

ETF3231/5231: Business forecasting

Week 4: The forecasters' toolbox

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- 1 A tidy forecasting workflow
- 2 Some simple forecasting methods
- 3 Residual diagnostics
- 4 Distributional forecasts and prediction intervals
- 5 Forecasting with transformations
- 6 Forecasting and decomposition

Time coving average validation

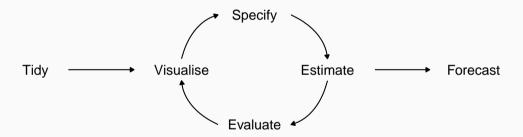
7 Evaluating forecast accuracy

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A tidy forecasting workflow



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Some simple forecasting methods - Benchmarks

- MEAN(y): Average method
- NAIVE(y): Naïve method
- SNAIVE(y ~ lag(m)): Seasonal naïve method
- RW(y ~ drift()): Drift method

Note: distinguish between a method and a model

Model fitting

- The model() function trains models to data.
- The forecast() function generates forecasts.

SNAIVE(y ~ lag(m)): Seasonal naïve method

- Forecasts equal to last value from same season.
- Forecasts: $\hat{y}_{T+h|T} = y_{T+h-m(k+1)}$, where m = seasonal period and k is the integer part of (h-1)/m.

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Forecasting residuals

Residuals in forecasting: difference between observed value and its

fitted value: $e_t = y_t - \hat{y}_{t|t-1}$.

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Assumptions

- $\{e_t\}$ uncorrelated. If they aren't, then information left in residuals that should be used in computing forecasts.
- $\{e_t\}$ have mean zero. If they don't, then forecasts are biased.

Useful properties (for distributions & prediction intervals)

- ${\bf e}_t$ have constant variance.
- $\{e_t\}$ are normally distributed.

ACF of residuals

- We assume that the residuals are white noise (uncorrelated, mean zero, constant variance). If they aren't, then there is information left in the residuals that should be used in computing forecasts.
- So a standard residual diagnostic is to check the ACF of the residuals of a forecasting method.
- We expect these to look like white noise.

Portmanteau tests

Consider a whole set of r_k values, and develop a test to see whether the set is significantly different from a zero set.

Ljung-Box test

$$Q^* = T(T+2) \sum_{k=1}^{\ell} (T-k)^{-1} r_k^2$$

where ℓ is max lag being considered and T is number of observations.

- My preferences: ℓ = 10 for non-seasonal data, ℓ = 2m for seasonal data.
- Better performance, especially in small samples.

Portmanteau tests

- If data are WN, Q^* has χ^2 distribution with (ℓK) degrees of freedom where K = no. parameters in model.
- When applied to raw data, set K = 0.
- lag = ℓ , dof = K

```
augment(fit) %>%
features(.resid, ljung_box, lag=10, dof=0)
```

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Forecast distributions

Assuming residuals: have zero mean, are uncorrelated, normal, with variance = $\hat{\sigma}^2$:

Mean: $y_{T+h|T} \sim N(\bar{y}, (1+1/T)\hat{\sigma}^2)$

Naïve: $y_{T+h|T} \sim N(y_T, h\hat{\sigma}^2)$

Seasonal naïve: $y_{T+h|T} \sim N(y_{T+h-m(k+1)}, (k+1)\hat{\sigma}^2)$

Drift: $y_{T+h|T} \sim N(y_T + \frac{h}{T-1}(y_T - y_1), h^{\frac{T+h}{T}}\hat{\sigma}^2)$

where k is the integer part of (h-1)/m.

Note that when h = 1 and T is large, these all give the same approximate forecast variance: $\hat{\sigma}^2$.

Prediction intervals

Assuming forecast errors are normally distributed, then a 95% PI is

$$\hat{\mathbf{y}}_{\mathsf{T}+h|\mathsf{T}} \pm 1.96\hat{\sigma}_{\mathsf{h}}$$

where $\hat{\sigma}_h$ is the st dev of the *h*-step distribution.

- When h = 1, $\hat{\sigma}_h$ can be estimated from the residuals.
- Point forecasts often useless without a measure of uncertainty (such as prediction intervals).
- Prediction intervals require a stochastic model (with random errors, etc).
 - Usually too narrow due to unaccounted uncertainty.

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Decomposition models

decomposition_model() creates a decomposition model

- You must provide a method for forecasting the season_adjust series.
- A seasonal naive method is used by default for the seasonal components.
- The variances from both the seasonally adjusted and seasonal forecasts are combined.

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Creating the rolling training sets

There are three main rolling types which can be used.

- Stretch: extends a growing length window with new data.
- Slide: shifts a fixed length window through the data.
- Tile: moves a fixed length window without overlap.

Three functions to roll a tsibble: stretch_tsibble(), slide_tsibble(), and tile_tsibble().

For time series cross-validation, stretching windows are most commonly used.