



UPPSALA  
UNIVERSITET

# Low Level Parallel Programming

David Håkansson & Christopher Kjellqvist



UPPSALA  
UNIVERSITET

# Introduction

- Optimizing for SIMD operations
- Design
- Performance





# Problems

- Square roots are expensive
- Divides are also expensive
- ‘for’ loops introduce expensive control

```
double diffX = destination->getx() - x;  
double diffY = destination->gety() - y;  
double len = sqrt(diffX * diffX + diffY * diffY);  
desiredPositionX = (int)round(x + diffX / len);  
desiredPositionY = (int)round(y + diffY / len);
```

$$\Delta x = d_x - x$$

$$\Delta y = d_y - y$$

$$l = \sqrt{\Delta x^2 + \Delta y^2}$$

$$m_x = \Delta x \div l, m_y = \Delta y \div l$$

$$x \Leftarrow x + m_x, y \Leftarrow y + m_y$$



UPPSALA  
UNIVERSITET

# Problems

$$\Delta x = d_x - x$$

$$\Delta y = d_y - y$$

$$l = \sqrt{\Delta x^2 + \Delta y^2}$$

$$m_x = \Delta x \div l > .5 \quad m_y = \Delta y \div l > .5$$

$$x \Leftarrow x + m_x, y \Leftarrow y + m_y$$



UPPSALA  
UNIVERSITET

# Problems

$$\Delta x = d_x - x$$

$$\Delta y = d_y - y$$

$$l = \sqrt{\Delta x^2 + \Delta y^2}$$

$$m_x = \Delta x \div l > .5$$

$$x \Leftarrow x + m_x$$





UPPSALA  
UNIVERSITET

# Problems

$$\Delta x = d_x - x$$

$$\Delta y = d_y - y$$

$$m_x = \frac{\Delta x}{\sqrt{\Delta x^2 + \Delta y^2}} > .5$$

$$x \leftarrow x + m_x$$



UPPSALA  
UNIVERSITET

# Problems

$$\Delta x = d_x - x$$

$$\Delta y = d_y - y$$

$$m_x = \Delta x > .5 \cdot \sqrt{\Delta x^2 + \Delta y^2}$$

$$x \Leftarrow x + m_x$$



UPPSALA  
UNIVERSITET

# Problems

$$\Delta x = d_x - x$$

$$\Delta y = d_y - y$$

$$m_x = \Delta x^2 > .25 \cdot (\Delta x^2 + \Delta y^2)$$

$$x \leftarrow x + m_x$$





UPPSALA  
UNIVERSITET

# Problems

$$\Delta x = d_x - x$$

$$\Delta y = d_y - y$$

$$m_x = 4 \cdot \Delta x^2 > \Delta x^2 + \Delta y^2$$

$$x \Leftarrow x + m_x$$



UPPSALA  
UNIVERSITET

# Problems

$$\Delta x = d_x - x$$

$$\Delta y = d_y - y$$

$$m_x = 3 \cdot \Delta x^2 > \Delta y^2$$

$$x \leftarrow x + m_x$$

Originally was  $\{-1, 0, 1\}$ , which was removed because  $\Delta x$  is now squared. Create a bitmask to be 1 if  $\Delta x$  is  $> 0$  or -1 if  $\Delta x$  is  $< 0$ . Multiply by the bitmask



# Problems

$$\Delta x = d_x - x$$

$$\Delta y = d_y - y$$

$$m_x = 3 \cdot \Delta x^2 > \Delta y^2$$

$$x \leftarrow x + m_x$$

3 add/subs

3 multiplies, (2 of which can be used later)

1 compare

0 sqrt

0 divides

A few bitmasks

```
double diffX = destination->getx() - x;  
double diffY = destination->gety() - y;  
double len = sqrt(diffX * diffX + diffY * diffY);  
desiredPositionX = (int)round(x + diffX / len);
```

4 add/subs

2 multiplies

1 sqrt

1 divide



# SIMD Implementation

- Simplified Operations
- 16-bit ints (also support 32-bit ints)
- No lists
  - Agent has a maximum of 2 waypoints on all tests so only need 1 bit to store current waypoint
  - Use bitmasks



UPPSALA  
UNIVERSITET

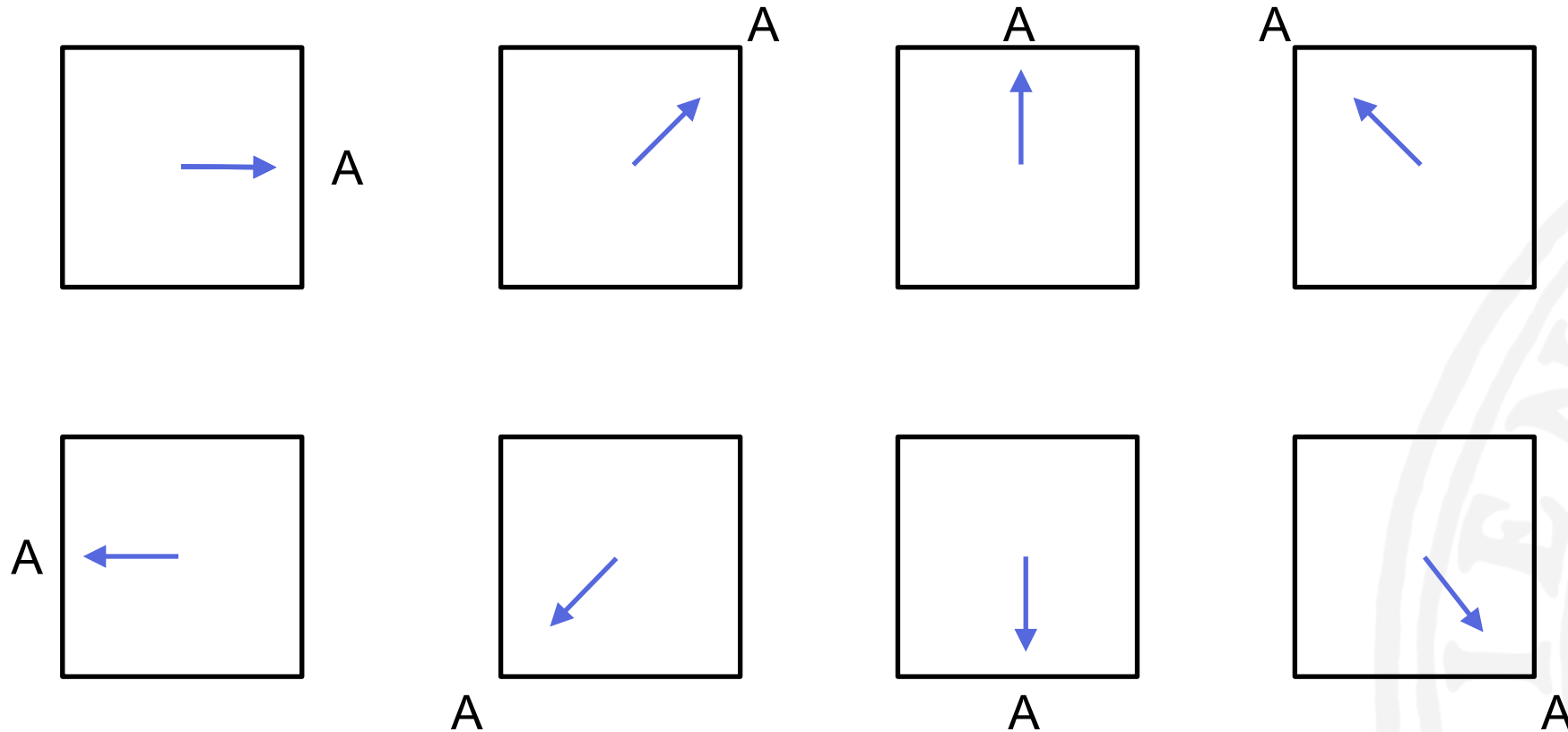
# Problem - Preferred Positions

- Uses for loop and lists to generate positions
- Not entirely obvious what positions are being generated for each direction



UPPSALA  
UNIVERSITET

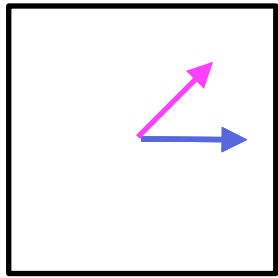
# Problem - Preferred Positions



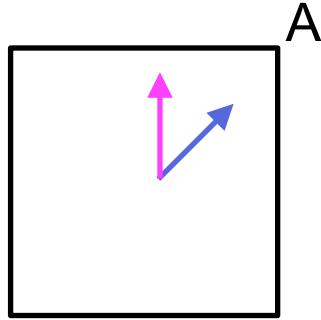


UPPSALA  
UNIVERSITET

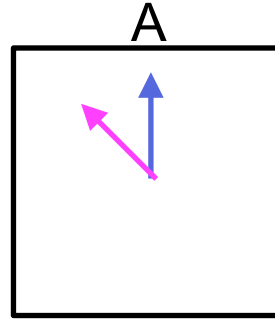
# Problem - Preferred Positions



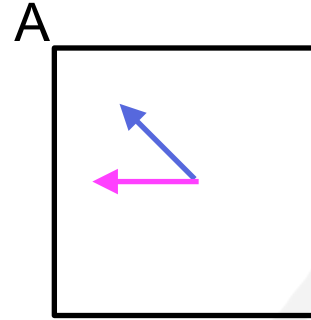
A



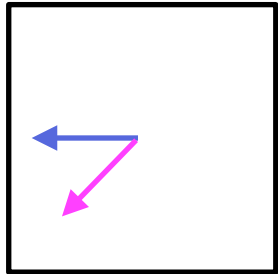
A



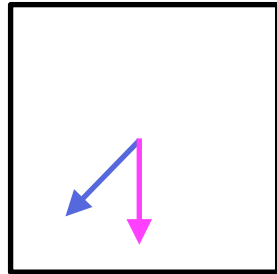
A



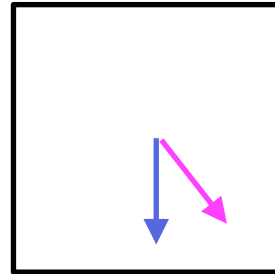
A



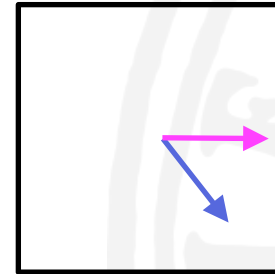
A



A



A

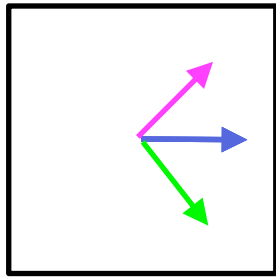


A

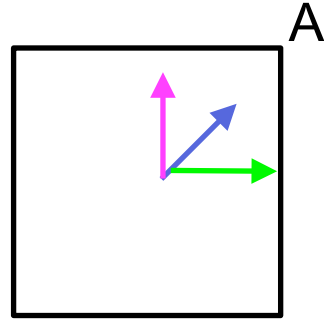


UPPSALA  
UNIVERSITET

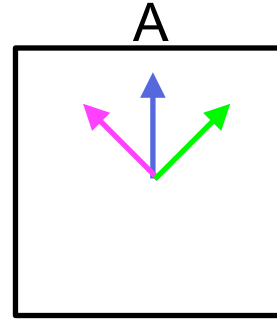
# Problem - Preferred Positions



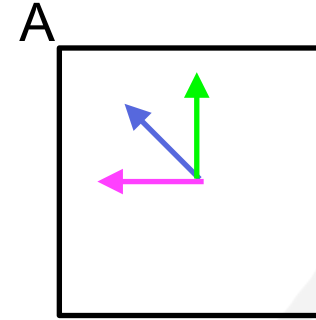
A



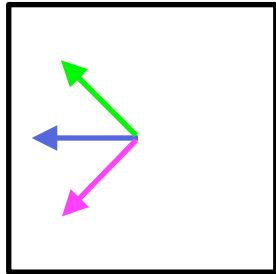
A



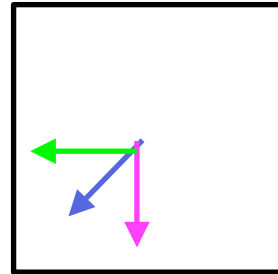
A



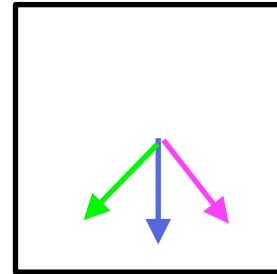
A



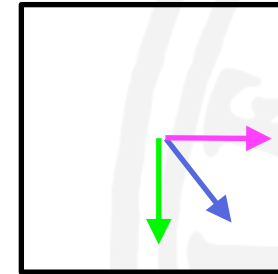
A



A



A



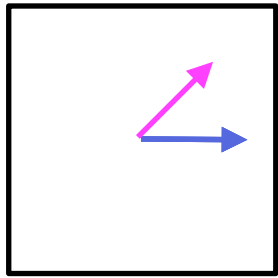
A



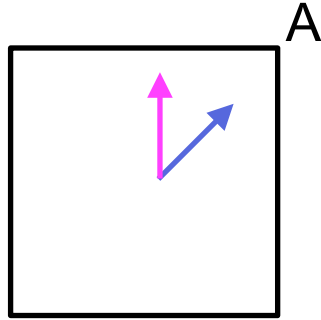


UPPSALA  
UNIVERSITET

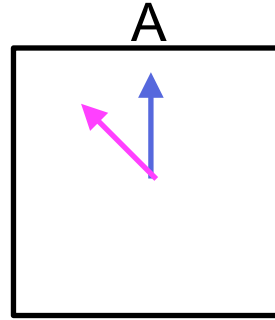
# Problem - Preferred Positions



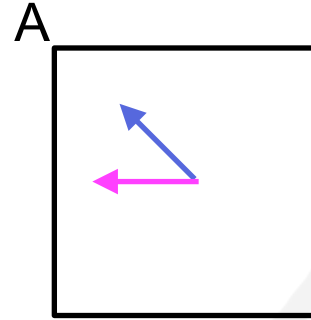
A



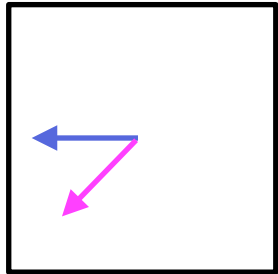
A



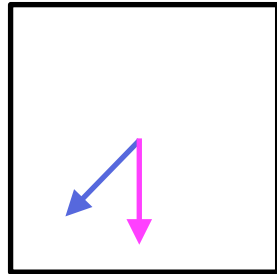
A



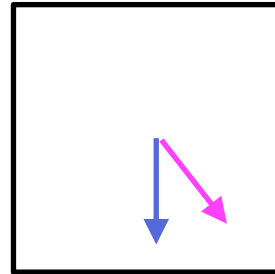
A



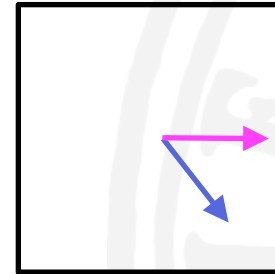
A



A



A



A



UPPSALA  
UNIVERSITET

# Problem - Preferred Positions

dx	dy	Bx	By
-1	-1	0	-1
-1	0	-1	-1
-1	1	-1	0
0	-1	1	-1
0	0	?	?
0	1	-1	1
1	-1	1	0
1	0	1	1
1	1	0	1





# Problem - Preferred Positions

dx	dy	Bx	By
-1	-1	0	-1
-1	0	-1	-1
-1	1	-1	0
0	-1	1	-1
0	0	?	?
0	1	-1	1
1	-1	1	0
1	0	1	1
1	1	0	1

$$-1_{10} = 111\dots1_2$$

$$1_{10} = 0000\dots01_2$$

$$0_{10} = 0000\dots0_2$$

Since we only have 3 cases, we can condense this to 2 bit numbers

$$-1_{10} = 11_2$$

$$1_{10} = 01_2$$

$$0_{10} = 00_2$$



# Problem - Preferred Positions

dx	dy	Bx	By
-1	-1	0	-1
-1	0	-1	-1
-1	1	-1	0
0	-1	1	-1
0	0	?	?
0	1	-1	1
1	-1	1	0
1	0	1	1
1	1	0	1

Hi-bits

dx	dy	Bx	By
11	11	0	1
11	0	1	1
11	1	1	0
0	11	0	1
0	0	?	?
0	1	1	0
1	11	0	0
1	0	0	0
1	1	0	0

Lo-bits

dx	dy	Bx	By
11	11	0	?
11	0	?	?
11	1	?	0
0	11	1	?
0	0	?	?
0	1	?	1
1	11	1	0
1	0	1	1
1	1	0	1



UPPSALA  
UNIVERSITET

# Problem - Preferred Positions

Lo-bits

dx	dy	Bx	By
11	11	0	?
11	0	?	?
11	1	?	0
0	11	1	?
0	0	?	?
0	1	?	1
1	11	1	0
1	0	1	1
1	1	0	1



UPPSALA  
UNIVERSITET

# Problem - Preferred Positions

Lo-bits

dx	dy	Bx
11	11	0
11	0	?
11	1	?
0	11	1
0	0	?
0	1	?
1	11	1
1	0	1
1	1	0



# Problem - Preferred Positions

Lo-bits

dx	dy	Bx
11	11	0
11	0	?
11	1	?
0	11	1
0	0	?
0	1	?
1	11	1
1	0	1
1	1	0

dy

	11	10	00	01
11	0	?	?	?
10	?	?	?	?
00	1	?	?	?
01	1	?	1	0

dx





# Problem - Preferred Positions

Lo-bits

dx	dy	Bx
11	11	0
11	0	?
11	1	?
0	11	1
0	0	?
0	1	?
1	11	1
1	0	1
1	1	0

dy

	11	10	00	01
11	0	?	?	?
10	?	?	?	?
00	1	?	?	?
01	1	?	1	0

dx

$$Bx\_lo = (dy \neq 1) \& (dx > -1)$$

Alternatively,  $Bx\_lo = dx \neq dy$





# Problem - Preferred Positions

Lo-bits		
dx	dy	Bx
11	11	0
11	0	?
11	1	?
0	11	1
0	0	?
0	1	?
1	11	1
1	0	1
1	1	0

		dy			
		11	10	00	01
dx	11	0	?	?	?
	10	?	?	?	?
	00	1	?	?	?
	01	1	?	1	0

$$Bx\_lo = (dy \neq 1) \& (dx > -1)$$

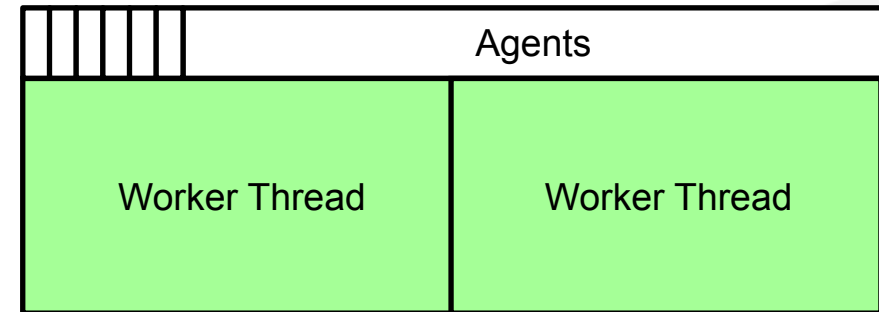
Alternatively,  $Bx\_lo = dx \neq dy$

Finally, calculate  $Bx\_hi$ , such that it either equals 0 or -1, and OR it with  $Bx\_lo$



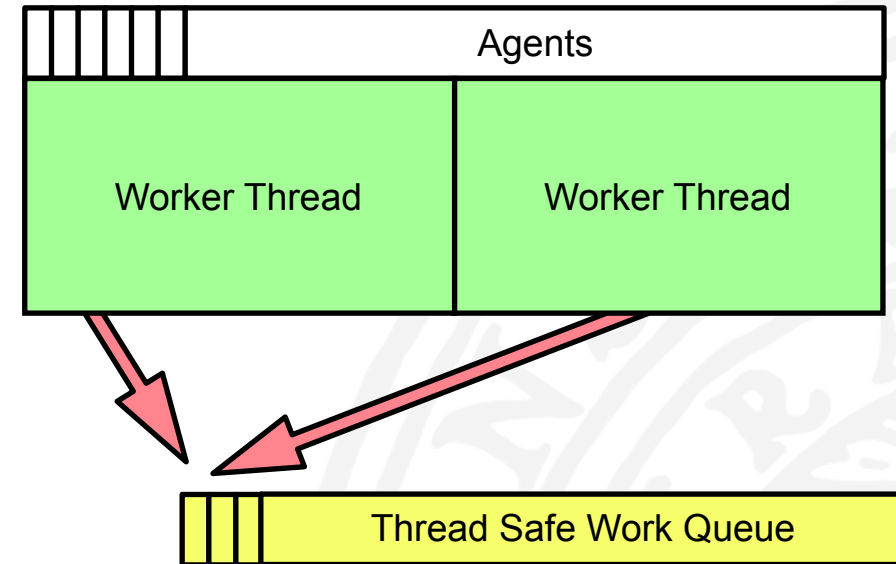
# Design - Collisions

- Producer Threads (worker)
  - Operations take constant time
  - static work allocation
- Consumer Threads



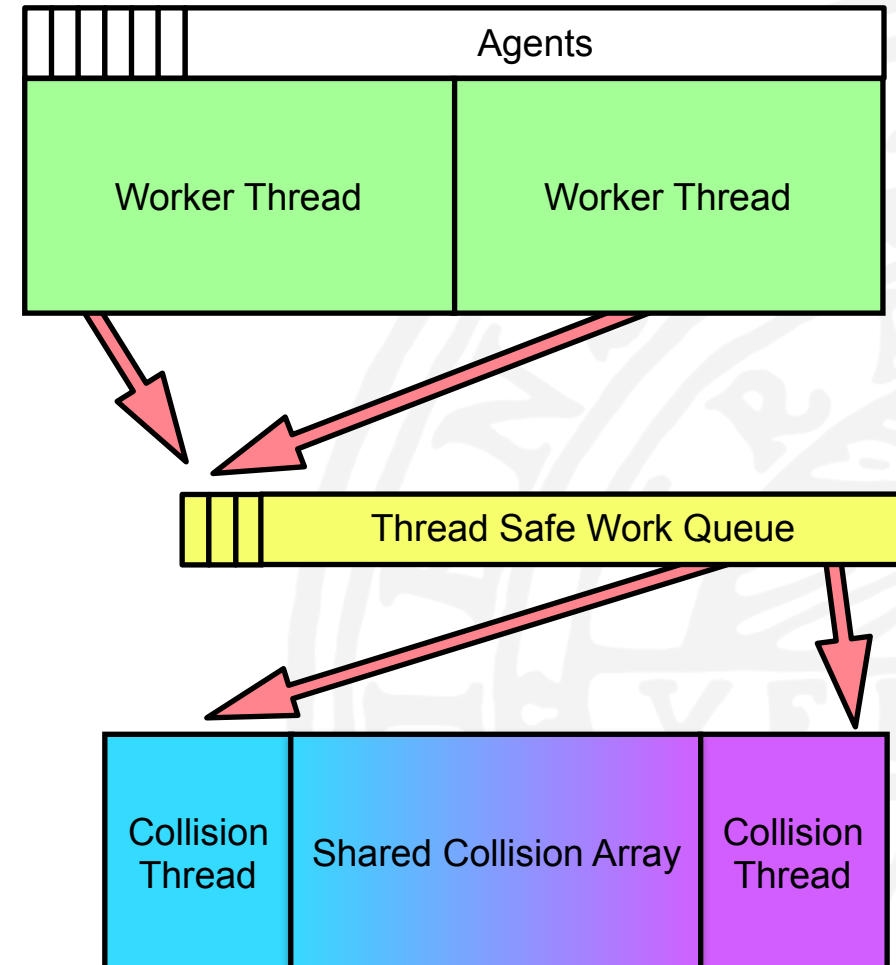
# Design - Collisions

- Producer Threads (worker)
  - Operations take constant time
  - static work allocation
- Consumer Threads
  - Non constant time ops
  - Non static work allocation



# Design - Collisions

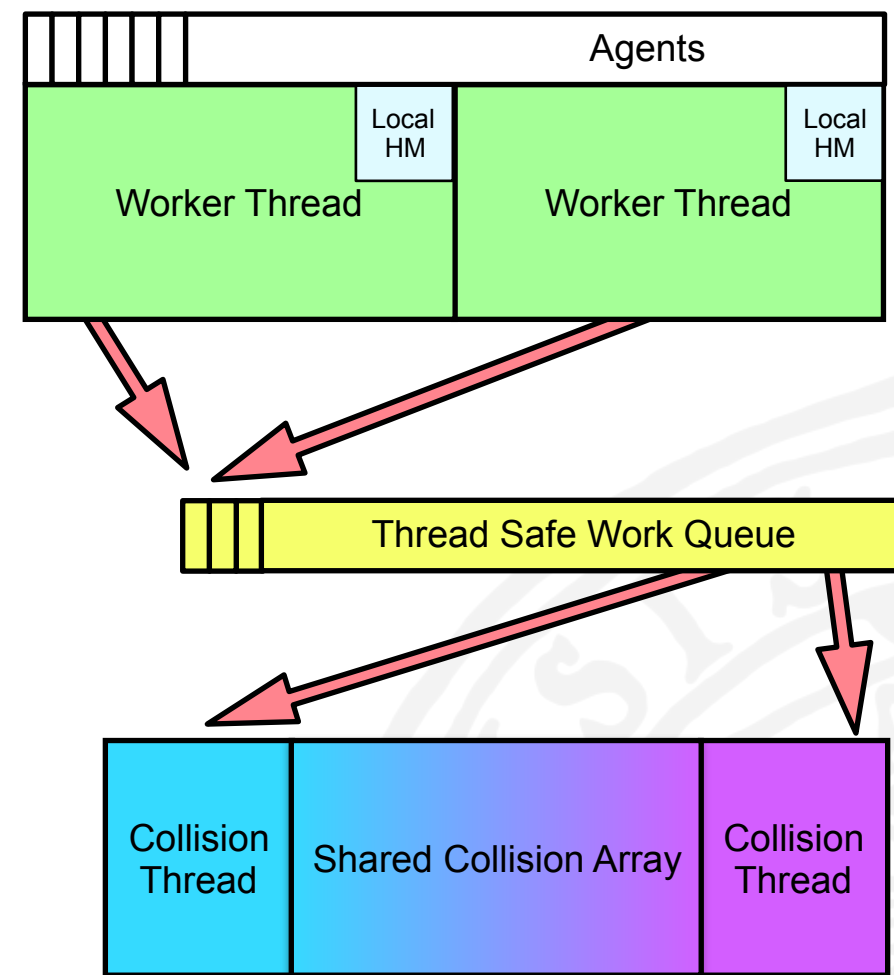
- Producer Threads (worker)
  - Operations take constant time
  - static work allocation
- Consumer Threads
  - Non constant time ops
  - Non static work allocation





# Design - Heatmap

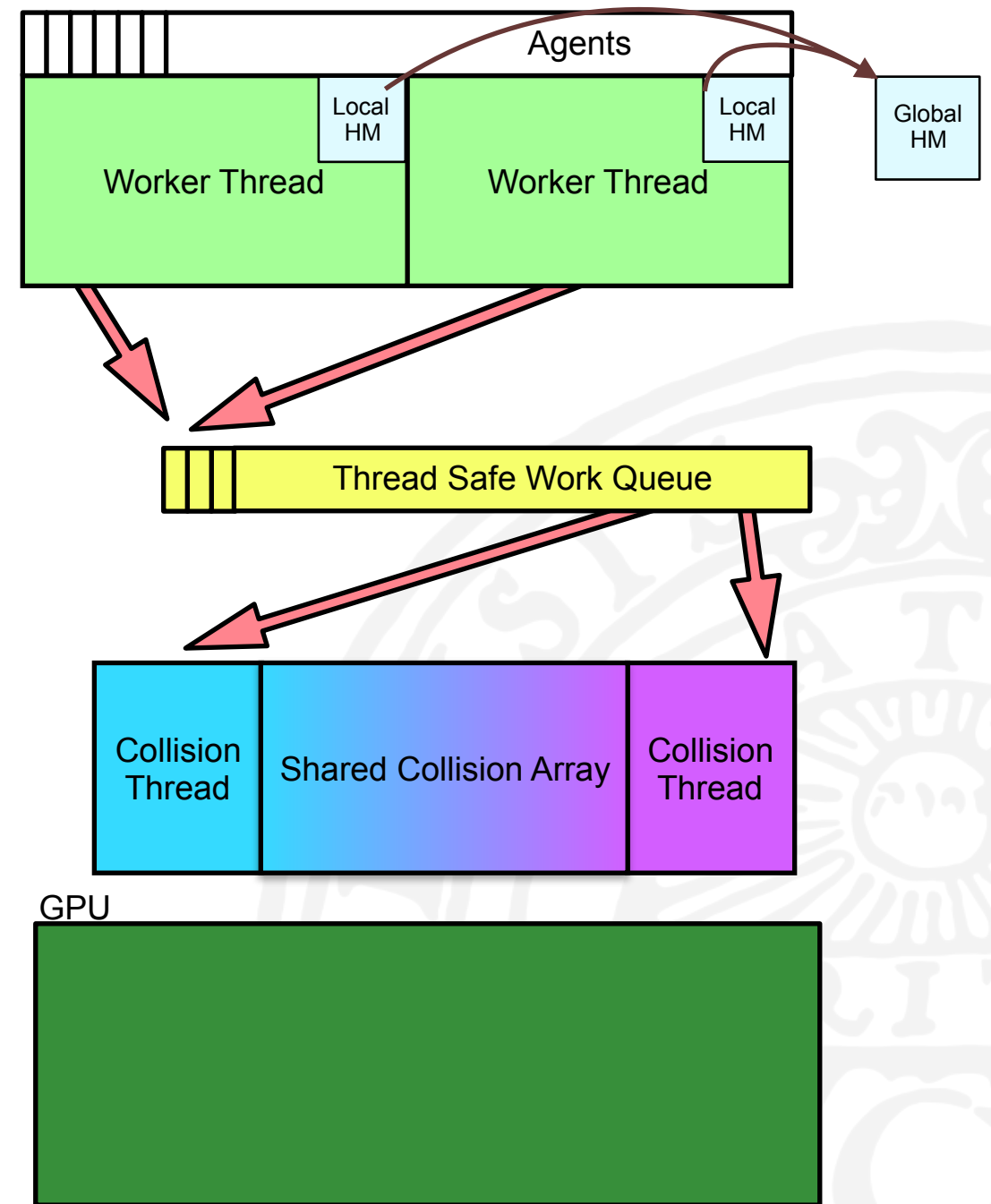
- Producer Threads (worker)
  - Operations take constant time
  - static work allocation
- Consumer Threads
  - Non constant time ops
  - Non static work allocation





# Design - Heatmap

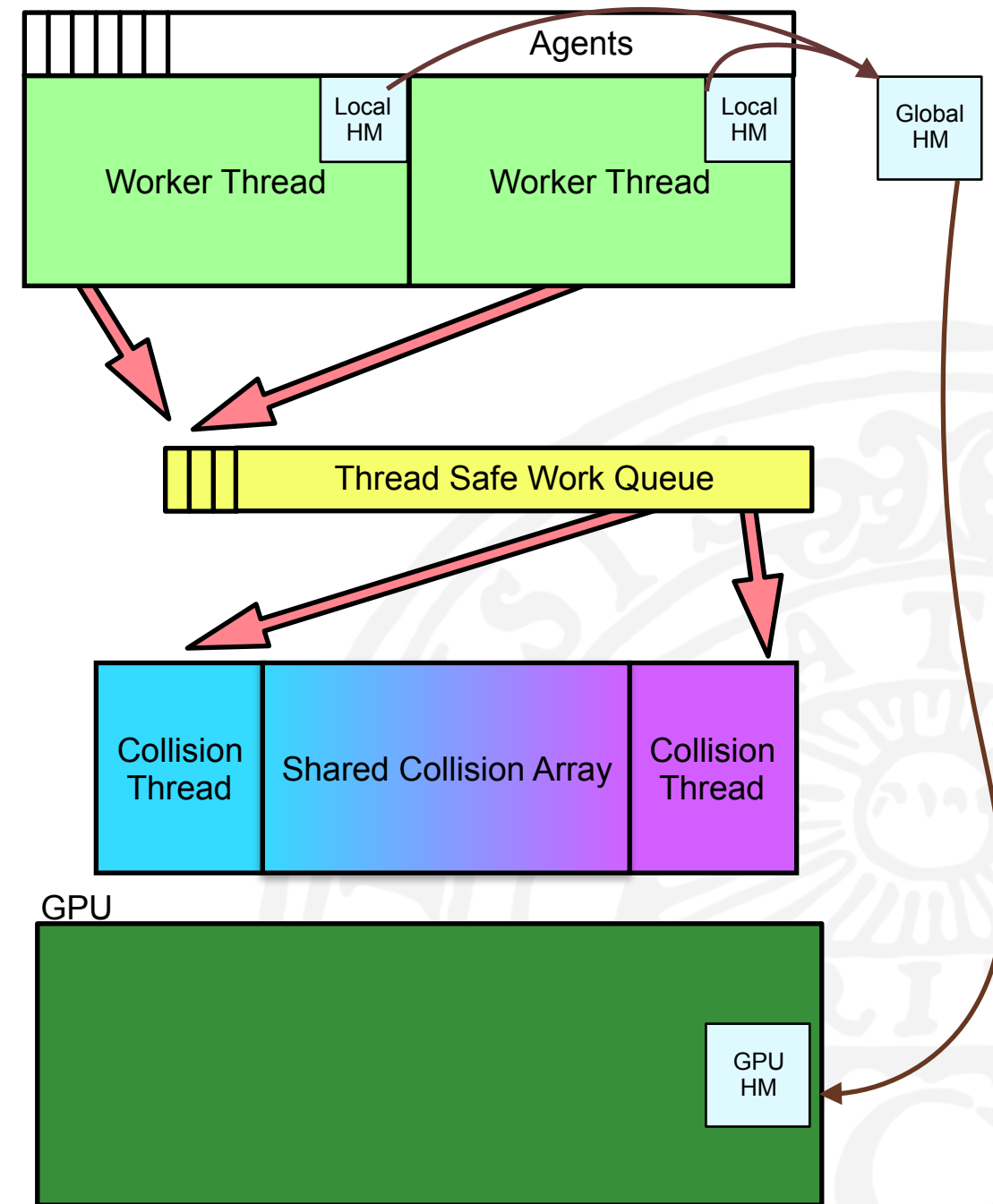
- Producer Threads (worker)
  - Operations take constant time
  - static work allocation
- Consumer Threads
  - Non constant time ops
  - Non static work allocation





# Design - Heatmap

- Producer Threads (worker)
  - Operations take constant time
  - static work allocation
- Consumer Threads
  - Non constant time ops
  - Non static work allocation

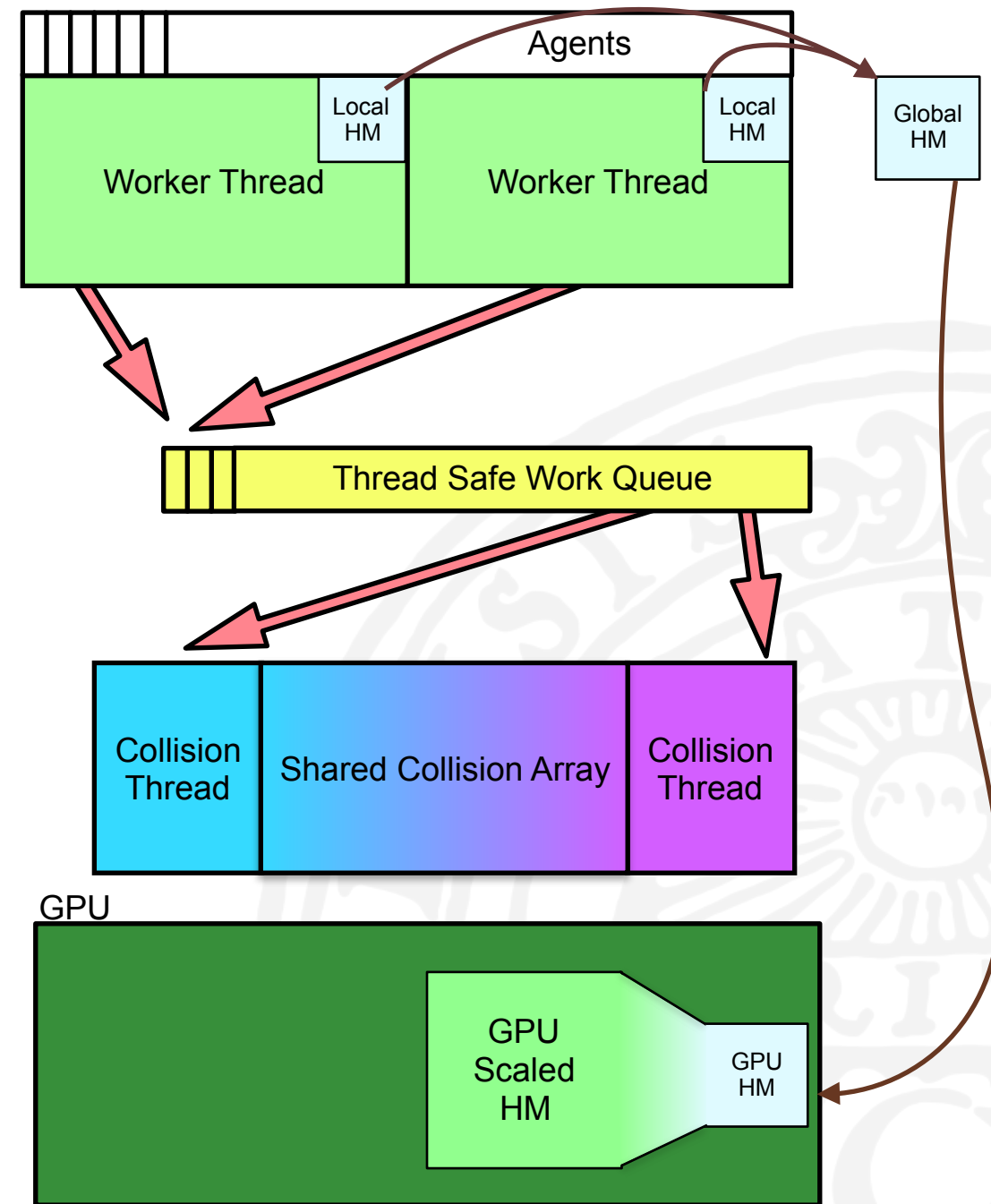




UPPSALA  
UNIVERSITET

# Design - Heatmap

- Producer Threads (worker)
  - Operations take constant time
  - static work allocation
- Consumer Threads
  - Non constant time ops
  - Non static work allocation



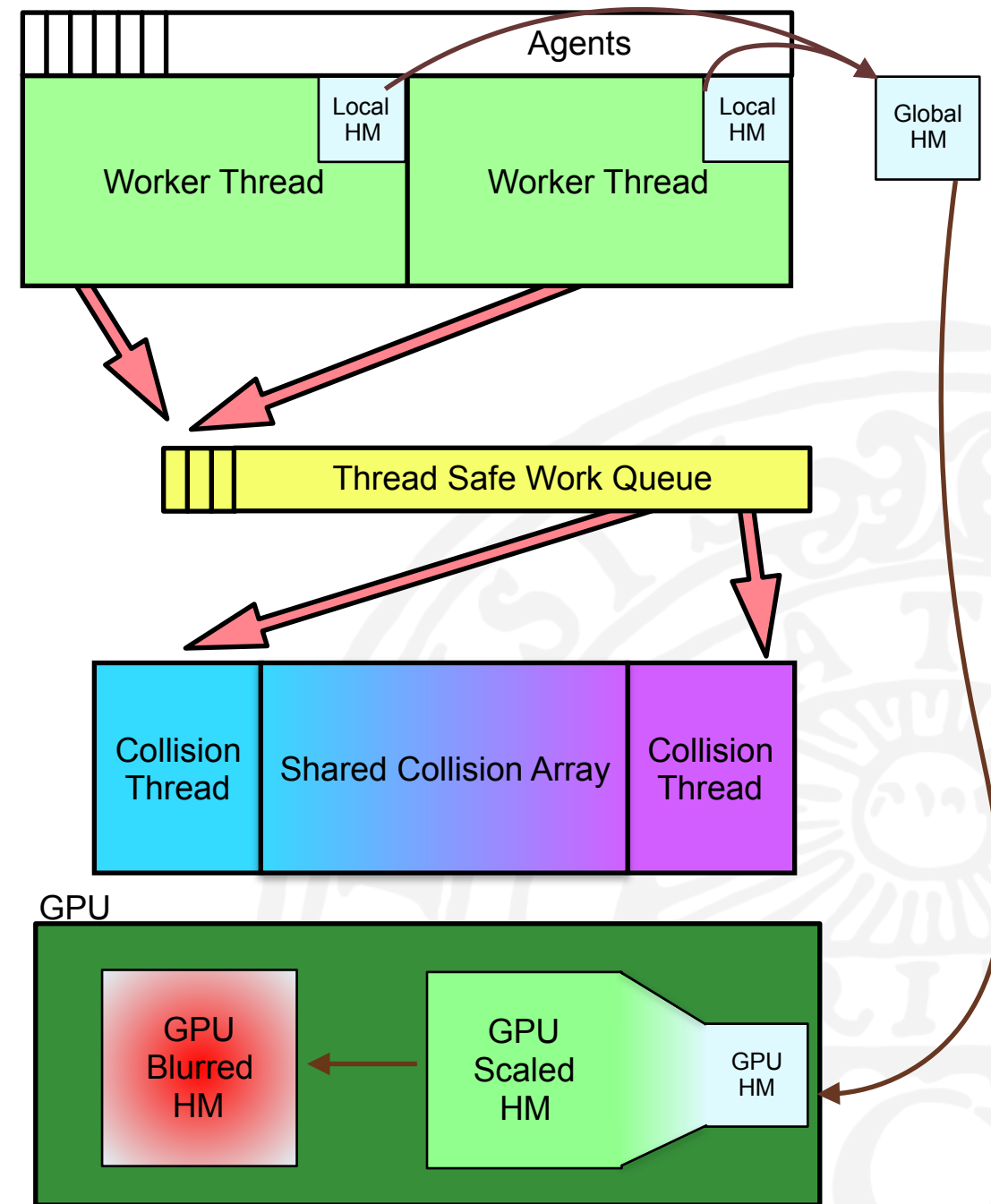




UPPSALA  
UNIVERSITET

# Design - Heatmap

- Producer Threads (worker)
  - Operations take constant time
  - static work allocation
- Consumer Threads
  - Non constant time ops
  - Non static work allocation





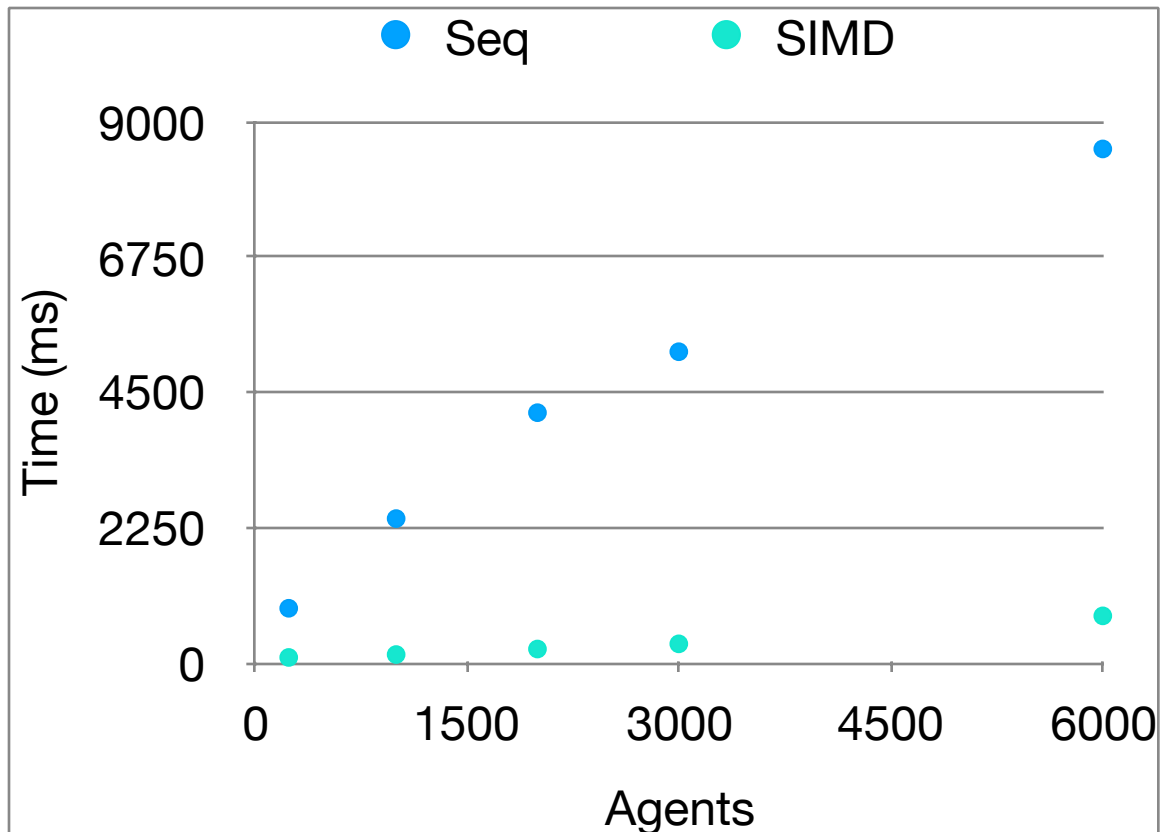
# Performance

- All numbers with 50 000 iterations done on varying number of agents (provided 50 000 iterations would take a reasonable amount of time)
- Used scenario.xml setup



# Performance

- SIMD gives us 10x speedup over original version

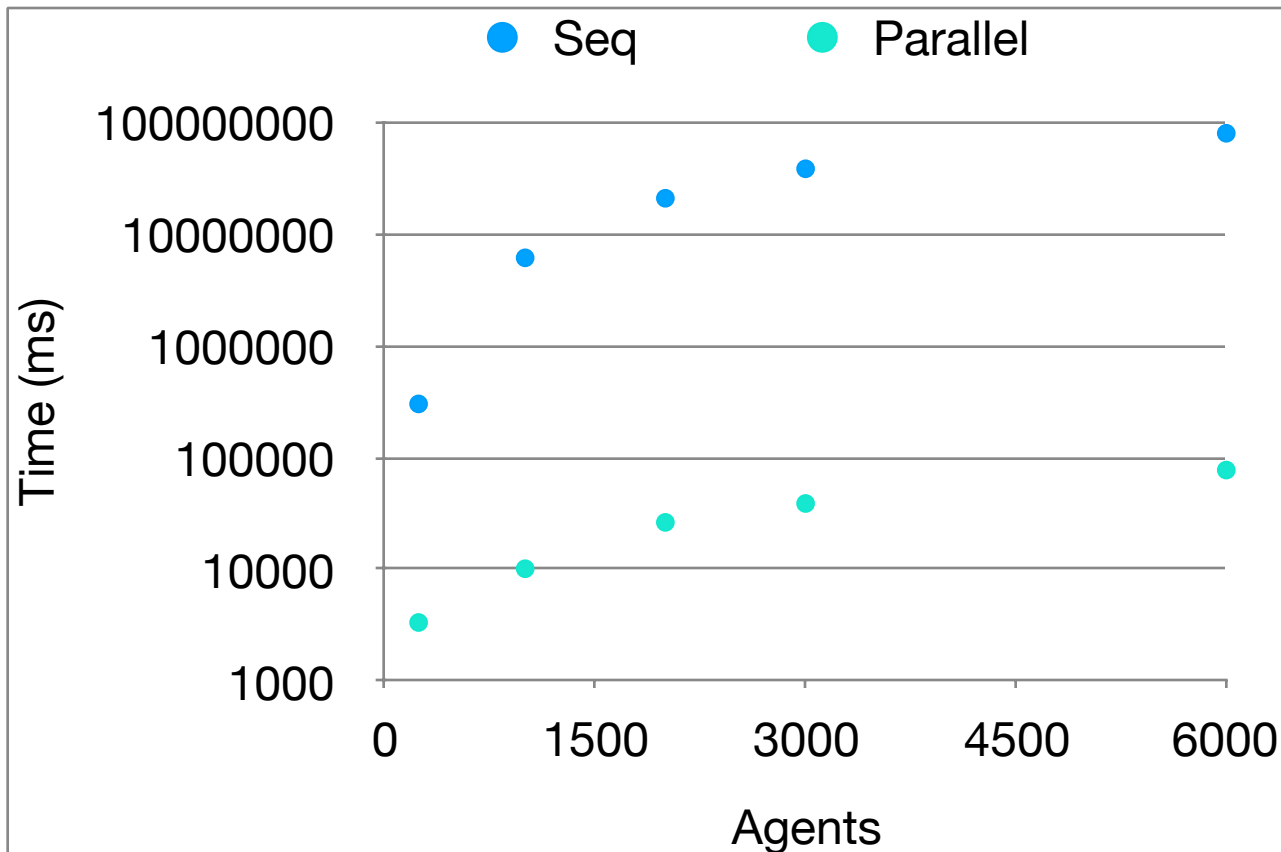


Agents	Seq(slow)	SIMD
240	908	91
1000	2398	139
2000	4159	231
3000	5172	317
6000	8542	782



# Performance

- 1000x speedup with collisions

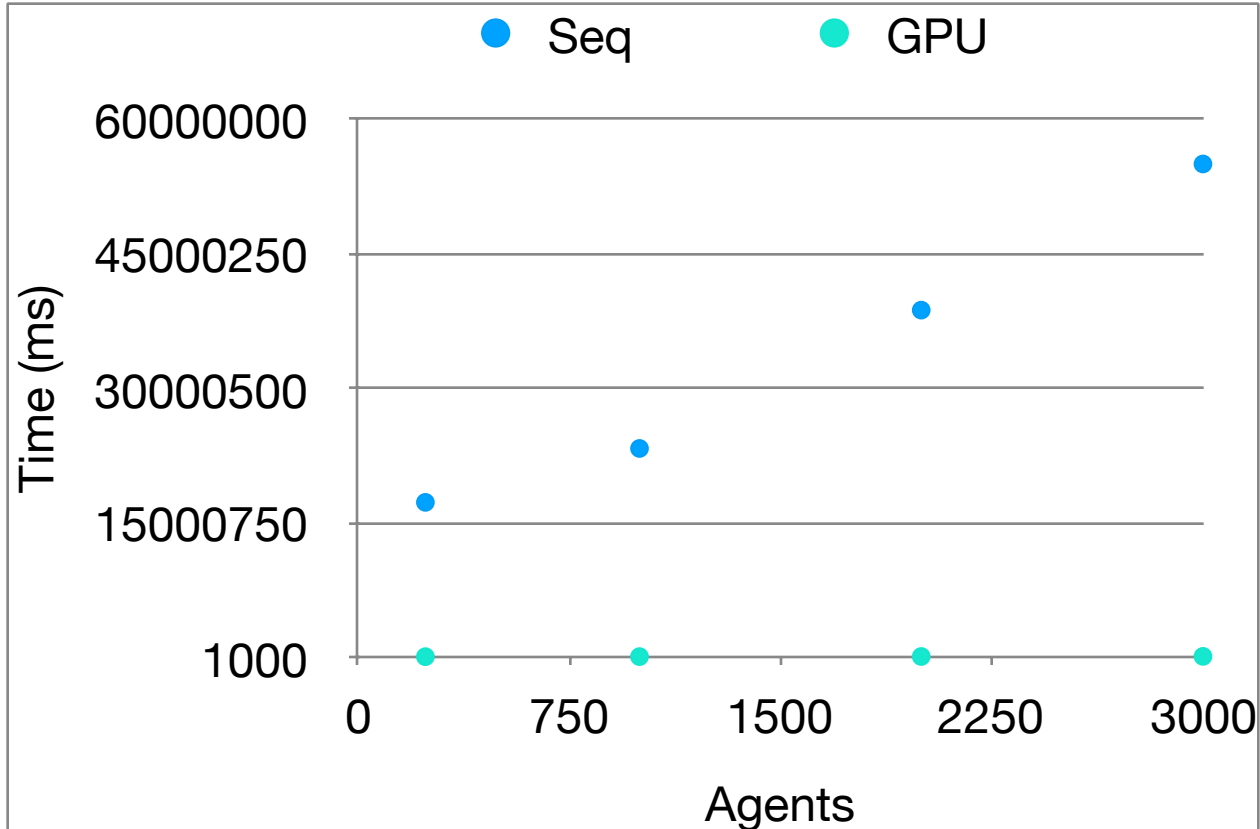


Agents	Coll_Thread4	Coll_seq
240	3334	303030
1000	10109	6172839
2000	26301	21097046
3000	38850	38759689
6000	77399	80645161



# Performance

- 385x speedup with heat map



Agents	GPU	Seq
240	110132	17314997
1000	115740	23325029
2000	129533	38750077
3000	142857	55044982



UPPSALA  
UNIVERSITET

# Takeaways

- “Effective code isn’t always good looking code”
- SIMD
- OpenMP