## **BasicProblemAnswers**

May 12, 2018

## 1 Starter Problems

### 1.1 Strang Matrix Problem

```
In [3]: N = 10
       A = zeros(N, N)
       for i in 1:N, j in 1:N
           abs(i-j) \le 1 \&\& (A[i,j] +=1)
           i == j \& \& (A[i, j] -= 3)
       end
       Α
Out[3]: 10×10 Array{Float64,2}:
        -2.0
              1.0
                    0.0
                        0.0
                                0.0
                                     0.0
                                           0.0
                                                 0.0
                                                      0.0
                                                            0.0
             -2.0
                   1.0
                          0.0
                                0.0
                                                 0.0
                                                      0.0
                                                            0.0
         1.0
                                     0.0
                                           0.0
             1.0 -2.0
         0.0
                         1.0
                               0.0
                                     0.0
                                           0.0
                                                0.0
                                                      0.0
                                                            0.0
         0.0
             0.0 	 1.0 	 -2.0
                              1.0
                                    0.0
                                           0.0
                                              0.0
                                                      0.0
                                                            0.0
         0.0
              0.0
                  0.0
                        1.0 -2.0
                                    1.0
                                           0.0
                                               0.0 0.0
                                                            0.0
         0.0
             0.0 0.0 0.0
                              1.0 - 2.0
                                           1.0
                                               0.0 0.0
                                                            0.0
         0.0 0.0 0.0 0.0
                              0.0
                                    1.0 - 2.0
                                               1.0
                                                      0.0
                                                            0.0
         0.0
              0.0 0.0 0.0
                               0.0
                                    0.0
                                           1.0 -2.0
                                                     1.0
                                                            0.0
         0.0
               0.0
                    0.0 0.0
                                0.0
                                    0.0
                                           0.0
                                               1.0 - 2.0
                                                          1.0
         0.0
                    0.0
               0.0
                        0.0
                                0.0
                                     0.0
                                           0.0
                                                 0.0 	 1.0 	 -2.0
```

#### 1.2 Factorial Problem

#### 1.3 Binomial Problem

```
In [1]: function binomial_rv(n, p)
           count = zero(n)
           U = rand(n)
           for i in 1:n
             U[i] 
           end
           count
       end
       bs = [binomial_rv(10, 0.5) for j in 1:10]
Out[1]: 10-element Array{Int64,1}:
        1
        5
        6
        2
        4
        3
        5
        5
```

#### **1.4** Monte Carlo $\pi$ Problem

```
In [17]: n = 10000000

count = 0
    for i in 1:n
        u, v = 2rand(2)-1
        d = sqrt(u^2 + v^2)  # Distance from middle of square
        d < 1 && (count += 1)
    end

area_estimate = count / n

print(area_estimate * 4)  # dividing by radius**2

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```

# 2 Integration Problems

## 2.1 Timeseries Generation Problem

```
In [22]: alphas = [0.0, 0.5, 0.98]
T = 200
```

```
series = []
labels = []

for alpha in alphas
    x = zeros(T + 1)
    x[1] = 0.0
    for t in 1:T
        x[t+1] = alpha * x[t] + randn()
    end
    push!(series, x)
    push!(labels, "alpha = $alpha")
end

plot(series, label=reshape(labels,1,length(labels)),lw=3)
```

#### 2.2 Logistic Equation Problem

```
In [9]: r = 2.9:.001:4; numAttract = 100
    steady = ones(length(r),1)*.25
    for i=1:400 ## Get to steady state
        steady .= r.*steady.*(1-steady)
    end
    x = zeros(length(steady), numAttract)
    x[:,1] = steady
    @inbounds for i=2:numAttract ## Grab values at the attractor
        x[:,i] = r.*x[:,i-1].*(1-x[:,i-1])
    end
    using Plots; gr()
    plot(collect(r),x,seriestype=:scatter,markersize=.002,legend=false,color=:R
```