# Introduction to data - Christophe Hunt

Some define Statistics as the field that focuses on turning information into knowledge. The first step in that process is to summarize and describe the raw information - the data. In this lab, you will gain insight into public health by generating simple graphical and numerical summaries of a data set collected by the Centers for Disease Control and Prevention (CDC). As this is a large data set, along the way you'll also learn the indispensable skills of data processing and subsetting.

# Getting started

The Behavioral Risk Factor Surveillance System (BRFSS) is an annual telephone survey of 350,000 people in the United States. As its name implies, the BRFSS is designed to identify risk factors in the adult population and report emerging health trends. For example, respondents are asked about their diet and weekly physical activity, their HIV/AIDS status, possible tobacco use, and even their level of healthcare coverage. The BRFSS Web site (http://www.cdc.gov/brfss) contains a complete description of the survey, including the research questions that motivate the study and many interesting results derived from the data.

We will focus on a random sample of 20,000 people from the BRFSS survey conducted in 2000. While there are over 200 variables in this data set, we will work with a small subset.

We begin by loading the data set of 20,000 observations into the R workspace. After launching RStudio, enter the following command.

```
setwd("C:/Users/Christophe/Documents/R/Lab1")
source("./more/cdc.R")
```

The data set cdc that shows up in your workspace is a *data matrix*, with each row representing a *case* and each column representing a *variable*. R calls this data format a *data frame*, which is a term that will be used throughout the labs.

To view the names of the variables, type the command

```
names(cdc)
```

This returns the names genhlth, exerany, hlthplan, smoke100, height, weight, wtdesire, age, and gender. Each one of these variables corresponds to a question that was asked in the survey. For example, for genhlth, respondents were asked to evaluate their general health, responding either excellent, very good, good, fair or poor. The exerany variable indicates whether the respondent exercised in the past month (1) or did not (0). Likewise, hlthplan indicates whether the respondent had some form of health coverage (1) or did not (0). The smoke100 variable indicates whether the respondent had smoked at least 100 cigarettes in her lifetime. The other variables record the respondent's height in inches, weight in pounds as well as their desired weight, wtdesire, age in years, and gender.

1. How many cases are there in this data set?

How many variables?

```
paste("There are ", length((cdc$genhlth)), "cases in the dataset")
## [1] "There are 20000 cases in the dataset"
```

```
paste("There are", length(names(cdc)), "variables")
```

#### ## [1] "There are 9 variables"

For each variable, identify its data type (e.g. categorical, discrete).

### str(cdc)

```
'data.frame':
                    20000 obs. of 9 variables:
##
   $ genhlth: Factor w/ 5 levels "excellent", "very good",..: 3 3 3 3 2 2 2 2 3 3 ...
   $ exerany : num
                     0 0 1 1 0 1 1 0 0 1 ...
##
   $ hlthplan: num
                     1 1 1 1 1 1 1 1 1 1 ...
                     0 1 1 0 0 0 0 0 1 0 ...
##
   $ smoke100: num
##
   $ height : num
                     70 64 60 66 61 64 71 67 65 70 ...
   $ weight : int
                     175 125 105 132 150 114 194 170 150 180 ...
                     175 115 105 124 130 114 185 160 130 170 ...
##
   $ wtdesire: int
##
              : int
                     77 33 49 42 55 55 31 45 27 44 ...
   $ age
             : Factor w/ 2 levels "m", "f": 1 2 2 2 2 2 1 1 2 1 ...
```

### summary(cdc)

```
##
         genhlth
                          exerany
                                            hlthplan
                                                               smoke100
##
    excellent:4657
                      Min.
                              :0.0000
                                         Min.
                                                 :0.0000
                                                           Min.
                                                                   :0.0000
                                                           1st Qu.:0.0000
                      1st Qu.:0.0000
##
    very good:6972
                                         1st Qu.:1.0000
##
              :5675
                      Median :1.0000
                                         Median :1.0000
                                                           Median :0.0000
    good
              :2019
                              :0.7457
                                                                   :0.4721
##
    fair
                      Mean
                                         Mean
                                                :0.8738
                                                           Mean
##
    poor
              : 677
                      3rd Qu.:1.0000
                                         3rd Qu.:1.0000
                                                           3rd Qu.:1.0000
##
                      Max.
                              :1.0000
                                         Max.
                                                 :1.0000
                                                                   :1.0000
                                                           Max.
##
                          weight
                                          wtdesire
        height
                                                                          gender
                                                              age
##
                                       Min.
    Min.
            :48.00
                             : 68.0
                                              : 68.0
                                                                :18.00
                                                                         m: 9569
                     Min.
                                                        Min.
                                       1st Qu.:130.0
    1st Qu.:64.00
                     1st Qu.:140.0
                                                                          f:10431
##
                                                        1st Qu.:31.00
##
    Median :67.00
                     Median :165.0
                                      Median :150.0
                                                        Median :43.00
    Mean
            :67.18
                     Mean
                             :169.7
                                       Mean
                                              :155.1
                                                        Mean
                                                                :45.07
##
    3rd Qu.:70.00
                     3rd Qu.:190.0
                                       3rd Qu.:175.0
                                                        3rd Qu.:57.00
            :93.00
                             :500.0
    Max.
                     Max.
                                       Max.
                                              :680.0
                                                        Max.
                                                                :99.00
```

genhlth is categorical, exerany is discrete, hlthplan is discrete, smoke100 is discrete, height is continious, weight is continuous, wtdesire is continuous, age is continuous but appears to be measured as discrete, and gender is discrete.

We can have a look at the first few entries (rows) of our data with the command

```
head(cdc)
```

and similarly we can look at the last few by typing

```
tail(cdc)
```

You could also look at *all* of the data frame at once by typing its name into the console, but that might be unwise here. We know cdc has 20,000 rows, so viewing the entire data set would mean flooding your screen. It's better to take small peeks at the data with head, tail or the subsetting techniques that you'll learn in a moment.

# Summaries and tables

The BRFSS questionnaire is a massive trove of information. A good first step in any analysis is to distill all of that information into a few summary statistics and graphics. As a simple example, the function summary returns a numerical summary: minimum, first quartile, median, mean, second quartile, and maximum. For weight this is

```
summary(cdc$weight)
```

R also functions like a very fancy calculator. If you wanted to compute the interquartile range for the respondents' weight, you would look at the output from the summary command above and then enter

```
190 - 140
```

R also has built-in functions to compute summary statistics one by one. For instance, to calculate the mean, median, and variance of weight, type

```
mean(cdc$weight)
var(cdc$weight)
median(cdc$weight)
```

While it makes sense to describe a quantitative variable like weight in terms of these statistics, what about categorical data? We would instead consider the sample frequency or relative frequency distribution. The function table does this for you by counting the number of times each kind of response was given. For example, to see the number of people who have smoked 100 cigarettes in their lifetime, type

```
table(cdc$smoke100)
```

```
## 0 1
## 10559 9441
```

or instead look at the relative frequency distribution by typing

```
table(cdc$smoke100)/20000
```

```
## 0.52795 0.47205
```

Notice how R automatically divides all entries in the table by 20,000 in the command above. This is similar to something we observed in the Introduction to R; when we multiplied or divided a vector with a number, R applied that action across entries in the vectors. As we see above, this also works for tables. Next, we make a bar plot of the entries in the table by putting the table inside the barplot command.

```
barplot(table(cdc$smoke100))
```

Notice what we've done here! We've computed the table of cdc\$smoke100 and then immediately applied the graphical function, barplot. This is an important idea: R commands can be nested. You could also break this into two steps by typing the following:

```
smoke <- table(cdc$smoke100)
barplot(smoke)</pre>
```

Here, we've made a new object, a table, called smoke (the contents of which we can see by typing smoke into the console) and then used it in as the input for barplot. The special symbol <- performs an assignment, taking the output of one line of code and saving it into an object in your workspace. This is another important idea that we'll return to later.

2. Create a numerical summary for height and age, and compute the interquartile range for each. Compute the relative frequency distribution for gender and exerany. How many males are in the sample? What proportion of the sample reports being in excellent health?

## data.frame(table(cdc\$height))

```
##
      Var1 Freq
## 1
         48
                2
## 2
               1
         49
## 3
         50
               1
## 4
               2
         51
## 5
         52
               2
## 6
         53
               7
## 7
         54
               3
## 8
         55
               4
## 9
         56
              17
## 10
         57
              20
## 11
         58
              51
## 12
         59
             170
## 13
         60
             613
  14
##
             594
         61
##
   15
         62 1272
##
  16
         63 1368
## 17
         64 1662
## 18
         65 1568
## 19
         66 1843
## 20
         67 1671
## 21
         68 1505
## 22
         69 1380
## 23
         70 1500
## 24
         71 1296
## 25
         72 1393
## 26
         73
             784
## 27
         74
             605
  28
##
         75
             321
##
   29
         76
             189
         77
##
  30
              80
##
   31
         78
              43
## 32
         79
              15
## 33
         80
               10
## 34
         81
               3
## 35
         82
               2
## 36
         83
                1
```

```
## 37
        84
               1
## 38
        93
               1
```

# data.frame(table(cdc\$age))

```
##
      Var1 Freq
## 1
        18
            306
## 2
        19
             283
## 3
        20
             318
## 4
        21
             350
## 5
        22
             358
## 6
        23
             381
## 7
        24
             367
## 8
        25
             365
## 9
        26
             342
## 10
        27
             393
## 11
        28
             400
## 12
        29
             415
## 13
        30
             456
## 14
        31
             353
## 15
        32
             417
## 16
        33
            414
## 17
        34
            394
            472
## 18
        35
## 19
        36
             435
## 20
        37
             465
## 21
        38
             430
## 22
        39
             432
## 23
             524
        40
## 24
            382
        41
## 25
        42
            448
## 26
        43
             450
## 27
             385
        44
## 28
        45
             462
## 29
             363
        46
## 30
        47
             393
## 31
        48
             369
## 32
        49
             335
## 33
        50
             405
## 34
        51
             283
## 35
        52
             369
## 36
        53
             331
## 37
             270
        54
## 38
        55
             294
## 39
        56
             244
## 40
             284
        57
## 41
        58
             252
## 42
        59
             230
## 43
        60
             237
## 44
        61
             191
## 45
        62
             222
## 46
        63
             195
## 47
        64
             204
## 48
             269
```

```
## 50
       67 210
## 51
       68 199
## 52
       69 191
## 53
       70 214
## 54
       71 182
## 55
       72 192
       73 187
## 56
## 57
       74 194
## 58
       75 180
## 59
       76 152
## 60
       77 124
## 61
       78 130
## 62
       79 108
## 63
       80 128
## 64
            70
       81
## 65
       82
           79
           80
## 66
       83
## 67
           67
       84
## 68
       85
           57
## 69
       86
            22
## 70
       87
## 71
       88
            24
## 72
       89
            15
## 73
       90
            9
## 74
       91
            10
## 75
       92
             6
## 76
       93
             7
## 77
             3
       94
## 78
       95
             2
## 79
       96
             1
## 80
       97
             1
## 81
       99
             2
summary(cdc$height)
     Min. 1st Qu. Median
                             Mean 3rd Qu.
                                             Max.
##
     48.00
           64.00
                   67.00
                            67.18 70.00
                                            93.00
summary(cdc$age)
##
     Min. 1st Qu. Median
                             Mean 3rd Qu.
                                             Max.
##
     18.00
            31.00
                    43.00
                            45.07
                                    57.00
                                            99.00
table(cdc$gender)/length(cdc$gender)
##
```

## 49

##

m ## 0.47845 0.52155

66 186

# table(cdc\$exerany)/length(cdc\$exerany)

##

0

```
##
## 0.2543 0.7457
genders <- data.frame(table(cdc$gender)/length(cdc$gender))</pre>
paste("The number of males in the sample is", length(cdc$gender) * genders$Freq[genders$Var1 == "m"] )
```

## [1] "The number of males in the sample is 9569"

```
health <- data.frame(table(cdc$genhlth)/length(cdc$genhlth))
paste("The proportion of the sample reporting being in excellent health is", health$Freq[health$Var1 ==
```

## [1] "The proportion of the sample reporting being in excellent health is 0.23285"

The table command can be used to tabulate any number of variables that you provide. For example, to examine which participants have smoked across each gender, we could use the following.

```
table(cdc$gender,cdc$smoke100)
```

Here, we see column labels of 0 and 1. Recall that 1 indicates a respondent has smoked at least 100 cigarettes. The rows refer to gender. To create a mosaic plot of this table, we would enter the following command.

```
mosaicplot(table(cdc$gender,cdc$smoke100))
```

We could have accomplished this in two steps by saving the table in one line and applying mosaicplot in the next (see the table/barplot example above).

3. What does the mosaic plot reveal about smoking habits and gender?

# Interlude: How R thinks about data

We mentioned that R stores data in data frames, which you might think of as a type of spreadsheet. Each row is a different observation (a different respondent) and each column is a different variable (the first is genhlth, the second exerany and so on). We can see the size of the data frame next to the object name in the workspace or we can type

```
dim(cdc)
```

which will return the number of rows and columns. Now, if we want to access a subset of the full data frame, we can use row-and-column notation. For example, to see the sixth variable of the 567th respondent, use the format

```
cdc[567,6]
```

which means we want the element of our data set that is in the 567th row (meaning the 567th person or observation) and the 6th column (in this case, weight). We know that weight is the 6th variable because it is the 6th entry in the list of variable names

## names(cdc)

To see the weights for the first 10 respondents we can type

## cdc[1:10,6]

In this expression, we have asked just for rows in the range 1 through 10. R uses the : to create a range of values, so 1:10 expands to 1, 2, 3, 4, 5, 6, 7, 8, 9, 10. You can see this by entering

#### 1:10

Finally, if we want all of the data for the first 10 respondents, type

### cdc[1:10,]

By leaving out an index or a range (we didn't type anything between the comma and the square bracket), we get all the columns. When starting out in R, this is a bit counterintuitive. As a rule, we omit the column number to see all columns in a data frame. Similarly, if we leave out an index or range for the rows, we would access all the observations, not just the 567th, or rows 1 through 10. Try the following to see the weights for all 20,000 respondents fly by on your screen

## cdc[,6]

Recall that column 6 represents respondents' weight, so the command above reported all of the weights in the data set. An alternative method to access the weight data is by referring to the name. Previously, we typed names(cdc) to see all the variables contained in the cdc data set. We can use any of the variable names to select items in our data set.

## cdc\$weight

The dollar-sign tells R to look in data frame cdc for the column called weight. Since that's a single vector, we can subset it with just a single index inside square brackets. We see the weight for the 567th respondent by typing

### cdc\$weight[567]

Similarly, for just the first 10 respondents

# cdc\$weight[1:10]

The command above returns the same result as the cdc[1:10,6] command. Both row-and-column notation and dollar-sign notation are widely used, which one you choose to use depends on your personal preference.

## A little more on subsetting

It's often useful to extract all individuals (cases) in a data set that have specific characteristics. We accomplish this through *conditioning* commands. First, consider expressions like

```
cdc$gender == "m"
```

or

```
cdc$age > 30
```

These commands produce a series of TRUE and FALSE values. There is one value for each respondent, where TRUE indicates that the person was male (via the first command) or older than 30 (second command).

Suppose we want to extract just the data for the men in the sample, or just for those over 30. We can use the R function subset to do that for us. For example, the command

```
mdata <- subset(cdc, cdc$gender == "m")</pre>
```

will create a new data set called mdata that contains only the men from the cdc data set. In addition to finding it in your workspace alongside its dimensions, you can take a peek at the first several rows as usual

```
head(mdata)
```

This new data set contains all the same variables but just under half the rows. It is also possible to tell R to keep only specific variables, which is a topic we'll discuss in a future lab. For now, the important thing is that we can carve up the data based on values of one or more variables.

As an aside, you can use several of these conditions together with & and |. The & is read "and" so that

```
m_and_over30 <- subset(cdc, gender == "m" & age > 30)
```

will give you the data for men over the age of 30. The | character is read "or" so that

```
m_or_over30 <- subset(cdc, gender == "m" | age > 30)
```

will take people who are men or over the age of 30 (why that's an interesting group is hard to say, but right now the mechanics of this are the important thing). In principle, you may use as many "and" and "or" clauses as you like when forming a subset.

3. Create a new object called under23\_and\_smoke that contains all observations of respondents under the age of 23 that have smoked 100 cigarettes in their lifetime. Write the command you used to create the new object as the answer to this exercise.

```
under23_and_smoke <- subset(cdc, cdc$age < 23 & cdc$smoke100 == 1)
summary(under23_and_smoke)</pre>
```

```
##
         genhlth
                         exerany
                                           hlthplan
                                                              smoke100
##
    excellent:110
                             :0.0000
                                                :0.0000
                                        Min.
                                                           Min.
                                                                  :1
                     Min.
##
    very good:244
                      1st Qu.:1.0000
                                        1st Qu.:0.0000
                                                           1st Qu.:1
##
    good
                     Median :1.0000
                                        Median :1.0000
              :204
                                                           Median:1
##
              : 53
                             :0.8145
                                                :0.6952
    fair
                     Mean
                                                           Mean
##
    poor
              : 9
                     3rd Qu.:1.0000
                                        3rd Qu.:1.0000
                                                           3rd Qu.:1
##
                             :1.0000
                                                :1.0000
                     Max.
                                        Max.
                                                           Max.
##
        height
                          weight
                                          wtdesire
                                                              age
                                                                          gender
##
    Min.
            :59.00
                     Min.
                             : 85.0
                                       Min.
                                               : 80.0
                                                        Min.
                                                                :18.00
                                                                          m:305
    1st Qu.:65.00
##
                     1st Qu.:130.0
                                       1st Qu.:125.0
                                                        1st Qu.:19.00
                                                                          f:315
    Median :68.00
                                                        Median :20.00
##
                     Median :155.0
                                       Median :150.0
##
    Mean
            :67.92
                     Mean
                             :158.9
                                               :152.2
                                                                :20.22
                                       Mean
                                                        Mean
##
    3rd Qu.:71.00
                     3rd Qu.:180.0
                                       3rd Qu.:175.0
                                                        3rd Qu.:21.00
            :79.00
                             :350.0
                                               :315.0
                                                                :22.00
##
    Max.
                     {\tt Max.}
                                       Max.
                                                        Max.
```

# Quantitative data

With our subsetting tools in hand, we'll now return to the task of the day: making basic summaries of the BRFSS questionnaire. We've already looked at categorical data such as **smoke** and **gender** so now let's turn our attention to quantitative data. Two common ways to visualize quantitative data are with box plots and histograms. We can construct a box plot for a single variable with the following command.

```
boxplot(cdc$height)
```

You can compare the locations of the components of the box by examining the summary statistics.

```
summary(cdc$height)
```

Confirm that the median and upper and lower quartiles reported in the numerical summary match those in the graph. The purpose of a boxplot is to provide a thumbnail sketch of a variable for the purpose of comparing across several categories. So we can, for example, compare the heights of men and women with

```
boxplot(cdc$height ~ cdc$gender)
```

The notation here is new. The ~ character can be read *versus* or *as a function of.* So we're asking R to give us a box plots of heights where the groups are defined by gender.

Next let's consider a new variable that doesn't show up directly in this data set: Body Mass Index (BMI) (http://en.wikipedia.org/wiki/Body\_mass\_index). BMI is a weight to height ratio and can be calculated as:

$$BMI = \frac{weight\ (lb)}{height\ (in)^2} * 703$$

703 is the approximate conversion factor to change units from metric (meters and kilograms) to imperial (inches and pounds).

The following two lines first make a new object called bmi and then creates box plots of these values, defining groups by the variable cdc\$genhlth.

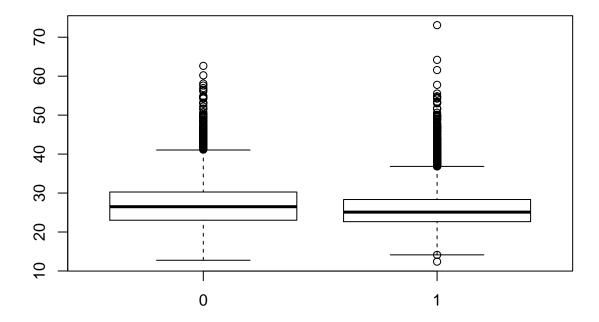
```
bmi <- (cdc$weight / cdc$height^2) * 703
boxplot(bmi ~ cdc$genhlth)</pre>
```

Notice that the first line above is just some arithmetic, but it's applied to all 20,000 numbers in the cdc data set. That is, for each of the 20,000 participants, we take their weight, divide by their height-squared and then multiply by 703. The result is 20,000 BMI values, one for each respondent. This is one reason why we like R: it lets us perform computations like this using very simple expressions.

4. What does this box plot show? Pick another categorical variable from the data set and see how it relates to BMI. List the variable you chose, why you might think it would have a relationship to BMI, and indicate what the figure seems to suggest.

This boxplot shows how feelings of health may be correlated with BMI which seems intuitively to make sense.

```
bmi <- (cdc$weight / cdc$height^2) * 703
boxplot(bmi ~ cdc$exerany)</pre>
```



I chose the exercise variable to see if there was an correlation with BMI and self-reporting that a perons exercises. I think this variable will have a link to BMI because I would assume that if a respondent is reporting that they exercise then they would, in general, have a lower BMI. The figure does suggest that those reporting that they exercise have a lower BMI. I was curious because this is self-reporting there is the possiblity that those that self-report exercise that they may be lying and you might not actual see a relationship.

Finally, let's make some histograms. We can look at the histogram for the age of our respondents with the command

```
hist(cdc$age)
```

Histograms are generally a very good way to see the shape of a single distribution, but that shape can change depending on how the data is split between the different bins. You can control the number of bins by adding an argument to the command. In the next two lines, we first make a default histogram of bmi and then one with 50 breaks.

```
hist(bmi)
hist(bmi, breaks = 50)
```

Note that you can flip between plots that you've created by clicking the forward and backward arrows in the lower right region of RStudio, just above the plots. How do these two histograms compare?

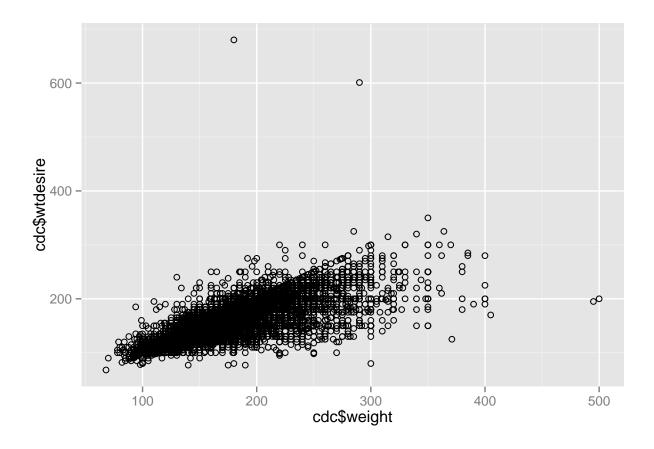
At this point, we've done a good first pass at analyzing the information in the BRFSS questionnaire. We've found an interesting association between smoking and gender, and we can say something about the

relationship between people's assessment of their general health and their own BMI. We've also picked up essential computing tools – summary statistics, subsetting, and plots – that will serve us well throughout this course.

# On Your Own

• Make a scatterplot of weight versus desired weight. Describe the relationship between these two variables.

```
library(ggplot2)
ggplot(cdc, aes(x=cdc$weight, y = cdc$wtdesire)) + geom_point(shape=1)
```



The relationship between the two variables is a positive correlation, higher the weight the heigher the desired weight. I believe this indicates that people maintain a goal weight based on their current weight and height and there is not on single goal weight.

• Let's consider a new variable: the difference between desired weight (wtdesire) and current weight (weight). Create this new variable by subtracting the two columns in the data frame and assigning them to a new object called wdiff.

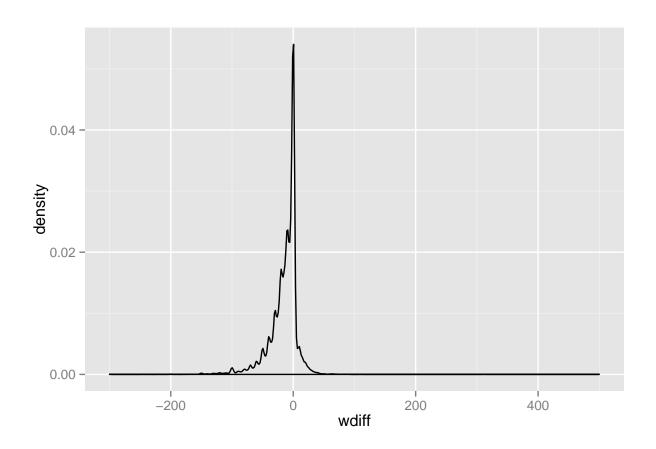
# cdc\$wdiff <- cdc\$wtdesire - cdc\$weight</pre>

• What type of data is wdiff? If an observation wdiff is 0, what does this mean about the person's weight and desired weight. What if wdiff is positive or negative?

wdiff is continious and its variance data. If the an observation of wdiff is 0 then the person weights their desired weight. If wdiff is positive then the person would like to gain weight, whereas if wdiff is negative then the person would like to lose weight.

• Describe the distribution of wdiff in terms of its center, shape, and spread, including any plots you use. What does this tell us about how people feel about their current weight?

```
library(ggplot2)
ggplot(cdc, aes(wdiff)) + geom_density()
```



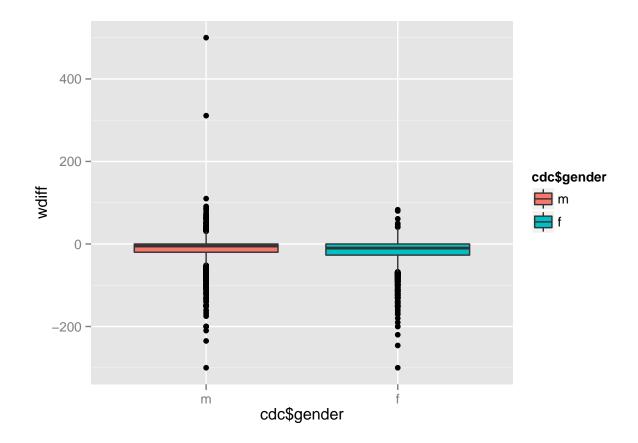
# summary(cdc\$wdiff)

```
## Min. 1st Qu. Median Mean 3rd Qu. Max. ## -300.00 -21.00 -10.00 -14.59 0.00 500.00
```

wdiff has a center at -10 lbs, it has a left skew which is expected that more people want to lose weight than gain it. This tells us that in general more people would like to lose weight than people would like to gain weight.

• Using numerical summaries and a side-by-side box plot, determine if men tend to view their weight differently than women.

```
summary(subset(cdc$wdiff, cdc$gender == "m"))
##
     Min. 1st Qu.
                   Median
                              Mean 3rd Qu.
                                              Max.
                                      0.00
## -300.00
           -20.00
                     -5.00
                           -10.71
                                            500.00
summary(subset(cdc$wdiff, cdc$gender == "f"))
     Min. 1st Qu.
##
                   Median
                              Mean 3rd Qu.
                                              Max.
## -300.00 -27.00 -10.00
                                      0.00
                                             83.00
                           -18.15
library(ggplot2)
ggplot(cdc, aes(cdc$gender, wdiff, fill = cdc$gender)) + geom_boxplot()
```



It does appear that men tend to report that they wish to lose less weight than the females surveyed. The difference is slight and it would be interesting to know if the difference was statistically significant.

• Now it's time to get creative. Find the mean and standard deviation of weight and determine what proportion of the weights are within one standard deviation of the mean.

```
mean(cdc$weight)

## [1] 169.683

sd(cdc$weight)

## [1] 40.08097

x <- length(subset(cdc$weight, cdc$weight < mean(cdc$weight) + sd(cdc$weight) & cdc$weight > mean(cdc$weight) - sd(cdc$weight) )) / length(cdc$weight)

paste("The proportion of values that are within one standard deviation of the mean is", x)
```

## [1] "The proportion of values that are within one standard deviation of the mean is 0.7076"

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