Problem 1

1.
$$v = x - (w \cdot x + b)w$$

 $w \cdot v + b = w \left[x - (w \cdot x + b)w \right] + b$
 $= w \cdot x - w \cdot (w \cdot x + b)w + b$
 $= w \cdot x - (||w||_{2}x + w \cdot b)w + b$
 $= w \cdot x - w \cdot x - b + b = 0$

Say: since min $||x-u||_2 = 0$ when u = xi. $v = u - (w \cdot u + b) \cdot w$ Since: $u \in \mathbb{R}^d$. S.t. $w \cdot u + b = 0$

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:. When:
$$u=v=x-(w\cdot x+b)w=-bw=x$$
 $||x-u||_2$ has the minimum

$$||x-u||_{2}^{2} = (x+bw)^{2} = x^{2}+2vxb+b^{2}w^{2}$$

= $x^{2}+2vxb+b^{2}$.

 $|w \cdot x + b|^2 = w^2 x^2 + 2 w x b + b^2$ = $x^2 + 2 w x b + b^2$

Vectors can not simply

You can not simply imp

=> \min $||x-u||_2 = ||wx+b||$ $u \in \mathbb{R}^d$ s.t. wu+b=0

| wxtb| can be shown (in 4) later that is the shortest distance from point x to the hyperlane defined by normal vector w and offset b, 11x-ullz is the Enclidean distance from point x to the point in that are on the hyperplane. Therefore, there is no solution to find point u that satisfies 11 x-ull < | w.x +b1, only exists ||x-n|| z = |w.x+b|, where x-w=tw, where "t" is a scalar that is a magnitude of the distance from & to the hyperplane. When t=0, xzn, and the "=" is hold (proven above); when the , 11x-ull2=1t/, lwx+b|= 1t|,"=" is hold, too,

|wx+b| w·u+b=0

Your conclusion (in this pa

1.5/3

3. v = -bv, when u = v = -bv, $||x - u||_2 = ||x - v||_2$ $||x - v||_2^2 = ||x||^2 - 2 \times v + ||v||^2$ $||x - u||_2^2 = ||x||^2 - 2 \times u + ||u||^2$ $||x - u||_2^2 = ||x||^2 - 2 \times u + ||u||^2$ $||x - u||_2^2 - ||x - v||_2^2 = 2 \times v - 2 \times u + ||u||^2 - ||v||^2 > 0$ $= 2 \times (|v - u|) + ||u||^2 - ||v||^2$

post sufficient conditions to decemministically saying that 11x-1117 11x-111, us v do share your conclusion the same properties and one on the same hyperplane. It only possible 11x-1112>11x-1111 when x is solveted that is closer to the point v that v in terms of Euclidean distance.

4. pick a point x from the hyperplane, its distance d = 10 this hyperplane: $d = 11 \times -11 = \frac{1(x - n) \cdot w}{\|w\|}$ $= \frac{\|w\| = 1}{\|w \cdot x - w \cdot u\|}$ $= \frac{\|w \cdot x - w \cdot u\|}{\|w \cdot x + b\|}$ $= \frac{|w \cdot x + b|}{\|w \cdot x + b\|}$

Problem 2

1.
$$Z = w^T \times$$
 $w' = w + \alpha t \times$
 $w'^T \times = (w + \alpha t \times)^T \times = (w^T + x^T t^T \alpha^T) \times$
 $= w^T \times + \alpha t \| x \|_2^2 = Z' \quad (\alpha = 0)$

if: $t = -1$, Z' will be smaller than Z

if: $t = 1$, Z' will be larger than Z
 \therefore it does not change the prediction

2 and 3:

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from sklearn.datasets import load_breast_cancer import numpy as np

import data

breast_cancer = load_breast_cancer()

X = breast_cancer.data

Y = breast_cancer.target

 $train_X = X[:450]$

 $test_X = X[450:]$

Convert "0" to "-1"

train Y = 2 * Y[:450] - np.ones(len(Y[:450]))

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test_Y = 2 * Y[450:] - np.ones(len(Y[450:]))
# perceptron
epoch = 100
alpha = 0.01
w = np.zeros(np.shape(train_X)[1])
z = np.matmul(train X, w)
for j in range(epoch):
  for i in range(450):
    if z[i] * train_Y[i] <= 0:
      #print z[i]
                                                     Ok!
      w = w + train_X[i] * train_Y[i] * alpha
      #print w
      z[i] = np.dot(train_X[i], w)
      #print z[i]
# normalize the data
for k in range(450):
  if z[k] > 0:
    z[k] = 1
  else:
    z[k] = -1
# calculate training accuracy
p_train = np.shape(np.nonzero(z - train_Y))[1]
precision_train = 1 - float(p_train)/450
print precision_train # 100%
z_prime = np.matmul/test_X,
for n in range(119):
  if z_prime[n] \neq 0:
    z_prime[n] = 1
  else:
    z prime[n] = -1
#calculate testing accuracy/
                                                                results are not correct
p = np.shape(np.nonzero(z_prime - test_Y))[1]
precision = 1 - float(p)/119
print precision # 77.3%
```