

4.43

$$\langle a \rangle \quad \min \lambda_{\max}(A(x)) \Rightarrow \min t$$

$$\text{subject to } \lambda_{\min}(A(x)) \leq t$$

$$\Rightarrow \min t$$

$$\text{subject to } \lambda_i(A(x) - tI) \leq 0, \quad i = 0, 1, \dots, n$$

$$\therefore A(x) - tI \text{ is ~~semi~~ negative semidefinite}$$

$$\therefore \min t$$

$$\text{subject to } A(x) - tI \leq 0$$

$$\langle b \rangle \quad \text{let } \lambda_{\min}(A(x)) = r, \text{ from above, we know}$$

$$\min t - r$$

$$\text{Subject to } \begin{aligned} A(x) - tI &\leq 0 \\ A(x) - rI &\geq 0 \end{aligned}$$