

# A simulator for repeated games

Manual

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#### 1 Introduction

This program is designed for scientific research in the field of game theory.

### 2 Getting started

When the program is first started, the home window will show as in Fig. 1. Since no simulations have been executed yet, it is mostly empty.

The home window is roughly divided into three areas. In the top area, a short summary of the currently active configuration is displayed (1) in Fig.1). If the user hasn't created a configuration of his own yet, a predefined one will be active. On the right-hand side of the summary reside two buttons (2) and (3)). The one labeled with a cog symbol opens up the configuration window, in which the currently active configuration can be modified (see 2.1). Pressing the Play-button will start a simulation with the currently active configuration. The left-hand side area (4) in Fig.1) will contain a list of all running, finished and cancelled simulations. If a finished simulation is selected, detailed information about its results will be displayed in area (5) (This area will from now on be referred as the "output view").

## 2.1 Edit the configuration

To edit the active configuration, press the cog-labeled button in the home window. This will open up the configuration window (see Fig.2). On the left-hand side, all configurable parameters of a simulation can be modified. If the selected pairing algorithm, success quantification, strategy adaption mechanism or equilibrium criterion has configurable parameters, they can be entered below the corresponding dropdown menu (see 1) in Fig.2). On the right-hand side, a short description and a table containing the payoffs of the selected game are displayed (see 2) in Fig.2). Below (3) in Fig.2), a multiconfiguration can be activated, see section 4.1.

The  $\bigcirc$  - button will reset all settings to the default configuration. Pressing the  $\checkmark$  -button will close the configuration window and apply the made changes to the active configuration.

It is possible to export the configuration to an external file by navigating to "File  $\rightarrow$  Save configuration" in the menu bar of the home window. Such a configuration file can be

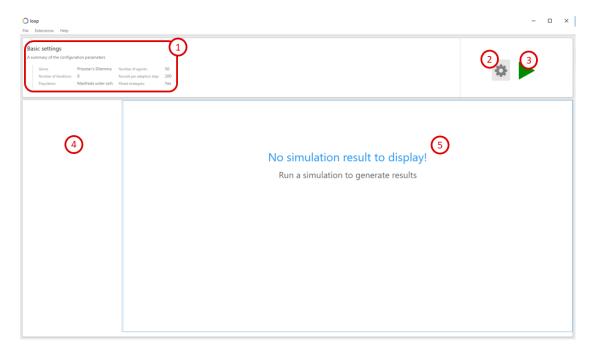


Figure 1: The home window after the first start of the program.

loaded and set as the active configuration via "File  $\rightarrow$  Load configuration". For important information on saving and exporting files see section 3.5.

#### 2.2 Start a simulation

Pressing the Play-button in the home window will start a simulation with the currently active configuration. It will then appear in the list in the left-hand side area of the home window. The list entry displays an estimate of the time left until the simulation finishes as well as how many iterations have already been executed. If the running simulation is selected, the output view will contain the same information as the list entry as well as a button labeled with an X. If pressed, the simulation is cancelled.

#### 2.3 View the simulation results

As soon as a simulation is finished, its list entry turns green and displays time and date of the moment it finsihed as well as the duration of its execution:

If selected, the output view will display detailed information about the simulations results. The output is divided into two subpages: the "Detailed output" and the "Abstracted output".

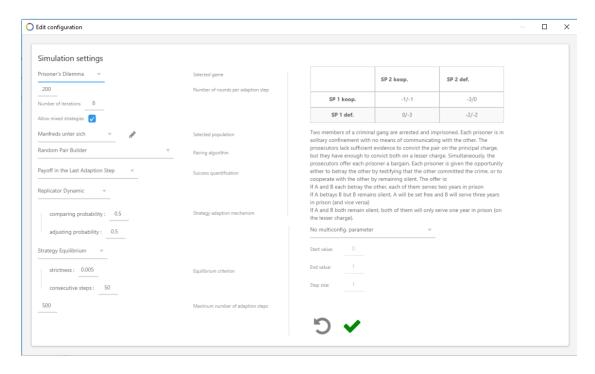


Figure 2: The configuration window.

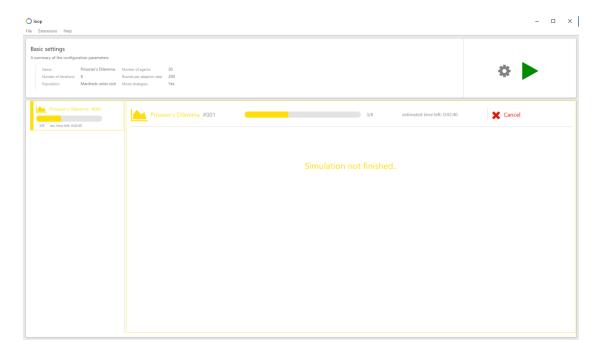


Figure 3: The home window with a running simulation selected.





Figure 4: The detailed output.

To switch between the two, the 
and 
buttons at the bottom of the output view can be used.

#### 2.3.1 Detailed Output

In the detailed output (see Fig.4), information about strategy and capital distribution of the agents are displayed for any selected iteration. To select an iteration, use the correspondingly labeled slider at the top of the output view  $\bigcirc$ 1). The iterations are sorted by their final efficiency, i.e. in the case of Fig.4, iteration 1/8 is the least, iteration 8/8 the most efficient among the eight executed iterations.

**Strategy distribution:** The line chart labeled "Strategy distribution" (2) displays the evolution of the mixture of strategies used by the agents over the time of the simulation. It contains one line for every used (pure) strategy. Each line indicates the relative frequency of the corresponding strategy being used by agents in every single adaption step. For example, consider the strategy distribution displayed in Fig. 5. It tells us that in the beginning of the simulation, all strategies appeared with a similar frequency of 21% to 29%. Towards the end, "grim" prevailed with a frequency of about 70%, while "never cooperate" and "tit

for tat" dropped below 20% and "always cooperate" basically vanished.

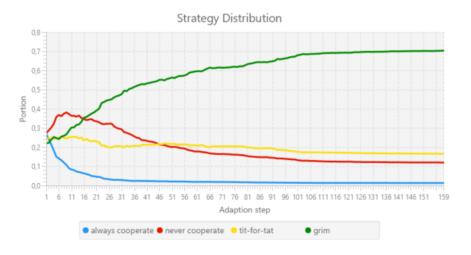


Figure 5: An exemplary strategy distribution.

**Capital distribution:** The bar chart labeled "Capital distribution" (3) displays a histogramm of the final total capitals of all agents at the end of the simulation. The width of the bins of the histogram are chosen in a way such that there is always about 15 bins. Each bin is then labeled with the mean of the interval covered by it. Note that final capitals might be negative (as in Fig.6) if the payoffs of the used game are negative (such as in the prisoner's dilemma).

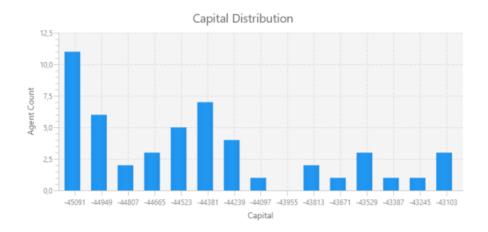


Figure 6: An exemplary capital distribution.



Figure 7: The abstracted output.

#### 2.3.2 Abstracted Output

The abstracted output (see Fig.7) contains information abstracted from all executed iterations. At the top ① the "equilibrium frequency", i.e. the portion of all iterations in which an equilibrium was reached is displayed. Below reside two histograms, the "Efficiency distribution" and the "Distribution of executed adaption steps".

**Efficiency distribution**: The efficiency distribution (2) is a histogram of the final efficiencies of all executed iterations. Consider Fig.8. In the corresponding simulation, five iterations finished with an efficiency of around 0.9 and the other three with efficiencies 0.67, 0.42 and 0.04 respectively. Again, bin width is chosen such that there is around 15 bins in total and the labels display the mean of the interval covered by the bins. Below the strategy distribution, the mean efficiency of all iterations is displayed, in this case 0.722 (see Fig.7).

**Distribution of executed adaption steps**: This chart 3 is a histogram of the amount of executed adaption steps of all iterations. Consider Fig.9. In the corresponding simulation, all but one iteration finished after 120 to 134 adaption steps, just one took around 160. Below the distribution, the mean amount of executed adaption steps is displayed, in this case 131 (see Fig.7).

Below the charts resides a dropdown menu labeled "Considered iterations" (4). It can be used to determine whether all iterations or just the ones where an equilibrium (or no

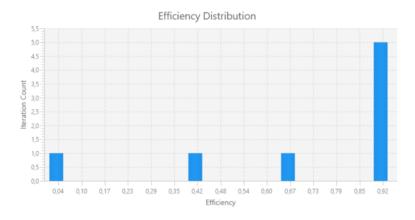


Figure 8: An exemplary efficiency distribution.

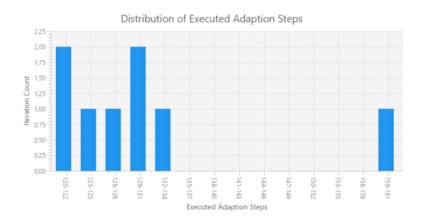


Figure 9: An exemplary distribution of executed adaption steps.

equilibrium) was reached shall be considered in the histograms above.

#### 2.4 Save the result

If you whish to save the result of a simulation so you can take a look at it again later, you may do so by clicking the button (Fig.4 4). This will open a file dialog where you can choose a place to save your result. To load a result that has been exported in this way, press "File" and then "Load simulation result" in the menu of the home window.

You can also set the configuration that was used for a selected simulation as the active configuration by pressing the  $\mathbb{C}$  button (Fig.4 (5)).

#### 3 Extensions

To further customise configurations, the user can create own strategies, games, groups and populations and use them in simulations.

#### 3.1 Create new strategies

The strategy creation lets you build strategies of the form

If 
$$X$$
 then  $A$ , otherwise  $B$ , (1)

where A and B are already existing strategies and X is a configurable expression, such as "The opponent is in the same group as me" or "The opponent cooperated in his last game against me".

The strategy creation window can be opened by clicking the "Create new strategy" entry in the "Extensions" menu in the home window:



It is divided into three vertically aligned sections. The topmost section (1) contains two text fields in which name and description of the new strategy must be entered.

Section (2) contains a set of predicates and operators, where most of the predicates can be configured using dropdown menus. They can be used to compound the expression X in (3.1). Clicking the  $\longrightarrow$  button adds the corresponding operator or predicate to the expression, which will be displayed in section (3).

When you add an operator to the expression, an empty box will be generated for every required operand (see Fig.11). To insert a predicate or operator as one of the operands, select the correspondig box (as in 4) and then add the desired predicate by clicking the button.

To remove a predicate or an operator from the expression, click the button next to it. A removed predicate will be replaced by an empty box. When you remove an operator, its operands will be removed as well.

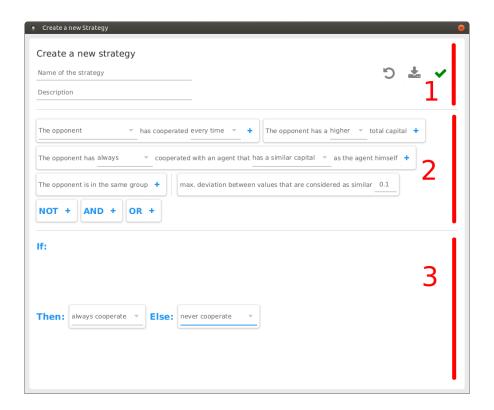


Figure 10: The strategy creation window.



Figure 11: The generated expression.

Below the displayed expression reside two drop down menus 5 and 6, in which the strategies A and B from (3.1) can be selected.

To reset all settings, press the 5 button in section 1.

To export the created strategy as a file, press the \_\_\_\_ button. To add the strategy to the local repository and close the window, press 
(Further details and important information on exporting and saving see section 3.5).

#### 3.2 Create new games

When the "Create new game" entry in the "Extensions" menu is pressed, the game creation window opens (see Fig.12). Here, a new game can be created. To do so, a name, a description and the players payoffs must be entered in the corresponding text fields. For example, an entry of the form "1/2" in the botom left part of the payoff table means: "If player 1 doensn't but player 2 does cooperate, player 1 will receive the payoff 1 and player 2 will receive the payoff 2".

To reset all settings, press the D button.

To export the created game as a file, press the \_\_\_\_ button. To add the game to the local repository and close the window, press 
(Further details and important information on exporting and saving see section 3.5).

To load an existing game press the \_\_\_ button. The following dropdown menu will pop up:

You can either import a game from a previously exported game file or open one of the locally stored games, i.e. the preconfigured games and the ones added to the repository

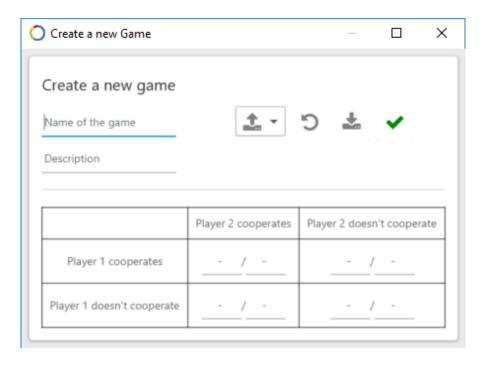
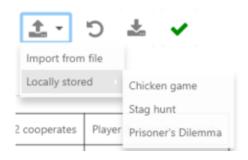


Figure 12: The game creation window.



by the user.

#### 3.3 Create new groups

When the "Create new group" entry in the "Extensions" menu is pressed, the group creation window opens (see Fig.13). To create a new group, name and description must be entered in the corresponding text fields and at least one segment must be configured. Segments can be added by pressing the "Add segment" button and removed by pressing the "X" button at the head of the corresponding tab.

For each segment, a capital distribution must be chosen and parametrised; it will be used

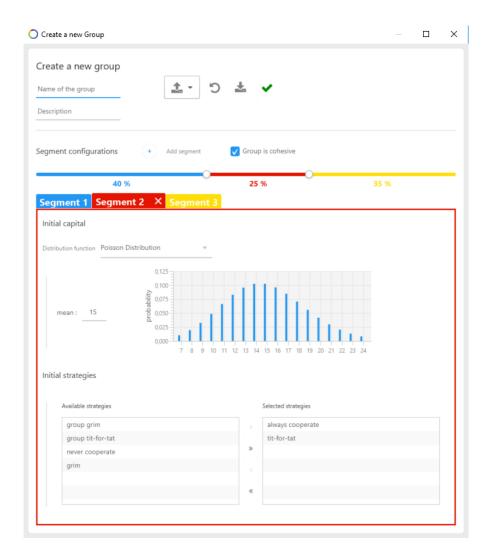


Figure 13: The group creation window.

to initialise agents of that segment with capital at the beginning of simulations. Secondly, a set of strategies must be selected out of all locally stored strategies. Those include the preconfigured ones as well as strategies created by the user (if existent).

The multislider can be used to configure the relative sizes of the segments. For example, if 100 agents of the group in Fig.13 were to be initialised, 25 of them would belong to segment 2, thus receiving an initial capital drawn out of a poisson distribution with mean 15 as well as "always cooperate" or "tit for tat" as initial strategy.

By deselecting the checkbox labeled "Group is cohesive", the group becomes "uncohesive", i.e. agents of this group do not consider each other as members of the same group anymore. This becomes relevant when strategies are used that refer to other agents' group affiliation. This can be used to model agents that "aren't part of any group", which is equivalent to being part of an uncohesive group.

To reset all settings, press the 🕽 button.

To export the created group as a file, press the \_\_\_\_ button. To add the group to the local repository and close the window, press 
(Further details and important information on exporting and saving see section 3.5).

To load an existing group press the \_\_\_\_ button. You can either import a group from a previously exported group file or open one of the locally stored groups, i.e. the preconfigured groups and the ones added to the repository by the user.

#### 3.4 Create new populations

When the "Create new population" entry in the "Extensions" menu is pressed, the population creation window opens (see Fig.14). To create a new population, name and description must be entered in the corresponding text fields and at least one group must be added.

In order to add a group, choose the group in the dropdownmenu 1 and enter the amount of agents of that group that shall be added in the textfield 2. Then press the button. To remove a group, press the corresponding  $\times$  button.

To reset all settings, press the button.

To export the created population as a file, press the  $\frac{1}{2}$  button. To add the population

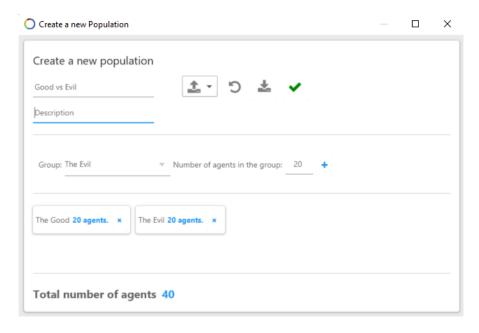


Figure 14: The population creation window.

to the local repository and close the window, press  $\checkmark$  (Further details and important information on exporting and saving see section 3.5).

To load an existing population press the \_\_\_ button. You can either import a population from a previously exported population file or open one of the locally stored populations, i.e. the preconfigured populations and the ones added to the repository by the user.

#### 3.5 Important Information on Saving and Exporting Extensions

There is an important difference between saving an extension (adding it to the local repository by pressing  $\checkmark$ ) and exporting it as a file (by pressing  $\checkmark$ ). If it is just saved, it will only be available until the program is closed, i.e. it is not stored persistently. If an extension shall be available persistently, it must be exported as a file and saved *inside the preconfigured folder*, which is C:/Users/<Username>/loop/personallib/X, where  $X \in \{\text{strategies}, \text{groups}, \text{populations}, \text{games}\}$ . All extensions that reside in those folders will be automatically loaded at program start.

There is another important note to make regarding the export of extensions. If an extension makes use of another extension (a population containing a group, a group containing certain strategies), then it will only store that extensions name. This means that when, for example, a previously exported population is loaded and it contains a group of name X,

the local repository will be searched for a group of name X, and if none is found, the import will fail and an error message will be displayed. This also applies to configurations, i.e. an exported configuration only stores the *names* of the used game, population, etc. This has mutliple consequences:

- Whenever you export an extension (or configuration) in order to store it persistently, make sure you also persistently store all referenced extensions (groups, strategies,...).
- When you export a configuration or an extension in order to send it to a colleague who also uses this program, make sure you send him all the referenced extensions as well.
- Since, for example, a population only stores the name of its contained groups, it can
  be modified by overwriting those groups. If a certain population contains a group
  with name X, and you were to delete that group and create a new one with the
  same name X, then the population would now contain that new group. This works
  in the same way for configurations with contained populations and games, and for
  groups with contained strategies.

#### 4 Advanced

#### 4.1 Multiconfigurations

A multiconfiguration can be regarded as a set of (normal) configurations (the "elementary configurations"), where all parameters but one (the "multiconfiguration parameter", short: multi-parameter) are fix and the multi-parameter varies through a certain set of values. For example, one could specify a multiconfiguration in which all parameters are as in the preconfigured configuration but the round count (the amount of rounds per adaption steps) varies from 100 to 200 in steps of 10 (see Fig.??).

To create a multiconfiguration, open the configuration window and choose the desired multi-parameter in the dropdown menu at the bottom right. Possible multi-parameters are:

- round count
- maximum number of adaption steps
- configurable numerical parameters in the success quantification, the pair building algorithm, the strategy adaption mechanism and the equilibrium criterion

- the size of a group in the selected population
- the size of the segments in one of the groups of the selected population<sup>1</sup>

Below the dropdown menu, start value, end value and step size of the multi-parameter can be entered.

The output changes slightly for multiconfigurations. In the two already known output pages "Detailed output" and "abstracted output", a new slider labeled "Configuration" is added, with which the considered configuration may be selected. Next to the slider, the name of the mutli-parameter and its value in the currently selected configuration are displayed. On top of that, a third output page is available, the "Multiconfiguration output" (see ?). It contains two line graphs:

**Efficiency and equilibrium frequency:** The first chart plots equilibrium frequency<sup>2</sup> and mean final efficiency against the value of the multi-parameter.

**Mean amount of executed adaption steps:** The second chart plots the mean amount of executed adaption steps against the value of the multi-parameter.

Below the charts resides a dropdown menu labeled "Considered iterations" (4). It can be used to determine whether all iterations or just the ones where an equilibrium (or no equilibrium) was reached shall be considered in the plots above.

#### 4.2 The Plugin-System

<sup>&</sup>lt;sup>1</sup>Works only for groups that consist of exactly two segments. If  $X \in [0, 1]$  is the value of the mult-parameter, then the first segment has relative size X and the second segment has relative size 1 - X.

<sup>&</sup>lt;sup>2</sup>The portion of iterations in which an equilibrium was reached