

# Stochastic SIR in continuous time using Gillespie.jl

Simon Frost

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```
using Gillespie
using Random
using Plots
using BenchmarkTools

function sir_rates(x,parms)
    (S,I,R) = x
    ( $\beta$ , $\gamma$ ) = parms
    N = S+I+R
    infection =  $\beta$ *S*I/N
    recovery =  $\gamma$ *I
    [infection,recovery]
end
sir_transitions = [[-1 1 0];[0 -1 1]]

2×3 Array{Int64,2}:
-1  1  0
 0 -1  1

u0 = [999,1,0]
p = [0.5,0.25]
Random.seed!(1235)
tf = 50.0

50.0

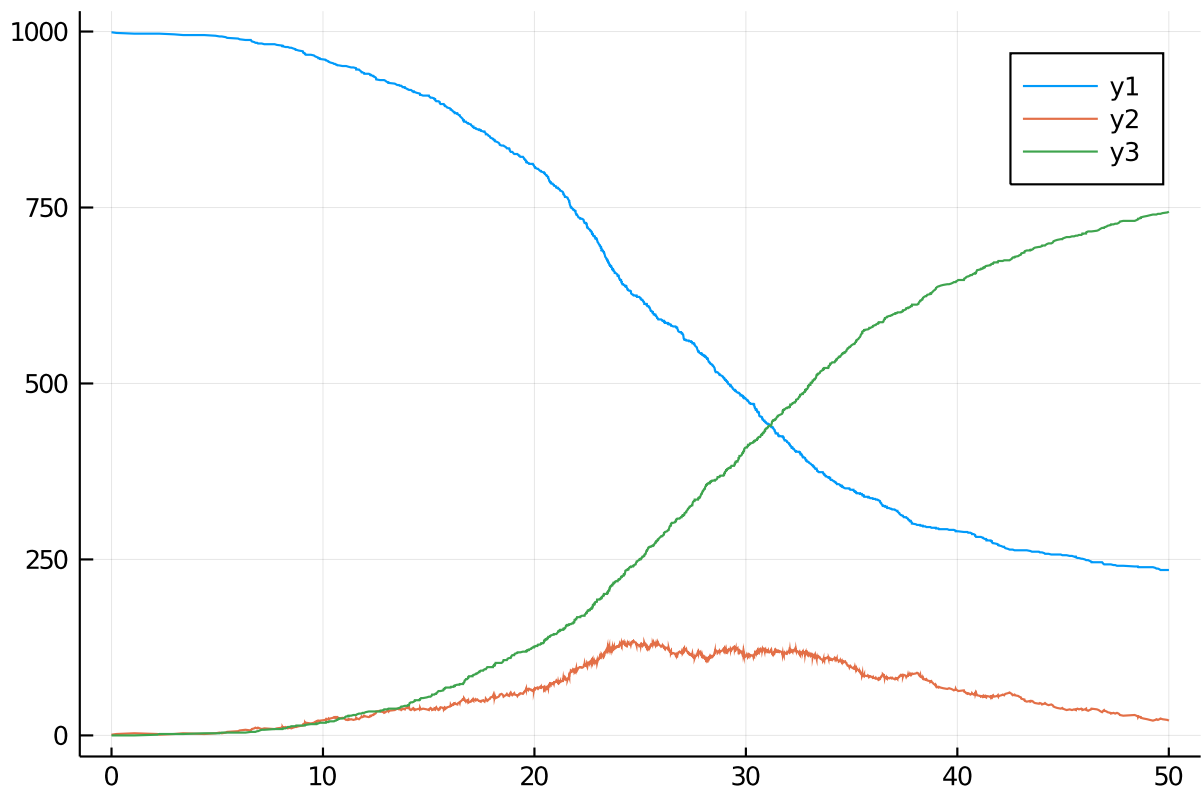
sir_result = ssa(u0,sir_rates,sir_transitions,p,tf)
data = ssa_data(sir_result)
```

|    | time     | x1    | x2    | x3    |
|----|----------|-------|-------|-------|
|    | Float64  | Int64 | Int64 | Int64 |
| 1  | 0.0      | 999   | 1     | 0     |
| 2  | 0.236916 | 998   | 2     | 0     |
| 3  | 1.07532  | 997   | 3     | 0     |
| 4  | 2.16728  | 997   | 2     | 1     |
| 5  | 2.25891  | 997   | 1     | 2     |
| 6  | 2.96813  | 996   | 2     | 2     |
| 7  | 3.38675  | 995   | 3     | 2     |
| 8  | 4.38327  | 995   | 2     | 3     |
| 9  | 4.92125  | 994   | 3     | 3     |
| 10 | 5.10805  | 993   | 4     | 3     |
| 11 | 5.21266  | 993   | 3     | 4     |
| 12 | 5.40139  | 992   | 4     | 4     |
| 13 | 5.46484  | 991   | 5     | 4     |
| 14 | 5.98918  | 990   | 6     | 4     |
| 15 | 6.05614  | 989   | 7     | 4     |
| 16 | 6.33437  | 988   | 8     | 4     |
| 17 | 6.58878  | 988   | 7     | 5     |
| 18 | 6.60951  | 987   | 8     | 5     |
| 19 | 6.63446  | 986   | 9     | 5     |
| 20 | 6.75001  | 985   | 10    | 5     |
| 21 | 6.80489  | 984   | 11    | 5     |
| 22 | 6.8854   | 984   | 10    | 6     |
| 23 | 6.92483  | 983   | 11    | 6     |
| 24 | 7.01135  | 983   | 10    | 7     |
| 25 | 7.10276  | 983   | 9     | 8     |
| 26 | 7.22309  | 982   | 10    | 8     |
| 27 | 7.71406  | 982   | 9     | 9     |
| 28 | 7.8201   | 981   | 10    | 9     |
| 29 | 8.08454  | 980   | 11    | 9     |
| 30 | 8.08558  | 979   | 12    | 9     |
| 31 | 8.1044   | 979   | 11    | 10    |
| 32 | 8.23118  | 978   | 12    | 10    |
| 33 | 8.30206  | 978   | 11    | 11    |
| 34 | 8.33912  | 978   | 10    | 12    |
| 35 | 8.42502  | 977   | 11    | 12    |
| 36 | 8.49962  | 977   | 10    | 13    |
| 37 | 8.58602  | 976   | 11    | 13    |
| 38 | 8.69091  | 975   | 12    | 13    |
| 39 | 8.70621  | 974   | 13    | 13    |
| 40 | 8.74195  | 974   | 12    | 14    |
| 41 | 8.85186  | 973   | 13    | 14    |
| 42 | 9.0465   | 972   | 14    | 14    |
| 43 | 9.0628   | 971   | 15    | 14    |
| 44 | 9.0656   | 970   | 16    | 14    |
| 45 | 9.1423   | 969   | 17    | 14    |
| 46 | 9.14598  | 968   | 18    | 14    |
| 47 | 9.16416  | 968   | 17    | 15    |
| 48 | 9.19151  | 967   | 18    | 15    |
| 49 | 9.42744  | 967   | 17    | 16    |
| 50 | 9.57617  | 966   | 18    | 16    |
| 51 | 9.6132   | 965   | 19    | 16    |
| 52 | 9.68246  | 964   | 20    | 16    |

```

plot(data[:,1],data[:,2])
plot!(data[:,1],data[:,3])
plot!(data[:,1],data[:,4])

```



```
@benchmark ssa(u0,sir_rates,sir_transitions,p,tf)
```

```

BenchmarkTools.Trial:
  memory estimate:  1.13 KiB
  allocs estimate:  18
  -----
  minimum time:     399.000 ns (0.00% GC)
  median time:      18.000 μs (0.00% GC)
  mean time:        116.258 μs (12.00% GC)
  maximum time:     11.313 ms (97.84% GC)
  -----
  samples:          10000
  evals/sample:     1

```

## 0.1 Appendix

Computer Information:

```

Julia Version 1.4.0
Commit b8e9a9ecc6 (2020-03-21 16:36 UTC)
Platform Info:
  OS: Windows (x86_64-w64-mingw32)

```

```

CPU: Intel(R) Core(TM) i7-8550U CPU @ 1.80GHz
WORD_SIZE: 64
LIBM: libopenlibm
LLVM: libLLVM-8.0.1 (ORCJIT, skylake)
Environment:
  JULIA_EDITOR = "C:\Users\sdwfr\AppData\Local\atom\app-1.45.0\atom.exe" -a
  JULIA_NUM_THREADS = 4

```

## Package Information:

```

Status `~\.julia\environments\v1.4\Project.toml`
[46ada45e-f475-11e8-01d0-f70cc89e6671] Agents 3.0.0
[b19378d9-d87a-599a-927f-45f220a2c452] ArrayFire 1.0.6
[c52e3926-4ff0-5f6e-af25-54175e0327b1] Atom 0.12.10
[6e4b80f9-dd63-53aa-95a3-0cdb28fa8baf] BenchmarkTools 0.5.0
[be33ccc6-a3ff-5ff2-a52e-74243cff1e17] CUDAnative 3.0.4
[3a865a2d-5b23-5a0f-bc46-62713ec82fae] CuArrays 2.0.1
[717857b8-e6f2-59f4-9121-6e50c889abd2] DSP 0.6.6
[2445eb08-9709-466a-b3fc-47e12bd697a2] DataDrivenDiffEq 0.2.0
[a93c6f00-e57d-5684-b7b6-d8193f3e46c0] DataFrames 0.20.2
[aae7a2af-3d4f-5e19-a356-7da93b79d9d0] DiffEqFlux 1.8.1
[41bf760c-e81c-5289-8e54-58b1f1f8abe2] DiffEqSensitivity 6.13.0
[6d1b261a-3be8-11e9-3f2f-0b112a9a8436] DiffEqTutorials 0.1.0
[0c46a032-eb83-5123-abaf-570d42b7fbba] DifferentialEquations 6.13.0
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[523d8e89-b243-5607-941c-87d699ea6713] Gillespie 0.1.0
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[1dea7af3-3e70-54e6-95c3-0bf5283fa5ed] OrdinaryDiffEq 5.34.1
[91a5bcd-d5d7-5caf-9e0b-520d859cae80] Plots 1.0.12
[e6cf234a-135c-5ec9-84dd-332b85af5143] RandomNumbers 1.4.0
[c5292f4c-5179-55e1-98c5-05642aab7184] ResumableFunctions 0.5.1
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[44d3d7a6-8a23-5bf8-98c5-b353f8df5ec9] Weave 0.9.4
[37e2e46d-f89d-539d-b4ee-838fcccc9c8e] LinearAlgebra
[cf7118a7-6976-5b1a-9a39-7adc72f591a4] UUIDs

```