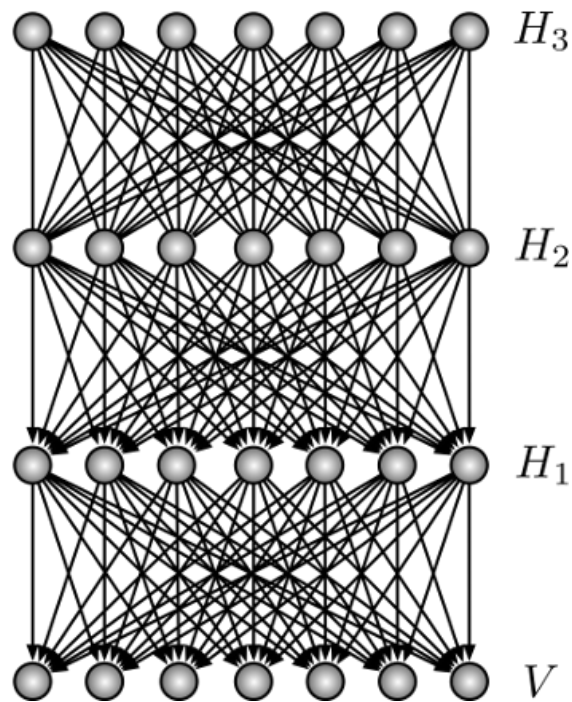


Computer Science 577 Notes

Machine Learning

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January 31, 2015



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1 Decision Tree Learning

Information gain is used to determine the (feature to) split

Information theory: entropy and information gain:

- (i) Entropy = $H(X) = -\sum_{x \in X} P(X = x) \log_2 P(X = x)$
- (ii) Conditional entropy = $H(Y|X) = -\sum_{x \in X} P(X = x) H(Y|X = x)$, where
 $H(Y|X = x) = -\sum_{y \in Y} P(Y = y|X = x) \log_2 P(Y = y|X = x)$
- (iii) Mutual information (information gain) = $I(X, Y) = H(Y) - H(Y|X)$

Alternative metric: Gini coefficient, i.e. product of probabilities for each of (2) outcomes for the feature

Limitation of information gain: biased toward tests with many outcomes (i.e. features with many possible values)

C4.5 uses gain ratio: $SplitInfo(D, S) = -\sum_{k \in S} |D_k|/|D| \log_2 (|D_k|/|D|)$, and $GainRatio = I(D, S)/SplitInfo(D, S)$

Overfitting: $h \in H$ overfits the training data D if there is an alternative model $h' \in H$ such that $error(h) > error(h')$ yet $error_D(h) < error_D(h')$

Avoiding overfitting in decision tree learning:

- (i) Early stopping: stop if further splitting not justified by statistical test
- (ii) Post-pruning: grow large tree, then prune nodes using tuning set
Iteratively eliminate nodes until further reductions reduce accuracy

Lookahead: instead of evaluating using information gain, look ahead to see what splits at the next level would be, and measure information gain at a deeper level

Continuous features: use threshold-based boolean attribute, threshold determined by sorting examples according to the feature and generating candidate thresholds between adjacent examples with different class values

Threshold chosen from candidates based on information gain

Training examples with missing attribute values: possible strategies

- (i) At node n , upon encountering a missing feature value, assign it the value most common among examples at node n , or most common among examples at the node n that also have the same class value
- (ii) Assign fractional value to attribute for the example and pass fractional example to children for purposes of evaluating information gain

2 Instance-Based Learning

k -nearest neighbor classification: given an instance x_q to classify, find k training-set instances that are most similar to x_q

Return the class value: $\hat{y} = \operatorname{argmax}_{v \in \text{values}(Y)} \sum_{i=1}^k \delta(v, y_i)$

Various determinations of distance:

(i) Hamming distance: number of features with differing values

(ii) Euclidean distance: $\delta(x_i, x_j) = \sqrt{\sum_f (x_{if} - x_{jf})^2}$

(iii) Manhattan distance: $\delta(x_i, x_j) = \sum_f (x_{if} - x_{jf})^2$

k -nearest neighbor regression: given an instance x_q , find the k nearest training-set instances and return $\sum_{i=1}^k \delta(v, y_i)$

Distance-weighted nearest neighbor: instances contribute to prediction according to their distance from x_q

k -nearest neighbor does almost nothing at training time, and offsets costs to classification/prediction time
Strategies to speed up k -nearest neighbor

(i) Don't retain every training instance: edited nearest neighbor
Select subset of instances that still provide accurate classifications:

(a) Incremental deletion: delete from memory all training instances redundant to classification

(b) Incremental growth: if training instances insufficient to classify training instance, add to memory

(ii) Use data structure to look up nearest neighbors (k - d tree)

k - d trees (A^* instance search): each node stores one instance, and splits on the median value of the feature having the highest variance

Nodes are pushed to the A^* priority queue with the value indicating the minimum possible distance to the query based on the threshold for the split

Strengths of instance based learning: simple, efficient training, easily adapts to on-line learning, robust to noisy data, etc.

Limitations: sensitive to range of feature values, sensitive to irrelevant and correlated features, inefficient classification, no insight into problem domain (i.e. lacks modeling of problem)

3 Probability and Bayesian Learning

3.1 Probabilistic Machine Learning Concepts

Recall Bayes theorem: $P(A|B) = P(B|A)P(A)/P(B)$

Brute-force MAP learning algorithm:

- (i) Given information D , for each hypothesis $h \in H$, calculate the posterior probability $P(h|D) = P(D|h)P(h)/P(D)$
- (ii) Output hypothesis h_{MAP} with highest posterior probability $h_{MAP} = \operatorname{argmax}_{h \in H} P(h|D)$

Other probabilistic concepts in machine learning:

- (i) Maximum likelihood and least-squared error hypotheses
- (ii) Maximum likelihood hypotheses for predicting probabilities
- (iii) Minimum description length principle
- (iv) Bayes optimal classification: $\operatorname{argmax}_{v_j \in V} \sum_{h_i \in H} P(v_j|h_i)P(h_i|D)$
- (v) Gibb's Algorithm: choose hypothesis $h \in H$ at random, according to posterior probability distribution over H , and use h to predict the classification of the next instance x

3.2 Bayesian networks

A Bayesian network consists of a directed acyclic graph and a set of conditional probability distributions. In the each Directed Acyclic Graph (DAG):

- (i) Each node denotes a random variable
- (ii) An edge from X to Y represents that X directly influences Y
- (iii) Each node X contains a conditional probability distribution representing $P(X|Parents(X))$
- (iv) Each variable X is independent of its non-descendants given its parents
- (v) Each variable X is independent of all others given its Markov blanket

Advantages of Bayesian network representation:

- (i) Captures independence and conditional independence where they exist
- (ii) Encodes the relevant portion of the full joint distribution
- (iii) Graphical representation gives insight into complexity of inference

Inference task: given values for some variables in the network (evidence) and set of query variables, compute posterior distribution over query variables

Hidden variables: neither evidence nor the query variables

Bayesian networks allow for any set to be evidence and any set to be query

Inference by enumeration: consider the chain rule $P(x_1, \dots, x_n) = P(x_1)P(x_2|x_1)P(x_3|x_2, x_1) \dots P(x_n|x_{n-1}, \dots, x_1)$

Posterior probability on query variables can be found via independence, chain rule, and marginalization

Parameter learning task: given set of training instances and graph structure, infer parameters of conditional probability distributions

Structure learning task: given set of training instances, infer graph structure (and possibly parameters of

CPDs)

For parameter learning, use maximum a posteriori (MAP) estimation: e.g. m-estimates $P(X = x) = (n_x + p_x m) / (\sum_{v \in \text{values}(X)} n_v + m)$, where p_x is prior probability of value x , m is number of virtual instances, and n_v is number of occurrences of value v

3.3 Expectation Maximization

Missing data (hidden variables, values missing at random): values can be imputed using Expectation Maximization (EM)

Iterate until convergence:

- (i) Expectation step: using current model, compute expectation over missing values (missing temporarily take expected values)
- (ii) Maximization step: update model parameters with those that maximize probability of data (MLE or MAP)

Note that k -means unsupervised clustering is a form of expectation maximization

Expectation maximization can be hard (takes most likely value) or soft (expectation is probability distribution)

Expectation maximization for parameter learning:

- (i) Expectation step: compute probability of each completion of incomplete data points, i.e. answering query over missing variables given others
- (ii) Maximization step: use completed data set to update Dirichlet distributions, except counts can be fractional, update conditional probability tables

Subtlety for parameter learning: overcounting based on number of iterations required to converge to settings for missing values. After each expectation step, reset Dirichlet distributions before repeating maximization step

Problems with expectation maximization: only finds local optimum, deterministic with respect to priors

3.4 Learning Network Structure

Chow-Liu algorithm: learns tree structure that maximizes likelihood of training data

- (i) Compute weight $I(X_i, X_j)$ of each possible edge (X_i, X_j)
- (ii) Find maximum-weight spanning tree: use mutual information to calculate $I(X, Y) = \sum_{x \in \text{values}_X} \sum_{y \in \text{values}_Y} P(x, y) \log_2 P(x, y) / (P(X)P(Y))$
- (iii) Assign edge directions in maximum-weight spanning tree

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