

The LOSVD of stars at projected radius R on the sky $\sigma_{\text{los}}(R)$ is given by

$$\sigma_{\text{los}}^2(R) = \frac{1}{\Sigma_{\star}(R)} \int_{R^2}^{\infty} \rho_{\star}(r) \sigma_r^2(r) \left[1 - \frac{R^2}{r^2} \beta(r) \right] \frac{dr^2}{\sqrt{r^2 - R^2}}, \quad (1)$$

where $\rho_{\star}(r)$ is the volume stellar density, $\Sigma_{\star}(R)$ is the surface stellar mass density projected on the sky, $\sigma_r(r)$ is the radial stellar VD, and $\beta(r)$ is the VD anisotropy.

Let $u \equiv \sqrt{r^2/R^2 - 1}$ with $0 \leq u < \infty$. Then equation (1) becomes

$$\sigma_{\text{los}}^2(R) = \frac{2R}{\Sigma_{\star}(R)} \int_0^{\infty} \rho_{\star}(R\sqrt{1+u^2}) \sigma_r^2(R\sqrt{1+u^2}) \left[1 - \frac{\beta(R\sqrt{1+u^2})}{1+u^2} \right] du. \quad (2)$$

Now let $v \equiv u + a$ with a positive constant a so that $a \leq v < \infty$. Finally, let $w \equiv e^{-v}$ so that $0 \leq w \leq e^{-a}$. Then equation (2) takes the following form with a finite integration range

$$\sigma_{\text{los}}^2(R) = \frac{2R}{\Sigma_{\star}(R)} \int_0^{e^{-a}} \rho_{\star}(R t(w)) \sigma_r^2(R t(w)) \left[1 - \frac{\beta(R t(w))}{t^2(w)} \right] \frac{dw}{w}, \quad (3)$$

where $t(w) \equiv \sqrt{1 + (\ln w + a)^2}$. We may choose $a = 1/2$ or some other positive number.