

## Queuing Systems

Queuing theory can be used to predict the effects of some change in load or design.

examples:

1. Time-shared computers
2. Statistical Multiplexer / Concentrator
3. Multiple Access (Random Access) Network e.g Ethernet or Wireless Network
4. Web Access e.g clients and server

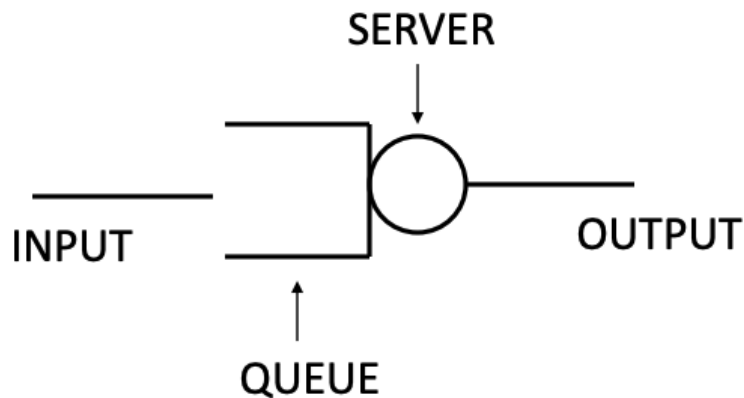
What does Queuing theory study?

- # number of users
- Arrival Characteristics
- Service Characteristics
- Resources

This leads to an indication of performance:

- Waiting Time
- Blocking?

Elements of a Queuing system



- Input
- Queue
- Server
- Output

## Models

Customers from some population can arrive at the system at random intervals

- $\lambda$  is the customer arrival rate
- There are  $c$  identical servers
- The  $j^{th}$  customer seeks service which requires  $s_j$  units of service time from one server.
- If all servers are busy then the arriving customer joins a queue until a server becomes available.

Orders in which customers can leave the queue. 1. FIFO 2. LIFO 3. Priority 4. Fair Queuing 5. etc.

The waiting time,  $t_{Qj}$  is the waiting time of a customer in the queue from entrance to the queue to entering service.

Total delay in the queue system  $\gamma_j = t_{Qj} + s_j$

$n$  = number of customers in the system

$n_q$  = number of customers in the queue

## a/b/m/K notation

### a

a represents the type of arrival process

- M for Markov. M denotes Poisson arrivals, so interarrival times are iid, exponential random variables.

### b

b represents the service time distribution

- M (Markov) denotes exponentially distributed
- D (Deterministic) denotes constant service times
- G (General) denotes iid service times following some general distribution

### m

m denotes the number of servers

### K

K denotes the maximum number of customers allowed in the system

## Acronyms