

IntermediateProblems

November 12, 2018

1 Intermediate Problems

1.1 MyRange and LinSpace Problem

Part 1

Let's create our own implementation of the range type. The Range type is what you get from `1:2:20`. Its form is `start:step:stop`. If you know `start`, `step`, and `stop`, how do you calculate the `i`th value? Create a type `MyRange` which stores `start`, `step`, and `stop`. Can you create a function `_MyRange(a,i)` which for `a` being a `MyRange`, it returns what `a[i]` should be? After getting this correct, use the [Julia array interface](#) in order to define the function for the `a[i]` syntax on your type.

Part 2

A `LinSpace` object is a lazy representation of `N` values from `start` to `stop`. Use the `Array` interface to implement a lazy version of the `LinSpace`. Test against `range(start,stop=stop,length=N)`.

<http://ucidatascienceinitiative.github.io/IntroToJulia/Html/ArrayIteratorInterfaces>

(Note, Base's range type has extra accuracy enhancing changes. Just do the "simple" implementation")

Part 3 Check out the call overloading notebook:

<http://ucidatascienceinitiative.github.io/IntroToJulia/Html/CallOverloading>

Overload the call on the `UnitStepRange` to give an interpolated value at intermediate points, i.e. if `a=1:2:10`, then `a(1.5)=2`.

Part 4 Do your implementations obey dimensional analysis? Try using the package `Unitful` to build arrays of numbers with units (i.e. an array of numbers who have values of Newtons), and see if you can make your `LinSpace` not give errors.

1.2 Operator Problem

In mathematics, a matrix is known to be a linear operator. In many cases, this can have huge performance advantages because, if you know a function which "acts like a matrix" but does not form the matrix itself, you can save the time that it takes to allocate the matrix (sometimes the matrix may not fit in memory!)

Recall the Strang matrix

$$\begin{bmatrix} -2 & 1 & & & \\ 1 & -2 & 1 & & \\ & \ddots & \ddots & \ddots & \\ & & \ddots & \ddots & 1 \\ & & & 1 & -2 \end{bmatrix}$$

Define a type `StrangMatrix` and define a dispatch such that `A*x` acts like a Strang matrix on a vector.

1.2.1 Advanced Bonus

Iterative solvers solve $Ax=b$ and only require the definition of matrix multiplication. Thus utilize `IterativeSolvers.jl` to solve $Ax=b$ for $b=\text{rand}(100)$ using your lazy matrix type. Hint: you will need to define `mul!` from `LinearAlgebra` (standard library). You will also need to define a different version of your Strang matrix which holds a size and has `Base.eltype` defined.

1.3 Regression Problem

In []: *#### Prepare Data For Regression Problem*

```
X = rand(1000, 3)           # feature matrix
a0 = rand(3)                # ground truths
y = X * a0 + 0.1 * randn(1000); # generate response

# Data For Regression Problem Part 2
X = rand(100);
y = 2X + 0.1 * randn(100);
```

Given an $N \times 3$ array of data (`randn(N,3)`) and a $N \times 1$ array of outcomes, produce the data matrix X which appends a column of 1's to the front of the data matrix, and solve for the 4×1 array β via $X\beta = y$ using `qr`fact, or `\`, or [the definition of the OLS estimator](#). (Note: This is linear regression).

Compare your results to that of using `llsq` from `MultivariateStats.jl` (note: you need to go find the documentation to find out how to use this!). Compare your results to that of using ordinary least squares regression from `GLM.jl`.

Regression Problem Part 2 Using your OLS estimator or one of the aforementioned packages, solve for the regression line using the (X,y) data above. Plot the (X,y) scatter plot using `scatter!` from `Plots.jl`. Add the regression line using `abline!`. Add a title saying "Regression Plot on Fake Data", and label the x and y axis.

1.4 Type Hierarchy Problem

Make a function `person_info(x)` where, if x is a any type of person, print their name. However, if x is a student, print their name and their grade. Make a new type which is a graduate student, and have it print their name and grade as well. If x is anything else, throw an error. Do not use branching (`if`), use multiple dispatch to solve the problem!