Final Project

Christophe Hunt May 13, 2017

Contents

1	Variable	2
	1.1 Variable Picked	2
2	Probability 2.1 a. $P(X>x Y>y)$	2 3 3 4
3	Descriptive and Inferential Statistics. 3.1 Univariate descriptive statistics and plots	5 5 6 7 8
4	Linear Algebra and Correlation. 4.1 Correlation Matrix	9 9 9
5	Calculus-Based Probability & Statistics 5.1 Location Shift	10 10 11 12 13
6	Modeling 6.1 Regression model. 6.2 Variable Selection 6.3 Variable Subset Matrix 6.4 First Model 6.5 Final Model 6.6 Prediction results with test data set using final model 6.7 Prediction results	14 14 22 22 26 28 30 31

1 Variable

Pick one of the quantitative independent variables from the training data set (train.csv), and define that variable as X.

Pick SalePrice as the dependent variable, and define it as Y for the next analysis.

1.1 Variable Picked

The variable we will set to X is LotArea, which is defined as the Lot size in square feet. I chose LotArea because an anecdotal assumption is that the larger the lot size is the higher the sale price. However, living in NYC, I know that tiny lots in very desirable places have sold for a high price so I believe there may be some interesting variability.

2 Probability

Calculate as a minimum the below probabilities a through c.

Assume the small letter "x" is estimated as the 4th quartile of the X variable, and the small letter "y" is estimated as the 2nd quartile of the Y variable. Interpret the meaning of all probabilities.

2.1 a. P(X > x | Y > y)

2.2 b. P(X > x, Y > y)

2.3 c. P(X < x | Y > y)

[1] 0.6876712

Does splitting the training data in this fashion make them independent?

In other words, does P(X|Y) = P(X)P(Y)?

I am understanding this to mean does the probability of X>x given Y>y, which was answered for in part a. above, equal the probability of X>x mutiplied by Y>y

2.4 Mathematical Check for P(X|Y) = P(X)P(Y)

```
X <- sum(prob.y.x$greaterLotArea)/ nrow(prob.y.x)
Y <- sum(prob.y.x$greaterSalePrice) / nrow(prob.y.x)
X * Y

## [1] 0.1875
a == (X * Y)

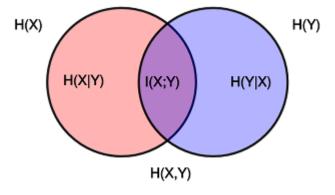
## [1] FALSE</pre>
```

2.5 Chi Square test for association.

```
## Pearson's Chi-squared test with Yates' continuity correction
##
## data: prob.table
## X-squared = 728, df = 1, p-value < 2.2e-16</pre>
```

We see that the p-value is quite low, lower than the assumptive .05, so we therefore reject the null hypothesis that the values are independent of each other.

The below venn diagram from Wikipedia may provide a clearer understanding of the differences in these measures:



¹By KonradVoelkel (Own work) [Public domain], via Wikimedia Commons

3 Descriptive and Inferential Statistics.

3.1 Univariate descriptive statistics and plots

3.1.1 Lot Area

					ı varı	iabies	140	u ubs	ervatio	ons				
LotArea											d	I		
n 1460	missing 0	distinct 1073	Info 1	Mean 10517	Gmd 5718	.05 3312	.10 5000	.25 7554		.75 11602	.90 14382	.95 17401		
lowest :	1300	1477	1491	1526	1533, h	ighest:	70761	115149	159000	164660 2	15245			

The histogram in the upper right corner of the table shows a right skewed distribution, which is not surprising since houses in cities would likely have similar lot areas versus instances of varied rural large lot areas.

3.1.2 Sale Price

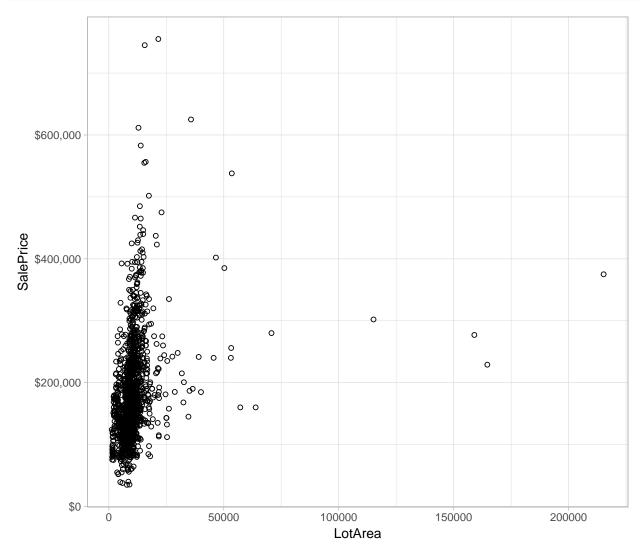
```
description <- describe(sub.train.df["SalePrice"], descript = "SalePrice")
latex(description, file = '')</pre>
```

	SalePrice 1 Variables 1460 Observations												
SalePı	ice												
n 1460	missing 0	distinct 663	Info 1	Mean 180921	Gmd 81086	.05 88000	.10 106475	.25 129975	.50 163000	.75 214000	.90 278000	.95 326100	
lowest :	34900	35311 3790	0 3930	40000,	highest:	582933	611657 6250	000 745000	755000				

As we can see from the histogram the shape of the data is near normal. It is interesting to visualize that lot area does not follow the same shape, this would hold with our original assumption that where the house is located has more impact than the size of the lot area.

3.2 Scatterplot of X and Y

```
ggplot(sub.train.df, aes(x = LotArea, y = SalePrice)) +
    geom_point(shape=1) +
    theme_light() +
    scale_y_continuous(labels = dollar)
```



I expected this type of scatter plot based on my anecdotal assumption of cities vs rural areas. I would think that the differences within the city limits have high variance in price but less variation in lot area. My assumption is that the large lot areas at the mid sale price is likely in a rural area.

3.3 Box-Cox transformations.

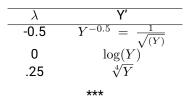
I am using the BoxCox.lambda function from the forecast package to determine the necessary transformations for the two variables.

```
library(forecast)
library(knitr)
l1 <- BoxCox.lambda(as.numeric(sub.train.df$SalePrice))
l2 <- BoxCox.lambda(as.numeric(sub.train.df$LotArea))

lamdas <- c(l1, l2)
Variables <- c("SalePrice", "LotArea")
dfBoxCox <- as.data.frame(cbind(round(as.numeric(lamdas),4), Variables))
colnames(dfBoxCox) <- c("$\\lambda$", "Variables")
kable(dfBoxCox, align = c("c", "c"))</pre>
```

λ	Variables
-0.3308	SalePrice
-0.1268	LotArea

Common Box-Cox Transformations^{2 3}



Lambda values were truncated to the nearest tenth that match a common transformation as per the below table.

variable	variable transformation
SalePrice	$SalePrice^{-0.5}$
LotArea	log(LotArea)

²Osborne, Jason W. "Improving your data transformations: Applying the Box-Cox transformation." Practical Assessment, Research & Evaluation 15.12 (2010): 1-9.

³By Understanding Both the Concept of Transformation and the Box-Cox Method, Practitioners Will Be Better Prepared to Work with Non-normal Data. "Making Data Normal Using Box-Cox Power Transformation." ISixSigma. N.p., n.d. Web. 29 Oct. 2016.

3.4 Correlation Analysis

3.4.1 Correlation analysis and interpetation

```
sub.train.df.trans <- sub.train.df %>%
                      mutate(SalePrice = SalePrice^(-.5),
                             LotArea = log(LotArea))
sub.train.cor <- cor.test(sub.train.df.trans$SalePrice,</pre>
                          sub.train.df.trans$LotArea,
                          method = "pearson", conf.level = .99)
sub.train.cor
##
##
   Pearson's product-moment correlation
##
## data: sub.train.df.trans$SalePrice and sub.train.df.trans$LotArea
## t = -15.968, df = 1458, p-value < 2.2e-16
## alternative hypothesis: true correlation is not equal to 0
## 99 percent confidence interval:
## -0.4417063 -0.3269282
## sample estimates:
##
          cor
## -0.3858091
```

The p-value of the correlation test is 2.2e-16 which is less than the significance level of alpha at .05. We are using the standard alpha as there is no indication another any other value for alpha should be used. We can therefore say that the log of lot size and sale price raised to the -.5 power are significantly correlated with a negative correlation coefficient of -0.386.

3.4.2 Null hypothesis test at a 99% confidence interval.

The correlation test has specifically done that for us and we can safely reject the null hypothesis as we see that our 99% confidence interval exists at the values (-0.441, -0.327) with a p-value < 2.2e-16.

3.4.3 Analysis Discussion

This means two possible things could have occured, there is no correlation and this data set is pulled from an unusual set of house sales. Or, more likely with the values obtained, our assumption of 0 correlation is incorect and we have obtained a very typical data set and must reject the null hypothesis because correlation does exist.

4 Linear Algebra and Correlation.

4.1 Correlation Matrix

A <- cor(sub.train.df.trans) kable(A)

	SalePrice	LotArea
SalePrice LotArea	1.0000000 -0.3858091	-0.3858091 1.0000000

4.2 Inverted correlation matrix (percision matrix)

B <- solve(A)
kable(B)</pre>

	SalePrice	LotArea
SalePrice	1.1748792	0.4532792
LotArea	0.4532792	1.1748792

4.3 Multiply the correlation matrix by the precision matrix, and then multiply the precision matrix by the correlation matrix.

corr.by.pre.M <- A %*% B
kable(corr.by.pre.M)</pre>

	SalePrice	LotArea
SalePrice	1	0
LotArea	0	1

pre.by.corr.M <- B %*% A
kable(pre.by.corr.M)</pre>

	SalePrice	LotArea
SalePrice	1	0
LotArea	0	1

5 Calculus-Based Probability & Statistics

5.1 Location Shift

Many times, it makes sense to fit a closed form distribution to data. For your non-transformed independent variable, location shift it so that the minimum value is above zero.

min(sub.train.df\$LotArea)

[1] 1300

For the independent variable chosen, there are no zero values observed. This makes sense as we would expect the lot area to have some value and I would expect it to never be unobserved (an assumption that at least estimates would be used without a true figure).

However, if a shift was required something like the below could be used.

shift <- sub.train.df\$LotArea + 1</pre>

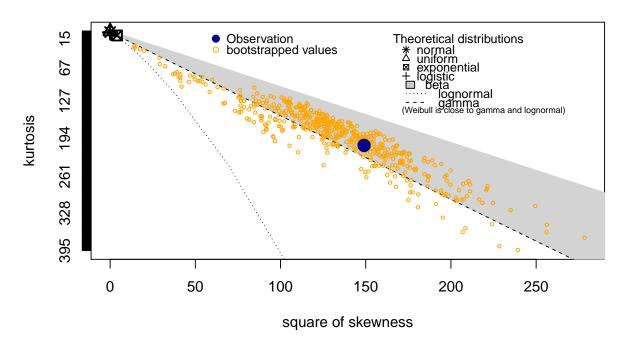
5.2 Mass and fitdistr

Then load the MASS package and run fitdistr to fit a density function of your choice. (See https://stat.ethz. ch/R-manual/R-devel/library/MASS/html/fitdistr.html).

5.2.1 Best fit distribution.

```
library(fitdistrplus)
descdist(sub.train.df$LotArea, discrete=FALSE, boot=500)
```

Cullen and Frey graph



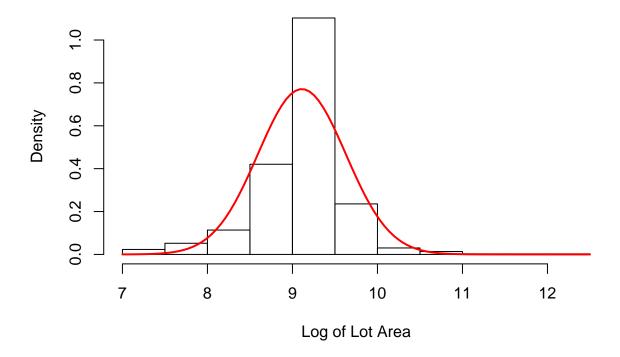
```
## summary statistics
## -----
## min: 1300 max: 215245
## median: 9478.5
## mean: 10516.83
## estimated sd: 9981.265
## estimated skewness: 12.20769
## estimated kurtosis: 206.2433
```

5.3 Fitting Distribution

There were too many issues in attempting to fit the beta distribution so the next best theoretical distribution was used - log normal.

```
library(MASS)
fit.log <- fitdistr(sub.train.df$LotArea, densfun = "log-normal")
fit.log

## meanlog sdlog
## 9.110838240 0.517270830
## (0.013537596) (0.009572526)
hist(log(sub.train.df$LotArea), prob=TRUE, xlab = "Log of Lot Area", main = "")
curve(dnorm(x, fit.log$estimate[1], fit.log$estimate[2]), col="red", lwd=2, add=T)</pre>
```



Our density plot indicates that the log normal distribution fits quite well.

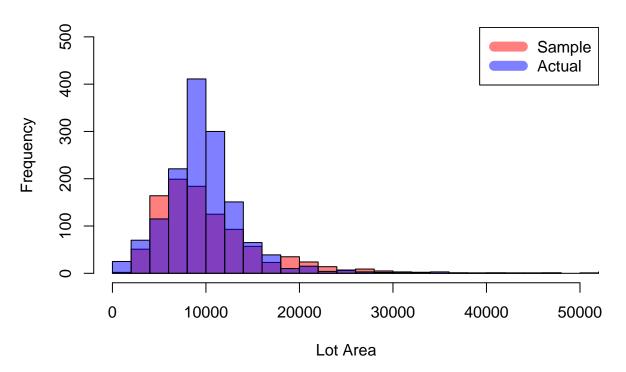
5.4 Sampling

Find the optimal value of the parameters for this distribution, and then take 1000 samples from this distribution (e.g., rexp(1000) for an exponential).

```
set.seed(1234)
sample <- rlnorm(1000, meanlog = fit.log$estimate[1], sdlog = fit.log$estimate[2])</pre>
```

Plot a histogram and compare it with a histogram of your non-transformed original variable.

Overlapping Histogram



It is clear that the distributions are very similar. Plotting them together gives a clear visual of how similar the distributions are and note that x has been limited to not extend to extreme values.

6 Modeling

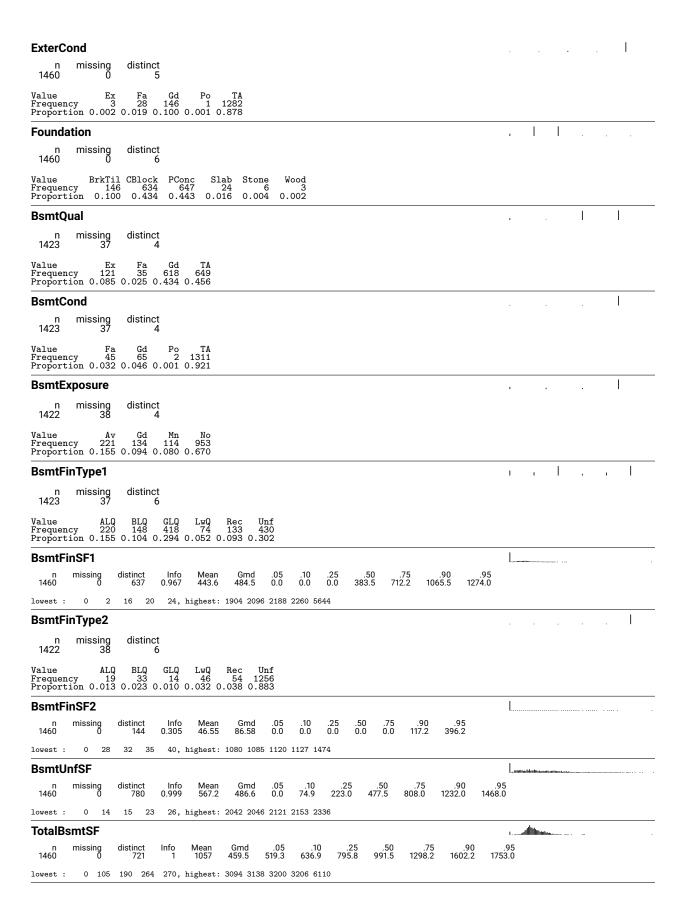
6.1 Regression model.

6.1.1 Variable Exploration

description <- describe(train.df %>% dplyr::select(-Id, -SalePrice), descript = "Training Data Set") latex(description, file = '') **Training Data Set** 1460 Observations 79 Variables **MSSubClass** missing Mean 56.9 Gmd 43.19 distinct 15 Info 0.94 .05 20 .10 20 1460 Value 190 Frequency 30 Proportion 0.021 **MSZoning** distinct missing 1460 Value C (all) Frequency 10 Proportion 0.007 FV 65 0.045 RH 16 0.011 LotFrontage distinct Info Mean 70.05 Gmd .05 .10 50 90 .95 107 80 96 0.998 24.61 69 lowest: 21 24 30 32 33, highest: 160 168 174 182 313 LotArea distinct 1073 .90 14382 n 1460 Mean 10517 Gmd 5718 .05 3312 .10 5000 .25 7554 .50 9478 .95 17401 missing Info .75 11602 lowest : 1300 1477 1491 1526 1533, highest: 70761 115149 159000 164660 215245 Street distinct 2 n 1460 missing Value Grvl Pave Frequency 6 1454 Proportion 0.004 0.996 Alley missing 1369 distinct n 91 Grvl Pave Frequency 50 41 Proportion 0.549 0.451 LotShape n 1460 missing distinct Value IR1 IR2 IR3 Reg Frequency 484 41 10 925 Proportion 0.332 0.028 0.007 0.634

LandContour						
n missing distinct 1460 0 4						
Value Bnk HLS Low Lv1 Frequency 63 50 36 1311 Proportion 0.043 0.034 0.025 0.898						
Utilities						
n missing distinct 1460 0 2						
Value AllPub NoSeWa Frequency 1459 1 Proportion 0.999 0.001						
LotConfig	, , , , <u>l</u>					
n missing distinct 1460 0 5						
Value Corner CulDSac FR2 FR3 Inside Frequency 263 94 47 4 1052 Proportion 0.180 0.064 0.032 0.003 0.721						
LandSlope	1					
n missing distinct 1460 0 3						
Value Gt1 Mod Sev Frequency 1382 65 13 Proportion 0.947 0.045 0.009						
Neighborhood						
n missing distinct 1460 0 25						
lowest : Blmngtn Blueste BrDale BrkSide ClearCr, highest: Somerst StoneBr SWISU Timber	Veenker					
Condition1						
n missing distinct 1460 0 9						
n missing distinct						
n missing distinct 1460 0 9 Value Artery Feedr Norm Posa Posn RRAe RRAn RRNe RRNn Frequency 48 81 1260 8 19 11 26 2 5	l					
n missing distinct 1460 0 9 Value Artery Feedr Norm PosA PosN RRAe RRAn RRNe RRNn Frequency 48 81 1260 8 19 11 26 2 5 Proportion 0.033 0.055 0.863 0.005 0.013 0.008 0.018 0.001 0.003	l					
n missing distinct 1460 0 9 9	l					
n missing distinct 1460 0 0 9 Value Artery Feedr Norm Posa Posn RRAe RRAn RRNe RRNn Frequency 48 81 1260 8 19 11 26 2 5 Proportion 0.033 0.055 0.863 0.005 0.013 0.008 0.018 0.001 0.003 Condition2 n missing distinct 1460 0 8 Value Artery Feedr Norm Posa Posn RRAe RRAn RRNn Frequency 2 6 1445 1 2 1 1 2	l					
n missing distinct 1460 0 0 9 Value Artery Feedr Norm Posa Posn RRAe RRAn RRNe RRNn Prequency 48 81 1260 8 19 11 26 2 5 Proportion 0.033 0.055 0.863 0.005 0.013 0.008 0.018 0.001 0.003 Condition2 n missing distinct 1460 0 8 Value Artery Feedr Norm Posa Posn RRAe RRAn RRNn Frequency 2 6 1445 1 2 1 1 2 Proportion 0.001 0.004 0.990 0.001 0.001 0.001 0.001 0.001	l					
Norm	l					
Norm	1					
Norm						
Nature						
Name						
National Parameters National Parameters	1					

OverallCond	
n missing distinct Info Mean Gmd 1460 0 9 0.814 5.575 1.111	
Value 1 2 3 4 5 6 7 8 9 Frequency 1 5 25 57 821 252 205 72 22 Proportion 0.001 0.003 0.017 0.039 0.562 0.173 0.140 0.049 0.015	
YearBuilt	
n missing distinct Info Mean Gmd .05 .10 .25 .50 .75 1460 0 112 1 1971 33.88 1916 1925 1954 1973 2000	.90 .95 2006 2007
lowest : 1872 1875 1880 1882 1885, highest: 2006 2007 2008 2009 2010	
YearRemodAdd n missing distinct Info Mean Gmd .05 .10 .25 .50 .75	.90 .95
1460 0 61 0.997 1985 23.05 1950 1967 1994 2004	2006 2007
lowest : 1950 1951 1952 1953 1954, highest: 2006 2007 2008 2009 2010	
RoofStyle	
n missing distinct 1460 0 6	
Value Flat Gable Gambrel Hip Mansard Shed Frequency 13 1141 11 286 7 2 Proportion 0.009 0.782 0.008 0.196 0.005 0.001	
RoofMatl	. 1
n missing distinct 1460 0 8	
Value ClyTile CompShg Membran Metal Roll Tar&Grv WdShake WdShngl Frequency 1 1434 1 1 1 1 5 6 Proportion 0.001 0.982 0.001 0.001 0.001 0.003 0.004	
Exterior1st	
n missing distinct 1460 0 15	
Value AsbShng AsphShn BrkComm BrkFace CBlock CemntBd HdBoard ImStuce MetalSd Prequency Proportion 20 1 2 50 1 61 222 1 220 Proportion 0.014 0.001 0.001 0.034 0.001 0.042 0.152 0.001 0.151	lywood 108 0.074
Value Stone Stucco VinylSd Wd Sdng WdShing Frequency 2 25 515 206 26 Proportion 0.001 0.017 0.353 0.141 0.018	
Exterior2nd	
n missing distinct 1460 0 16	
Value AsbShng AsphShn Brk Cmn BrkFace CBlock CmentBd HdBoard ImStuce MetalSd Frequency 20 3 7 25 1 60 207 10 214 Proportion 0.014 0.002 0.005 0.017 0.001 0.041 0.142 0.007 0.147	Other 1 0.001
Value Plywood Stone Stucco VinylSd Wd Sdng Wd Shng Frequency 142 5 26 504 197 38 Proportion 0.097 0.003 0.018 0.345 0.135 0.026	
MasVnrType	. ı l .
n missing distinct 1452 8 4	
Value BrkCmn BrkFace None Stone Frequency 15 445 864 128 Proportion 0.010 0.306 0.595 0.088	
MasVnrArea	L
n missing distinct Info Mean Gmd .05 .10 .25 .50 .75 .90 1452 8 327 0.791 103.7 156.9 0 0 0 0 166 335	.95 456
lowest: 0 1 11 14 16, highest: 1115 1129 1170 1378 1600	
ExterQual	
n missing distinct 1460 0 4	
Value Ex Fa Gd TA Frequency 52 14 488 906 Proportion 0.036 0.010 0.334 0.621	



Heating	. 1
n missing distinct 1460 0 6	
Value Floor GasA GasW Grav OthW Wall Frequency 1 1428 18 7 2 4 Proportion 0.001 0.978 0.012 0.005 0.001 0.003	
HeatingQC	l
n missing distinct 1460 0 5	
Value Ex Fa Gd Po TA Frequency 741 49 241 1 428 Proportion 0.508 0.034 0.165 0.001 0.293	
CentralAir	
n missing distinct 1460 0 2	
Value N Y Frequency 95 1365 Proportion 0.065 0.935	
Electrical	
n missing distinct 1459 1 5	
Value FuseA FuseF FuseP Mix SBrkr Frequency 94 27 3 1 1334 Proportion 0.064 0.019 0.002 0.001 0.914	
X1stFirSF	
n missing distinct Info Mean Gmd .05 .10 .25 .50 .75 .90 1460 0 753 1 1163 416.4 673.0 756.9 882.0 1087.0 1391.2 1680.0	.95 1831.2
lowest : 334 372 438 480 483, highest: 2633 2898 3138 3228 4692	
X2ndFlrSF	
n missing distinct Info Mean Gmd .05 .10 .25 .50 .75 .90 .95 1460 0 417 0.817 347 450.2 0.0 0.0 0.0 0.0 728.0 954.2 1141.0	
lowest: 0 110 167 192 208, highest: 1611 1796 1818 1872 2065	
LowQualFinSF	
n missing distinct Info Mean Gmd .05 .10 .25 .50 .75 .90 .95 1460 0 24 0.052 5.845 11.55 0 0 0 0 0 0 0	
lowest : 0 53 80 120 144, highest: 513 514 515 528 572	
GrLivArea	
n missing distinct Info Mean Gmd .05 .10 .25 .50 .75 .90 1460 0 861 1 1515 563.1 848 912 1130 1464 1777 2158	.95 2466
lowest: 334 438 480 520 605, highest: 3627 4316 4476 4676 5642	
BsmtFullBath	l
n missing distinct Info Mean Gmd 1460 0 4 0.733 0.4253 0.5085	
Value 0 1 2 3 Frequency 856 588 15 1 Proportion 0.586 0.403 0.010 0.001	
BsmtHalfBath	l
n missing distinct Info Mean Gmd 1460 0 3 0.159 0.05753 0.1088	
Value 0 1 2 Frequency 1378 80 2 Proportion 0.944 0.055 0.001	
FullBath	<u> </u>
n missing distinct Info Mean Gmd 1460 0 4 0.766 1.565 0.5521	
Value 0 1 2 3 Frequency 9 650 768 33 Proportion 0.006 0.445 0.526 0.023	

HalfBath	l
n missing distinct Info Mean Gmd 1460 0 3 0.706 0.3829 0.4852	
Value 0 1 2 Frequency 913 535 12 Proportion 0.625 0.366 0.008	
BedroomAbvGr	
n missing distinct Info Mean Gmd 1460 0 8 0.815 2.866 0.818	
Value 0 1 2 3 4 5 6 8 Frequency 6 50 358 804 213 21 7 1 Proportion 0.004 0.034 0.245 0.551 0.146 0.014 0.005 0.001	
KitchenAbvGr	. 1
n missing distinct Info Mean Gmd 1460 0 4 0.133 1.047 0.09174	
Value 0 1 2 3 Frequency 1 1392 65 2 Proportion 0.001 0.953 0.045 0.001	
KitchenQual	
n missing distinct 1460 0 4	
Value Ex Fa Gd TA Frequency 100 39 586 735 Proportion 0.068 0.027 0.401 0.503	
TotRmsAbvGrd	1
n missing distinct Info Mean Gmd .05 .10 .25 .50 .75 .90 .95 1460 0 12 0.958 6.518 1.762 4 5 5 6 7 9 10	
Value 2 3 4 5 6 7 8 9 10 11 12 14 Frequency 1 17 97 275 402 329 187 75 47 18 11 1 Proportion 0.001 0.012 0.066 0.188 0.275 0.225 0.128 0.051 0.032 0.012 0.008 0.001	
Functional	1
n missing distinct 1460 0 7	
Value Maj1 Maj2 Min1 Min2 Mod Sev Typ Frequency 14 5 31 34 15 1 1360 Proportion 0.010 0.003 0.021 0.023 0.010 0.001 0.932	
Fireplaces	l l
n missing distinct Info Mean Gmd 1460 0 4 0.806 0.613 0.6566	
Value 0 1 2 3 Frequency 690 650 115 5 Proportion 0.473 0.445 0.079 0.003	
FireplaceQu	1 . 1
n missing distinct 770 690 5	
Value Ex Fa Gd Po TA Frequency 24 33 380 20 313 Proportion 0.031 0.043 0.494 0.026 0.406	
GarageType	. l
n missing distinct 1379 81 6	
1379 8 6 Value 2Types Attchd Basment BuiltIn CarPort Detchd Frequency 6 870 19 88 9 387	
1379 8 6 Value 2Types Attchd Basment BuiltIn CarPort Detchd Frequency 6 870 19 88 9 387 Proportion 0.004 0.631 0.014 0.064 0.007 0.281	.95

GarageFinish	1	ı l
n missing distinct 1379 81 3		
Value Fin RFn Unf Frequency 352 422 605 Proportion 0.255 0.306 0.439		
GarageCars		i I
n missing distinct Info Mean Gmd 1460 0 5 0.802 1.767 0.7609		
Value 0 1 2 3 4 Frequency 81 369 824 181 5 Proportion 0.055 0.253 0.564 0.124 0.003		
GarageArea	I	utantilillulara
n missing distinct Info Mean Gmd .05 .10 .25 .50 .75 1460 0 441 1 473 234.9 0.0 240.0 334.5 480.0 576.0	.90 757.1	.95 850.1
lowest : 0 160 164 180 186, highest: 1220 1248 1356 1390 1418		
GarageQual		
n missing distinct 1379 81 5		
Value Ex Fa Gd Po TA Frequency 3 48 14 3 1311 Proportion 0.002 0.035 0.010 0.002 0.951		
GarageCond		
n missing distinct 1379 81 5		
Value Ex Fa Gd Po TA Frequency 2 35 9 7 1326 Proportion 0.001 0.025 0.007 0.005 0.962		
PavedDrive		. 1
n missing distinct 1460 0 3		
Value N P Y Frequency 90 30 1340 Proportion 0.062 0.021 0.918		
WoodDeckSF	<u> </u>	
n missing distinct Info Mean Gmd .05 .10 .25 .50 .75 .90 1460 0 274 0.858 94.24 125 0 0 0 0 168 262	.95 335	
lowest : 0 12 24 26 28, highest: 668 670 728 736 857		
OpenPorchSF	<u> </u>	
n missing distinct Info Mean Gmd .05 .10 .25 .50 .75 .90 1460 0 202 0.909 46.66 62.43 0 0 0 25 68 130	.95 175	
lowest: 0 4 8 10 11, highest: 406 418 502 523 547		
EnclosedPorch	1.	······································
n missing distinct Info Mean Gmd .05 .10 .25 .50 .75 .90 .95 .1460 0 120 0.369 21.95 39.39 0.0 0.0 0.0 0.0 0.0 112.0 180.1		
lowest: 0 19 20 24 30, highest: 301 318 330 386 552		
X3SsnPorch		
1460 Ŏ 20 0.049 3.41 6.739 0 0 0 0 0 0	.95 0	
Value 0 23 96 130 140 144 153 162 168 180 182 196 Frequency 1436 1 1 1 1 1 2 1 1 3 2 1 1 Proportion 0.984 0.001 0.001 0.001 0.001 0.001 0.001 0.001 0.001 0.001 0.001 0.001 0.001 0.001	2	238 1 2001
Value 245 290 304 320 407 508 Frequency 1 1 1 1 1 1 1 Proportion 0.001 0.001 0.001 0.001 0.001 0.001		

ScreenPorch
n missing distinct Info Mean Gmd .05 .10 .25 .50 .75 .90 .95 1460 0 76 0.22 15.06 28.27 0 0 0 0 0 160
lowest: 0 40 53 60 63, highest: 385 396 410 440 480
PoolArea
n missing distinct Info Mean Gmd 1460 0 8 0.014 2.759 5.497
Value 0 480 512 519 555 576 648 738 Frequency 1453 1 1 1 1 1 1 1 Proportion 0.995 0.001 0.001 0.001 0.001 0.001 0.001
PoolQC I I
n missing distinct 7 1453 3
Value Ex Fa Gd Frequency 2 2 3 Proportion 0.286 0.286 0.429
Fence
n missing distinct 281 1179 4
Value GdPrv GdWo MnPrv MnWw Frequency 59 54 157 11 Proportion 0.210 0.192 0.559 0.039
MiscFeature
n missing distinct 54 1406 4
Value Gar2 Othr Shed TenC Frequency 2 2 49 1 Proportion 0.037 0.037 0.907 0.019
MiscVal
n missing distinct Info Mean Gmd .05 .10 .25 .50 .75 .90 .95 1460
Value 0 50 350 400 450 500 550 600 700 800 1150 1200 1300 1400 Frequency 1408 1 1 11 4 10 1 5 5 1 1 2 1 1 Proportion 0.964 0.001 0.001 0.008 0.003 0.007 0.001 0.003 0.003 0.001 0.001 0.001 0.001 0.001
Value 2000 2500 3500 8300 15500 Frequency 4 1 1 1 1 Proportion 0.003 0.001 0.001 0.001
MoSold
n missing distinct Info Mean Gmd .05 .10 .25 .50 .75 .90 .95 1460 0 12 0.985 6.322 3.041 2 3 5 6 8 10 11
Value 1 2 3 4 5 6 7 8 9 10 11 12 Frequency 58 52 106 141 204 253 234 122 63 89 79 59 Proportion 0.040 0.036 0.073 0.097 0.140 0.173 0.160 0.084 0.043 0.061 0.054 0.040
YrSold IIII
n missing distinct Info Mean Gmd 1460 0 5 0.955 2008 1.498
Value 2006 2007 2008 2009 2010 Frequency 314 329 304 338 175 Proportion 0.215 0.225 0.208 0.232 0.120
SaleType
n missing distinct 1460 0 9
Value COD Con ConLD ConLI ConLw CWD New Oth WD Frequency 43 2 9 5 5 4 122 3 1267 Proportion 0.029 0.001 0.006 0.003 0.003 0.003 0.0084 0.002 0.868
SaleCondition
n missing distinct 1460 0 6
Value Abnorml AdjLand Alloca Family Normal Partial Frequency 101 4 12 20 1198 125 Proportion 0.069 0.003 0.008 0.014 0.821 0.086

6.2 Variable Selection

In the previous tables we see a number of variables with NAs. For simplicity, we will exclude the columns containing NAs and attempt to identify the variables of greatest importance.

6.3 Variable Subset Matrix

	1(1)	2(1)	3(1)	4(1)	5(1)	6(1)	7(1)	8(1)	9(1)
Id									
MSSubClass						*	*	*	*
MSZoningFV									
MSZoningRH									
MSZoningRL									
MSZoningRM									
LotArea									
StreetPave									
LotShapeIR2									
LotShapelR3									
LotShapeReg									
LandContourHLS									
LandContourLow									
LandContourLvl									
UtilitiesNoSeWa									
LotConfigCulDSac									
LotConfigFR2									
LotConfigFR3									
LotConfigInside									
LandSlopeMod									
LandSlopeSev									
NeighborhoodBlueste									
NeighborhoodBrDale									
NeighborhoodBrkSide									
NeighborhoodClearCr									
NeighborhoodCollgCr									
NeighborhoodCrawfor									
NeighborhoodEdwards									
NeighborhoodGilbert									
NeighborhoodIDOTRR									
NeighborhoodMeadowV									
NeighborhoodMitchel									
NeighborhoodNAmes									
NeighborhoodNoRidge								*	*
NeighborhoodNPkVill					*	*	*	*	*
NeighborhoodNridgHt					*	*	*	*	*
NeighborhoodNWAmes									
NeighborhoodOldTown									
NeighborhoodSawyer									
NeighborhoodSawyerW									
NeighborhoodSomerst							*	*	*
NeighborhoodStoneBr							*	*	*
NeighborhoodSWISU									
NeighborhoodTimber									
NeighborhoodVeenker Condition1Feedr									
ConditionTreed									

	1(1)	2(1)	3(1)	4(1)	5(1)	6(1)	7(1)	8(1)	9(1)
Condition1Norm									
Condition1PosA									
Condition1PosN									
Condition1RRAe									
Condition1RRAn Condition1RRNe									
Condition1RRNn									
Condition2Feedr									
Condition2Norm									
Condition2PosA									
Condition2PosN									
Condition2RRAe									
Condition2RRAn									
Condition2RRNn BldgType2fmCon									
BldgTypeDuplex									
BldgTypeTwnhs									
BldgTypeTwnhsE									
HouseStyle1.5Unf									
HouseStyle1Story									
HouseStyle2.5Fin									
HouseStyle2.5Unf									
HouseStyle2Story HouseStyleSFoyer									
HouseStyleSLvl									
OverallQual	*	*	*	*	*	*	*	*	*
OverallCond									
YearBuilt						*	*	*	
YearRemodAdd									*
RoofStyleGable									
RoofStyleGambrel RoofStyleHip									
RoofStyleMansard									
RoofStyleShed									
RoofMatlCompShg									
RoofMatlMembran									
RoofMatlMetal									
RoofMatlRoll									
RoofMatlTar&Grv RoofMatlWdShake									
RoofMatlWdShngl									
Exterior1stAsphShn									
Exterior1stBrkComm									
Exterior1stBrkFace									
Exterior1stCBlock									
Exterior1stCemntBd									
Exterior1stHdBoard Exterior1stImStucc									
Exterior1stMetalSd									
Exterior1stNetalod Exterior1stPlywood									
Exterior1stStone									
Exterior1stStucco									
Exterior1stVinylSd									
Exterior1stWd Sdng									
Exterior1stWdShing									
Exterior2ndAsphShn Exterior2ndBrk Cmn									
Exterior2ndBrkFace									
Exterior2ndCBlock									
Exterior2ndCmentBd									
Exterior2ndHdBoard									
Exterior2ndImStucc									
Exterior2ndMetalSd									
Exterior2ndOther									
Exterior2ndPlywood Exterior2ndStone									
LACTIOIZIUSIONE									

	1(1)	2(1)	3(1)	4(1)	5(1)	6(1)	7(1)	8(1)	9(1)
Exterior2ndStucco	- (-)	_(',	- (·)	- (·)	- (·)	- (·)	. (.)	- (·)	- (·)
Exterior2ndVinylSd									
Exterior2ndWd Sdng Exterior2ndWd Shng									
ExterQualFa									
ExterQualGd									
ExterQualTA									
ExterCondFa ExterCondGd									
ExterCondPo									
ExterCondTA									
FoundationCBlock									
FoundationPConc FoundationSlab									
FoundationStone									
oundationWood									
BsmtFinSF1			*	*	*	*	*	*	*
BsmtFinSF2									
BsmtUnfSF FotalBsmtSF									
HeatingGasA									
HeatingGasW									
HeatingGrav									
HeatingOthW									
HeatingWall HeatingQCFa									
HeatingQCGd									
HeatingQCPo									
HeatingQCTA									
CentralAirY K1stFlrSF									
(2ndFlrSF									
_owQualFinSF									
GrLivArea		*	*	*	*	*	*	*	*
BsmtFullBath BsmtHalfBath									
FullBath									
HalfBath									
BedroomAbvGr									
KitchenAbvGr KitchenQualFa									
KitchenQualGd									
KitchenQualTA									
TotRmsAbvGrd									
FunctionalMaj2 FunctionalMin1									
FunctionalMin2									
FunctionalMod									
FunctionalSev									
FunctionalTyp									
Fireplaces GarageCars				*	*				*
GarageArea									
PavedDriveP									
PavedDriveY									
WoodDeckSF OpenPorchSF									
EnclosedPorch									
(3SsnPorch									
ScreenPorch									
PoolArea									
MiscVal MoSold									
rSold/rSold									
TOOIG									
SaleTypeCon SaleTypeConLD									

	1(1)	2(1)	3(1)	4(1)	5(1)	6(1)	7(1)	8(1)	9(1)
SaleTypeConLl									
SaleTypeConLw									
SaleTypeCWD									
SaleTypeNew									
SaleTypeOth									
SaleTypeWD									
SaleConditionAdjLand									
SaleConditionAlloca									
SaleConditionFamily									
SaleConditionNormal									
SaleConditionPartial									

6.4 First Model

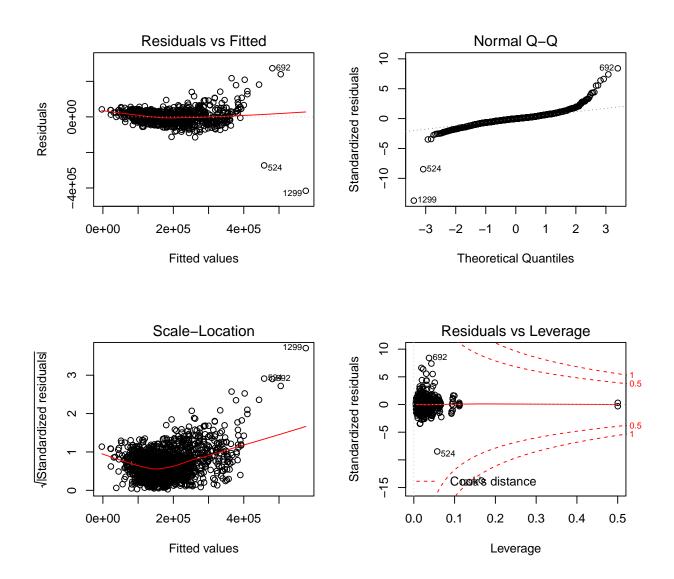
Based on the last best model we will limit the data set to the following variables MSSubClass, NeighborhoodNoRidge, NeighborhoodNridgHt, NeighborhoodStoneBr, OverallQual, YearRemodAdd, BsmtFinSF1, GrLivArea, GarageCars.

Table 7:

	Table 7:
	Dependent variable:
	SalePrice
Constant	-621,777.700*** (111,442.300)
MSSubClass	-252.678*** (24.405)
NeighborhoodBlueste	-12,510.880 (24,882.880)
NeighborhoodBrDale	-16,417.030 (11,866.240)
NeighborhoodBrkSide	-14,640.440 (9,753.068)
NeighborhoodClearCr	7,771.633 (10,647.930)
NeighborhoodCollgCr	-8,855.995 (8,742.258)
NeighborhoodCrawfor	7,447.104 (9,729.488)
NeighborhoodEdwards	-24,629.000*** (9,317.138)
NeighborhoodGilbert	-12,303.590 (9,065.933)
NeighborhoodIDOTRR	-25,820.490** (10,379.870)
NeighborhoodMeadowV	1,205.989 (11,879.710)
NeighborhoodMitchel	-18,072.460* (9,692.696)
NeighborhoodNAmes	-18,834.730** (8,971.063)
NeighborhoodNoRidge	40,530.480*** (10,050.780)
NeighborhoodNPkVill	-9,409.847 (13,823.590)
NeighborhoodNridgHt	49,514.520*** (9,100.426)
NeighborhoodNWAmes	-21,429.510** (9,344.861)
NeighborhoodOldTown	-31,650.010*** (9,111.020)
NeighborhoodSawyer	-19,047.140** (9,502.20 <u>5</u>)
NeighborhoodSawyerW	-15,759.290* (9,404.611)
NeighborhoodSomerst	7,011.384 (8,880.182)
NeighborhoodStoneBr	55,104.420*** (10,602.380)
NeighborhoodSWISU	-27,693.620** (11,081.320)
NeighborhoodTimber	3,500.186 (9,974.428)
NeighborhoodVeenker	25,505.000* (13,027.270)
OverallQual	16,039.450*** (1,094.370)
YearRemodAdd	310.102*** (56.246)
BsmtFinSF1	23.326*** (2.113)
GrLivArea	52.970*** (2.326)
GarageCars	11,974.750*** (1,614.394)
Observations	1,460
R^2	0.829
Adjusted R ²	0.826
Residual Std. Error	33,181.540 (df = 1429)
F Statistic	231.137*** (df = 30; 1429) (p = 0.000)
Note:	*p<0.1; **p<0.05; ***p<0.01

6.4.1 Diagnostic Plots

```
p <- par(mfrow=c(2,2))
plot(fit)</pre>
```



The residual plot does not look like a shotgun pattern and we may be violating the assumption of random variance. My assumption is that the high influence points and/or outliers may be impacting the model. Therefore, we will exclude the high influence points from our final model. We will also take the log of SalePrice as we began to get negative predictions after removing the high influence points.

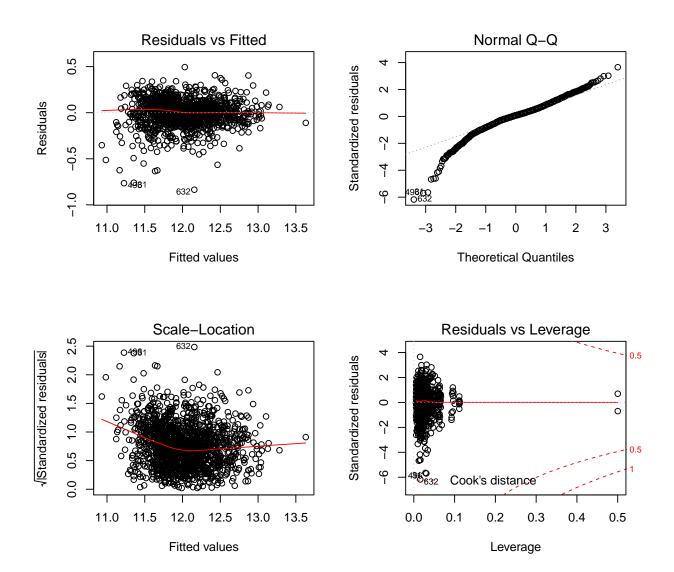
6.5 Final Model

Table 8: Final Model

	C O. 1 IIIUI IVIOUCI
	Dependent variable:
	I(log(SalePrice))
Constant	5.914*** (0.458)
MSSubClass	-0.001*** (0.0001)
NeighborhoodBlueste	-0.096 (0.102)
NeighborhoodBrDale	-0.209*** (0.049)
NeighborhoodBrkSide	-0.110*** (0.040)
NeighborhoodClearCr	0.067 (0.044)
NeighborhoodCollgCr	-0.029 (0.036)
NeighborhoodCrawfor	0.046 (0.040)
NeighborhoodEdwards	-0.126*** (0.038)
NeighborhoodGilbert	-0.030 (0.037)
NeighborhoodIDOTRR	-0.265*** (0.043)
NeighborhoodMeadowV	-0.157*** (0.049)
NeighborhoodMitchel	-0.078* (0.040)
NeighborhoodNAmes	-0.064*(0.037)
NeighborhoodNoRidge	-0.012 (0.042)
NeighborhoodNPkVill	-0.061 (0.057)
NeighborhoodNridgHt	0.072* (0.038)
NeighborhoodNWAmes	-0.067* (0.038)
NeighborhoodOldTown	-0.212*** (0.037)
NeighborhoodSawyer	-0.079** (0.039)
NeighborhoodSawyerW	-0.078** (0.039)
NeighborhoodSomerst	0.019 (0.037)
NeighborhoodStoneBr	0.093** (0.044)
NeighborhoodSWISU	-0.131*** (0.046)
NeighborhoodTimber	-0.004 (0.041)
NeighborhoodVeenker	0.105** (0.054)
OverallQual	0.091*** (0.005)
YearRemodAdd	0.003*** (0.0002)
BsmtFinSF1	0.0002*** (0.00001)
GrLivArea	0.0003*** (0.00001)
GarageCars	0.069*** (0.007)
Observations	1,457
R^2	0.885
Adjusted R ²	0.882
Residual Std. Error	0.136 (df = 1426)
F Statistic	365.465*** (df = 30; 1426) (p = 0.000)
Note:	*p<0.1; **p<0.05; ***p<0.01

There are some interesting coeffecients in our final model. It is unsurprising that we see certain neighboorhoods have greater impact to the sale price but it is interesting to see the specific ones. I am also surprised that the number of cars that a garage can hold has such a great impact. Intuitively, it makes sense that more cars indicates greater wealth and a higher sale price but it was expected to see it represented in our model.

6.5.1 Diagnostic Plots



Now we see a more random variance in our diagnostic plots and I am more comfortable with our model. Taking the log of our outcome variable has improved our ability to validate this model.

6.5.2 Multicollinearity

```
library(car)
library(data.table)
rmfit <- setDT(as.data.frame(car::vif(fit)), keep.rownames = TRUE)[]
rmfit$Adjusted_GVIF <- (rmfit$`GVIF^(1/(2*Df))`^2)
kable(rmfit, align = c("l", "c", "c", "c", "c"))</pre>
```

rn	GVIF	Df	GVIF^(1/(2*Df))	Adjusted_GVIF
MSSubClass	1.413403	1	1.188866	1.413403
Neighborhood	5.812676	24	1.037348	1.076091
OverallQual	2.988764	1	1.728804	2.988764
YearRemodAdd	1.784746	1	1.335944	1.784746
BsmtFinSF1	1.238327	1	1.112801	1.238327
GrLivArea	1.968825	1	1.403148	1.968825
GarageCars	1.936513	1	1.391587	1.936513

Using GVIF^(1/(2*Df)) ⁴ in order to verify that the VIF threshold of 5 for multicollinearity is not exceed. Fortunately, we find that no variable exceeds the threshold and we do not need to adjust for multicollinearity.

6.6 Prediction results with test data set using final model

First there are some observations that are missing values included in our model. For this reason, we will use imputation to complete the cases so our predictions can be carried out.

6.6.1 Imputation

The test data provided by Kaggle has NAs for some of our independent variables. As such, we will use a non-parametic method of imputation so that we can run our final model.

 $^{^{4}}$ "Which Variance Inflation Factor Should I Be Using: GVIF or $textGVIF^{1/(2cdottextdf)}$?" R. N.p., n.d. Web. 13 Nov. 2016.

6.7 Prediction results

SalePrice
116767
153700
177987
188130
207117
172621

6.7.1 Prediction results for submission

```
gz1 <- gzfile("submission.csv.gz", "w")
write.csv(test.df.wpredict, gz1, row.names = FALSE)
close(gz1)</pre>
```

6.8 Kaggle Results

Kaggle.com user name: Blastophe

Kaggle.com score: 0.15033