


**[Re] A circuit model of auditory cortex**Parvathy Neelakandan<sup>1</sup> and Christoph Metzner<sup>1,2, </sup><sup>1</sup>Neural Information Processing Group, Institute of Software Engineering and Theoretical Computer Science, Technische Universität Berlin, Berlin, Germany – <sup>2</sup>Biocomputation Group, Centre for Computer Science and Informatics Research, University of Hertfordshire, Hatfield, United KingdomEdited by  
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–**Introduction**

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**Methods**

In this replication, we focus on the rate models proposed in the original article. The firing rate model was an extensions of the traditional Wilson-Cowan model<sup>1</sup> and represented an iso-frequency unit of the auditory cortex. This iso-frequency unit consisted of one excitatory and two inhibitory populations. Building on this unit a more complex three-unit rate models was developed, to investigate stimulus-specific adaptation, forward suppression, tunig-curve adaptation and feedforward functional connectivity.

**Iso-Frequency Unit Model** The iso-frequency unit model was based on the Wilson-Cowan model<sup>1</sup> but was modified to include two different types of inihbitory interneurons. The two inhibitory population are meant to represent parvalbumin-psoitve (PV) and somatostatin (SST) cells. The single unit model is given by

$$\tau_u \frac{du(t)}{dt} = -u(t) + f(w_{ee}u(t) - w_{ep}p(t) - w_{es}s(t) + qg(t)i(t)), \quad (1)$$

$$\tau_p \frac{dp(t)}{dt} = -p(t) + f(w_{pe}u(t) - w_{pp}p(t) - w_{ps}s(t) + I_{Opt,PV}(t) + qg(t)i(t)), \quad (2)$$

$$\tau_s \frac{ds(t)}{dt} = -s(t) + f(w_{se}u(t) - w_{sp}p(t) - w_{ss}s(t) + I_{Opt,SST}(t)), \quad (3)$$

with  $u(t)$ ,  $p(t)$ , and  $s(t)$  being the normalized firing rates (in  $[0, 1]$ ) of the pyramidal cell population, the PV population and the SST population, respectively. Furthermore,  $w_{xy}$  represents the strengths of connections from population  $y$  to population  $x$ . The two terms  $I_{Opt,PV}$  and  $I_{Opt,SST}$  describe the input current to cells due to optogenetic stimulation of the PV population and SST population, respectively.  $\tau_i$ ,  $i \in u, p, s$  defines the time constants for the respective populaitons. The function  $f$  is realised as a threshold linear function given by

$$f(x) = \begin{cases} 0 & \text{if } x \leq 0 \\ rx & \text{if } 0 < x \leq 1/r \\ 1 & \text{if } x > 1/r, \end{cases}$$

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The authors have declared that no competing interests exists.  
Code is available at <https://github.com/ChristophMetzner/Park-Geffen-Replication>.

**Table 1.** Overview of the model parameters

a	b	c
1	2	3

(4)

which coarsely approximates a sigmoid function. Furthermore, the function  $f$  is thresholded by simply subtracting a constant  $u_i$  from the input  $x$  (i.e.  $f(x - u_i)$ ) which varied for the different populations. Lastly, afferent auditory input is fed into the unit is given by  $qg(t)i(t)$ , which is subdivided into the 'raw' input  $i(t)$  and a slow modulation  $g(t)$  mimicking synaptic depression at thalamic synapses. The input function  $i(t)$  is simply an instantaneous rise with amplitude  $q$  and an exponential decay with a time constant of  $\tau_q$ . The synaptic depression  $g(t)$  is governed by the following equation

$$\frac{dg(t)}{dt} = \frac{g_0 - g(t)}{\tau_{d_1}} - \frac{g(t)i(t)}{\tau_{d_2}}. \quad (5)$$

The parameter values can be found in Table 1

**ToDo: Add parameter values to the table.**

**Three-Unit Model** Building on the single unit a three-unit model was implemented, with each single unit representing a different input frequency, thus creating a simple tonotopic layout that allowed to explore more complex auditory inputs. Intra-unit connectivity was as described before for the single-unit model. Inter-unit connectivity was restricted to immediate neighbours and included the following connection types: Exc to exc, exc to PV and SST to exc. Together, the activity of the three populations of each unit was governed by

$$\tau_u \frac{du_i(t)}{dt} = -u_i(t) + f(w_{ee}u_i(t) - (w_{ep} - a(1 - D_i(t)))p_i(t) - w_{es}s_i(t) + J_{1,i}(t)), \quad (6)$$

$$\tau_p \frac{dp_i(t)}{dt} = -p_i(t) + f(w_{pe}u_i(t) - w_{pp}p_i(t) - w_{ps}s_i(t) + I_{Opt,PV}(t) + J_{2,i}(t)), \quad (7)$$

$$\tau_s \frac{ds_i(t)}{dt} = -s_i(t) + f(w_{se}u_i(t) - w_{sp}p_i(t) - w_{ss}s_i(t) + I_{Opt,SST}(t) + J_{3,i}(t)), \quad (8)$$

with

$$J_{1,i}(t) = \begin{cases} -F_i(t)s_2(t) + qI_i(t) + w_{ee}^*u_2(t) & \text{if } i = 1, 3 \\ -F_s(t)(s_1(t) + s_3(t)) + qI_2(t) + \frac{w_{ee}^*(u_1(t) + u_3(t))}{2} & \text{if } i = 2 \end{cases} \quad (9)$$

and

$$J_{2,i}(t) = \begin{cases} qI_i(t) + w_{pe}^*u_2(t) & \text{if } i = 1, 3 \\ qI_2(t) + \frac{w_{pe}^*(u_1(t) + u_3(t))}{2} & \text{if } i = 2 \end{cases} \quad (10)$$

and

$$J_{3,i}(t) = \begin{cases} qI_i(t) + w_{se}^*u_2(t) & \text{if } i = 1, 3 \\ qI_2(t) + \frac{w_{se}^*(u_1(t) + u_3(t))}{2} & \text{if } i = 2. \end{cases} \quad (11)$$

Here,  $I_i(t)$  is described by

$$I_k(t) = g_k(t)i_k(t) + g_2(t)i_2(t)\alpha \quad \text{for } k = 1, 3 \quad (12)$$

and

$$I_2(t) = (g_1(t)i_1(t) + g_3(t)i_3(t))\alpha + g_2(t)i_2(t). \quad (13)$$

Here,  $i_k(t)$  represents thalamic inputs to each of the three units. Taken together, the description of the three-unit model is the same than for the single-unit model, except for the addition of lateral inter-unit connectivity and short-term synaptic dynamics. Short-term facilitation is modelled by  $F_i(t)$  and increases from 0 to positive values whereas depression is modelled by  $D_i(t)$ , which decreases from 1 towards 0. Facilitating synapses were added to Exc to SST inputs and depressing terms to PV to Exc synapses (see<sup>2</sup>). The facilitating term  $F_j(t)$  obeys

$$\frac{dF_j(t)}{dt} = -\frac{F_j(t)}{\tau_{D_1}} + \frac{i_j(t)}{\tau_{D_2}}, \quad (14)$$

where  $\tau_{D_1}$  and  $\tau_{D_2}$  are again the depression time constants from the input functions of the single-unit model given in Equation 5. Analogously, the depression term  $D_j(t)$  follows

$$\frac{dD_j(t)}{dt} = \frac{1 - D_j(t)}{\tau_{D_1}} - \frac{D_j(t)i_j(t)}{\tau_{D_2}}. \quad (15)$$

The choices for the parameters can again be found in Table 1 and were based on experimental studies<sup>3,4,5</sup>.

Park and Geffen note that, when matching model behaviour to experimental findings, two distinct parameter sets emerged and a unified rate model description required a paradigm-dependent baseline inhibition, which reflected high thalamic activity (corresponding to weak baseline inhibition) versus low thalamic activity (corresponding to strong baseline inhibition). This was implemented using another variable  $\bar{F}$  governed by

$$\frac{d\bar{F}(t)}{dt} = \frac{\bar{F}^2(t)}{\tau_{F_1}} - \frac{\bar{I}(t)}{\tau_{F_2}}. \quad (16)$$

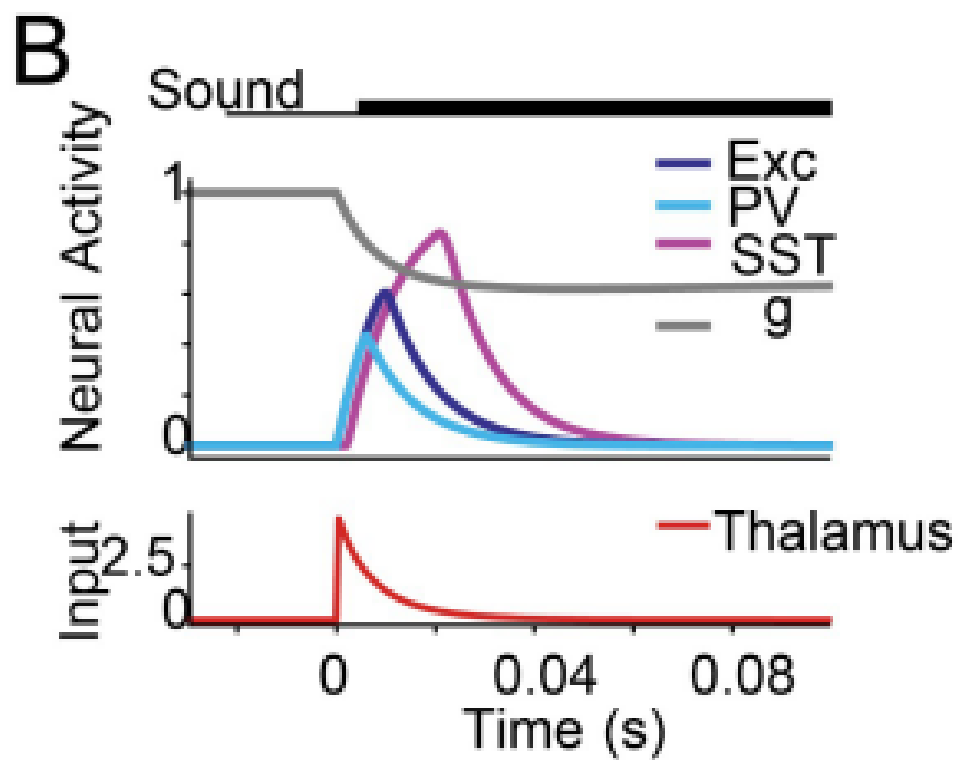
**ToDo:** Add paragraph on the variable  $F$

## Reimplementation

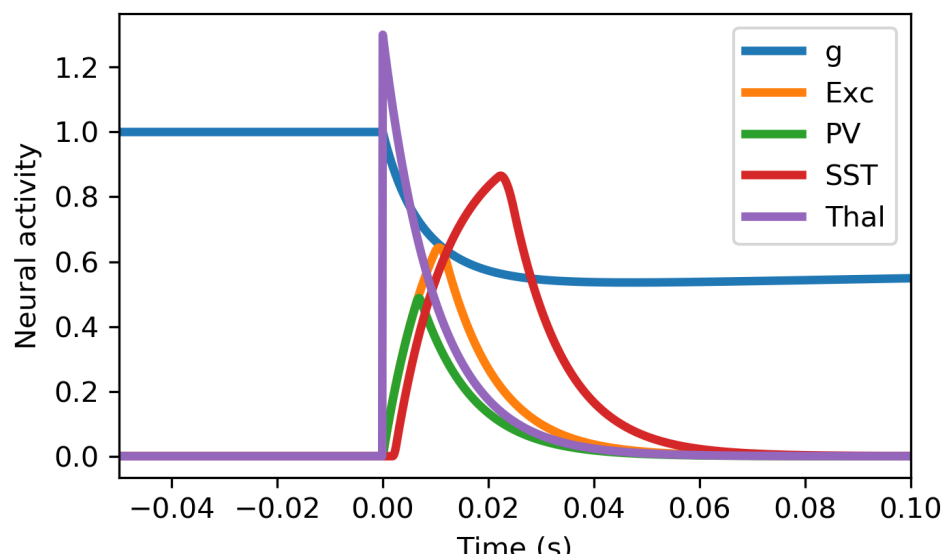
The iso-frequency unit model and the three-unit model were both implemented in Python and integrated into the neurolib framework<sup>6</sup>.

## Reproduction of experiments

**ToDo:** Describe results



(a) original



(b) replication

Figure 1. Replicates Figure 1B.

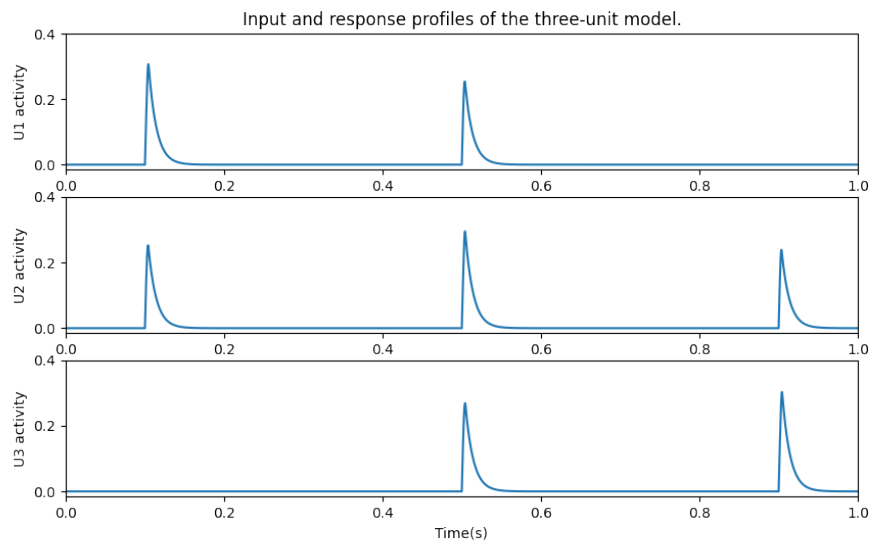


Figure 2. ReFig2

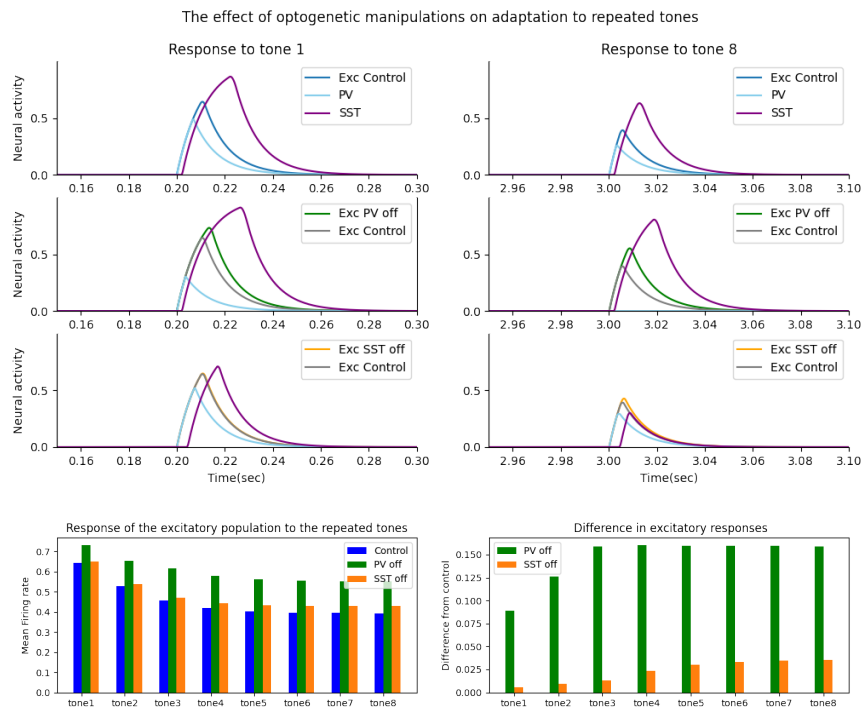


Figure 3. ReFig3

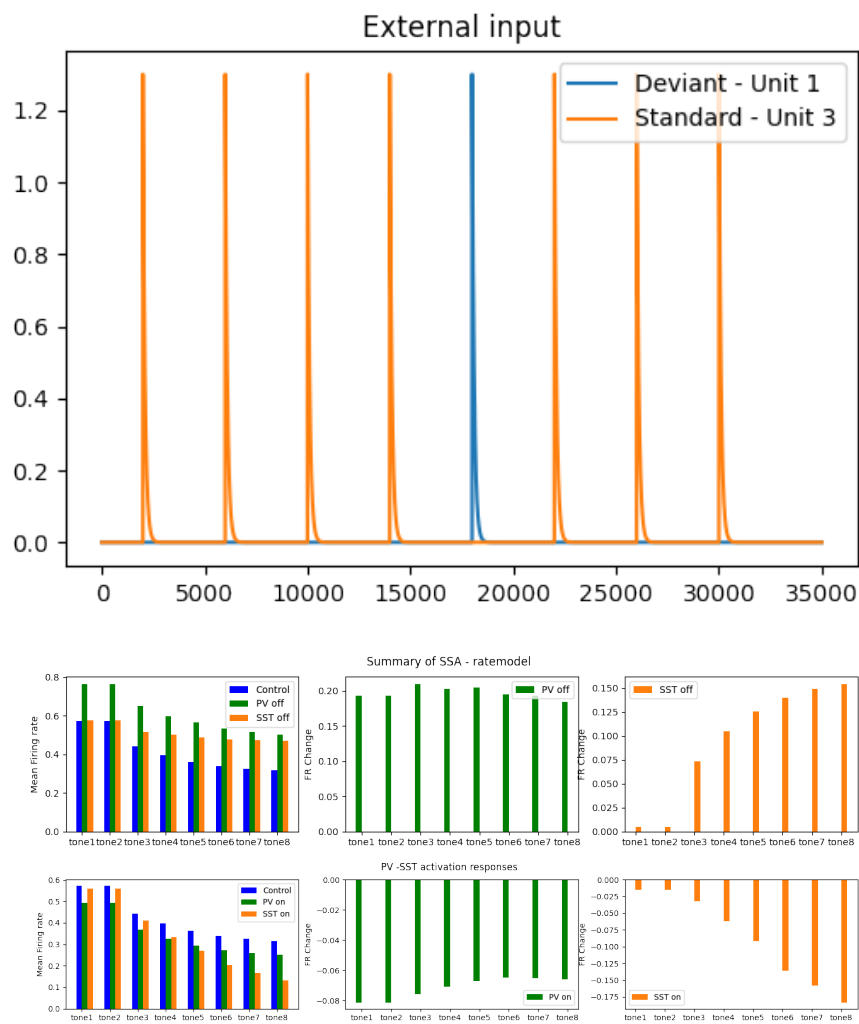


Figure 4. ReFig4

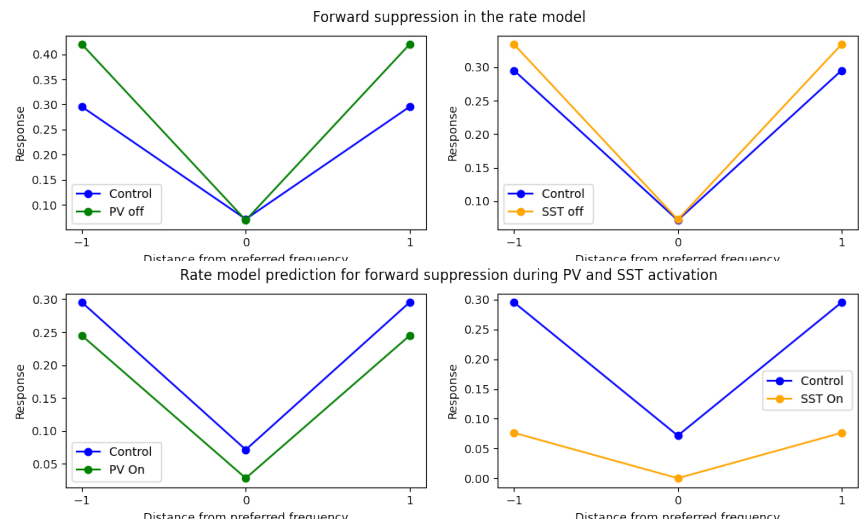


Figure 5. ReFig6

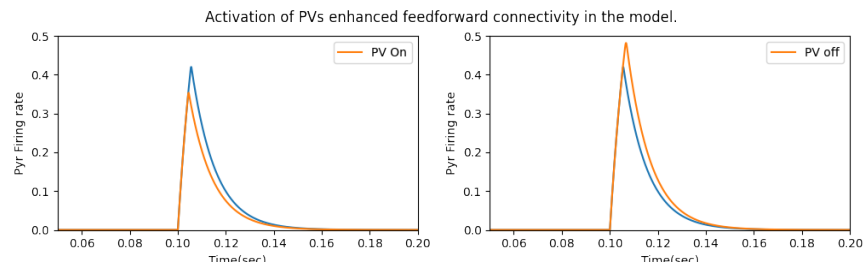


Figure 6. ReFig8

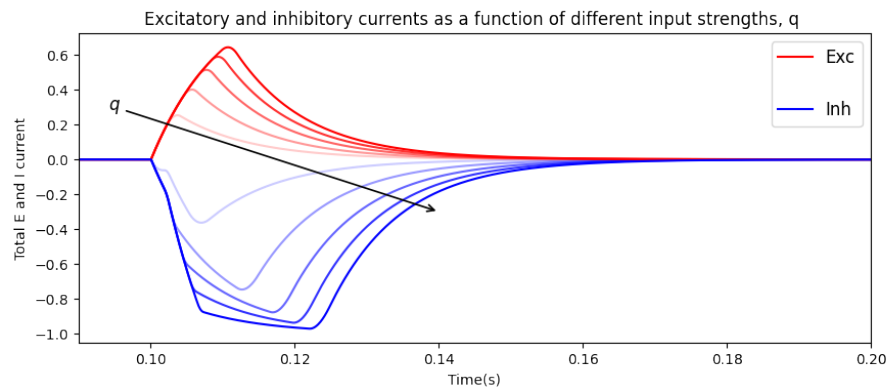


Figure 7. ReFig9

## Discussion

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