

Ordinary differential equation SIR model

Simon Frost

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The classical ODE version of the SIR model is:

- Deterministic
- Continuous in time
- Continuous in state

$$\frac{dS}{dt} = -\beta \frac{SI}{N} \quad \frac{dI}{dt} = \beta \frac{SI}{N} - \gamma I \quad \frac{dR}{dt} = \gamma I \quad N = S + I + R$$

```
using DifferentialEquations
using SimpleDiffEq
using Plots
using BenchmarkTools
```

The following function provides the derivatives of the model, which it changes in-place. State variables and parameters are unpacked from **u** and **p**; this incurs a slight performance hit, but makes the equations much easier to read.

```
function sir_ode!(du,u,p,t)
    (S,I,R) = u
    (β,γ) = p
    N = S+I+R
    @inbounds begin
        du[1] = -β*S*I/N
        du[2] = β*S*I/N - γ*I
        du[3] = γ*I
    end
    nothing
end;
```

We set the timespan for simulations, **tspan**, initial conditions, **u0**, and parameter values, **p** (which are unpacked above as $[\beta, \gamma]$).

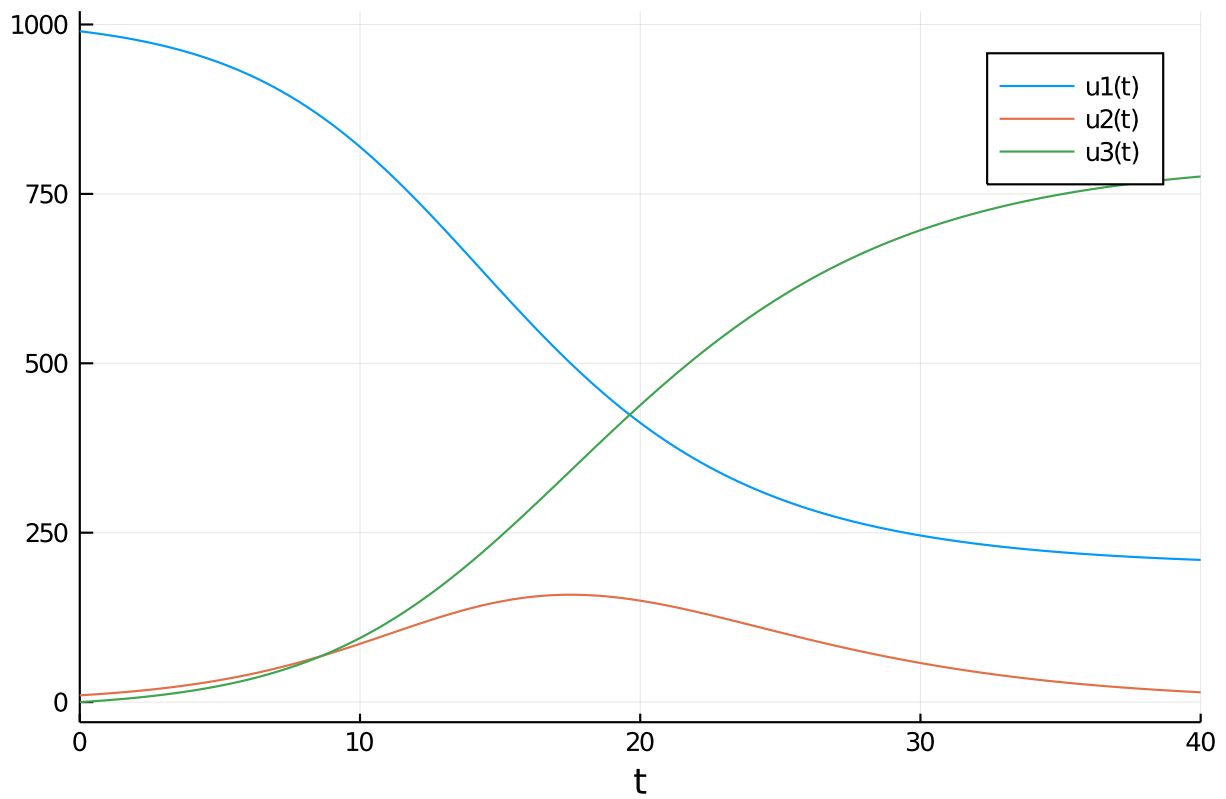
```
tspan = (0.0,40.0)
u0 = [990.0,10.0,0.0]
p = [0.5,0.25];
```

```
prob_sir_ode = ODEProblem(sir_ode!,u0,tspan,p)
```

```
ODEProblem with uType Array{Float64,1} and tType Float64. In-place: true
timespan: (0.0, 40.0)
u0: [990.0, 10.0, 0.0]
```

```
sol_sir_ode = solve(prob_sir_ode);

plot(sol_sir_ode, vars=[(0,1),(0,2),(0,3)])
```



```
@benchmark solve(prob_sir_ode)
```

```
BenchmarkTools.Trial:
 memory estimate: 31.23 KiB
  allocs estimate: 334
  -----
 minimum time:      35.000 μs (0.00% GC)
 median time:      48.100 μs (0.00% GC)
 mean time:        56.945 μs (5.04% GC)
 maximum time:     9.923 ms (99.15% GC)
  -----
 samples:          10000
 evals/sample:     1
```