

# [Re] Modeling GABA Alterations in Schizophrenia: A Link Between Impaired Inhibition and Gamma and Beta Auditory Entrainment

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## A reference implementation of

→ Modeling GABA Alterations in Schizophrenia: A Link Between Impaired Inhibition and Gamma and Beta Auditory Entrainment, D. Vierling-Claassen, P. Siekmeier, S. Stufflebeam and N. Kopell, *Journal of Neurophysiology*(99):2656-2671, 2008, doi:10.1152/jn.00870.2007

## Introduction

We provide an implementation of [2], which models impaired auditory entrainment in the gamma range for schizophrenic patients. Particularly, we only reimplement the simplified network model and do not replicate the biophysically more detailed Genesis model which is also developed in the article.

In the original article the authors conduct an MEG study of auditory entrainment and find changes in gamma and beta range entrainment found in schizophrenic patients. These changes in oscillatory dynamics in patients are important for two reasons: first, gamma range oscillations emerge in a variety of different tasks and are thought to underlie many cognitive processes (see e.g. [Fries2005, Fries2015]). Furthermore, impaired gamma range oscillations in schizophrenic patients have been found in most of these tasks and might offer an explanation for the cognitive deficits found in patients. Therefore, the study of the mechanisms underlying oscillatory entrainment might shed light on the basic principles that are responsible for a wide range of deficits in schizophrenic patients. Second, oscillatory entrainment is a promising candidate for a neurophysiological biomarker for schizophrenia [Siekmeier2015]. In the original article they develop two models that are able to account for the changes they find in their experimental data. One is a biophysically detailed network model and the other one a simplified network model. In both models a prolonged decay at GABAergic inhibitory synapses causes the reduction in gamma entrainment and the increase in beta entrainment. The simplified network model, despite its many simplifications, offers insight into the mechanisms underlying these entrainment deficits while focusing on a few key parameters. This makes it easy to distill and understand underlying dynamics and mechanisms and, at the same time, makes simulations computationally very inexpensive allowing for an extensive exploration of the parameter space. Additionally, again because of the simplicity, the model can easily be extended to study the effect other parameters (e.g. sparsity of connections, different populations of inhibitory neurons, different types of synaptic receptors,...), without losing much of its simplicity.

We focus on the main results of the original article: an increase in inhibitory decay time constants leads to a reduction of power in the gamma range and an increase in power in the beta range, replicating experimental findings for schizophrenic patients. Therefore, we reproduce Figures 4, 5, 6, 7, 10 and 11 of the original paper. The original model is implemented using Matlab but the source code is not publicly available. The model and analysis scripts are implemented using Python 2.7.9. All simulations were run under Ubuntu 15.04.

## Methods

The model was implemented solely from the paper description, since the original code is not publicly available. The model is a simple model consisting of two neural populations (excitatory and inhibitory cells). Individual cells are modeled as theta neurons (for a detailed discussion of this neuron model see [1]). The  $k$ th neuron in a network is described by a single variable  $\theta_k$ , which can be regarded as the neuron state, subject to the following dynamics

$$\frac{d\theta_k}{dt} = 1 - \cos \theta_k + (b + S_k + N(t)) \cdot (1 + \cos \theta_k),$$

where  $b$  is an externally applied current,  $S$  is the total synaptic input to the cell and  $N(t)$  is a time-varying noise input. Total synaptic input to a cell in a network is calculated as

$$S_k = \sum_{j=1}^n \alpha_j \cdot g_{jk} \cdot s_{jk},$$

where  $n$  is the number of presynaptic neurons,  $\alpha_j$  controls excitation and inhibition, i.e. is +1 for excitatory synapses and -1 for inhibitory ones,  $g_{jk}$  is the synaptic strength from cell  $j$  to cell  $k$  and  $s_{jk}$  is the synaptic gating variable from cell  $j$  to cell  $k$ . Synaptic gating variables are subject to the following dynamics

$$\frac{ds_{jk}}{dt} = -\frac{s_{jk}}{\tau_j} + e^{-\eta \cdot (1 + \cos \theta_j)} \cdot \frac{1 - s_{jk}}{\tau_R},$$

where  $\tau_j$  is the synaptic decay time,  $\tau_R$  the synaptic rise time and  $\eta$  is a scaling parameter. The network receives excitatory drive input at click train frequency from a single pacemaker cell. Additionally, Poissonian noise input is also given to all cells in the network. A noise spike at time  $t_n$  elicits the following excitatory postsynaptic potential ('EPSC')

$$N = H(t - t_n) \cdot \frac{A \cdot g_{gmax} \cdot (e^{-(t-t_n)/\tau_{exc}} - e^{-(t-t_n)/\tau_R})}{\tau_{exc} - \tau_R},$$

where  $A \cdot g_{gmax}$  is the strength of the noise and again  $\tau_{exc}$  is the synaptic decay time and  $\tau_R$  the synaptic rise time.

Each population connects to itself and to the other with an all-to-all connectivity. Both populations also have two sources of input, the oscillatory drive input and a background noise input. The drive input periodically sends spikes to both populations with a given frequency. In order to generate the spikes a drive cell is implemented (also a theta neuron), which receives an applied current so that its spike frequency matches the driving frequency. This drive cell is then connected to all cells in the network. The background noise input sends noise spikes at times drawn from a Poisson distribution. Table 1 summarizes the network model. Tables 2 and 3 list the parameters of the model and the simulations, their definitions and values, respectively.

The model was implemented using Python 2.7.9 and numpy 1.9.3. Visualisation of results was also done in Python using the matplotlib module (matplotlib 1.4.3).

Furthermore, since the model is computationally very inexpensive, we did not aim to provide the most efficient implementation but rather an implementation that is clear, and easy to understand and use.

All differential equations were solved using a simple forward Euler scheme. As in the original article a single simulation simulated a 500ms trial and the time step was chosen such that this results in  $2^{13} = 8192$  data points. However, the main results are unaffected by a smaller time step.

**Table 1: Model summary**

Populations	One excitatory and one inhibitory population
Topology	None
Connectivity	All-to-all
Neuron model	Theta model
Synapse model	(Quasi-)Instantaneous rise, exponential decay
External input	Poisson noise and periodic drive to both populations
Recordings	Theta variables (both populations); ‘MEG’ signal (summed EPSCs at exc. neurons)

**Table 2: Model parameters**

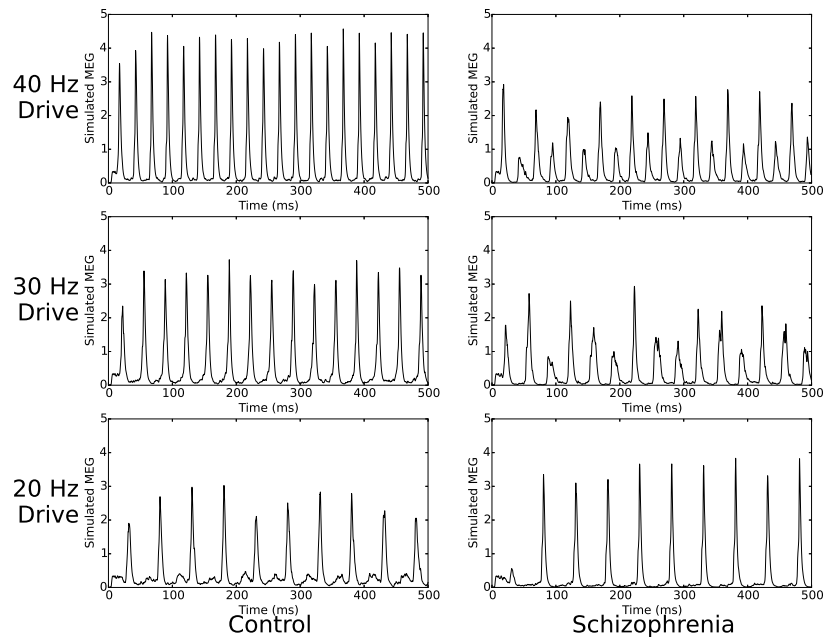
Parameter	Definition	Value
$n_E$	Exc. population size	20
$n_I$	Inh. population size	10
$\tau_R$	Synaptic rise time	0.1
$\tau_{exc}$	Excitatory decay time	2.0
$\tau_{inh}$	Inhibitory decay time (control)	8.0
$\tau_{inh}$	Inhibitory decay time (schizophrenia)	28.0
$g_{ee}$	E-E synaptic strength	0.015
$g_{ei}$	E-I synaptic strength	0.025
$g_{ie}$	I-E synaptic strength	0.015
$g_{ii}$	I-I synaptic strength	0.02
$g_{de}$	Synaptic strength of drive to E cells	0.3
$g_{di}$	Synaptic strength of drive to I cells	0.08
$b$	Applied current (regardless of cell type)	-0.1
$Ag_{max}$	Scaling factor for noise EPSCs	0.5

**Table 3: Simulation parameters**

Parameter	Value
Time step ( $dt$ )	0.061
Number of data points	8192 ( $= 2^{13}$ )
Total time	500ms

## Results

As explained in the introduction, we only replicated the simple model from [2], and **not** the GENESIS model. We aimed to reproduce Figures 4 (raw, simulated MEG signal) and 5 (power spectra for MEG signals from Figure 4) from [2], which show the main results of the model (summarized in Table 4).



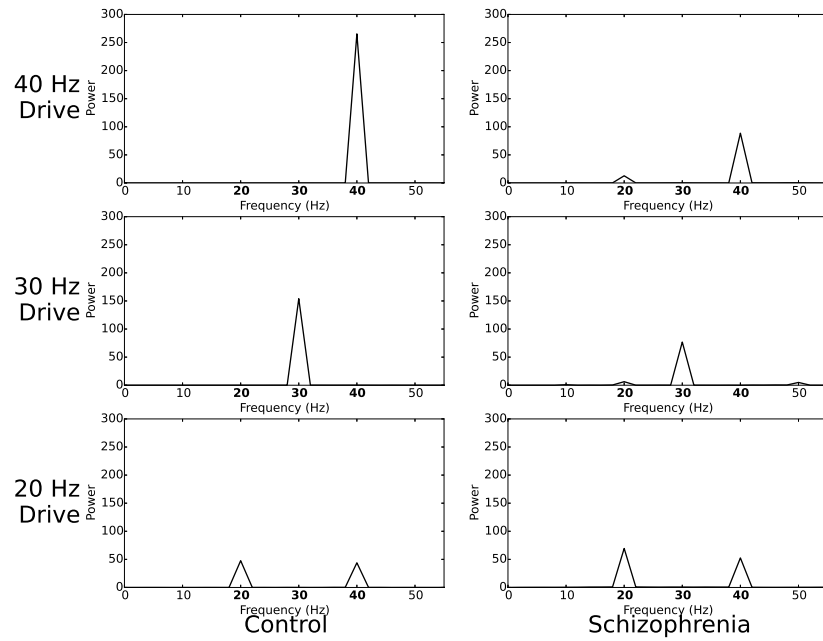
**Figure 1:** Replication of Figure 4: Raw simulated MEG signals (averaged over 20 trials) for the control and the schizophrenic network at the three different driving frequencies.

**Table 4:** Main model result features

Drive	Control subjects	Schizophrenic patients
40 Hz	Strong entrainment to the drive, no power in frequency bands apart from 40 Hz	Weaker entrainment to the drive, emergence of a subharmonic component (at 20 Hz)
30 Hz	Strong entrainment to the drive, no power in frequency bands apart from 30 Hz	Strong entrainment to the drive, no power in frequency bands apart from 30 Hz
20 Hz	Entrainment to the drive, however, more power in the harmonic 40 Hz band	Stronger entrainment to the drive, less power in the harmonic band

Figures 1 and 2 show the output of the replicated model for the same simulations as for Figures 4 and 5 from the original article. The main characteristics described above can be clearly seen. However, in our model these main features are a little bit less pronounced than in the original model. Since the network model receives Poissonian noise (which is quite strong), this difference may simply stem from a difference in noise. Furthermore, we have to mention the differences in amplitude for the simulated MEG signals (and accordingly the power spectra thereof) between the original model and our replication, which we believe stems from a scaling in the original model. However, since the original source code is not available, we cannot verify that.

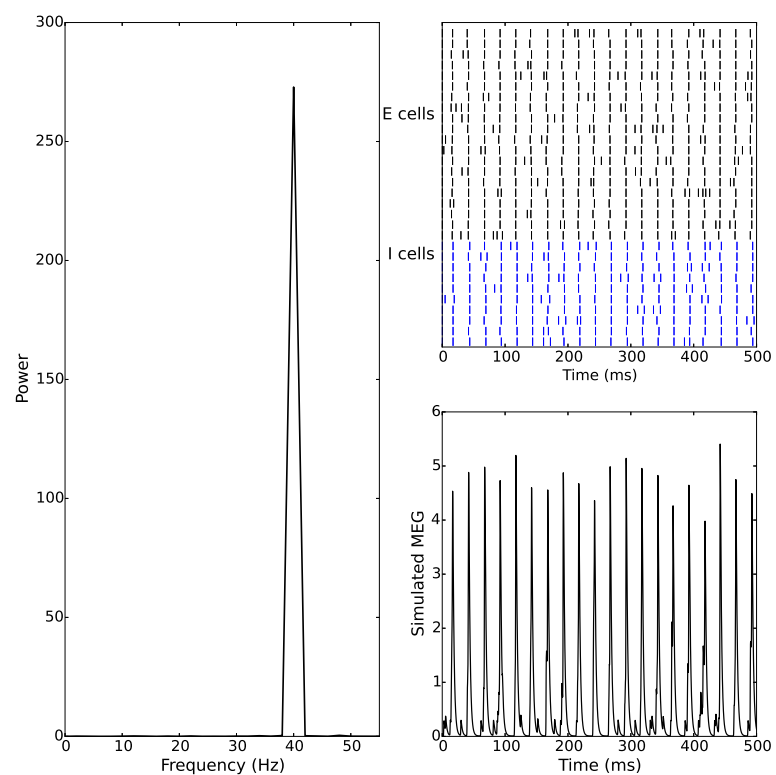
After having looked at the model output averaged over 20 trials with different noise, we also show single trial data which exemplify the main model features, as was done in the original article. Figures 3 and 4 show the model output in response to 40 Hz drive input for the control and the schizophrenia network, respectively. The strong entrainment in the control case, the reduction of entrainment and the emergence of



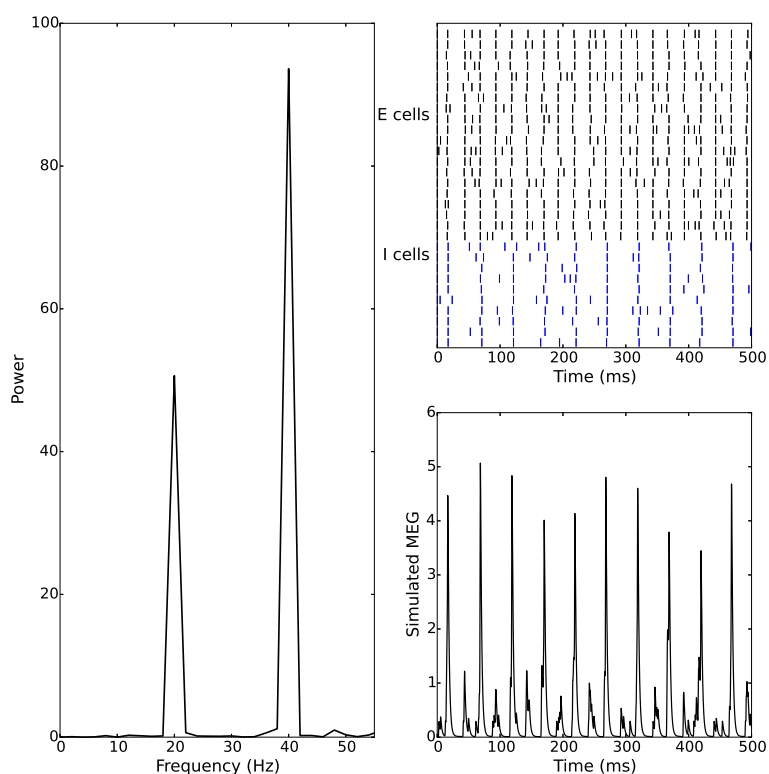
**Figure 2:** Replication of Figure 5: Power spectra of the averaged MEG signals from [1](#)

a subharmonic 20 Hz component are again clearly visible. However, as before, in our model implementation the emergent 20 Hz component is less pronounced than in the original implementation (best seen in the excitatory population activity displayed in the raster plot of [4](#)).

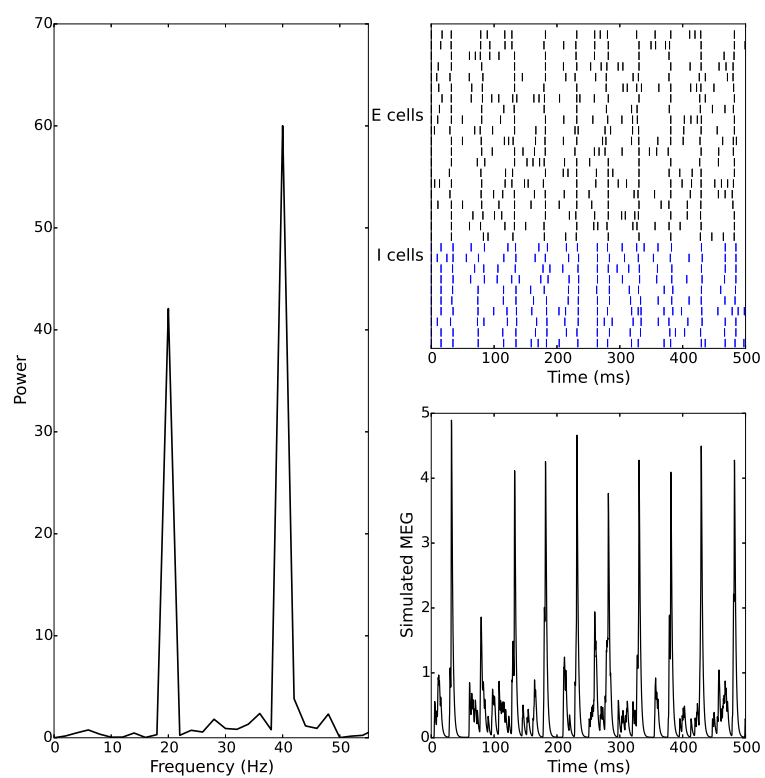
Figures [5](#) and [6](#) show the model output in response to 20 Hz drive for the control and the schizophrenia network, respectively. Again, main features of the original model are faithfully reproduced.



**Figure 3:** Replication of Figure 6: Single trial from the control network. 40 Hz drive. Network entrains to 40 Hz, as can be seen in the frequency diagram, raster plot and MEG trace.

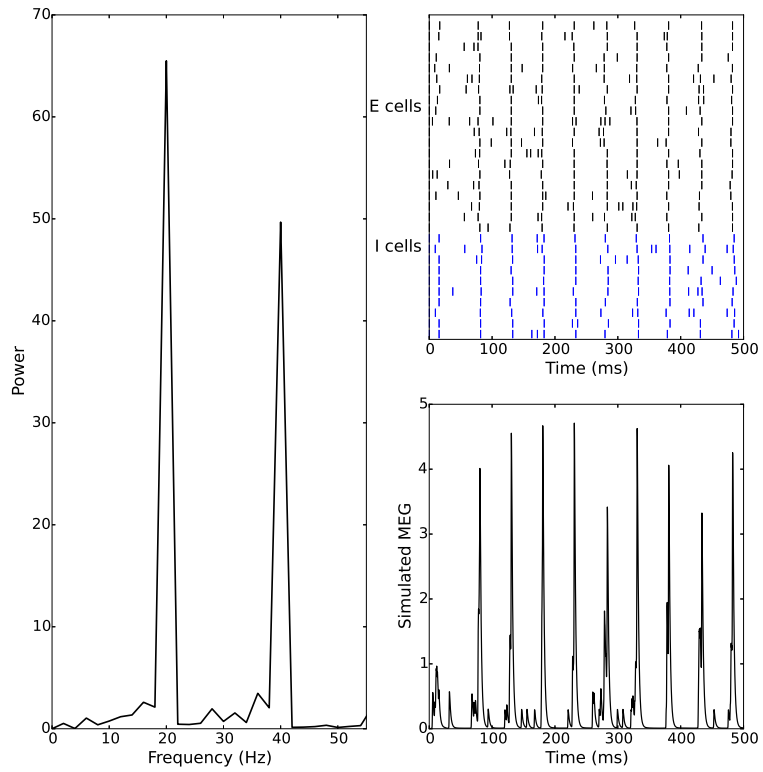


**Figure 4:** Replication of Figure 7: Single trial from the schizophrenia network. 40 Hz drive. Network entrains to 40 Hz but also shows a strong 20 Hz component, as can be seen in the frequency diagram, raster plot and MEG trace. Especially the inhibitory neurons only entrain to a 20 Hz rhythm (see raster plot).

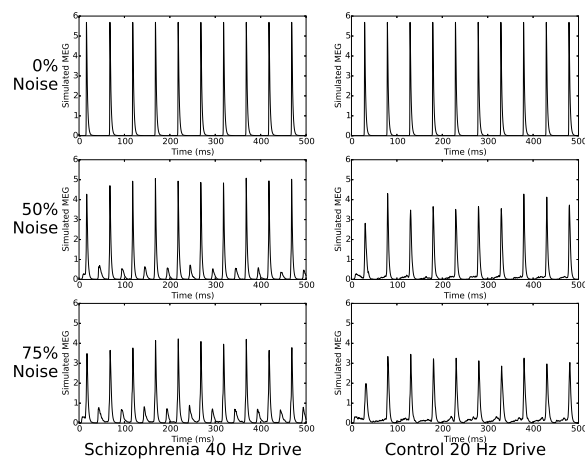


**Figure 5:** Replication of Figure 10: Single trial from the control network. 20 Hz drive. Network entrains to 20 Hz but also shows a 40 Hz component, as can be seen in the frequency diagram, raster plot and MEG trace.





**Figure 6:** Replication of Figure 11: Single trial from the schizophrenia network. 20 Hz drive. Network entrains to 20 Hz without 40 Hz component, as can be seen in the frequency diagram, raster plot and MEG trace. note that the 40 Hz power in the power spectrum is a harmonic.



**Figure 7:** Raw simulated MEG signals (averaged over 20 trials) for the control and the schizophrenic network at 20 and 40 Hz driving frequencies for three different levels of noise strength (0, 50 and 75 % of the strength in the standard model).

## Exploration of the Discrepancies between Original and Reimplementation

In this section we explore possible scenarios that might explain the less pronounced main features in the reimplementation. We explore the influence of the background noise. The main mechanism behind the emergence of a 20 Hz component in response to 40 Hz drive in the schizophrenia network is the prolonged inhibition which suppresses activity in every second 40 Hz cycle.

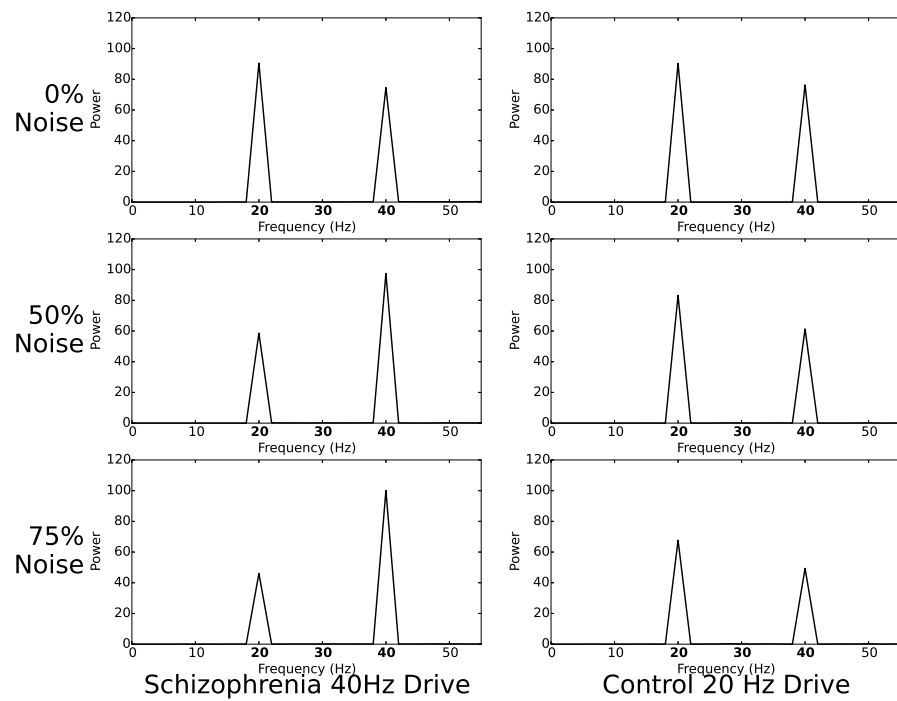
In the absence of noise the network responds with a pure 20 Hz oscillation (see Figures 7 left upper panel and 8 left upper panel). However, the background noise gives sufficient input to some excitatory cells to overcome this suppression and also fire in between the 20 Hz cycles. This results in a mixed response, where power is split between 20 Hz and 40 Hz. The ratio of this split depends on the strength of the noise. Therefore, we asked whether the less pronounced 20 Hz component in our reimplementation might simply come from a too high background noise amplitude. Figures 7 (left middle and lower panels and 8 left middle and lower panels, show the response (MEG signal and power spectral density, respectively) to a 40 Hz drive in the cases, where we scaled down the noise to 75% and 50%, respectively. It can clearly be seen that the 20 Hz component increases, when the noise strength decreases. However, as can be seen in right panels, showing the response of the control network to 20 Hz drive, is that downscaling of the background noise reduces the 40 Hz component in response to 20 Hz drive. This is not surprising since background noise drives excitatory cells to fire in between 20 Hz cycles in the control network, resulting in the 40 Hz component. This component is suppressed in the schizophrenia network due to the prolonged inhibition. Summarising, a difference in the strength of the background noise might be an explanation for the discrepancy between original and reimplementation. However, only a reduction of noise solely for the schizophrenia network fully replicates the original results.

## Conclusion

Overall, we believe we have faithfully reproduced the main features of the simple model from [2]. However, we note that overall features are a little bit less pronounced in our reimplementation compared to the original model. We have explored possible explanations for this discrepancy and conclude that it might come from minor inconsistencies with respect to parameters in the original model. Nevertheless, the mechanism proposed in the original model could be reproduced and presents a possible explanation for deficits in auditory steady-state responses in patients suffering from schizophrenia.

## References

- [1] Christoph Börgers and Nancy Kopell. "Synchronization in networks of excitatory and inhibitory neurons with sparse, random connectivity". In: *Neural computation* 15.3 (2003), pp. 509–538.
- [2] Dorea Vierling-Claassen et al. "Modeling GABA alterations in schizophrenia: a link between impaired inhibition and altered gamma and beta range auditory entrainment". In: *Journal of Neurophysiology* 99.5 (2008), pp. 2656–2671.



**Figure 8:** Power spectra of the raw MEG signals from 7