

Hierarchical architectures for spiking Winner-Take-All networks

Christoph Rieger,

Supervisor: Univ.-Prof. Dipl.-Ing. Dr.techn. Robert Legenstein

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Outline

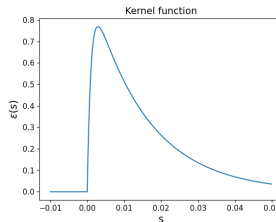
1 Introduction

2 Experiments

3 Results

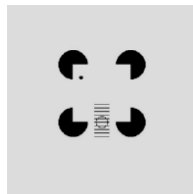
Biological background

- Spiking neural networks
 - resemble biological neural networks closely
 - generate and propagate neural spikes
- Winner-Take-All networks
- Probabilistic brain
- Synaptic plasticity



Biological background

- Networks are organized in hierarchical structure
- Feedback used for attention / biased competition
- Lee TS (2003) found that feedback could let neurons see illusory contour



Kanizsa square, Lee TS (2003)

Theoretical background

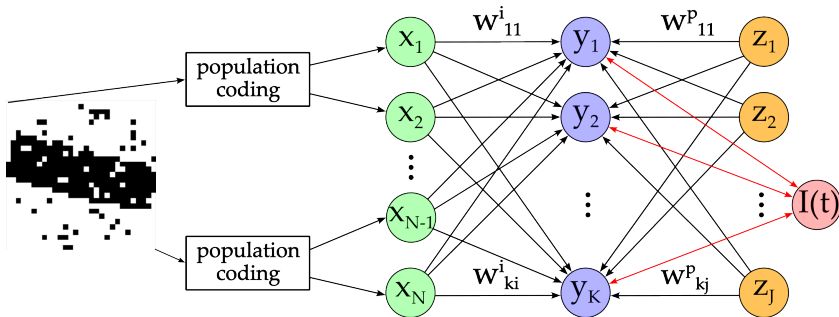
- Bayesian inference gives the probability of an hypothesis given related evidence



$$P(Y = k|X, Z) = \frac{P(X|Y = k)P(Y = k|Z)}{\sum_{k'} P(X|Y = k')P(Y = k'|Z)} \quad (1)$$

- Network model of Nessler et al. (2013) used and expanded
- Nessler et al. (2013) claimed that synaptic weights converge towards the log of probability

The network



Goals

- Further the understanding of the network model
- Simulate feedback found in the visual cortex
- Show connection between Bayesian inference and network model

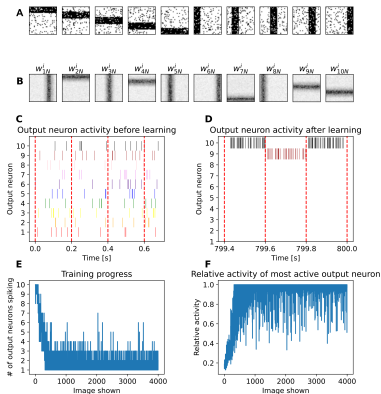
Methodology

- Simulation was performed in Python
- Simulation step size was 1 ms
- Pixels of input images and the prior had a noise level of 10%
- Kullback-Leibler divergence was chosen to evaluate performance of model

Ambiguous visual stimuli 1

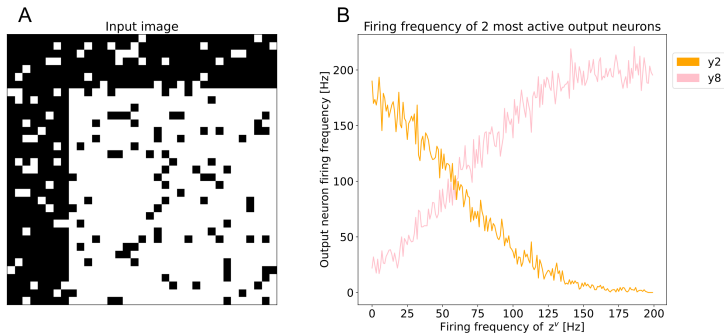
- Network learned to group horizontal and vertical bars into 10 groups
- After training ambiguous images with 1 horizontal and 1 vertical bar were shown
- Network was able to focus on individual bars, due to prior neurons

Ambiguous visual stimuli 2



Training plot

Ambiguous visual stimuli 3

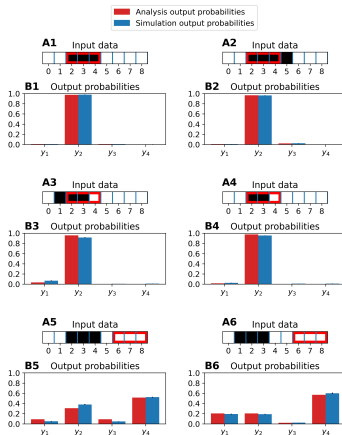


Variable prior activity

Analysis and simulation of the network 1

- usage of smaller 1-D images to make network easier to analyse
- Mathematical derivation of Bayesian likelihood, prior and posterior
- Derived synaptic weights from Bayesian likelihood and prior
- Simulated network with those weights and fitted hyperparameters
- Compared Bayesian posterior to output of the simulation

Analysis and simulation of the network 2

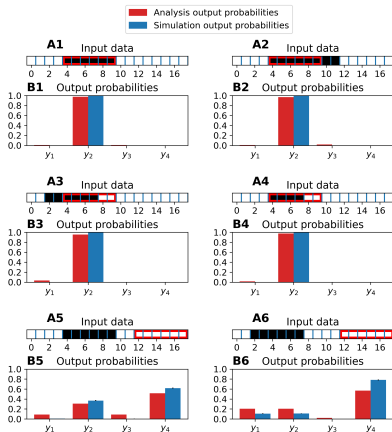


Kullback-Leibler divergence = 0.0101 ± 0.0009

Transferability of hyperparameters 1

- Network was simulated with same hyperparameters of smaller network, to check if they are applicable to any network size
- Input size and prior neuron firing rate was doubled

Transferability of hyperparameters 2

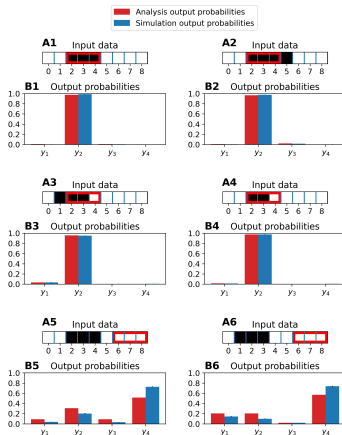


Kullback-Leibler divergence = 0.2392 ± 0

Training with predetermined hyperparameters 1

- Determined hyperparameters were used to train weights
- Trained weights were compared to analytically determined weights

Training with predetermined hyperparameters 2



Kullback-Leibler divergence = 0.0342 ± 0.0016

Training with predetermined hyperparameters 3

A $\theta^{\text{learned input weights}}$

0.52	0.49	0.53	0.06	0.1	0.08	0.12	0.11	0.06
0.09	0.07	0.49	0.49	0.51	0.09	0.09	0.09	0.06
0.07	0.08	0.08	0.06	0.51	0.5	0.52	0.07	0.1
0.11	0.1	0.12	0.07	0.09	0.06	0.53	0.46	0.51

B $\theta^{\text{calculated input weights}}$

0.9	0.9	0.9	0.1	0.1	0.1	0.1	0.1	0.1
0.1	0.1	0.9	0.9	0.9	0.1	0.1	0.1	0.1
0.1	0.1	0.1	0.1	0.9	0.9	0.9	0.1	0.1
0.1	0.1	0.1	0.1	0.1	0.1	0.9	0.9	0.9

C $\theta^{\text{learned prior weights}}$

1.14	0.02	0.02	0.02
0.03	1.17	0.03	0.01
0.02	0.02	1.15	0.02
0.02	0.03	0.03	1.17

D $\theta^{\text{calculated prior weights}}$

0.9	0.03	0.03	0.03
0.03	0.9	0.03	0.03
0.03	0.03	0.9	0.03
0.03	0.03	0.03	0.9

Results

- Connection between model and Bayesian inference was shown
 - Network outputs spikes according to Bayesian posterior
 - Trained weights converge towards the log of their respective probabilities
- Importance of neural feedback was shown for
 - Attention / Ambiguity resolution
 - Illusory contour effect

Results

- Optimal hyperparameters are dependent on network size
- Training process could not achieve perfectly trained weights

Conclusion

- Thesis provided insight to hierarchical spiking Winner-Take-All network model
- Showed that the network model can simulate effects like attention and changing beliefs through feedback
- Provided ideas on how to further analyse and improve the model

Sources

- Lee TS, Mumford D. (July 2003). “Hierarchical Bayesian inference in the visual cortex.” In: J Opt Soc Am A Opt Image Sci Vis. DOI: doi:10.1364/josaa.20.001434
- Nessler, Bernhard et al. (Apr. 2013). “Bayesian Computation Emerges in Generic Cortical Microcircuits through Spike-Timing-Dependent Plasticity.” In: PLOS Computational Biology 9.4, pp. 1–30. doi: 10.1371/journal.pcbi.1003037. url: <https://doi.org/10.1371/journal.pcbi.1003037>