# Introduction of Generative Adversarial Network (GAN)

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# Generative Adversarial Network (GAN)

How to pronounce "GAN"?



Google 小姐

#### Yann LeCun's comment

## What are some recent and potentially upcoming breakthroughs in unsupervised learning?



Yann LeCun, Director of Al Research at Facebook and Professor at NYU Written Jul 29 · Upvoted by Joaquin Quiñonero Candela, <u>Director Applied Machine Learning at Facebook</u> and Huang Xiao 有史以來



Adversarial training is the coolest thing since sliced bread.

I've listed a bunch of relevant papers in a previous answer.

Expect more impressive results with this technique in the coming years.

What's missing at the moment is a good understanding of it so we can make it work reliably. It's very finicky. Sort of like ConvNet were in the 1990s, when I had the reputation of being the only person who could make them work (which wasn't true).

https://www.quora.com/What-are-some-recent-and-potentially-upcoming-breakthroughs-in-unsupervised-learning

#### Yann LeCun's comment

## What are some recent and potentially upcoming breakthroughs in deep learning?



**Yann LeCun**, Director of Al Research at Facebook and Professor at NYU Written Jul 29 · Upvoted by Joaquin Quiñonero Candela, Director Applied Machine Learning at Facebook and Nikhil Garg, I lead a team of Quora engineers working on ML/NLP problems



• • • • •

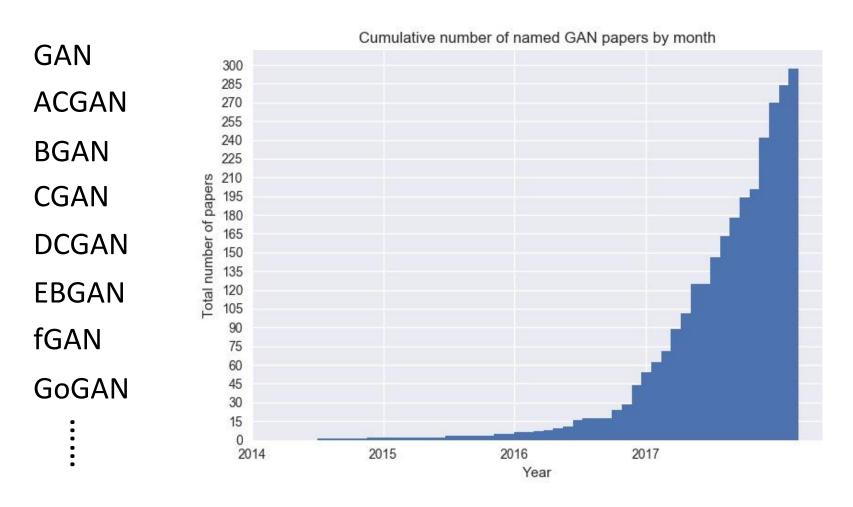
The most important one, in my opinion, is adversarial training (also called GAN for Generative Adversarial Networks). This is an idea that was originally proposed by Ian Goodfellow when he was a student with Yoshua Bengio at the University of Montreal (he since moved to Google Brain and recently to OpenAI).

This, and the variations that are now being proposed is the most interesting idea in the last 10 years in ML, in my opinion.

https://www.quora.com/What-are-some-recent-and-potentially-upcoming-breakthroughs-in-deep-learning

#### All Kinds of GAN ...

https://github.com/hindupuravinash/the-gan-zoo



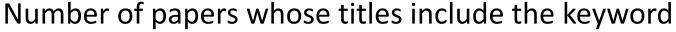
Mihaela Rosca, Balaji Lakshminarayanan, David Warde-Farley, Shakir Mohamed, "Variational Approaches for Auto-Encoding Generative Adversarial Networks", arXiv, 2017

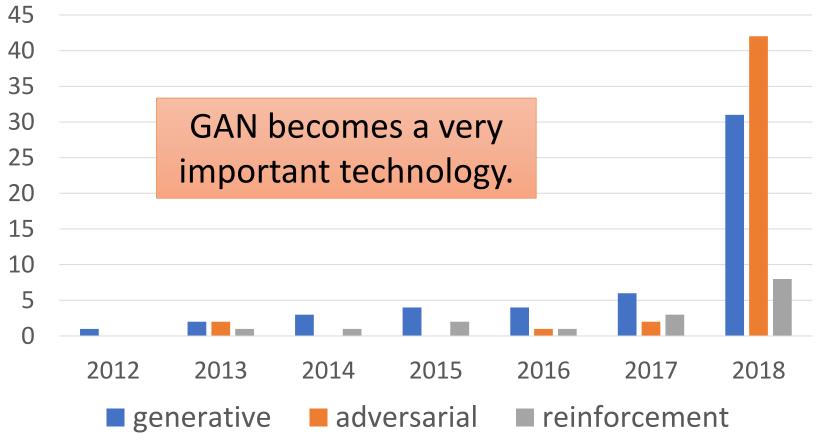
<sup>&</sup>lt;sup>2</sup>We use the Greek  $\alpha$  prefix for  $\alpha$ -GAN, as AEGAN and most other Latin prefixes seem to have been taken https://deephunt.in/the-gan-zoo-79597dc8c347.

#### **Signal Processing Conference**

#### **ICASSP**

Keyword search on session index page, so session names are included.





#### Outline

Basic Idea of GAN

GAN as structured learning

Can Generator learn by itself?

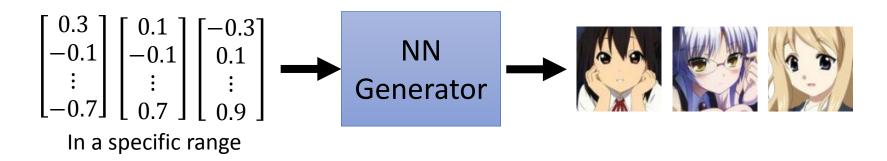
Can Discriminator generate?

A little bit theory

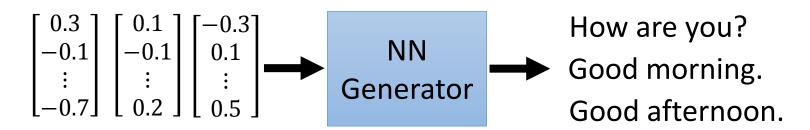
#### Generation

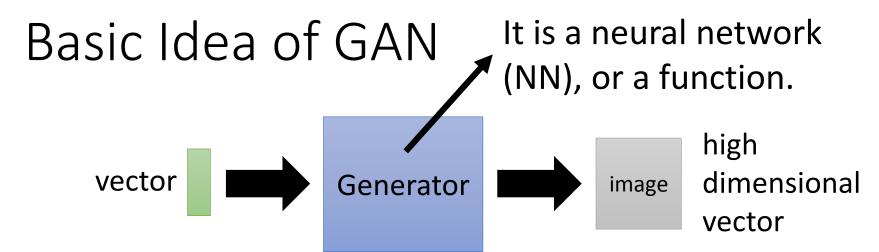
## We will control what to generate latter. → Conditional Generation

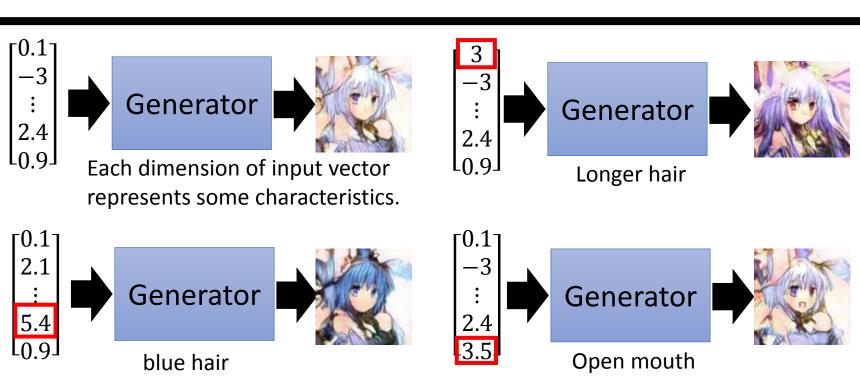
#### **Image Generation**

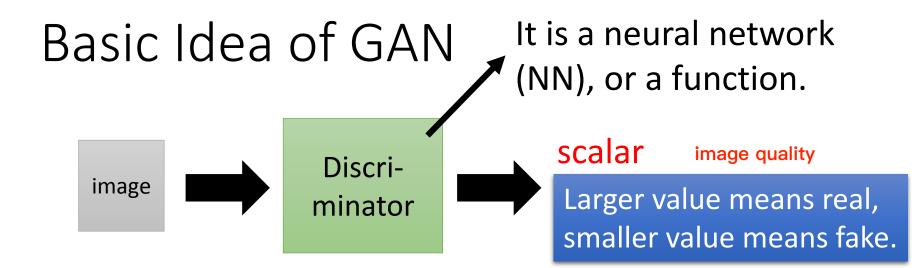


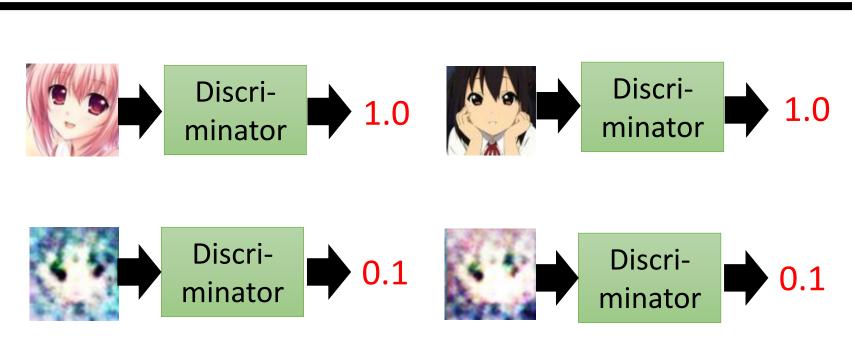
#### Sentence Generation



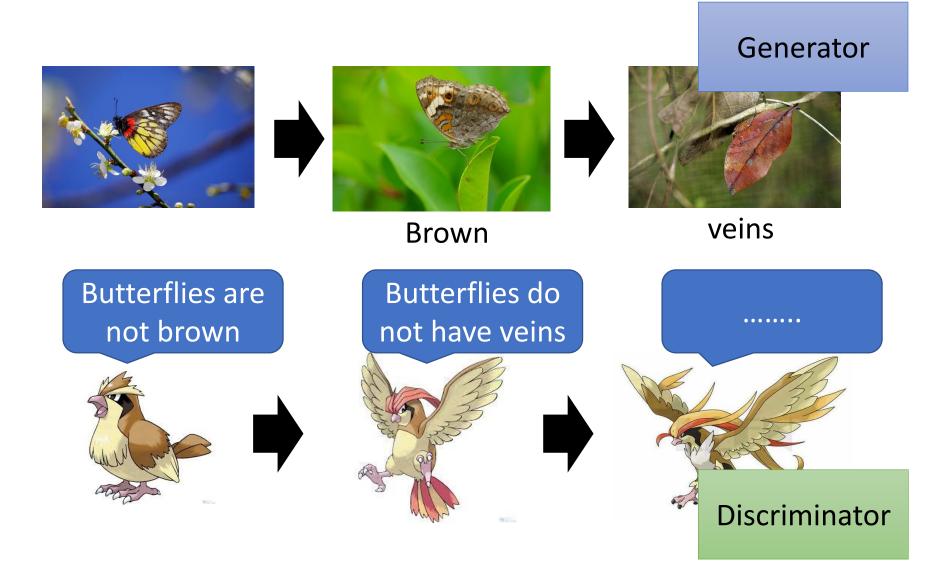








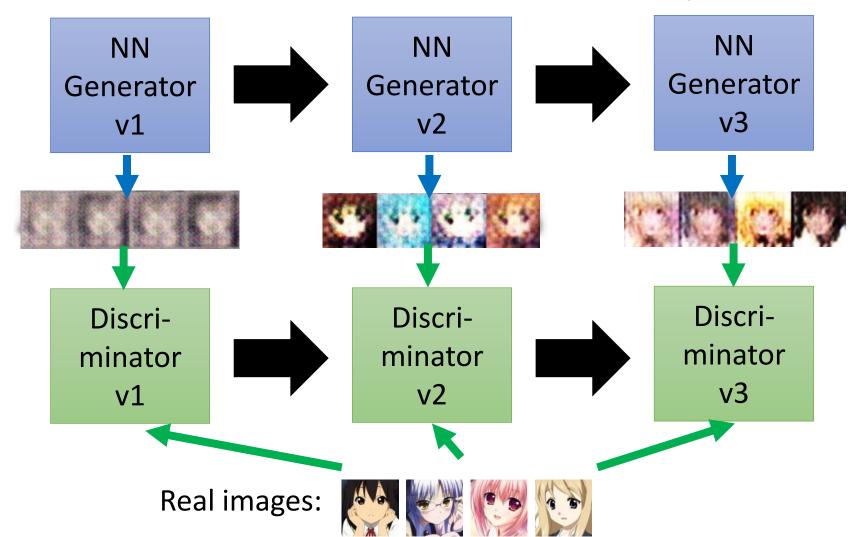
#### Basic Idea of GAN



#### Basic Idea of GAN

This is where the term "adversarial" comes from.

You can explain the process in different ways......



# Basic Idea of GAN (和平的比喻)

Generator (student)

Discriminator (teacher)



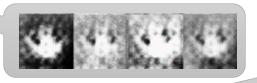
Generator v1



Discriminator v1

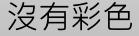
Generator v2

沒有兩個圈



Discriminator v2

Generator v3





為什麼不自己學?

為什麼不自己做?

## Generator v.s. Discriminator

• 寫作敵人, 唸做朋友





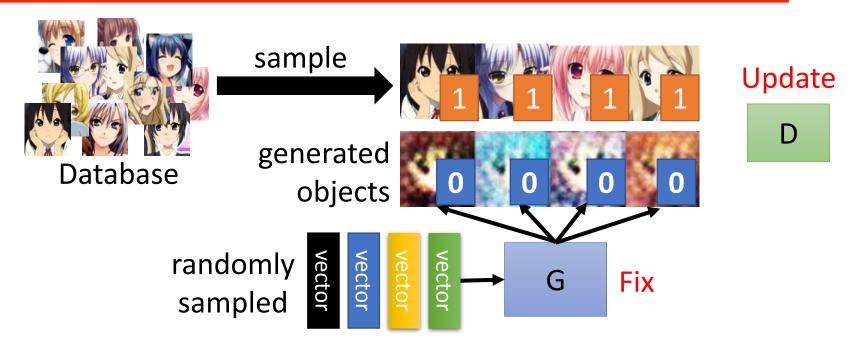


#### Algorithm

- Initialize generator and discriminator
- G
- D

In each training iteration:

**Step 1**: Fix generator G, and update discriminator D



Discriminator learns to assign high scores to real objects and low scores to generated objects.

#### Algorithm

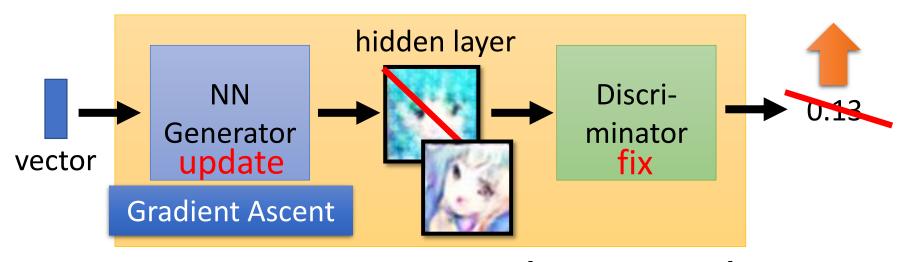
- Initialize generator and discriminator
- G

D

In each training iteration:

Step 2: Fix discriminator D, and update generator G

Generator learns to "fool" the discriminator



large network

**Algorithm** Initialize  $\theta_d$  for D and  $\theta_q$  for G

- In each training iteration:
  - Sample m examples  $\{x^1, x^2, ..., x^m\}$  from database
  - Sample m noise samples  $\{z^1, z^2, ..., z^m\}$  from a distribution

## Learning

- Obtaining generated data  $\{\tilde{x}^1, \tilde{x}^2, ..., \tilde{x}^m\}, \tilde{x}^i = G(z^i)$
- Update discriminator parameters  $heta_d$  to maximize

• 
$$\tilde{V} = \frac{1}{m} \sum_{i=1}^{m} log D(x^i) + \frac{1}{m} \sum_{i=1}^{m} log \left(1 - D(\tilde{x}^i)\right)$$

• 
$$\theta_d \leftarrow \theta_d + \eta \nabla \tilde{V}(\theta_d)$$

Sample m noise samples $\{z^1, z^2, ..., z^m\}$  from a distribution

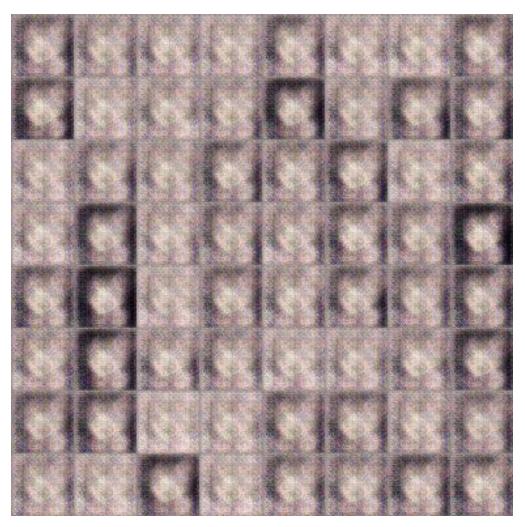
#### Learning

G

• Update generator parameters 
$$heta_q$$
 to maximize

• 
$$\tilde{V} = \frac{1}{m} \sum_{i=1}^{m} log\left(D\left(G(z^{i})\right)\right)$$
 分數越大越好

• 
$$\theta_g \leftarrow \theta_g + \eta \nabla \tilde{V}(\theta_g)$$



100 updates

Source of training data: https://zhuanlan.zhihu.com/p/24767059



1000 updates



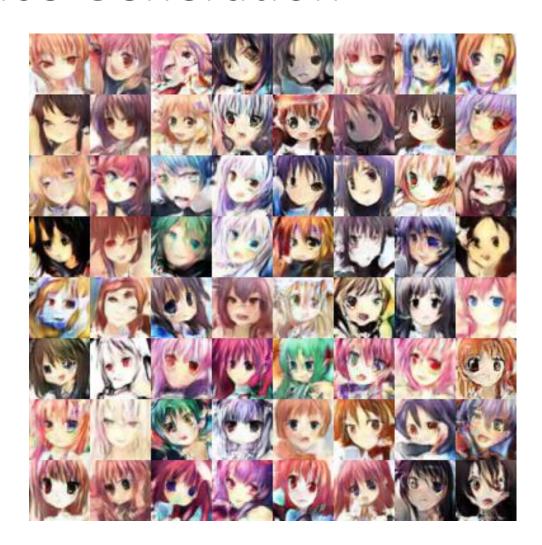
2000 updates



5000 updates



10,000 updates



**20,000** updates

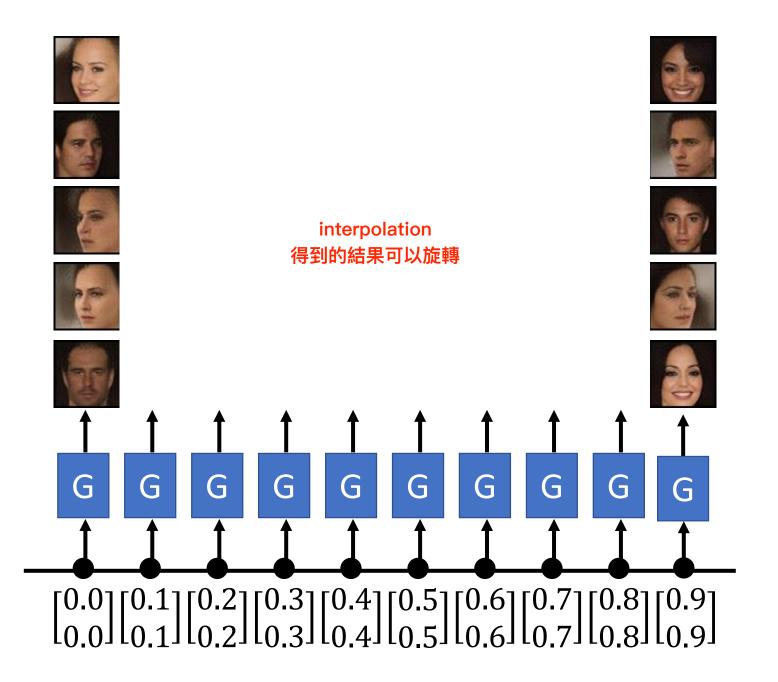


50,000 updates



The faces generated by machine.

圖片生成: 吳宗翰、謝濬丞、 陳延昊、錢柏均



感謝陳柏文同學提供實驗結果

#### Outline

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Can Generator learn by itself?

Can Discriminator generate?

A little bit theory

## Structured Learning

Machine learning is to find a function f

$$f: X \to Y$$

**Regression**: output a scalar

Classification: output a "class" (one-hot vector)



Structured Learning/Prediction: output a output更複雜的情況 sequence, a matrix, a graph, a tree ......

Output is composed of components with dependency

## Output Sequence

$$f: X \to Y$$

#### **Machine Translation**

X:"機器學習及其深層與 結構化" (sentence of language 1) Y: "Machine learning and having it deep and structured" (sentence of language 2)

#### Speech Recognition

X: (speech)

*Y*: 感謝大家來上課" (transcription)

#### Chat-bot 可以加GAN

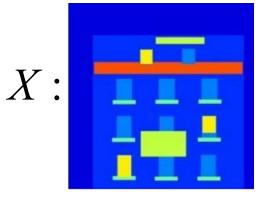
X: "How are you?" (what a user says)

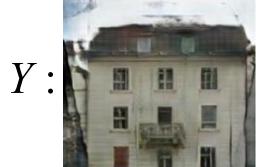
Y: "I'm fine." (response of machine)

## Output Matrix

## $f: X \to Y$

#### Image to Image





#### Colorization:



Ref: https://arxiv.org/pdf/1611.07004v1.pdf

#### Text to Image

X: "this white and yellow flower have thin white petals and a round yellow stamen"





ref: https://arxiv.org/pdf/1605.05396.pdf

## Why Structured Learning Challenging?

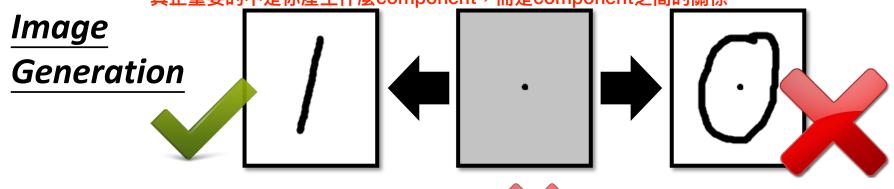
只有少數的paired training data是否能做起來

- One-shot/Zero-shot Learning:
   <sub>假設有些類別根本沒有麼範例</sub>,依然能夠做起來嗎
   In classification, each class has some examples.
  - In structured learning,
    - If you consider each possible output as a "class" ...... 把每一個output視為一種class,則structure learning可以視為一種one shot learning
    - Since the output space is huge, most "classes" do not have any training data.
    - Machine has to create new stuff during testing. 如何學到generalization ability
    - Need more intelligence

在testing的時候想要辨別的分類問題,或許在training data中根本沒有看過或是很少個data 這時候要做得好就有難度

# Why Structured Learning Challenging? 要讓機器有大局觀

- Machine has to learn to do planning
  - Machine generates objects component-by-component, but it should have a big picture in its mind.
  - Because the output components have dependency, they should be considered globally. 真正重要的不是你產生什麼component,而是component之間的關係



<u>Sentence</u> Generation 這個婆娘不是人

九天玄女下凡塵



## Structured Learning Approach

#### component分開去產生的物件

#### **Generator**

Learn to generate the object at the component level



一個一個產生,不知道大局觀

從整體的方向來看到底好不好

#### Discriminator

Evaluating the whole object, and find the best one



Top Down

大局觀,判斷整體而言是不是正確的

#### Outline

Basic Idea of GAN

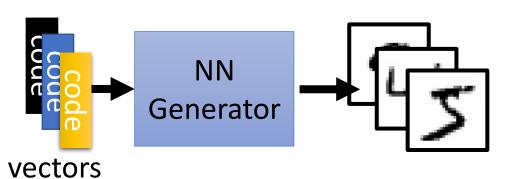
GAN as structured learning

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#### Generator



code:

(where does they come from?)

Image:





$$\begin{bmatrix} 0.1 \\ 0.9 \end{bmatrix}$$



$$\begin{bmatrix} 0.2 \\ -0.1 \end{bmatrix}$$









$$\begin{bmatrix} 0.1 \\ 0.9 \end{bmatrix} \longrightarrow \begin{matrix} NN \\ Generator \end{matrix} \longrightarrow \begin{matrix} image \\ supervised learning \end{matrix}$$

As close as possible Classifier

#### Generator

NN Generator vectors

code:

(where does they come from?)

Image:

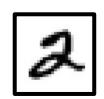
 $\begin{bmatrix} 0.1 \\ -0.5 \end{bmatrix}$ 



 $\begin{bmatrix} 0.1 \\ 0.9 \end{bmatrix}$ 



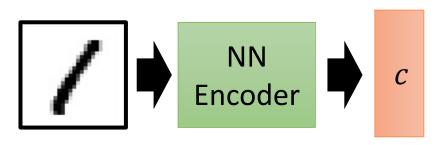
 $\begin{bmatrix} 0.2 \\ -0.1 \end{bmatrix}$ 

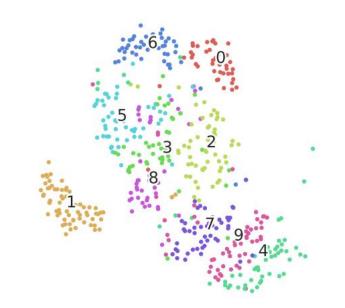


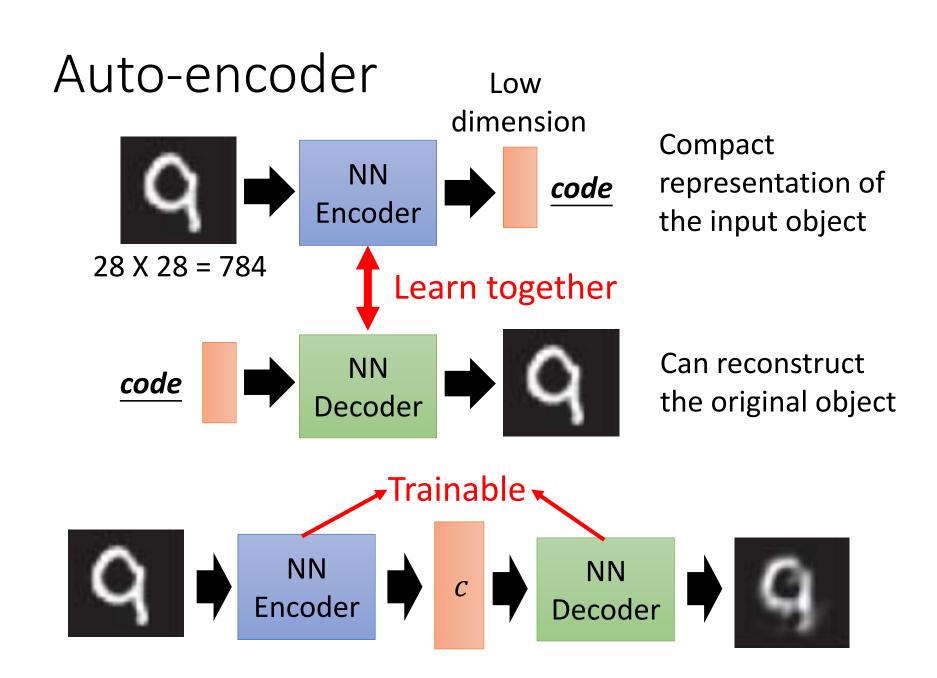
 $\begin{bmatrix} 0.3 \\ 0.2 \end{bmatrix}$ 

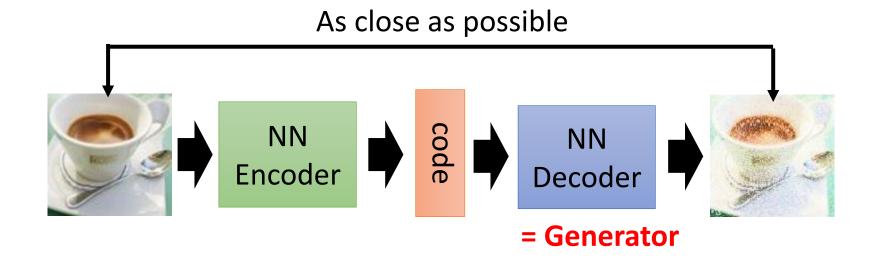


Encoder in auto-encoder provides the code ©







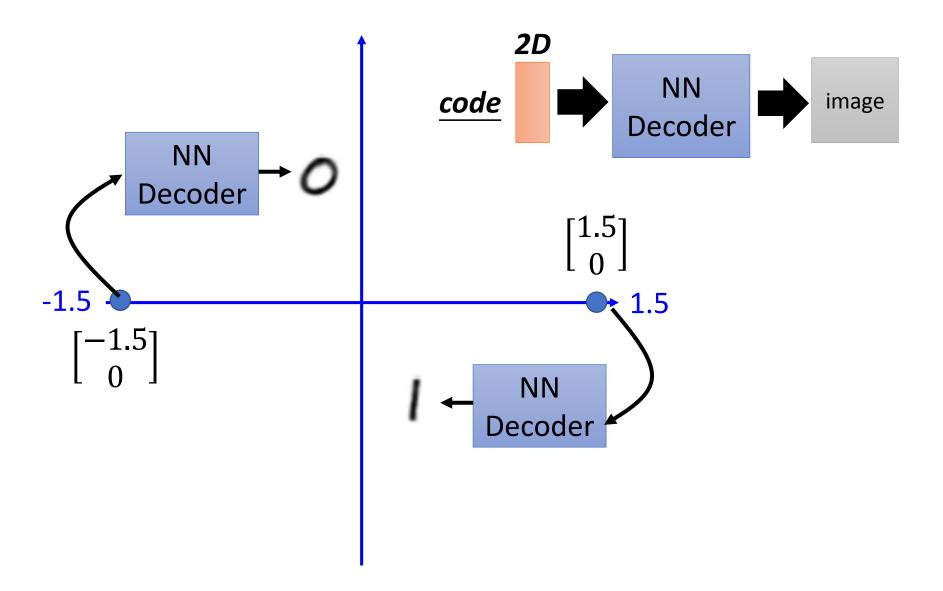


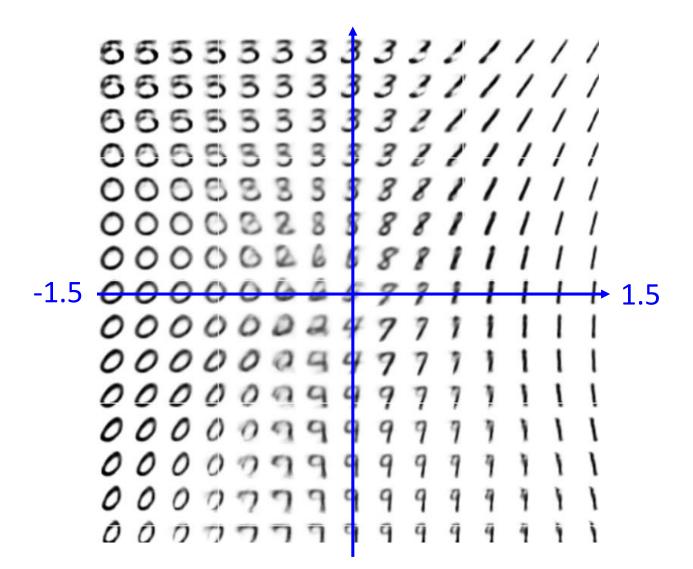
Randomly generate a vector as code

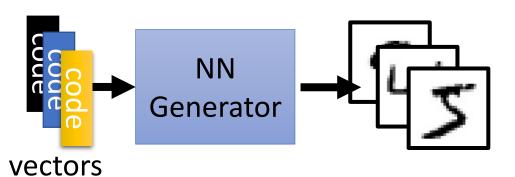
NN
Decoder

Image ?

Generator







code: (where does them

Image:

come from?)

 $\begin{bmatrix} 0.1 \\ -0.5 \end{bmatrix}$ 

 $\begin{bmatrix} 0.1 \\ 0.9 \end{bmatrix}$ 

 $\begin{bmatrix} 0.2 \\ -0.1 \end{bmatrix}$ 

 $\begin{bmatrix} 0.3 \\ 0.2 \end{bmatrix}$ 

/





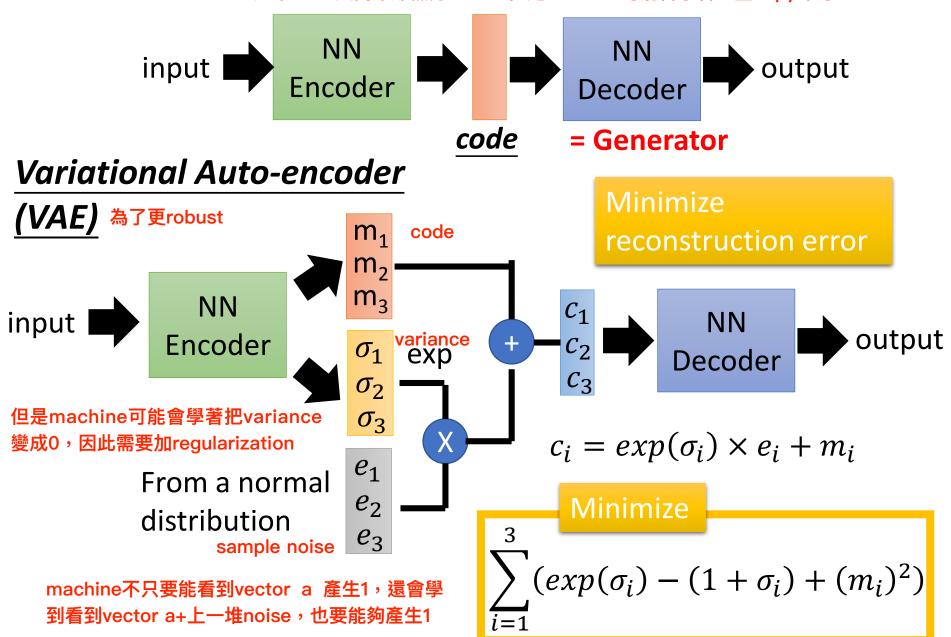


network是非線性的,所以不能直接weight sum

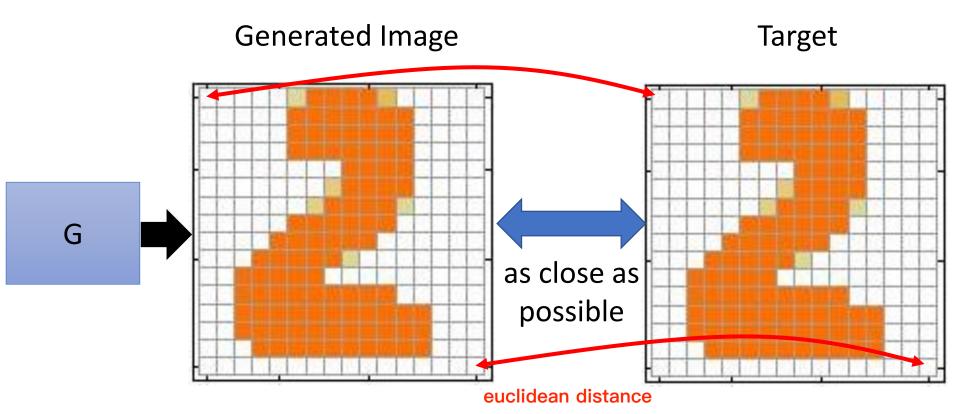
$$0.5x$$
 a  $+ 0.5x$  b  $\longrightarrow$  NN Generator  $\longrightarrow$  ? 可能是noise

相信這些high dimension的影像的manifold其實就是這個code

如果code太高維雖然好train,但是machine可能會學著一直copy即可



### What do we miss?

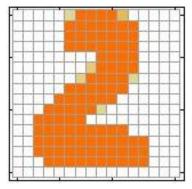


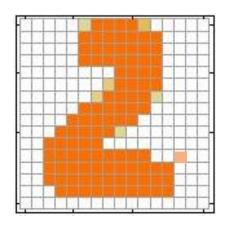
It will be fine if the generator can truly copy the target image. What if the generator makes some mistakes ......

Some mistakes are serious, while some are fine.

### What do we miss?

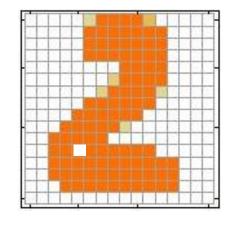
Target





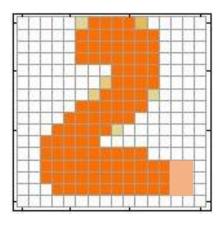
1 pixel error

我覺得不行



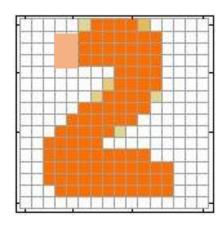
1 pixel error

我覺得不行



6 pixel errors

我覺得其實可以

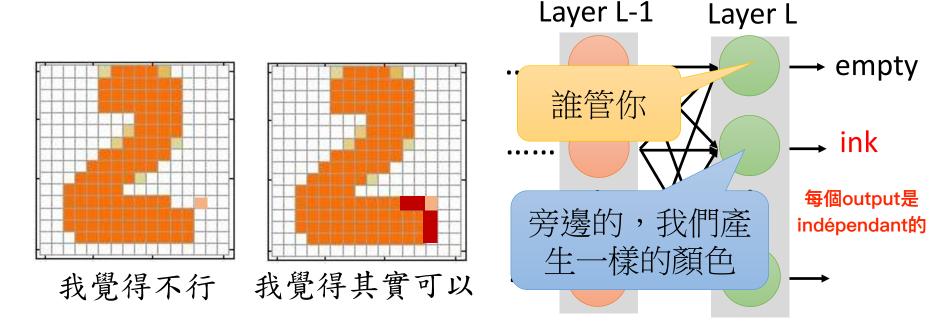


6 pixel errors

我覺得其實 可以

### What do we miss?

Each neural in output layer corresponds to a pixel.



The relation between the components are critical.

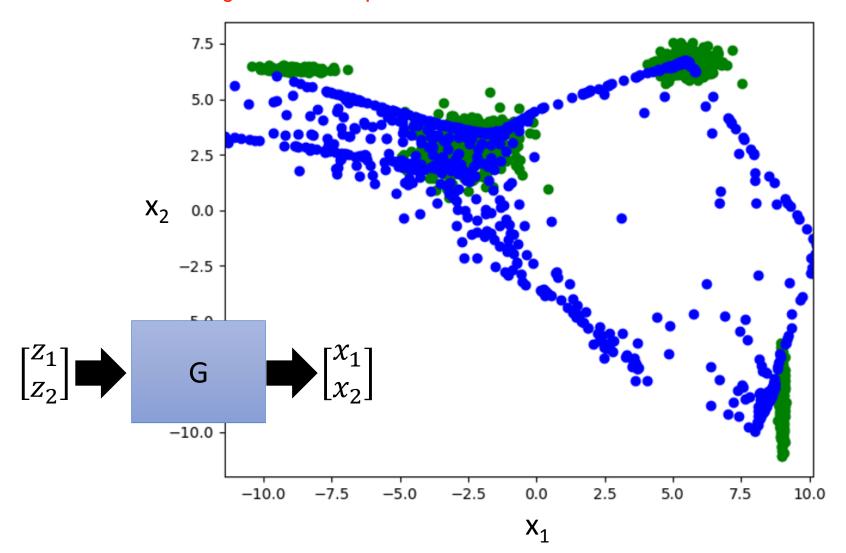
Although highly correlated, they cannot influence each other.

Need deep structure to catch the relation between components.

如果今天train一個GAN vs auto-encoder,往往auto-encoder的架構要更深才能達到接近GAN的結果

### (Variational) Auto-encoder

對generator要考慮pixel之間的correlation是很難的



### Outline

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GAN as structured learning

Can Generator learn by itself?

Can Discriminator generate?

A little bit theory

## Evaluation function, Potential Function, Energy Function ...

Discriminator is a function D (network, can deep)

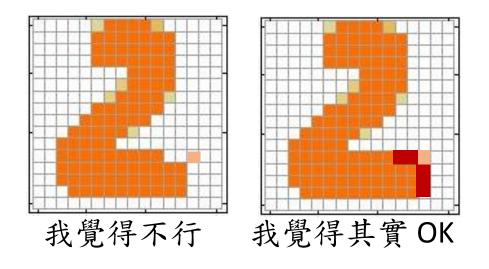
$$D: X \to R$$

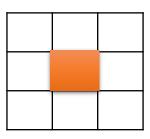
- Input x: an object x (e.g. an image)
- Output D(x): scalar which represents how "good" an object x is



Can we use the discriminator to generate objects?

• It is easier to catch the relation between the components by top-down evaluation.





This CNN filter is good enough.

### Inference

ullet Generate object  $ilde{x}$  that

$$\widetilde{x} = \arg \max_{x \in X} D(x)$$

Enumerate all possible x !!!

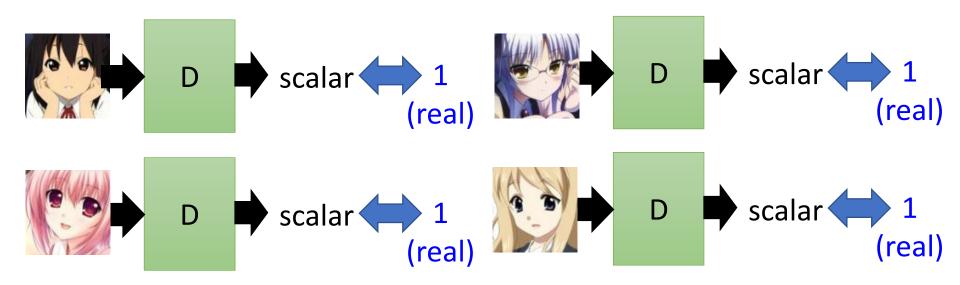
It is feasible ???

How to learn the discriminator?

D是擅長批評的,因此生成東西很痛苦

data只有positive example的情況

I have some real images

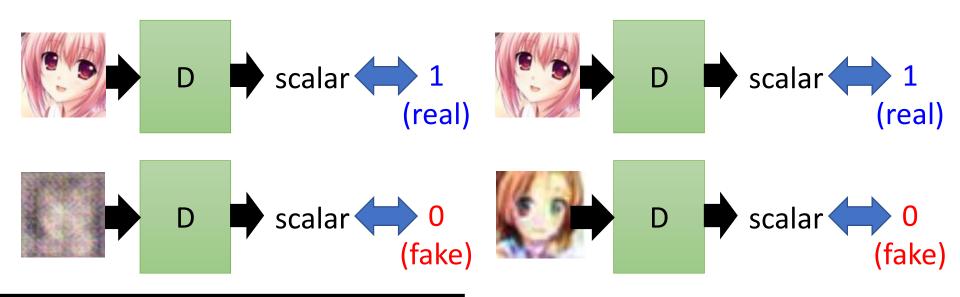


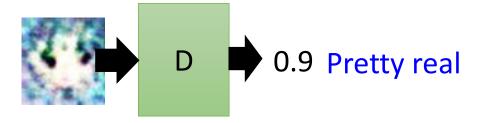
Discriminator only learns to output "1" (real).

Discriminator training needs some negative examples.

如何產生好的negative example,這樣D才能真的學會辨別 好的negative example就是逼近真實的negative example

Negative examples are critical.





How to generate realistic negative examples?

### General Algorithm



- Given a set of positive examples, randomly generate a set of negative examples.
- In each iteration



 Learn a discriminator D that can discriminate positive and negative examples.



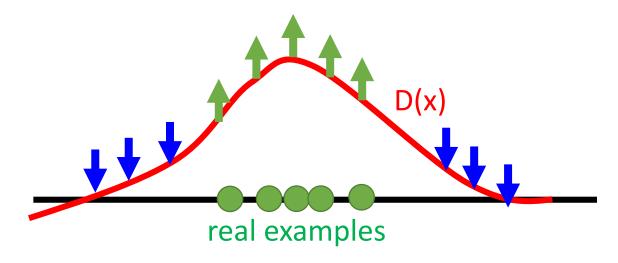




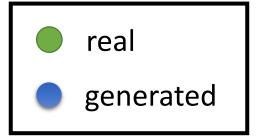
Generate negative examples by discriminator D

$$\widetilde{x} = \arg\max_{x \in X} D(x)$$

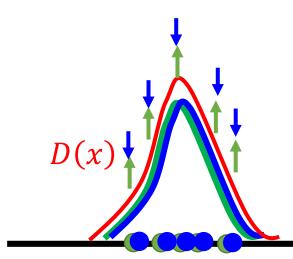


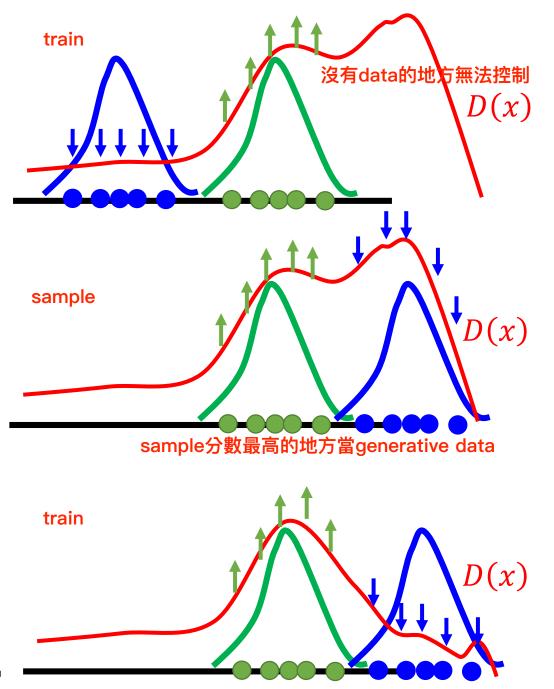


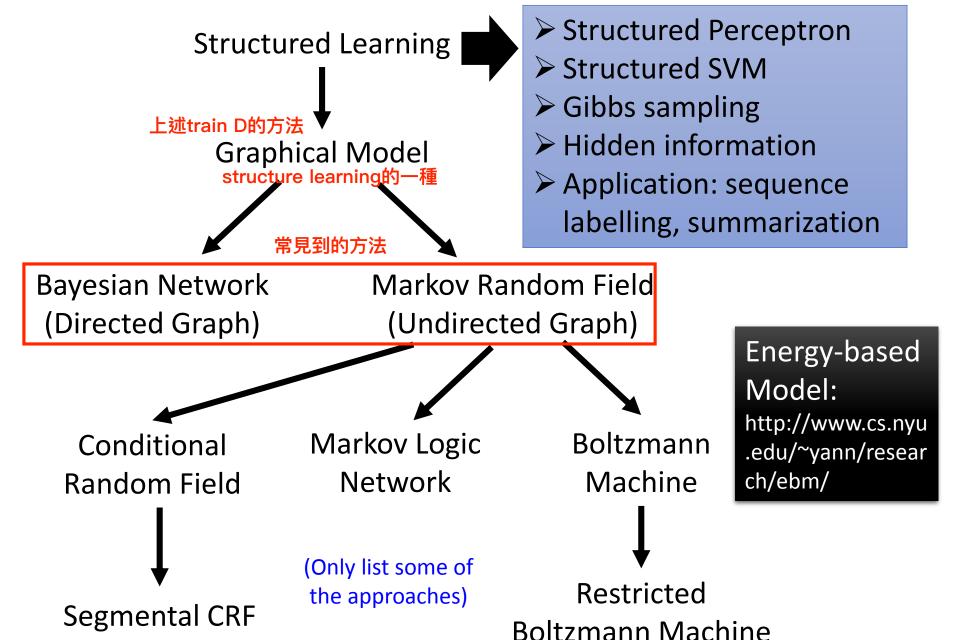
In practice, you cannot decrease all the x other than real examples.



In the end .....







### Generator v.s. Discriminator

### Generator

- Pros: 容易生成
  - Easy to generate even with deep model
- Cons:

  - 不容易考慮component之間的correlation
     Imitate the appearance
  - Hard to learn the correlation between components

### **Discriminator**

- 可以考慮大局 • Pros:
  - Considering the big picture
- Cons: 生個東西真的千難萬難
  - Generation is not always feasible
    - Especially when your model is deep
  - How to do negative sampling?

要假設D是線性的才能去解argmax問題 但是假設線性的又限制他的能力

### Generator + Discriminator

generator就是在學怎麼解argmax Generator可以取代解argmax這個problem

### General Algorithm



- Given a set of positive examples, randomly generate a set of negative examples.
- In each iteration



 Learn a discriminator D that can discriminate positive and negative examples.



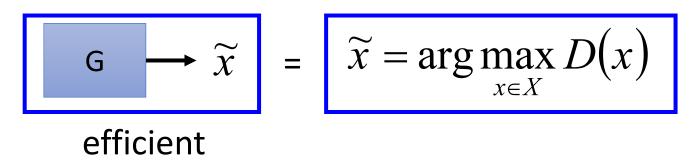


Generate negative examples by discriminator D

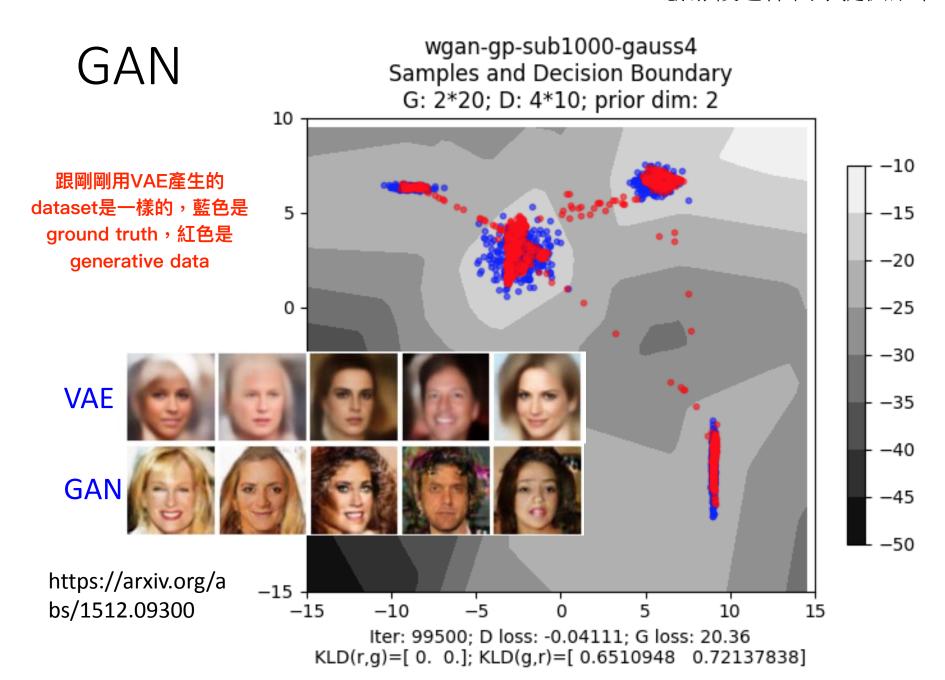
$$\longrightarrow \widetilde{x} = \widetilde{x} = \arg \max_{x \in X} D(x)$$

### Benefit of GAN

- From Discriminator's point of view
  - Using generator to generate negative samples

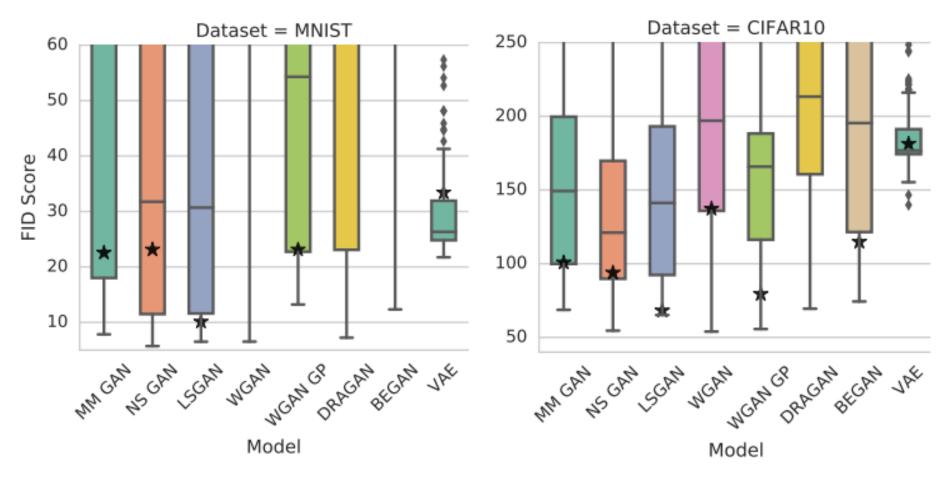


- From Generator's point of view
  - Still generate the object component-bycomponent
  - But it is learned from the discriminator with global view.



### [Mario Lucic, et al. arXiv, 2017]

### 調整不同參數後得到的結果,可以發現GAN的變化是很大的但是upper bound比較好值得一提的是VAE相較起來穩定許多



比較各種不同的GAN的結果

結論是結果都差不多

FID[Martin Heusel, et al., NIPS, 2017]: Smaller is better

google 的paper

FID越小代表越像真實的圖片

### Next Time

- Preview
  - https://youtu.be/0CKeqXI5IY0
  - https://youtu.be/KSN4QYgAtao

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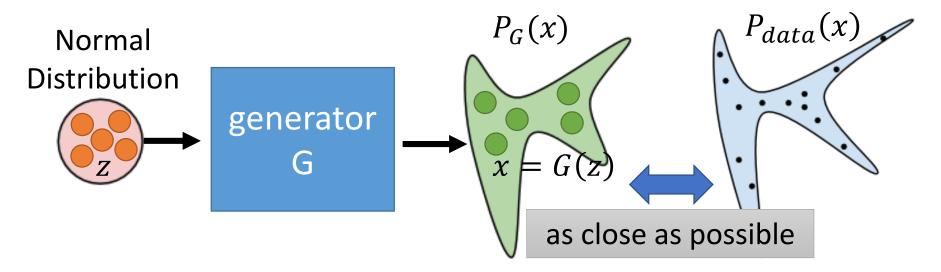
Can Discriminator generate?

A little bit theory

### Generator

x: an image (a high-dimensional vector)

• A generator G is a network. The network defines a probability distribution  $P_G$ 

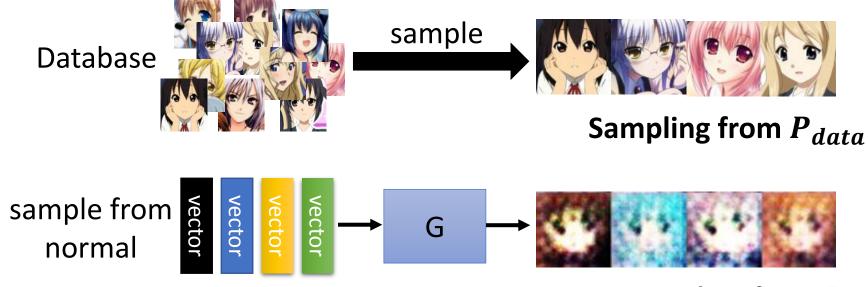


$$G^* = arg \min_{G} \underline{Div(P_G, P_{data})}$$

Divergence between distributions  $P_G$  and  $P_{data}$ How to compute the divergence?

$$G^* = arg \min_{G} Div(P_G, P_{data})$$

Although we do not know the distributions of  $P_G$  and  $P_{data}$ , we can sample from them.



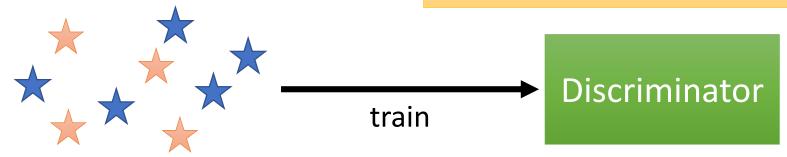
Sampling from  $P_G$ 

$$G^* = arg \min_{G} Div(P_G, P_{data})$$

 $\star$  : data sampled from  $P_{data}$ 

 $\uparrow$  : data sampled from  $P_G$ 

Using the example objective function is exactly the same as training a binary classifier.



**Example** Objective Function for D

$$V(G,D) = E_{x \sim P_{data}}[logD(x)] + E_{x \sim P_G}[log(1 - D(x))]$$
(G is fixed)

Training: 
$$D^* = arg \max_{D} V(D, G)$$

The maximum objective value is related to JS divergence.

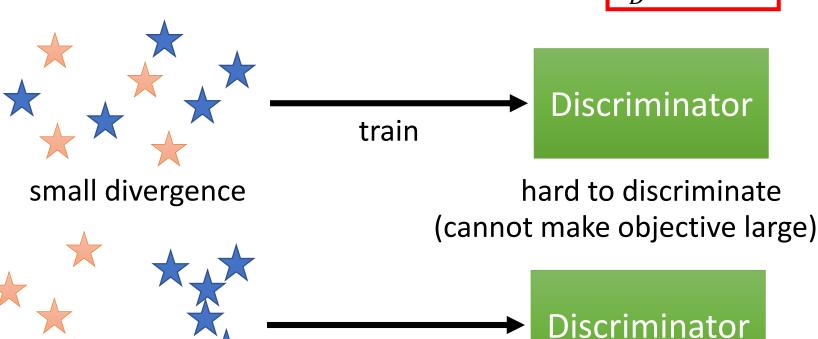
Discriminator 
$$G^* = arg \min_{G} Div(P_G, P_{data})$$

 $\star$ : data sampled from  $P_{data}$ 

: data sampled from  $P_G$ 

### **Training:**

$$D^* = \arg\max_{D} V(D, G)$$



train

large divergence

easy to discriminate

$$G^* = arg \min_{G} \max_{D} V(G, D)$$

$$D^* = \arg\max_{D} V(D, G)$$

The maximum objective value is related to JS divergence.

- Initialize generator and discriminator
- In each training iteration:

**Step 1**: Fix generator G, and update discriminator D

Step 2: Fix discriminator D, and update generator G

### Can we use other divergence?

Name	$D_f(P  Q)$	Generator $f(u)$
Total variation	$\frac{1}{2} \int  p(x) - q(x)   \mathrm{d}x$	$\frac{1}{2} u-1 $
Kullback-Leibler	$\int p(x) \log \frac{p(x)}{q(x)} dx$	$u \log u$
Reverse Kullback-Leibler	$\int q(x) \log \frac{\hat{q}(x)}{p(x)} dx$	$-\log u$
Pearson $\chi^2$	$\int \frac{(q(x)-p(x))^2}{p(x)} dx$	$(u-1)^2$
Neyman $\chi^2$	$\int \frac{(p(x) - q(x))^2}{q(x)}  \mathrm{d}x$	$\frac{(1-u)^2}{u}$
Squared Hellinger	$\int \left(\sqrt{p(x)} - \sqrt{q(x)}\right)^2 dx$	$\left(\sqrt{u}-1\right)^2$
Jeffrey	$\int (p(x) - q(x)) \log \left(\frac{p(x)}{q(x)}\right) dx$	$(u-1)\log u$
Jensen-Shannon	$ \frac{1}{2} \int p(x) \log \frac{2p(x)}{p(x) + q(x)} + q(x) \log \frac{2q(x)}{p(x) + q(x)} dx  \int p(x) \pi \log \frac{p(x)}{\pi p(x) + (1 - \pi)q(x)} + (1 - \pi)q(x) \log \frac{q(x)}{\pi p(x) + (1 - \pi)q(x)} dx  \int p(x) \log \frac{2p(x)}{p(x) + q(x)} + q(x) \log \frac{2q(x)}{p(x) + q(x)} dx - \log(4) $	$-(u+1)\log\frac{1+u}{2} + u\log u$
Jensen-Shannon-weighted	$\int p(x)\pi \log \frac{p(x)}{\pi p(x) + (1-\pi)q(x)} + (1-\pi)q(x) \log \frac{q(x)}{\pi p(x) + (1-\pi)q(x)} dx$	$\pi u \log u - (1 - \pi + \pi u) \log(1 - \pi + \pi u)$
GAN	$\int p(x) \log \frac{2p(x)}{p(x) + q(x)} + q(x) \log \frac{2q(x)}{p(x) + q(x)} dx - \log(4)$	$u\log u - (u+1)\log(u+1)$

# Using the divergence you like ©

Conjugate $f^*(t)$
t
$\exp(t-1)$
$-1 - \log(-t)$
$\frac{1}{4}t^2 + t_{\underline{}}$
$\frac{1}{2} - 2\sqrt{1-t}$
$\frac{t}{1-t}$
$W(e^{1-t}) + \frac{1}{W(e^{1-t})} + t - 2$ $-\log(2 - \exp(t))$
$-\log(2-\exp(t))$
$(1-\pi)\log\frac{1-\pi}{1-\pi e^{t/\pi}}$
$-\log(1-\exp(t))$
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