

Homework 1 - IS 605 FUNDAMENTALS OF COMPUTATIONAL MATHEMATICS

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1 Problem Set 1

1.1 (1) Calculate the dot product $u.v$ where $u = [0.5; 0.5]$ and $v = [3; -4]$

```
u <- c(.5, .5)
v <- c(3, -4)

dotProduct <- function(x, y)
if (length(x) != length(y)){
  return("vectors are not equal lengths")
} else {
  product <- c()
  for (i in 1:length(x)){
    product <- append(product, (x[[i]] * y[[i]]))
  }
  return(sum(product))
}

dotProduct(u,v)

## [1] -0.5
```

1.2 (2) What are the lengths of u and v ?

Please note that the mathematical notion of the length of a vector is not the same as a computer science definition.

```
u <- c(.5, .5)
v <- c(3, -4)

print(paste0("the length of $u$ = ", round(sqrt(dotProduct(u,u)), 2)))
```

```
[1] "the length of  $u$  = 0.71"
```

```
print(paste0("the length of $v$ = ", round(sqrt(dotProduct(v,v)), 2)))
```

```
[1] "the length of  $v$  = 5"
```

1.3 (3) What is the linear combination: $3u - 2v$?

```
u <- c(.5, .5)
v <- c(3, -4)

linearCombo <- function(xMulti, x, yMulti, y, subtract = TRUE){
  xResults <- c()
  yResults <- c()
  linCombo <- c()
  for (i in 1:length(x)){
    xResults <- append(xResults, (xMulti * x[[i]]))
  }
  for (i in 1:length(y)){
    yResults <- append(yResults, (yMulti* y[[i]]))
  }
  if (subtract == TRUE){
    for (i in 1:length(xResults))
      linCombo <- append(linCombo, (xResults[[i]] - yResults[[i]]))
  } else {
    for (i in 1:length(xResults))
      linCombo <- append(linCombo, (xResults[[i]] + yResults[[i]]))
  }
  return(linCombo)
}

x <- linearCombo(xMulti = 3, u, yMulti = 2, v)

paste0("[",x[1], " , " , x[2], "]" )

## [1] "[-4.5 , 9.5]"
```

1.4 (4) What is the angle between u and v

```
angle <- acos((dotProduct(u,v) / (sqrt(dotProduct(u,u)) * sqrt(dotProduct(v,v)))))
angle
```

Please test it with the system below and it should produce a solution $x = [-1.55, -0.32, 0.95]$

$$\begin{bmatrix} 1 & 1 & 3 \\ 2 & -1 & 5 \\ -1 & -2 & 4 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} = \begin{bmatrix} 1 \\ 2 \\ 6 \end{bmatrix} \quad (1)$$

Figure 1: img

```
## [1] 1.712693
```

2 Problem Set 2

Set up a system of equations with 3 variables and 3 constraints and solve for x . Please write a function in R that will take two variables (matrix A & constraint vector b) and solve using elimination. Your function should produce the right answer for the system of equations for any 3-variable, 3-equation system. You don't have to worry about degenerate cases and can safely assume that the function will only be tested with a system of equations that has a solution. Please note that you do have to worry about zero pivots, though. Please note that you should not use the built-in function `solve` to solve this system or use matrix inverses. The approach that you should employ is to construct an Upper Triangular Matrix and then back-substitute to get the solution. Alternatively, you can augment the matrix A with vector b and jointly apply the Gauss Jordan elimination procedure.