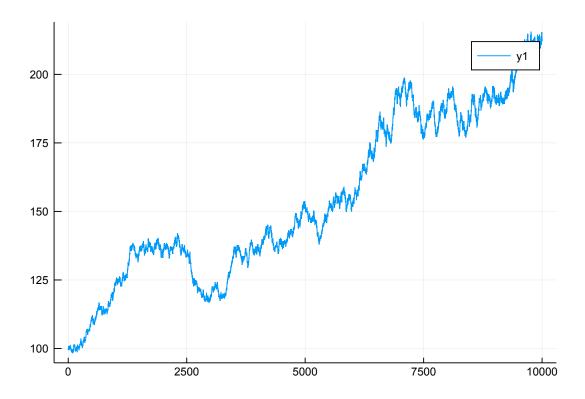
StockProblemAnswers

September 11, 2018

0.1 Problem 1 a)

```
In [6]: using Plots
        S = 100
        r = 0.08
        T = 1
        n = 10000
        sigma = 0.3
        h = T/n
        u = exp(r*h + sigma * sqrt(h))
        d = exp(r*h - sigma * sqrt(h))
        p_star = (exp(r*h) - d) / (u - d)
        path = Array{Float64}(undef,n + 2)
        #add in the starting price
        path[1] = S
        for k in 2:n+2
            if rand() < p_star</pre>
                #then we go up
                path[k] = path[k-1] * u
            else
                path[k] = path[k-1] * d
            end
        end
        plot(path)
   Out[6]:
```



0.2 Problem 1 b)

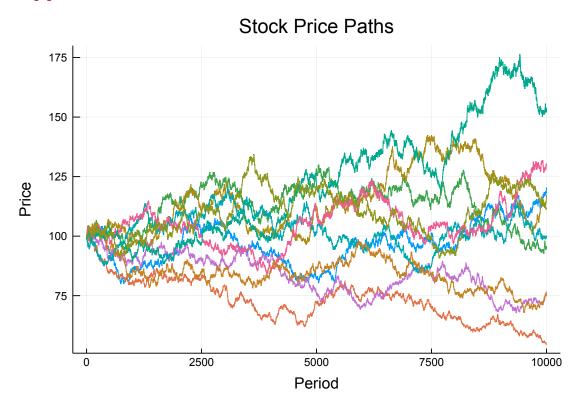
```
In [8]: using Plots
```

```
end
    path
end

p = plot(createPath(100.0, 0.08, 0.3, 1.0, 10000));
plot!(p, title="Stock Price Paths", xlabel="Period", ylabel="Price", legend=false)

for k in 1:9
    plot!(p, createPath(100.0, 0.08, 0.3, 1.0, 10000))
end
p
```

Out[8]:

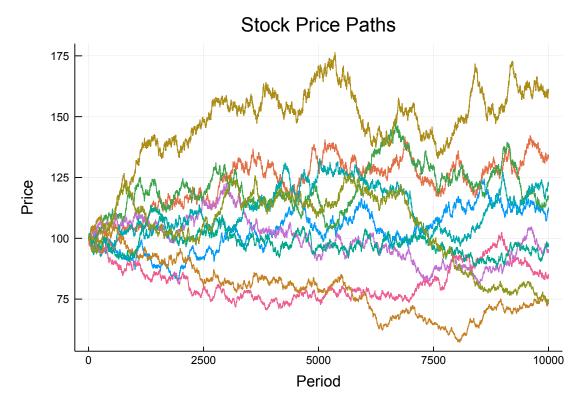


0.3 1 c) (Optional)

```
p = plot(paths[1]);
plot!(p, title="Stock Price Paths", xlabel="Period", ylabel="Price", legend=false)

for k in 2:10
    plot!(p, paths[k])
end
p
```

Out[4]:



In [2]: # Distributed parallelism
 # This will work across multiple computers and multiple nodes of a cluster

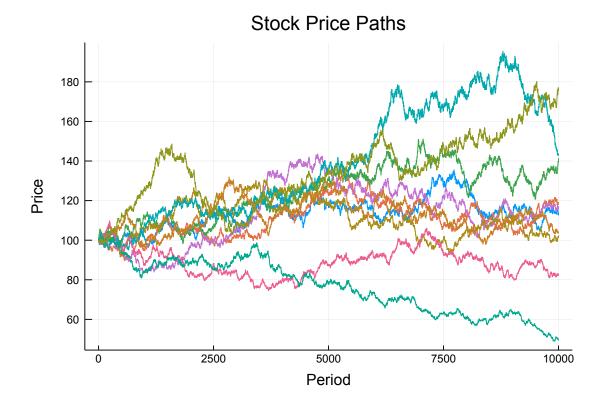
using Distributed
addprocs()

@everywhere function createPath(S, r, sigma, T, n)
 h = T / n
 u = exp(r*h + sigma * sqrt(h))
 d = exp(r*h - sigma * sqrt(h))

 p_star = (exp(r*h) - d) / (u - d)

path = Array{Float64}(undef, n + 2)

```
#add in the starting price
         path[1] = S
         for k in 2:n+2
             if rand() < p_star</pre>
                 #then we go up
                 path[k] = path[k-1] * u
                 path[k] = path[k-1] * d
             end
         end
         path
     end
     f = (i) -> createPath(100.0, 0.08, 0.3, 1.0, 10000)
     paths = pmap(f,1:10)
     using Plots
     p = plot(paths[1]);
     plot!(p, title="Stock Price Paths", xlabel="Period", ylabel="Price", legend=false)
     for k in 2:10
         plot!(p, paths[k])
     end
     p
Out[2]:
```



0.4 2 a

The probabilities follow the binomial formula. Let S_T denote the final price.

$$\mathbb{P}[S_T = u^{n-k} d^k S] = \binom{n}{k} p^{*(n-k)} (1 - p^*)^k$$

0.5 2 b

for n = 100

In [3]: function computeDistribution(S, r, sigma, T, n)

```
h = T / n
u = exp(r*h + sigma * sqrt(h))
d = exp(r*h - sigma * sqrt(h))

p_star = (exp(r*h) - d) / (u - d)

prices = Array{Float64}(undef, n + 1)

probs = Array{Float64}(undef, n + 1)

for k in 1:n+1
    prices[k] = S * (u ^ (n-k)) * (d ^ k)
    probs[k] = binomial(BigInt(n), BigInt(k)) * p_star^(n-k) * (1 - p_star)^k
```

end

```
scatter(prices, probs)
title = "Distrbution for Binomial Model with $n periods \n S = $S, r = $r, sigma =
scatter!(title = title, xlabel= "Stock Price", ylabel = "Probability", legend = fal
end
computeDistribution(100.0, 0.08, 0.3, 1.0, 100)
```

Out[3]:

