

Find the General Solution

$$y'' - 4y = 0$$

$$p(x)y'' + Q(x)y' + R(x)y = G(x)$$

$$y'' + 0y' + 4y = 0$$

$$ar^2 + br + c = 0$$

$$1r^2 + 0r - 4 = 0$$

$$r^2 - 4 = 0$$

$$+4 \quad +4$$

$$\sqrt{r^2 - 4}$$

$$r_1 = 2$$

$$r_2 = -2$$

$$r = \pm 2$$

$$\begin{aligned} ay'' + by' + cy &= 0 & y &= e^{rx} \\ & & y' &= re^{rx} \\ & & y'' &= r^2 e^{rx} \end{aligned}$$

$$\begin{aligned} &\Downarrow \\ ar^2 e^{rx} + br e^{rx} + ce^{rx} &= 0 \\ &\Downarrow \\ e^{rx} [ar^2 + br + c] &= 0 \\ &\Downarrow \\ ar^2 + br + c &= 0 \end{aligned}$$

$$y = C_1 e^{r_1 x} + C_2 e^{r_2 x}$$

$$y = C_1 e^{2x} + C_2 e^{-2x}$$

General solution

discriminant is greater than zero, 2 real solutions occur