

# Hierarchical architectures for spiking Winner-Take-All networks

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### Outline

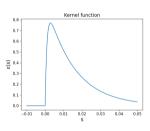


- 1 Introduction
- 2 Experiments
- 3 Results

### Biological background



- Spiking neural networks
  - resemble biological neural networks closely
  - generate and propagate neural spikes
- Winner-Take-All networks
- Probabilistic brain
- Synaptic plasticity



### Biological background



- Networks are organized in hierarchical structure
- Feedback used for attention / biased competition
- Lee TS (2003) found that feedback could let neurons see illusory lines



## Theoretical background



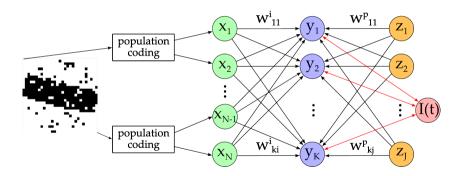
 Bayesian inference gives the probability of an hypothesis given related evidence

$$P(Y = k|X,Z) = \frac{P(X|Y = k)P(Y = k|Z)}{\sum_{k'} P(X|Y = k')P(Y = k'|Z)}$$
(1)

- Network model of Nessler et al. (2013) used and expanded
- Nessler et al. (2013) claimed that synaptic weights converge towards the log of probability

#### The network





#### Goals



- Further the understanding of the network model
- Simulate feedback found in the visual cortex
- Show connection between Bayesian inference and network model

### Methodology



- Simulation was performed in Python
- Simulation step size was 1 ms
- Pixels of input images and the prior had a noise level of 10%
- Kullback-Leibler divergence was chosen to evaluate performance of model

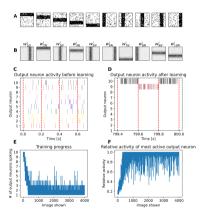
### Ambiguous visual stimuli 1



- Network learned to group horizontal and vertical bars into 10 groups
- After training ambiguous images with 1 horizontal and 1 vertical bar were shown
- Network was able to focus on individual bars, due to prior neurons

### Ambiguous visual stimuli 2

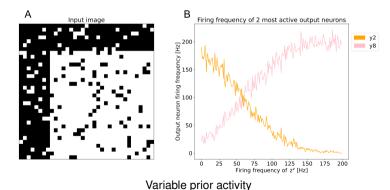




Training plot

#### Ambiguous visual stimuli 3





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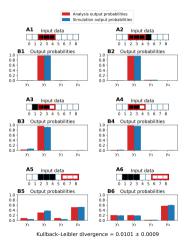
#### Analysis and simulation of the network 1



- usage of smaller 1-D images to make network easier to analyse
- Mathematical derivation of Bayesian likelihood, prior and posterior
- Derived synaptic weights from Bayesian likelihood and prior
- Simulated network with those weights and fitted hyperparameters
- Compared Bayesian posterior to output of the simulation

#### Analysis and simulation of the network 2





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### Transferability of hyperparameters 1

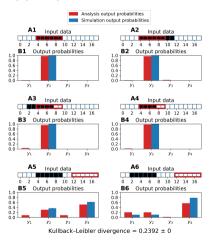


- Input size and prior neuron firing rate was doubled
- Network was simulated with same hyperparameters of smaller network, to check if they are applicable to any network size

### L

### Transferability of hyperparameters 2





### Training with predetermined hyperparameters 1

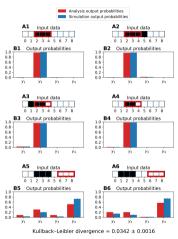


- Determined hyperparameters were used to train weights
- Trained weights were compared to analytically determined weights

### L

### Training with predetermined hyperparameters 2







### Training with predetermined hyperparameters 3



Α	Learned P <sup>X Y</sup>								
	0.52	0.49	0.53	0.06	0.1	0.08	0.12	0.11	0.06
	0.09	0.07	0.49	0.49	0.51	0.09	0.09	0.09	0.06
	0.07	0.08	0.08	0.06	0.51	0.5	0.52	0.07	0.1
	0.11	0.1	0.12	0.07	0.09	0.06	0.53	0.46	0.51

В	Calculated P^I'								
	0.9	0.9	0.9	0.1	0.1	0.1	0.1	0.1	0.1
	0.1	0.1	0.9	0.9	0.9	0.1	0.1	0.1	0.1
	0.1	0.1	0.1	0.1	0.9	0.9	0.9	0.1	0.1
	0.1	0.1	0.1	0.1	0.1	0.1	0.9	0.9	0.9

	Learned $P^{Y\mid Z}$					
С	1.14	0.02	0.02	0.02		
	0.03	1.17	0.03	0.01		
	0.02	0.02	1.15	0.02		
	0.02	0.03	0.03	1.17		

Calculated P <sup>Y Z</sup>					
0.9	0.03	0.03	0.03		
0.03	0.9	0.03	0.03		
0.03	0.03	0.9	0.03		
0.03	0.03	0.03	0.9		

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#### Results



- Connection between model and Bayesian inference was shown
  - Network outputs spike according to Bayesian posterior
  - Trained weights converge towards the log of their respective probabilities
- Importance of neural feedback was shown for
  - Attention / Ambiguity resolution
  - Illusory contour effect



- Optimal hyperparameters are dependent on network size
- Training process could not achieve perfectly trained weights

#### Conclusion



- Thesis provided insight to hierarchical spiking Winner-Take-All network model
- Showed that the network model can simulate effects like attention and changing beliefs through feedback
- Provided ideas on how to further analyse and improve the model

#### Sources



- Lee TS, Mumford D. (July 2003). "Hierarchical Bayesian inference in the visual cortex." In: J Opt Soc Am A Opt Image Sci Vis. DOI: doi:10.1364/josaa.20.001434
- Nessler, Bernhard et al. (Apr. 2013). "Bayesian Computation Emerges in Generic Cortical Microcircuits through Spike-Timing-Dependent Plastic ity." In: PLOS Computational Biology 9.4, pp. 1–30. doi: 10.1371/journal. pcbi.1003037. url: https://doi.org/10.1371/journal.pcbi.1003037