int p = 0;
13
                for(int i = n - k; i < n; i++) y[p++] = i;
14
                for(int i = 0; i < n; i++) if(sa[i] >= k) y[p++] = sa[i] - k;
15
16
                for(int i = 0; i < m; i++) c[i] = 0;
17
                for(int i = 0; i < n; i++) c[x[y[i]]]++;
18
                for(int i = 1; i < m; i++) c[i] += c[i - 1];
                for(int i = n - 1; i \ge 0; i--) sa[--c[x[y[i]]]] = y[i];
19
                swap(x, y);
20
                p = 1; x[sa[0]] = 0;
21
                for(int i = 1; i < n; i++)</pre>
22
                    x[sa[i]] = y[sa[i - 1]] == y[sa[i]] && y[sa[i - 1] + k] == y[sa[i] + k]
23
       ? p - 1 : p++;
                if(p >= n) break;
24
25
                m = p;
26
            }
27
28
        void buildHeight() {
29
            int k = 0;
```

```
for(int i = 0; i < n; i++) rank[sa[i]] = i;</pre>
30
             for(int i = 0; i < n; i++) {</pre>
31
32
                  if(k) k--;
                 int j = sa[rank[i] - 1];
33
                 while(s[i + k] == s[j + k]) k++;
34
                 height[rank[i]] = k;
35
             }
36
37
        void init() {
38
             n = strlen(s) + 1;
39
             build(z' + 1);
40
             buildHeight();
41
        }
42
43
    }
```

#### 3.2.2 Suffix Automaton

```
namespace SAM{
1
2
        int scnt, root, last;
        int fa[MAXN<<1], len[MAXN<<1], ch[MAXN<<1][26];</pre>
3
4
        int sc[MAXN<<1], tmpl[MAXN<<1], minl[MAXN<<1];</pre>
5
6
        int newnode(int _len, int q = 0) {
            fa[++scnt] = fa[q]; len[scnt] = _len;
7
8
            sc[scnt] = 0;tmpl[scnt] = 0; minl[scnt] = INF;
9
            for(int i = 0; i < 26; i++) ch[scnt][i] = ch[q][i];
10
            return scnt;
11
12
        void init() {
13
            scnt = 0;
14
            root = last = newnode(0);
15
        void extend(int c) {
16
            int p = last, np = newnode(len[p] + 1);
17
            for(;p \&\& ch[p][c] == 0; p = fa[p]) ch[p][c] = np;
18
            if(!p) fa[np] = root;
19
20
            else{
                 int q = ch[p][c];
21
                 if(len[p] + 1 == len[q]) fa[np] = q;
22
23
24
                     int nq = newnode(len[p] + 1, q);
25
                     fa[np] = fa[q] = nq;
                     for(; p && ch[p][c] == q; p = fa[p]) ch[p][c] = nq;
26
                 }
27
28
29
            last = np;
30
        int c[MAXN], rs[MAXN << 1];</pre>
31
32
        void radix_sort(int n){
33
            for(int i = 0; i <= n; i++) c[i] = 0;
            for(int i = 1; i <= scnt; i++) c[len[i]]++;</pre>
34
            for(int i = 1; i <= n; i++) c[i] += c[i-1];</pre>
35
            for(int i = scnt; i >= 1; i--) rs[c[len[i]]--] = i;
36
37
        void go(){
38
            scanf("%s",s);
39
            int n = strlen(s);
40
41
            for(int i = 0; i < n; ++i)</pre>
42
                 extend(s[i] - 'a');
43
            radix_sort(n);
```

```
//以下sc集合意义不同
44
            {//每个节点对应的位置之后有多少个不同子串
45
46
                for(int i = scnt; i >= 1; i--) {
                    int S = 0;
47
                    for(int j = 0; j < 26; j++)
48
                        S += sc[ch[rs[i]][j]];
49
                    sc[rs[i]] = S + 1;
50
                }
51
52
            {//right集合大小
53
                int cur = root;
54
                for(int i = 0; i < n; ++i) {</pre>
55
                    cur = ch[cur][s[i] - 'a'];
56
57
                    sc[cur]++;
58
                for(int i = scnt; i >= 1; --i) {
59
                    sc[ fa[rs[i]] ] += sc[rs[i]];
60
61
62
63
            //公共子串
64
            //tmpl,当前字符串:在状态cur,与模板串的最长公共后缀
            //minl, 多个字符串:在状态cur,与模板串的最长公共后缀
65
            //注意:在状态cur匹配成功时,cur的祖先状态与字符串的最长公共后缀
66
            for(; ~scanf("%s",s);) {
67
                int cur = root, Blen = 0;
68
69
                for(int i = 0; i <= scnt; i++)</pre>
70
                    tmpl[i] = 0;
                n = strlen(s);
71
72
                for(int i = 0, x; i < n; i++) {
                    x = s[i] - a';
73
                    if(ch[cur][x]) {
74
75
                        ++Blen;
                        cur = ch[cur][x];
76
                    }else{
77
                        for(; cur \&\& ch[cur][x] == 0; cur = fa[cur]);
78
79
                        if(cur) {
                            Blen = len[cur] + 1;
80
                            cur = ch[cur][x];
81
82
                        }else{
83
                            cur = root; Blen = 0;
84
85
                    tmpl[cur] = max(tmpl[cur], Blen);
86
87
                for(int i = scnt; i ; --i) {
88
                    if( tmpl[ fa[rs[i]] ] < tmpl[ rs[i] ])</pre>
89
90
                        tmpl[ fa[rs[i]] ] = len[ fa[rs[i]] ];
                    minl[ rs[i] ] = min(minl[ rs[i] ], tmpl[ rs[i] ]);
91
92
                }
93
            }
94
95
    namespace exSAM{
96
97
        int scnt, root;
        int fa[MAXN<<1], len[MAXN<<1], ch[MAXN<<1][26];</pre>
98
        int sc[MAXN<<1], tmpl[MAXN<<1];</pre>
99
100
        int newnode(int _len, int q = 0) {
101
            fa[++scnt] = fa[q]; len[scnt] = _len;
102
            sc[scnt] = 0;tmpl[scnt] = 0; minl[scnt] = INF;
103
104
            for(int i = 0; i < 26; i++) ch[scnt][i] = ch[q][i];
```

```
105
            return scnt;
106
         void init() {
107
108
             scnt = 0;
             root = newnode(0);
109
110
         int work(int p,int c){
111
112
             int q = ch[p][c];
             int nq = newnode(len[p] + 1, q);
113
             fa[q] = nq;
114
             for(; p \& ch[p][c] == q; p = fa[p]) ch[p][c] = nq;
115
             return nq;
116
117
         int extend(int p, int c) {
118
119
             if (ch[p][c]){
120
                  int q = ch[p][c];
                  if (len[p] + 1 == len[q]) return q;
121
122
                  return work(p, c);
123
             }
             int np = newnode(len[p] + 1);
124
             for(;p \&\& ch[p][c] == 0; p = fa[p]) ch[p][c] = np;
125
             if (!p) fa[np] = root;
126
             else{
127
                  int q = ch[p][c];
128
129
                  if (len[p] + 1 == len[q]) fa[np] = q;
130
                  else fa[np] = work(p, c);
             }
131
132
             return np;
133
         void solve() {
134
             int n; scanf("%d",&n);
135
             for(int i = 1; i <= n; i++) {
    scanf("%s", s);</pre>
136
137
                  int sn = strlen(s);
138
                  int last = root;
139
                  for(int j = 0; j < sn; ++j)
140
                      last = extend(last, s[j] - 'a');
141
142
             }
143
         }
144
```

#### 3.3 Palindrome Related

#### 3.3.1 Manacher

```
namespace Manachar {
 1
 2
            char S[MAXN << 1];</pre>
3
            int scnt, ans;
           int p[MAXN << 1]; //p[i] - 1
void init(char *s0, int sn0) {
    S[0] = '$'; S[1] = '#';
    for(int i = 0; i < sn0; i++) {</pre>
 4
 5
 6
 7
                         S[2 * i + 2] = s0[i];
 8
                        S[2 * i + 3] = '\#';
9
10
                  scnt = sn0 * 2 + 2;
11
                  S[scnt] = \frac{1}{2};
12
13
           void manachar() {
14
```

STRING 36

```
int id = 0, mx = 0;
15
16
            for(int i = 1; i < scnt; i++) {</pre>
                 p[i] = mx > i ? min(p[2 * id - i], mx - i) : 1;
17
18
                 while(S[i + p[i]] == S[i - p[i]]) p[i]++;
19
                 if(i + p[i] > mx) {
20
                     mx = i + p[i];
21
                     id = i;
                 }
22
            }
23
        }
24
   }
25
```

## 3.3.2 Palindromic Automaton

```
namespace PAM {
1
       int scnt, S[MAXN];
2
3
       int pcnt, last, len[MAXN], fail[MAXN], ch[MAXN][26];
       int cnt[MAXN]; //节点i表示的本质不同的串的个数(调用count())
4
5
       int\ num[MAXN];\ //以节点i表示的最长回文串的最右端点为回文串结尾的回文串个数
6
       int newnode(int _len) {
7
           len[pcnt] = _len;
8
           cnt[pcnt] = num[pcnt] = 0;
           for(int i = 0; i < 26; i++) ch[pcnt][i] = 0;
9
10
           return pcnt++;
11
       inline void init() {
12
           S[scnt = 0] = -1;
13
           pcnt = 0;newnode(0);newnode(-1);
14
           fail[0] = 1; last = 0;
15
16
       int getfail(int x) {
17
           while(S[scnt - len[x] - 1] != S[scnt]) x = fail[x];
18
19
           return x;
20
21
       void extend(int c) {
22
           S[++scnt] = c;
23
           int cur = getfail(last);
           if(!ch[cur][c]) {
24
               int now = newnode(len[cur] + 2);
25
               fail[now] = ch[getfail(fail[cur])][c];
26
27
               ch[cur][c] = now;
28
               num[now] = num[fail[now]] + 1;
29
           last = ch[cur][c];
30
           cnt[last]++;
31
32
33
       void count() {
           for(int i = pcnt - 1; i >= 0; i--) cnt[fail[i]] += cnt[i];
34
35
       }
36
   };
```

# 4 Math

# 4.1 Algebra

## 4.1.1 FFT

```
const double pi = acos(-1.0);
   const int MAXN = 300003;
   struct comp {
4
        double x, y;
        comp operator + (const comp a) const { return (comp) \{x + a.x, y + a.y\}; }
5
6
        comp operator - (const comp a) const { return (comp) {x - a.x, y - a.y}; }
        comp operator * (const comp a) const { return (comp) \{x * a.x - y * a.y, x * a.y + y\}
7
        * a.x}; }
8
   };
   int rev[MAXN], T;
9
   comp tmp;
10
   void fft(comp *a, int r) {
11
12
        if(r == -1) for(int i = 0; i < T; i++) a[i] = a[i] * a[i];
        for(int i = 0; i < T; i++) if(rev[i] > i) swap(a[rev[i]], a[i]);
13
14
        for(int i = 2, mid = 1; i \le T; mid = i, i \le 1) {
            comp step = (comp) \{\cos(pi / mid), r * \sin(pi / mid)\};
15
            for(int j = 0; j < T; j += i) {
16
                 comp cur = (comp) \{1, 0\};
17
                 for(int k = j; k < j + mid; k++, cur = cur * step) {
    tmp = a[k + mid] * cur;</pre>
18
19
                     a[k + mid] = a[k] - tmp;
20
                     a[k] = a[k] + tmp;
21
                 }
22
            }
23
24
25
        if(r == -1) for(int i = 0; i < T; i++) a[i].y = (int)(a[i].y / T / 2 + 0.5);
26
   }
27
   int n, m;
   comp A[MAXN];
28
29
   void init() {
        for(T = 1; T \le n + m; T \le 1);
30
31
        for(int i = 1; i < T; i++) {</pre>
32
            if(i & 1) rev[i] = (rev[i >> 1] >> 1) ^ (T >> 1);
33
            else rev[i] = rev[i >> 1] >> 1;
34
        }
35
   }
```

## 4.1.2 NTT

```
const int MAXN = 300005, G = 3, mod = 998244353; //or (479LL << 21) + 1
   int rev[MAXN], T;
   LL qpow(LL x, LL y) {
3
       LL res = 1;
4
       while(y) {
5
           if(y \& 1) res = res * x % mod;
6
7
           x = x * x % mod;
8
           y >>= 1;
9
       }
10
       return res;
11
   }
   void ntt(LL *a, int r) {
   if(r == -1) for(int i = 0; i < T; i++) A[i] = A[i] * B[i] % mod;
```

```
for(int i = 0; i < T; i++) if(rev[i] > i) swap(a[rev[i]], a[i]);
14
        for(int i = 2, mid = 1; i <= T; mid = i, i <<= 1) {
15
             LL gn = qpow(G, (mod - 1) / i);
16
17
             if(r == -1) gn = qpow(gn, mod - 2);
             for(int j = 0; j < T; j += i) {
18
                 LL cur = 1, tmp;
19
                 for(int k = j; k < j + mid; k++, cur = cur * gn % mod) {
    tmp = a[k + mid] * cur % mod;</pre>
20
21
                      a[k + mid] = ((a[k] - tmp) \% mod + mod) \% mod;
22
                      a[k] = (a[k] + tmp) \% mod;
23
                 }
24
            }
25
26
        if(r == -1) {
27
             LL inv = qpow(T, mod - 2);
28
             for(int i = 0; i < T; i++) a[i] = a[i] * inv % mod;
29
30
        }
   }
31
   int n, m;
32
  LL A[MAXN], B[MAXN];
33
   void init() {
34
        for(T = 1; T \le n + m; T \le 1);
35
        for(int i = 0; i < T; i++) {</pre>
36
            if(i & 1) rev[i] = (rev[i >> 1] >> 1) ^ (T >> 1);
37
38
            else rev[i] = rev[i >> 1] >> 1;
39
        }
40
   }
```

## 4.1.3 FWT

```
void FWT(LL *a,int n) {
        for(int i = 2;i <= n; i <<= 1) {
2
             for(int j = 0; j < n; j += i) {
   for(int d = 0, w = i >> 1; d < w; d++){</pre>
3
4
                     LL u = a[j + d], v = a[j + d + w];
5
6
                      //xor: a[j + d] = u + v, a[j + d + w] = u - v;
                      //and: a[j + d] = u + v;
7
8
                      //or : a[j + d + w] = u + v;
9
                 }
            }
10
        }
11
12
    void UFWT(LL *a, int n) {
13
        for(int i = 2; i <= n; i <<= 1) {</pre>
14
             for(int j = 0; j < n; j += i) {
15
                 for(int d = 0, w = i >> 1; d < w; d++) {
16
                     LL u = a[j + d], v = a[j + d + w];
17
                      //xor: a[j + d] = (u + v) / 2, a[j + d + w] = (u - v) / 2;
18
19
                      //and: a[j + d] = u - v;
                      //or : a[j + d + w] = v - u;
20
21
                 }
22
            }
        }
23
24
    void solve(int n) {
25
        FWT(a, n); FWT(b, n);
26
        for(int i = 0; i < n; i++) a[i] = a[i] * b[i];
27
        UFWT(a, n);
28
29
   }
```

# 4.1.4 Linear Basis

```
//dynamic
1
   const int D = 60;
3
   struct Basis {
4
        vector<int> ind;
5
        vector<LL> base;
6
        Basis() {
            ind.resize(D, -1);
7
8
            base.resize(D);
9
10
        bool update(LL x, int id) {
            for(int i = 0; i < D; i++) if(~ind[i] && x >> i & 1) {
11
12
                x \sim base[i];
13
            if(!x) return 1;
14
            int pos = __builtin_ctzll(x);
15
            ind[pos] = id;
16
17
            base[pos] = x;
            return 0;
18
19
        }
20
   };
   //array
21
22
   int Gauss(int n, int m) {
        int num = 1;
23
        for(int x = 1; x <= n && x <= m; x++) {
24
25
            int t = 0;
            for(int j = x; j \le m; j++) if(g[j][x]) { t = j; break; }
26
27
            if(t) {
                swap(g[x], g[t]);
28
29
                for(int i = x + 1; i \le n; i++) {
                     if(g[i][x]) {
30
                         for(int k = 1; k \le m; k++) g[i][k] ^= g[x][k];
31
32
33
                }
34
                num++;
35
            }
36
        return --num;
37
   }
38
39
    //long long
   int Gauss() {
40
        int num = 1;
41
42
        for(int k = 61; k >= 0; k--) {
43
            int t = 0;
44
            for(int j = num; j \le cnt; j++) if((A[j] >> k) & 1) { t = j; break; }
45
            if(t) {
46
                swap(A[t], A[num]);
                for(int j = num + 1; j \le cnt; j++) if((A[j] >> k) & 1) A[j] ^- A[num];
47
48
                num++;
49
            }
        }
50
51
        return --num;
52
   }
```

# 4.2 Math Theory

#### **4.2.1** Inverse

```
1
   //O(logn)求n的逆元
   const int mod = 1e6 + 3;
2
   int exgcd(int a, int b, int &x, int &y) {
3
        int d = a;
4
        if(b != 0) {
5
6
            d = exgcd(b, a \% b, y, x);
7
            y -= (a / b) * x;
8
9
        else {
            x = 1; y = 0;
10
11
12
        return d;
13
   int inverse(int a) {
14
15
        int x, y;
        exgcd(a, mod, x, y);
16
        return (x % mod + mod) % mod;
17
18
19
   int inverse(int a) { return qpow(a, mod - 2); }
20
   //O(n) 求1~n的 逆元
   int inv[MAXN];
21
   void init() {
22
23
        inv[0] = inv[1] = 1;
        for(int i = 2; i < MAXN; i++) inv[i] = (long long)(mod - mod / i) * inv[mod % i] %</pre>
24
       mod;
25
   }
```

## 4.2.2 Lucas

```
//mod很小可以预处理逆元的情况
2
   void init() {
3
        fac[0] = 1;
        for(int i = 1; i < mod; i++) fac[i] = (long long)fac[i - 1] * i % mod;
4
        inv[0] = inv[1] = 1;
5
        for(int i = 2; i < mod; i++) inv[i] = (long long)(mod - mod / i) * <math>inv[mod \% i] \%
6
       mod;
        for(int i = 1; i < mod; i++) inv[i] = (long long)inv[i] * <math>inv[i - 1] % mod;
7
   }
8
9
   int C(int a, int b) {
10
        if(b > a) return 0;
        if(a < mod) return (long long)fac[a] * inv[b] % mod * inv[a - b] % mod;</pre>
11
        return (long long)C(a / mod, b / mod) * C(a % mod, b % mod) % mod;
12
13
    //mod过大不能预处理逆元的情况
14
   LL qpow(LL x, LL y) {
15
16
        LL res = 1;
17
       while(y) {
18
           if(y \& 1) res = res * x % mod;
            x = x * x % mod;
19
20
            y >>= 1;
       }
21
22
        return res;
23
   LL C(LL a, LL b) {
24
25
        if(b > a) return 0;
        if(b > a - b) b = a - b;
26
27
        LL s1 = 1, s2 = 1;
28
        for(LL i = 0; i < b; i++) {</pre>
            s1 = s1 * (a - i) % mod;
29
            s2 = s2 * (i + 1) % mod;
30
```

```
31     }
32     return s1 * qpow(s2, mod - 2) % mod;
33     }
34     LL lucas(LL a, LL b) {
        if(a < mod) return C(a, b);
        return lucas(a / mod, b / mod) * C(a % mod, b % mod);
37     }</pre>
```

# 4.2.3 CRT && exCRT

 $x \equiv a_i \pmod{m_i}$ 

```
namespace CRT {
1
2
        LL m[MAXN], a[MAXN];
3
        LL exgcd(LL _a, LL _b, LL &x, LL &y) {
             if(!_b) {
4
5
                 x = 1; y = 0;
6
                 return _a;
7
             LL d = exgcd(_b, _a % _b, y, x);
y -= (_a / _b) * x;
8
9
10
             return d;
11
        LL crt(int n) {
12
             LL M = 1, tmp, res = 0, x, y;
13
             for(int i = 1; i <= n; i++) M *= m[i];</pre>
14
             for(int i = 1; i <= n; i++) {
15
                 tmp = M / m[i];
16
                 exgcd(tmp, m[i], x, y);
17
                 x = (x + m[i]) % m[i];
18
                  res = (a[i] * x % M * tmp % M + res) % M;
19
20
             }
21
             return res;
22
        }
23
   }
24
    namespace EXCRT {
        LL m[MAXN], a[MAXN];
25
        LL exgcd(LL _a, LL _b, LL &x, LL &y) {
26
27
             if(!_b) {
28
                 x = 1; y = 0;
                 return _a;
29
30
             LL d = exgcd(_b, _a % _b, y, x);
y -= (_a / _b) * x;
31
32
             return d;
33
34
        LL excrt(int n) {
35
             LL M = m[1], A = a[1], x, y, d, tmp;
for(int i = 2; i <= n; i++) {
36
37
                  d = exgcd(M, m[i], x, y);
38
                 if((A - a[i]) % d) return -1; //No solution
39
                 tmp = M / d; M *= m[i] / d;
40
                 y = (A - a[i]) / d % M * y % M;
41
                 y = (y + tmp) \% tmp;
42
                 A = (m[i] \% M * y \% M + a[i]) \% M;
43
                 A = (A + M) \% M;
44
             }
45
             return A;
46
```

#### 4.2.4 BSGS

```
const int MOD = 76543;
1
   int hs[MOD + 5], head[MOD + 5], nxt[MOD + 5], id[MOD + 5], ecnt;
2
3
   void insert(int x, int y) {
4
        int k = x \% MOD;
5
        hs[ecnt] = x, id[ecnt] = y, nxt[ecnt] = head[k], head[k] = ecnt++;
6
   int find(int x) {
7
        int k = x \% MOD;
8
        for(int i = head[k]; i; i = nxt[i])
9
            if(hs[i] == x)
10
                return id[i];
11
        return -1;
12
   }
13
   int BSGS(int a, int b, int c){
14
        memset(head, 0, sizeof head); ecnt = 1;
15
16
        if(b == 1) return 0;
17
        int m = sqrt(c * 1.0), j;
18
        LL x = 1, p = 1;
        for(int i = 0; i < m; i++, p = p * a % c)
19
            insert(p * b % c, i);
20
        for(LL i = m; ; i += m){
21
            if((j = find(x = x * p % c)) != -1) return i - j;
22
23
            if(i > c) break;
24
        }
25
        return -1;
26
```

### 4.2.5 Miller-Rabin && PollardRho

```
LL ksc(LL a,LL n,LL mod){
1
        LL ret=0;
2
        for(;n;n>>=1){
3
             if(n&1){ret+=a;if(ret>=mod)ret-=mod;}
4
            a <<=1; if(a >= mod)a -= mod;
5
6
        }
7
        return ret;
   }
8
9
   LL ksm(LL a,LL n,LL mod){
10
        LL ret = 1;
11
        for(;n;n>>=1){
12
             if(n&1)ret=ksc(ret,a,mod);
13
            a=ksc(a,a,mod);
14
        }
        return ret;
15
16
    int millerRabin(LL n){
17
        if(n<2 || (n!=2 && !(n&1)))return 0;
18
19
        LL d=n-1; for(;!(d&1);d>>=1);
20
        for(int i=0;i<20;++i){
21
             LL a=rand()\%(n-1)+1;
             LL t=d, m=ksm(a,d,n);
22
            for(;t!=n-1 && m!=1 && m!=n-1;m=ksc(m,m,n),t<<=1);</pre>
23
             if(m!=n-1 && !(t&1)) return 0;
24
```

```
25
        }
26
        return 1;
27
   LL cnt,fact[100];
28
   LL gcd(LL a,LL b){return !b?a:gcd(b,a%b);}
29
   LL pollardRho(LL n, int a){
30
31
        LL x=rand()%n, y=x, d=1, k=0, i=1;
32
        while(d==1){
33
            ++k;
            x=ksc(x,x,n)+a;if(x>=n)x-=n;
34
            d=gcd(x>y?x-y:y-x,n);
35
            if(k==i){y=x;i<<=1;}
36
37
        if(d==n)return pollardRho(n,a+1);
38
39
        return d;
40
   }
    void findfac(LL n){
41
42
        if(millerRabin(n)){fact[++cnt]=n;return;}
43
        LL p=pollardRho(n,rand()%(n-1)+1);
44
        findfac(p);
        findfac(n/p);
45
   }
46
```

# **4.2.6** $\varphi(n)$

```
int phi(int x) {
1
2
        int res = x;
3
        for(int i = 2; i * i <= x; i++) {</pre>
            if(x \% i == 0) {
4
                 res = res / i * (i - 1);
5
6
                 while(x % i == 0) x /= i;
            }
7
8
        if(x > 1) res = res / x * (x - 1);
9
10
        return res;
11
   }
```

#### 4.2.7 Euler Sieve

```
int prime[MAXN], cnt, phi[MAXN], mu[MAXN];
1
   bool isp[MAXN];
2
3
                        //最小质因子最高次幂
   int min_pow[MAXN];
4
5
   int min_sum[MAXN];
                        //1+p+p^2+...+p^k
6
   int div_sum[MAXN];
                        //约数和
7
   int min_index[MAXN]; //最小质因子的指数
8
   int div_num[MAXN];
9
                        //约数个数
   void Euler(int n) {
10
       mu[1] = phi[1] = div_num[1] = div_sum[1] = 1;
11
12
       for(int i = 2; i <= n; i++) {
13
           if(!isp[i]) {
               prime[++cnt] = min_pow[i] = i;
14
               phi[i] = i - 1;
15
16
               mu[i] = -1;
               min_index[i] = 1; div_num[i] = 2;
17
               div_sum[i] = min_sum[i] = i + 1;
18
19
```

```
for(int j = 1; j <= cnt && i * prime[j] <= n; j++) {</pre>
20
                isp[i * prime[j]] = 1;
21
22
                if(i % prime[j] == 0) {
                    phi[i * prime[j]] = phi[i] * prime[j];
23
                    mu[i * prime[j]] = 0;
24
25
                    min_index[i * prime[j]] = min_index[i] + 1;
26
                    div_num[i * prime[j]] = div_num[i] / (min_index[i] + 1) * (min_index[i *
27
        prime[j]] + 1);
28
                    min_sum[i * prime[j]] = min_sum[i] + min_pow[i] * prime[j];
29
                    div_sum[i * prime[j]] = div_sum[i] / min_sum[i] * min_sum[i * prime[j]];
30
                    min_pow[i * prime[j]] = min_pow[i] * prime[j];
31
32
                    break:
33
                phi[i * prime[j]] = phi[i] * (prime[j] - 1);
34
                mu[i * prime[j]] = -mu[i];
35
36
                div_num[i * prime[j]] = div_num[i] << 1;</pre>
37
                min_index[i * prime[j]] = 1;
38
39
                div_sum[i * prime[j]] = div_sum[i] * (prime[j] + 1);
40
                min_pow[i * prime[j]] = prime[j];
41
                min_sum[i * prime[j]] = prime[j] + 1;
42
43
            }
44
        }
45
   }
```

## 4.2.8 DuJiao Sieve

$$\sum_{i=1}^{n} \phi(i)$$

```
vector<int> prime;
   int phi[MAXN], P[MAXN];
   bool isp[MAXN];
   unordered_map<LL, int> mp;
5
   void Euler(int n) {
6
        phi[1] = 1;
        for(int i = 2; i <= n; i++) {</pre>
7
8
            if(!isp[i]) {
                prime.push_back(i);
9
                 phi[i] = i - 1;
10
11
            for(auto x : prime) {
12
                 if(i * x > n) break;
13
                 isp[i * x] = 1;
14
                 if(i \% x == 0) {
15
                     phi[i * x] = phi[i] * x;
16
17
                     break;
18
                phi[i * x] = phi[i] * (x - 1);
19
            }
20
21
        for(int i = 1; i \le n; i++) P[i] = (P[i - 1] + phi[i]) % mod;
22
23
   LL cal(LL n) {
24
        if(n < MAXN) return P[n];</pre>
```

```
if(mp.count(n)) return mp[n];
26
        LL res = 0;
27
        for(LL i = 2, last; i <= n; i = last + 1) {</pre>
28
            last = n / (n / i);
29
            res += (last - i + 1) \% mod * cal(n / i) \% mod;
30
31
            res %= mod;
32
        mp[n] = ((_int128)n * (n + 1) / 2 % mod + mod - res) % mod;
33
34
        return mp[n];
35
```

$$\sum_{i=1}^{n} \mu(i)$$

```
LL cal(LL n) {
1
2
        if(n < MAXN) return M[n];</pre>
3
        if(mp.count(n)) return mp[n];
        LL res = 0;
4
5
        for(LL i = 2, last; i \le n; i = last + 1) {
6
            last = n / (n / i);
            res += (last - i + 1) * cal(n / i);
7
8
9
        mp[n] = 1 - res;
10
        return 1 - res;
11
```

## 4.2.9 Möbius Inversion

$$\sum_{i}^{n} \sum_{j}^{m} lcm(i, j) (mod \ p)$$

```
int mu[MAXN], prime[MAXN], sum[MAXN], cnt;
   bool isp[MAXN];
2
3
    void getmu(int n) {
        mu[1] = 1;
4
5
        for(int i = 2; i <= n; i++) {
6
            if(!isp[i]) {
7
                mu[i] = -1;
8
                prime[++cnt] = i;
9
10
            for(int j = 1; j <= cnt && i * prime[j] <= n; j++) {</pre>
                isp[i * prime[j]] = 1;
11
                if(i % prime[j] == 0) {
12
13
                    mu[i * prime[j]] = 0;
14
                    break;
15
                mu[i * prime[j]] = -mu[i];
16
            }
17
        }
18
19
   ll n, m, ans;
20
   ll query(ll x, ll y) { return (x * (x + 1) / 2 % mod) * (y * (y + 1) / 2 % mod) % mod; }
21
   ll F(ll x, ll y) {
22
        ll res = 0, last;
23
        for(ll i = 1; i \le min(x, y); i = last + 1) {
24
25
            last = min(x / (x / i), y / (y / i));
26
            res = (res + (sum[last] - sum[i - 1]) * query(x / i, y / i) % mod) % mod;
27
        }
```

```
return res;
28
29
    }
30
   int main() {
31
         cin>>n>>m;
32
         getmu(min(n, m));
         for(ll\ i = 1;\ i \leftarrow min(n,\ m);\ i++)\ sum[i] = (sum[i - 1] + (i * i * mu[i]) % mod) %
33
        mod;
ll last;
34
         for(ll d = 1; d <= min(n, m); d = last + 1) {</pre>
35
             last = min(n / (n / d), m / (m / d));
ans = (ans + (last - d + 1) * (d + last) / 2 % mod * F(n / d, m / d) % mod) %
36
37
        mod;
         }
38
39
         ans = (ans + mod) \% mod;
         cout<<ans<<endl;</pre>
40
41
         return 0;
42
```

# 5 Geometry

# 5.1 Commonly Definition and Functions

## 5.1.1 Const and Functions

```
namespace CG{
1
        #define Point Vector
2
3
        const double pi=acos(-1.0);
        const double inf=1e100;
4
5
        const double eps=1e-9;
        template <typename T> inline T Abs(T x){return x>0?x:-x;}
6
        template <typename T> inline bool operator == (T x, T y){return Abs(x-y)<eps;}
7
8
        int sqn(double x){
9
            if (Abs(x)<eps) return 0;</pre>
            if (x>0) return 1;
10
            else return -1;
11
12
        }
13
   }
```

## 5.1.2 Point Definition

```
1
   namespace CG{
2
       struct Point{
3
            double x,y;
4
           Point(double x=0, double y=0):x(x),y(y){}
5
6
       Vector operator + (const Vector a,const Vector b){return Vector(a.x+b.x,a.y+b.y);}
       Vector operator - (const Vector a,const Vector b){return Vector(a.x-b.x,a.y-b.y);}
7
       Vector operator * (const Vector a,const double k){return Vector(a.x*k,a.y*k);}
8
       Vector operator / (const Vector a,const double k){return Vector(a.x/k,a.y/k);}
9
10
       bool operator < (const Vector a,const Vector b) {return a.x==b.x?a.y<b.y:a.x<b.x;}</pre>
11
       bool operator == (const Vector a,const Vector b) {return a.x==b.x && a.y==b.y;}
12
       double Dot(const Vector a,const Vector b){return a.x*b.x+a.y*b.y;}
       double Cross(const Vector a,const Vector b){return a.x*b.y-a.y*b.x;}
13
       double mult_Cross(const Vector a,const Vector b,const Vector c){return (a.x-c.x)*(b.
14
       y-c.y)-(b.x-c.x)*(a.y-c.y);}
       double mult_Dot(const Vector a,const Vector b,const Vector c){return (a.x-c.x)*(b.x-
15
       c.x)+(a.y-c.y)*(b.y-c.y);}
       double Norm(const Vector a){return sqrt(Dot(a,a));}
16
       double Angle(const Vector a,const Vector b){return acos(Dot(a,b)/Norm(a)/Norm(b));}
17
18
       Vector Rotate(const Vector a, const double theta){return Vector(a.x*cos(theta)-a.y*
       sin(theta),a.x*sin(theta)+a.y*cos(theta));}
       bool ToLeftTest(const Vector a,const Vector b){return Cross(a,b)<0;}</pre>
19
       double DisPP(const Vector a,const Vector b){return sqrt((a.x-b.x)*(a.x-b.x)+(a.y-b.y
20
       )*(a.y-b.y));}
21
   }
```

## 5.1.3 Line Definition

```
namespace CG{
struct Line{
    point p0,v,p1;
    double t,theta;
    Line(Point _p0=0,Point _v=0,double _t=1):p0(_p0),v(_v),t(_t){p1=p0+v*t; theta=
    atan2(v.y,v.x);}
```

```
6
                              // Line(Point \_p0=0, Point \_v=0, double \_t=1): p0(\_p0), p1(\_v)\{v=(p1-p0)/t; theta=0, double \_t=1): p0(\_v)\{v=(p1-p0)/t; theta=0, double \_t=1): p0(\_v)\{v=(p1-p0)/t; theta=0, d
                   atan2(v.y,v.x);
  7
                   };
 8
                   bool operator < (const Line n,const Line m) {return n.theta<m.theta;}</pre>
                   Point GetIntersection(const Line n,const Line m){return n.p0+n.v*Cross(m.v,(n.p0-m.
 9
                   p0))/Cross(n.v,m.v);}
                   bool OnLine(const Vector a, const Line 1){return Cross(1.p0-a,1.p1-a)==0;}
10
                   bool OnSegment(const Point a,const Line 1){return sgn(Cross(l.p0-a,l.p1-a))==0 &&
11
                   sgn(Dot(l.p0-a,l.p1-a))<0;}
                   double DisPL(const Point a,const Line 1){return Abs(Cross(1.p1-1.p0,a-1.p0)/Norm(1.
12
                   p1-l.p0));}
                   double DisPS(const Point a,const Line 1){
13
                              if (l.p0==l.p1) return Norm(a-l.p0);
14
                              Vector v1=l.p1-l.p0,v2=a-l.p0,v3=a-l.p1;
15
                              if (sgn(Dot(v1,v2))<0) return Norm(v2);</pre>
16
                              if (sgn(Dot(v1,v3))>0) return Norm(v3);
17
                              return DisPL(a,1);
18
19
20
                    Point GetProjection(const Point a, const Line 1){
21
                              Vector v=l.p1-l.p0;
                              return 1.p0+v*(Dot(v,a-1.p0)/Dot(v,v));
22
23
                    bool SegmentIntersection(const Line n,const Line m,bool p){
24
                              double c1=Cross(n.p1-n.p0,m.p1-m.p0);
25
                              double c2=Cross(n.p1-n.p0,m.p1-n.p0);
26
27
                              double c3=Cross(m.p1-m.p0,n.p0-m.p0);
28
                              double c4=Cross(m.p1-m.p0,n.p1-m.p0);
                              if (p){
29
                                         if (!sgn(c1) || !sgn(c2) || !sgn(c3) || !sgn(c4)){
30
                                                    return OnSegment(n.p0,m) | OnSegment(n.p1,m) | OnSegment(m.p0,n) |
31
                   OnSegment(m.p0,m);
32
                                        }
33
                              }
34
35
                              return (sgn(c1)*sgn(c2)<0 && sgn(c3)*sgn(c4)<0);</pre>
36
                   }
37
        }
```

## 5.1.4 Get Area

```
namespace CG{
    double GetArea(Point *p,int n){
        double area=Cross(p[n],p[1]);
        for (int i=2;i<=n;i++) area+=0.5*Cross(p[i-1],p[i]);
        return Abs(area);
    }
}</pre>
```

# 5.1.5 Get Circumference

## 5.1.6 Anticlockwise Sort

```
1
   namespace CG{
2
        void clockwise_sort(Point *p,int n){
3
             for(int i=0;i<n-2;i++){</pre>
4
                 double tmp = mult_Cross(p[i+1],p[i+2],p[i]);
5
                 if(tmp>0) return;
6
                 else if(tmp<0){</pre>
7
8
                      reverse(p,p+n);
9
                      return;
10
                 }
11
            }
12
        }
13
   }
```

# 5.2 Convex Hull

## 5.2.1 Get Convex Hull

```
namespace CG{
1
2
        Point p[MAXN],s[MAXN];
        int ConvexHull(Point *p,int n,Point *s){
3
4
            sort(p,p+n,cmp); //x从小到大,y从小到大;
5
            int m=0;
            for (int i=0;i<n;i++){</pre>
6
                 for (;m>=2 && Cross(s[m-1]-s[m-2],p[i]-s[m-1])<=0;m--);</pre>
7
8
                s[++m]=p[i];
            }
9
            int k=m;
10
            for (int i=n-2;i;i--){
11
                 for (;m>=k+1 && Cross(s[m-1]-s[m-2],p[i]-s[m-1])<=0;m--);</pre>
12
                s[++m]=p[i];
13
14
15
            return m-1;
16
        }
17
   }
```

# 5.2.2 Point in Convex Hull

```
namespace CG{
1
2
        bool PointInConvexHull(Point A){
            int l=1,r=tot-2,mid;
3
            while(l<=r){</pre>
4
5
                 mid=(l+r)>>1;
                 double a1=Cross(p[mid]-p[0],A-p[0]);
6
7
                 double a2=Cross(p[mid+1]-p[0],A-p[0]);
                 if(a1>=0 \&\& a2<=0){
8
                     if(Cross(p[mid+1]-p[mid],A-p[mid])>=0) return true;
9
10
                     return false;
11
                 else if(a1<0) r=mid-1;</pre>
12
13
                 else l=mid+1;
14
            return false;
15
16
        }
17
   }
```

## 5.3 Minkowski Sum

```
1
    namespace CG{
2
        void Minkowski(Point *C1,int n,Point *C2,int m){
            for(int i=1;i<=n;i++) s1[i]=C1[i]-C1[i-1];</pre>
3
            for(int i=1;i<=m;i++) s2[i]=C2[i]-C2[i-1];</pre>
4
5
            A[tot=1]=C1[1]+C2[1];
6
            int p1=1,p2=1;
            while (p1<=n && p2<=m) ++tot,A[tot]=A[tot-1]+(s1[p1]*s2[p2]>=0?s1[p1++]:s2[p2
7
        ++]);
8
            while (p1<=n) ++tot,A[tot]=A[tot-1]+s1[p1++];</pre>
9
            while (p2<=m) ++tot,A[tot]=A[tot-1]+s2[p2++];</pre>
10
            tot=ConvexHull(A,tot);
11
        }
12
    }
```

# 5.4 Rotating Calipers

#### 5.4.1 The Diameter of Convex Hull

```
namespace CG{
1
2
        double RotatingCalipers(Point *p,int n){
3
            double dis=0;
4
            for(int i=0, j=2; i<n;++i){</pre>
                 while (abs(Cross(p[i+1]-p[i],p[j]-p[i]))<abs(Cross(p[i+1]-p[i],p[j+1]-p[i]))</pre>
5
        ) j=(j+1)%n;
                 dis=max(dis,max(DisPP(p[j],p[i]),DisPP(p[j],p[i+1])));
6
7
8
            return dis;
9
        }
10
   }
```

#### 5.4.2 The Min Distance Bewteen two Convex Hull

```
1
   namespace CG{
2
       ///点c到线段ab的最短距离
       double GetDist(Point a,Point b,Point c){
3
           if(dis(a,b) < esp) return dis(b,c); ///a,b是同一个点
4
           if(mult_Dot(b,c,a)<-esp) return dis(a,c); ///投影
5
6
           if(mult_Dot(a,c,b)<-esp) return dis(b,c);</pre>
7
           return fabs(mult_Cross(b,c,a)/dis(a,b));
8
       }
9
       ///求一条线段ab的两端点到另外一条线段bc的距离,反过来一样, 共4种情况
10
       double MinDist(Point a, Point b, Point c, Point d){
11
12
           return min(min(GetDist(a,b,c),GetDist(a,b,d)),min(GetDist(c,d,a),GetDist(c,d,b))
       );
       }
13
       double RotatingCalipers(Point *p,int n,Point *q,int m){
14
           int yminP = 0,ymaxQ=0;
15
           for(int i=1;i< n;i++){ ///找到点集p组成的凸包的左下角
16
               if(p[i].y<p[yminP].y||(p[i].y==p[yminP].y)&&(p[i].x<p[yminP].x)) yminP = i;</pre>
17
18
19
           for(int i=1;i<m;i++){ ///找到点集q组成的凸包的右上角
               if(q[i].y>q[ymaxQ].y||(q[i].y==q[ymaxQ].y)&&(q[i].x>q[ymaxQ].x))              ymaxQ = i;
20
21
           double ans = DisPP(p[yminP],q[ymaxQ]); ///距离(yminP,ymaxQ)维护为当前最小值。
22
```

```
for(int i=0;i<n;i++){</pre>
23
                 double tmp;
24
                 while(tmp=(mult_Cross(q[ymaxQ+1],p[yminP],p[yminP+1])-mult_Cross(q[ymaxQ],p[
25
       yminP],p[yminP+1]))>esp)
26
                     ymaxQ = (ymaxQ+1)%m;
                 if(tmp<-esp) ans = min(ans,GetDist(p[yminP],p[yminP+1],q[ymax0]));</pre>
27
                 else ans=min(ans,MinDist(p[yminP],p[yminP+1],q[ymaxQ],q[ymaxQ+1]));
28
29
                yminP = (yminP+1)%n;
30
31
            return ans;
        }
32
   }
33
```

# 5.5 Half Plane Intersection

```
1
   namespace CG{
        void HalfPlaneIntersection(Line 1[],int n){
2
3
            deque <Point> p;
4
            sort(l+1,l+1+n);
            deque <Line> q;
5
            q.push_back(l[1]);
6
            for (int i=2;i<=n;i++){</pre>
7
                for (;!p.empty() && !ToLeftTest(p.back()-l[i].p0,l[i].v);q.pop_back(),p.
8
       pop_back());
                for (;!p.empty() && !ToLeftTest(p.front()-l[i].p0,l[i].v);q.pop_front(),p.
9
       pop_front());
                if (sqn(Cross(l[i].v,q.back().v))==0)
10
                    if (ToLeftTest(l[i].p0-q.back().p0),q.back().v){
11
12
                        q.pop_back();
13
                        if (!p.empty()) p.pop_back();
14
                if (!q.empty()) p.push_back(GetIntersection(q.back(),l[i]));
15
                q.push_back(l[i]);
16
17
            for (;!p.empty() && !ToLeftTest(p.back()-q.front().p0,q.front().v);q.pop_back(),
18
       p.pop_back());
            p.push_back(GetIntersection(q.back(),q.front()));
19
            double area=0.5*Cross(p.back(),p.front()); Point last=p.front();
20
21
            for (p.pop_front();!p.empty();last=p.front(),p.pop_front()) area+=0.5*Cross(last
        ,p.front());
            printf("%.1f", Abs(area));
22
23
24
   }
```

# 5.6 Min Circle Cover

```
namespace CG{
1
       Point GetCircleCenter(const Point a, const Point b, const Point c){
2
3
           Point p=(a+b)/2.0, q=(a+c)/2.0;
           Vector v=Rotate(b-a,pi/2.0),w=Rotate(c-a,pi/2.0);
4
           if (sgn(Norm(Cross(v,w)))==0){
5
                if (sgn(Norm(a-b)+Norm(b-c)-Norm(a-c))==0) return (a+c)/2;
6
                if (sgn(Norm(b-a)+Norm(a-c)-Norm(b-c))==0) return (b+c)/2;
7
                if (sgn(Norm(a-c)+Norm(c-b)-Norm(a-b))==0) return (a+c)/2;
8
9
           }
10
            return GetIntersection(Line(p,v),Line(q,w));
       }
11
       void MinCircleCover(Point p[],int n){
```

```
13
             random_shuffle(p+1,p+1+n);
             Point c=p[1];
14
             double r=0;
15
             for (int i=2;i<=n;i++)</pre>
16
                  if (sgn(Norm(c-p[i])-r)>0){
17
                      c=p[i],r=0;
18
                      for (int j=1;j<i;j++)</pre>
19
20
                           if (sgn(Norm(c-p[j])-r)>0){
                               c=(p[i]+p[j])/2.0;
21
22
                               r=Norm(c-p[i]);
                               for (int k=1;k<j;k++)</pre>
23
                                    if (sgn(Norm(c-p[k])-r)>0){
24
                                        c=GetCircleCenter(p[i],p[j],p[k]);
25
                                        r=Norm(c-p[i]);
26
27
                                    }
28
                          }
29
             printf("%.10f\n%.10f %.10f",r,c.x,c.y);
30
31
        }
32
   }
```

## 5.7 Circle Union Area

```
1
   //k次覆盖
2
    //圆并去重后s[0]
3 typedef pair<double, int> P;
   const double pi = acos(-1.0);
   const int MAXN = 10003;
6 P arc[MAXN << 1];</pre>
7
   int acnt, cnt;
   double s[1003];
8
   bool del[1003];
10
   void add(double st, double en) {
11
        if(st < -pi) {
12
            add(st + 2 * pi, pi);
13
            add(-pi, en);
            return;
14
15
        if(en > pi) {
16
            add(st, pi);
17
            add(-pi, en - 2 * pi);
18
19
            return;
20
        arc[++acnt] = P(st, 1);
21
       arc[++acnt] = P(en, -1);
22
23
24
   double F(double x) {
        return (x - \sin(x)) / 2;
25
   }
26
27
   struct Node {
28
        int x, y, r;
       Node(int _x = 0, int _y = 0, int _r = 0):x(_x), y(_y), r(_r) {}
29
       bool operator == (const Node& t) {
30
31
            return x == t.x & y == t.y & r == t.r;
32
        inline void read() {
33
            scanf("%d%d%d", &x, &y, &r);
34
35
   }a[1003];
36
```

```
int main() {
37
38
        int n;
        scanf("%d", &n);
39
40
        for(int i = 1; i <= n; i++) a[i].read();</pre>
41
        //去重
42
43
        int nn = 0;
        for(int \ i = 1; \ i \ll n; \ i++)
44
45
            bool\ same = 0;
46
            for(int \ j = 1; \ j < i; \ j++)  {
                 if(a/i) == a/j) {
47
                     same = 1; break;
48
49
50
51
            if(!same) \ a[++nn] = a[i];
52
53
        n = nn;
        //去包含
54
        for(int \ i = 1; \ i <= n; \ i++) 
55
56
            for(int \ j = 1; \ j \le n; \ j++) \ if(i != j) 
                 if(hypot(a[i].x - a[j].x, a[i].y - a[j].y) < (double)(a[i].r - a[j].r)) del[i]
57
        j / = 1;
58
59
        nn = 0;
60
61
        for(int \ i = 1; \ i \le n; \ i++) \ if(!del[i])  {
62
            a/++nn/ = a/i/;
63
64
        n = nn;
65
        for(int i = 1; i <= n; i++) {
66
            acnt = 0;
67
            for(int j = 1; j <= n; j++) if(i != j) {
68
                 int dis = (a[i].x - a[j].x) * (a[i].x - a[j].x) + (a[i].y - a[j].y) * (a[i].
69
       y - a[j].y);
                if(a[j].r > a[i].r \& dis <= (a[j].r - a[i].r) * (a[j].r - a[i].r)) add(-pi,
70
        pi);
                else if(dis > (a[i].r - a[j].r) * (a[i].r - a[j].r) & dis < (a[i].r + a[j].
71
        r) * (a[i].r + a[j].r)){
72
                     double c = sqrt(dis);
                     double angle = a\cos((a[i].r * a[i].r + c * c - a[j].r * a[j].r) / (2 * a
73
        [i].r * c));
                     double k = atan2(a[j].y - a[i].y, a[j].x - a[i].x);
74
                     add(k - angle, k + angle);
75
76
77
            }
            arc[++acnt] = P(pi, -1);
78
            sort(arc + 1, arc + acnt + 1);
79
80
            cnt = 0;
            double last = -pi;
81
            for(int j = 1; j <= acnt; j++) {</pre>
82
                 s[cnt] += F(arc[j].first - last) * a[i].r * a[i].r; //扇形 - 三角形
83
                double xa = a[i].x + a[i].r * cos(last);
84
                double ya = a[i].y + a[i].r * sin(last);
85
                last = arc[j].first;
86
                double xb = a[i].x + a[i].r * cos(last);
87
                double yb = a[i].y + a[i].r * sin(last);
88
                s[cnt] += (xa * yb - xb * ya) / 2; //到圆心的三角形面积
89
                cnt += arc[j].second;
90
            }
91
92
```

# 5.8 Simpson Integrate

```
1
   double Simpson(double 1,double r){
2
        return (r-1)*(F(1)+4*F((1+r)/2)+F(r))/6;
3
   double Integrate(double l,double r,double S){
4
       double mid=(l+r)/2;
5
       double A=Simpson(l,mid);
6
7
       double B=Simpson(mid,r);
8
       if(A+B-S<eps)return S;</pre>
9
       return Integrate(l,mid,A)+Integrate(mid,r,B);
10
   }
```

# 6 Others

# 6.1 Sample

## 6.1.1 vimrc

```
1  set cindent
2  set number
3  set mouse=a
4  set tabstop=4
5  set shiftwidth=4
6  syntax on
7  inoremap { {}<left>
8  map <F9> :w<CR> :! g++ % -o %< -Wall --std=c++14 -g && ./%< <CR>
```

#### 6.1.2 Check

```
while true; do
./data > in
./tmp < in > out
./std < in > ans
diff out ans
if [ $? -ne 0 ]; then exit; fi
echo Passed
done
```

# 6.1.3 FastIO

```
namespace IO {
1
        const int MB = 1048576;
2
        const int RMAX = 16 * MB;
3
        const int WMAX = 16 * MB;
4
        #define getchar() *(rp++)
5
        #define putchar(x) (*(wp++) = (x))
6
7
        char rb[RMAX], *rp = rb, wb[WMAX], *wp = wb;
8
        inline void init() {
9
             fread(rb, sizeof(char), RMAX, stdin);
10
        template <class _T> inline void read(_T &_a) {
11
            _a = 0; register bool _f = 0; register int _c = getchar(); while (_c < '0' \mid | _c > '9') _f \mid = _c = '-', _c = getchar();
12
13
             while (_c >= '0' \& _c <= '9') _a = _a * 10 + (_c ^ '0'), _c = getchar();
14
             _a = _f ? -_a : _a;
15
16
        template <class _T> inline void write(_T _a) {
17
             static char buf[20], *top = buf;
18
19
             if (_a) {
20
                 while (_a) {
                      register _T tm = _a / 10;
21
                      *(++top) = char(_a - tm * 10) | '0';
22
23
                      _a = tm;
24
                 while (top != buf) putchar(*(top--));
25
26
             else putchar('0');
27
28
```

```
void output() {
    fwrite(wb, sizeof(char), wp - wb, stdout);
}
```

#### 6.1.4 Java BigNum

```
import java.math.*;
   import java.util.*;
3
   import java.lang.*;
   public class Main{
5
       public static void main(String []args){}
6
7
   }
    //IO
8
9
   Scanner in = new Scanner(System.in);
10 while(in.hasNext()){} //EOF
   //fast-IO
11
   public static void main(String argv[]) throws IOException{}
13 StreamTokenizer cin = new StreamTokenizer(new BufferedReader(new InputStreamReader(
       System.in)));
14 PrintWriter cout = new PrintWriter(new OutputStreamWriter(System.out));
while(cin.nextToken() != StreamTokenizer.TT_EOF);//EOF
16 cin.nextToken();int n = (int)cin.nval;String s = cin.sval;
   cout.println( Type );cout.flush();
17
   cin.ordinaryChar('/');
18
19
   BufferedReader br = new BufferedReader(new InputStreamReader(System.in));
20
   br.ready()//EOF
21
22
   while ((valueString=bf.readLine())!=null);
23
   br.close();
24
   //true\ fast-IO
25
   static class InputReader {
       public BufferedReader reader;
26
       public StringTokenizer tokenizer;
27
28
29
       public InputReader(InputStream stream) {
            reader = new BufferedReader(new InputStreamReader(stream), 32768);
30
            tokenizer = null;
31
       }
32
33
       public String next() {
34
           while (tokenizer == null || !tokenizer.hasMoreTokens()) {
35
36
                try {
                    tokenizer = new StringTokenizer(reader.readLine());
37
38
                } catch (IOException e) {
39
                    throw new RuntimeException(e);
40
           }
41
            return tokenizer.nextToken();
42
43
44
       public int nextInt() {
45
            return Integer.parseInt(next());
46
47
48
   }
49
   //类 Number
50
51
   //double Value ()
   //intValue()
```

```
//long Value()
53
54
    //shortValue()
55
   //类 BigDecimal
   //ROUND_CEILING 接近正无穷大的舍入模式。
56
57
    //ROUND_FLOOR 接近负无穷大的舍入模式。
58
    //ROUND_DOWN 接近零的舍入模式
    //ROUND_HALF_UP 四舍五入 >=0.5向上舍入
59
    //ROUND_HALF_DOWN 四舍五入 >0.5向上舍入
60
61
    //BigDecimal(BigInteger\ val)
62
    //BigDecimal(BigInteger\ unscaledVal,\ int\ scale)
    //BigDecimal(char[] in, int offset, int len, MathContext mc)
63
    //BigDecimal(double val, MathContext mc)不建议
64
    //BigDecimal(int val, MathContext mc)
65
66
    //BigDecimal(long val, MathContext mc)
67
    //BigDecimal(String val, MathContext mc)
68
    //abs()
    //add(BigDecimal augend, MathContext mc)
69
70 //compareTo(BigDecimal val)
   //divide (BigDecimal divisor, MathContext mc)
71
72
   //divideToIntegralValue(BigDecimal divisor, MathContext mc)
73 //max(BigDecimal\ val)
74
   //min(BigDecimal\ val)
    //multiply (BigDecimal\ multiplicand\ ,\ MathContext\ mc)
75
76
    //negate() 其值为 (-this), 其标度为 this.scale()
    //pow(int n)
77
    //remainder(BigDecimal divisor) 返回其值为 (this % divisor) 的 BigDecimal
78
79
    //round(Math Context mc) 返回根据 Math Context 设置进行舍入后的 Big Decimal。
80
    //caleByPowerOfTen(int n) 返回其数值等于 (this * 10^n) 的 BigDecimal。
    //subtract(BigDecimal\ subtrahend\ ,\ MathContext\ mc)
81
82
    //setScale(int newScale, RoundingMode roundingMode)
83
    //toString()
    //ulp()返回此 BigDecimal 的 ulp (最后一位的单位) 的大小
84
    //String s = b.stripTrailingZeros().toPlainString();让bigdecimal不用科学计数法显示
85
    //类 BigInteger
86
    //parseInt
87
88
    //BigInteger\ zero = BigInteger.valueOf(0);
    //BigInteger\ a = in.nextBigInteger();
89
90
   //abs()
   //and(BigInteger val) 返回其值为 (this & val)
91
92
   //or(BigInteger val) 返回其值为 (this | val)
93
   //andNot(BigInteger val) 返回其值为 (this & ~val)
94
   //compareTo(BigInteger\ val)
95
   //add(BigInteger\ val)
96
    //divide(BigInteger\ val)
    //BigInteger[] divideAndRemainder(BigInteger val) 返回包含 (this / val) 后跟 (this %
97
        val) 的两个 BigInteger 的数组。
    //equals(Object x)
98
99
    //gcd(BigInteger\ val)
100
    //isProbablePrime(int certainty) e.g. a.isProbablePrime(4)
    //max(BigInteger val) min(BigInteger val)
101
102
    //mod(BigInteger m)
    //modInverse(BigInteger m) 返回其值为 (this ~-1 mod m)
103
104
    //modPow(BigInteger exponent, BigInteger m) 返回其值为 (this exponent mod m)
    //multiply(BigInteger val)
105
106
    //not() 返回其值为 (~this)
    //shiftLeft(int n) 返回其值为 (this << n)
107
    //shiftRight(int n) 返回其值为 (this >> n)
108
    //toString()
109
110
    //valueOf(long val)
    //xor(BigInteger val) 返回其值为 (this ^ val)
111
112
    //other
```

113 //Arrays.sort(array);

# 6.2 Offline Algorithm

# 6.2.1 CDQ Divide and Conquer

```
1
    struct Node {
2
        int x, y, z, ans;
3
        Node() {}
        Node(int _x, int _y, int _z):x(_x), y(_y), z(_z) {}
4
        bool operator < (const Node &b) const {</pre>
5
6
             if(y == b.y) {
7
                 if(z == b.z) return x < b.x;
                 return z < b.z;</pre>
8
9
10
             return y < b.y;</pre>
11
   }A[MAXN], B[MAXN], C[MAXN];
12
   int bit[MAXN];
13
   void add(int k, int v) {
15
        for(; k <= m; k += k & -k) bit[k] = max(bit[k], v);</pre>
16
   }
   void clear(int k) {
17
        for(; k <= m; k += k & -k) bit[k] = 0;</pre>
18
19
20
   int sum(int k) {
        int res = 0;
21
22
        for(; k; k \rightarrow k - k) res = max(res, bit[k]);
23
        return res;
24
   }
25
    void solve(int l, int r) {
26
        if(l == r) {
27
             B[l] = A[l];
28
             return;
29
        int mid = (l + r) >> 1;
30
31
        solve(l, mid);
        for(int i = mid + 1; i <= r; i++) B[i] = A[i];</pre>
32
        //sort(B + l, B + mid + 1);
33
        sort(B + mid + 1, B + r + 1);
34
35
        int L = 1;
        for(int R = mid + 1; R <= r; R++) {</pre>
36
             while(L \leftarrow mid && B[L].y \leftarrow B[R].y) add(B[L].z, B[L].ans), L++;
37
             A[B[R].x].ans = max(A[B[R].x].ans, sum(B[R].z - 1) + 1);
38
             B[R].ans = A[B[R].x].ans;
39
40
41
        for(int i = 1; i <= L; i++) clear(B[i].z);</pre>
42
        solve(mid + 1, r);
43
        L = 1;
        int p = 1, q = mid + 1;
44
        while(p \ll mid \mid | q \ll r) {
45
             if(q > r | | (p \le mid \&\& B[p].y \le B[q].y)) C[L++] = B[p++];
46
             else C[L++] = B[q++];
47
48
        for(int i = 1; i <= r; i++) B[i] = C[i];</pre>
49
50
```

```
1
   struct Node{
2
        int 1, r, t, id;
3
        bool operator < (const Node& a) const {</pre>
4
             if(l /sz == a.l / sz) {
                 if(r == a.r) return t < a.t;</pre>
5
6
                 return r < a.r;</pre>
7
8
             return l / sz < a.l / sz;</pre>
9
    }q[MAXN];
10
    void solve() {
11
        while (t < q[i].t) addTime(t++, 1);</pre>
12
        while (t > q[i].t) addTime(--t, -1);
13
14
        while(L < q[i].l) add(L++, -1);
        while(L > q[i].l) add(--L, 1);
15
        while(R < q[i].r) add(++R, 1);
16
        while(R > q[i].r) add(R--, -1);
17
18
```

## 6.2.3 Mo's Algorithm On Tree

```
struct Edge {
1
       int to, nxt;
2
   }e[MAXN << 1];
3
   int head[MAXN], ecnt;
4
   int stack[MAXN], top, belong[MAXN], cnt, sz;
5
   struct Node {
6
7
        int l, r, id, ti;
8
        bool operator < (const Node &x) const {</pre>
            return belong[1] < belong[x.1] || (belong[1] == belong[x.1] && belong[r] <</pre>
9
       belong[x.r]) || (belong[l] == belong[x.l] && belong[r] == belong[x.r] && ti < x.ti);
10
   }q[MAXN];
11
   struct Node2 {
12
       int l, r, ti;
13
   }qq[MAXN];
14
   int n, m, Q, Q0, Q1;
15
   int V[MAXN], W[MAXN], C[MAXN];
16
   int fa[MAXN][S + 3], dep[MAXN];
17
   long long ans[MAXN], tans;
19
   int vis[MAXN], cur[MAXN];
20 long long sum[MAXN];
21
   int l, r, tm;
22
   inline int read() {
23
        int x = 0; char ch = getchar(); bool fg = 0;
       while(ch < '0' || ch > '9') { if(ch == '-') fg = 1; ch = getchar(); }
24
       while(ch >= 0, && ch <= 9) { x = x * 10 + ch - 0; ch = getchar(); }
25
       return fg ? -x : x;
26
27
   inline void add_edge(int u, int v) {
28
        e[++ecnt] = (Edge) \{v, head[u]\}; head[u] = ecnt;
29
        e[++ecnt] = (Edge) \{u, head[v]\}; head[v] = ecnt;
30
31
   void dfs(int u, int f) {
32
        fa[u][0] = f;
33
        dep[u] = dep[f] + 1;
34
        int bot = top;
35
36
        for(int i = head[u]; i; i = e[i].nxt) {
37
            int v = e[i].to;
            if(v == f) continue;
```

```
39
            dfs(v, u);
            if(top - bot >= sz) {
40
41
                while(top != bot) belong[stack[top--]] = cnt;
42
43
44
        stack[++top] = u;
45
46
    void G(int &u, int step) {
47
        for(int i = 0; i < S; i++) if((1 << i) & step) u = fa[u][i];
48
49
   int lca(int u, int v) {
50
        if(dep[u] > dep[v]) swap(u, v);
51
        G(v, dep[v] - dep[u]);
52
        if(u == v) return u;
53
        for(int i = S; i >= 0; i--) if(fa[u][i] != fa[v][i]) {
54
            u = fa[u][i]; v = fa[v][i];
55
56
        return fa[u][0];
57
58
   inline void modify(int u) {
59
        tans -= V[C[u]] * sum[cur[C[u]]];
60
        cur[C[u]] += vis[u];
61
        vis[u] = -vis[u];
62
        tans += V[C[u]] * sum[cur[C[u]]];
63
64
65
    inline void update(int u, int v) {
66
        if(u == v) return;
67
        if(dep[u] > dep[v]) swap(u, v);
        while(dep[v] > dep[u]) {
68
69
            modify(v);
            v = fa[v][0];
70
71
        while(u != v) {
72
            modify(u); modify(v);
73
            u = fa[u][0]; v = fa[v][0];
74
        }
75
   }
76
   inline void upd(int t) {
77
78
        if(vis[qq[t].l] == -1) {
79
            modify(qq[t].1);
80
            swap(C[qq[t].1], qq[t].r);
81
            modify(qq[t].l);
82
        else swap(C[qq[t].1], qq[t].r);
83
84
    inline void moveto(int u, int v) {
85
        update(l, u); update(r, v);
86
        l = u; r = v;
87
88
89
    int main() {
        n = read(); m = read(); Q = read();
90
        sz = (int)pow(n, 2.0 / 3.0);
91
        for(int i = 1; i <= m; i++) V[i] = read();</pre>
92
        for(int i = 1; i \le n; i++) W[i] = read();
93
        for(int i = 1, u, v; i < n; i++) {
94
            u = read(); v = read();
95
96
            add_edge(u, v);
97
        for(int i = 1; i <= n; i++) {
98
99
            C[i] = read();
```

```
100
             vis[i] = 1;
             sum[i] = sum[i - 1] + W[i];
101
102
103
         for(int i = 1, tp; i <= Q; i++) {
             tp = read();
104
             if(tp) {
105
                  ++01
106
107
                 q[Q1].l = read(); q[Q1].r = read();
108
                 q[Q1].id = Q1;
                 q[Q1].ti = i;
109
110
             else {
111
                 ++00:
112
                 qq[Q0].l = read(); qq[Q0].r = read();
113
114
                 qq[Q0].ti = i;
115
             }
116
         dfs(1, 0);
117
         while(top) belong[stack[top--]] = cnt;
118
119
         sort(q + 1, q + Q1 + 1);
         for(int k = 1; k <= S; k++) {
120
             for(int i = 1; i <= n; i++) {</pre>
121
                  fa[i][k] = fa[fa[i][k - 1]][k - 1];
122
123
124
125
         for(int i = 1; i <= Q1; i++) {
126
             if(belong[q[i].l] > belong[q[i].r]) swap(q[i].l, q[i].r);
127
             moveto(q[i].l, q[i].r);
128
             int lc = lca(l, r);
             modify(lc);
129
             while(qq[tm + 1].ti < q[i].ti && tm < Q0) upd(++tm);</pre>
130
             while(qq[tm].ti > q[i].ti) upd(tm--);
131
             ans[q[i].id] = tans;
132
             modify(lc);
133
134
135
         for(int i = 1; i <= Q1; i++) printf("%lld\n", ans[i]);</pre>
136
         return 0;
137
    }
```

# 6.3 Randomized Algorithm

# 6.3.1 Simulated Annealing

```
void solve() {
1
2
        while(T > eps) {
             double alpha = ((rand() % 30001) / 15000.0) * pi;
double theta = ((rand() % 10001) / 10000.0) * pi;
3
4
             tmp.x = cur.x + T * sin(theta) * cos(alpha);
5
             tmp.y = cur.y + T * sin(theta) * sin(alpha);
6
             tmp.z = cur.z + T * cos(theta);
7
             tmp.dis = cal(tmp);
8
             if(tmp.dis < cur.dis || (tmp.dis * 0.999 < cur.dis && (rand() & 7) == 7)) cur =
9
        tmp;
10
             //if(exp((cur.d - tmp.d) / T) > ((double)rand() / RAND_MAX)) cur = tmp;
11
             T *= 0.999;
12
13
        }
14
   }
```

# 6.4 Other Method

#### 6.4.1 Enumerate Subset

```
for(int i = 0; i < (1 << k); i++) {
  for(int j = i; ; --j &= i) {
      // work();
      if(j == 0) break;
    }
}</pre>
```

# **6.4.2** Enumerate $\lfloor \frac{n}{d} \rfloor \lfloor \frac{m}{d} \rfloor$

```
int cal(int n, int m) {
   if(n > m) swap(n, m);
   int res = 0, last;
   for(int i = 1; i <= n; i = last + 1) {
        last = min(n / (n / i), m / (m / i));
        res += (n / i) * (m / i) * (sum(last) - sum(i - 1));
   }
   return res;
}</pre>
```

## 6.5 Formula

## 6.5.1 Euler's Theorem

$$a^b \equiv \begin{cases} a^{b\%\varphi(p)} & \gcd(a,p) = 1 \\ a^b & \gcd(a,p) \neq 1, b < \varphi(p) \\ a^{b\%\varphi(p) + \varphi(p)} & \gcd(a,p) \neq 1, b \geq \varphi(p) \end{cases} \end{cases} (mod \ p)$$

## 6.5.2 Möbius Inversion Formula

Dirichlet Convolution is  $(f\times g)(N)=\sum_{d\mid N}f(d)*g(\frac{N}{d})$  Theorem:

$$\begin{cases} f = g \times 1 \\ g = f \times \mu \end{cases}$$

## 6.5.3 Math Theory Tips

$$\begin{cases} id(n) = \sum_{d|n} \varphi(d) \\ e(n) = \sum_{d|n} \mu(d) \end{cases}$$
 (1)

$$\begin{cases}
\sum_{i}^{n} \sum_{j}^{m} gcd(i,j) = \sum_{d}^{\max(n,m)} \varphi(d) * \lfloor \frac{n}{d} \rfloor \lfloor \frac{m}{d} \rfloor \\
\sum_{i}^{n} \sum_{j}^{m} e(gcd(i,j)) = \sum_{d}^{\min(n,m)} \mu(d) * \lfloor \frac{n}{d} \rfloor \lfloor \frac{m}{d} \rfloor \\
\sum_{i=1}^{n} |\mu(i)| = \sum_{i=1}^{\lfloor \sqrt{n} \rfloor} \mu(i) * \lfloor \frac{n}{i * i} \rfloor
\end{cases} \tag{2}$$

$$\begin{cases} sum(x,y) = \sum_{i}^{x} \sum_{j}^{y} i * j = \frac{x * (x+1)}{2} * \frac{y * (y+1)}{2} \\ F(x,y) = \sum_{i=1}^{\min(x,y)} i^{2} * \mu(i) * sum(\lfloor \frac{x}{i} \rfloor, \lfloor \frac{y}{i} \rfloor) \\ \sum_{i}^{n} \sum_{j}^{m} lcm(i,j) = \sum_{i=1}^{\min(n,m)} d * F(\lfloor \frac{n}{i} \rfloor, \lfloor \frac{y}{i} \rfloor) \end{cases}$$

$$(3)$$

# 6.5.4 Sieve Tips

$$\varphi(n) = \sum_{i=1}^{n} [(n,i) = 1] \cdot i = \frac{n * \varphi(n) + [n=1]}{2}$$
(4)

$$\begin{cases}
id = \varphi \times 1 \\
\frac{n \cdot (n+1)}{2} = \sum_{i=1}^{n} i = \sum_{i=1}^{n} \sum_{d|i} \cdot \varphi(d) = \sum_{\frac{i}{d}=1}^{n} \sum_{d=1}^{\lfloor \frac{n}{d} \rfloor} \varphi(d) = \sum_{i=1}^{n} \phi(\lfloor \frac{n}{i} \rfloor)
\end{cases}$$
(5)

$$\begin{cases} e = \mu \times 1 \\ 1 = \sum_{i=1}^{n} [i = 1] = \sum_{i=1}^{n} \sum_{d \mid i} \mu(d) = \sum_{i=1}^{n} \sum_{d=1}^{\lfloor \frac{n}{i} \rfloor} \mu(d) = \sum_{i=1}^{n} M(\lfloor \frac{n}{i} \rfloor) \end{cases}$$
(6)

$$\begin{cases}
id^{2} = (id \cdot \varphi) \times id \\
\phi'(n) = \sum_{i=1}^{n} i \cdot \varphi(i) \\
\frac{n \cdot (n+1) \cdot (2n+1)}{6} = \sum_{i=1}^{n} i^{2} = \sum_{i=1}^{n} \sum_{d \mid i} d \cdot \varphi(d) \cdot \frac{i}{d} = \sum_{\frac{i}{d}=1}^{\lfloor \frac{n}{i} \rfloor} d \cdot \varphi(d) = \sum_{i=1}^{n} i \cdot \phi'(\lfloor \frac{n}{i} \rfloor)
\end{cases}$$
(7)