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What measure of effect size when comparing two groups based on their means?	
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10 Abstract

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12 Keywords: keywords

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What measure of effect size when comparing two groups based on their means?

15 Intro

During decades, researchers in social science (Henson & Smith, 2000) and education

(Fan, 2001) have overestimated the ability of the null hypothesis (H0) testing to determine

the importance of their results. The standard for researchers in social science is to define H0

as the absence of effect (Meehl, 1990). For example, when comparing the mean of two

groups, researchers commonly test the H0 that there is no mean differences between groups

(Steyn, 2000). Any effect that is significantly different from zero will be seen as sole support

for a theory.

Such an approach has faced many criticisms among which the most relevant to our concern is that the null hypothesis testing highly depends on sample size: for a given alpha level and a given difference between groups, the larger the sample size, the higher the probability of rejecting the null hypothesis (Fan, 2001; Kirk, 2009; Olejnik & Algina, 2000; Sullivan & Feinn, 2012). It implies that even tiny differences could be detected as statistically significant with very large sample sizes (McBride, Loftis, & Adkins, 1993)¹.

Facing this argument, it has become an adviced practice to report the *p*-value assorted by a measure of the effect size, that is, a quantitative measure of the magnitude of the experimenter effect (Cohen, 1965; Fan, 2001; Hays, 1963). This practice is also highly endorsed by the American Psychological Association (APA) and the American Educational Research Association (AERA) (American Educational Research Association, 2006; American Psychological Association, 2010). However, limited studies properly report effect size in the

¹ This is especially problematic since these tiny differences might be due to other factors than the one of interest: even under the assumption of random assignent (which is a necessary but not sufficient condition), it is almost impossible to be sure that the only difference between two conditions is the one defined by the factor of interest. Other tiny factors of no theoretical interest might slighly influence results, making the probability of getting an actual zero effect very low. This is what Meehl (1990) calls 'systematic noise'

last several decades.

First, there is a high confusion between the effect size and other related concepts such as the clininal significance of a result (i.e. the relevance of an effect in real life). Moreover, there are several situations that call for effect size measures and in the current litterature, it's not always easy to know which measure using in specific context.

Second, when used for inference, the main measures of effect sizes are submitted to a range of assumptions (i.e. normality and heteroscedasticity) and these assumptions are known to be unrealistic in many research designs (Cain, Zhang, & Yuan, 2017; Erceg-Hurn & Mirosevich, 2008; Glass, Peckham, & Sanders, 1972; Grissom, 2000; Micceri, 1989; Yuan, Bentler, & Chan, 2004). As consequences many estimations of effect size are inaccurate and alter the robustness of the statistical conclusions. In the context of comparing two groups based on their means, Cohen's d_s is the dominant effect size measure used by researchers (Peng, Chen, Chiang, & Chiang, 2013). We will argue that, like Student's t-test, this measure rely on the often untenable assumptions of normality and homogeneity of variances. 2 .

In sum the aim of this paper is threefold: 1. Clearly define what is (and what is not) a measure of effect size; 2. Listing the different situations that call for effect sizes measure and reviewing which measure is appropriate in which circumstance; 3. Define different properties of a good effect size estimator and discuss the impact of assumptions violations on the

² encore à implémenter dans le texte: Bcp d'autres chercheurs avant nous étaient arrivés à la même conclusion. Pourtant, beaucoup moins d'auteurs se sont penchés sur les mesures de taille d'effet à utiliser en complément du test de welch. Il existe de la littérature sur la question, mais pas vraiment d'accord (parce que grande confusion quant à la questino suivante: à quoi sert la mesure de taille d'effet?) Par ailleurs, s'il est de plus en plus communément admis que les conditions d'application des tests de comparaison de moyennes (dominant toujours la recherche) sont peu réalistes et rarement respectées, pourtant et que de nombreux chercheurs recommandent d'utiliser le Welch au lieu du test de Student, peu de littérature suggère quelle taille d'effet associer à ce test. Même Jamovi ne propose comme mesure de taille d'effet que le d de Cohen, souffrant des mêmes limites que le test de Student.

robustness of the measures of effect size, based on simulations.

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Measure of effect size: what it is, what it is not

The effect size is commonly refered to the practical significance of a test. Grissom and Kim (2005) define the effect size as the extent to which results differ from what is implied by the null hypothesis. In the context of the comparison of two groups based on their mean, depending on the defined null hypothesis (considering the absence of effect as the null hypothesis), we could define the effect size either as the magnitude of differences between parameters of two populations groups are extracted from (e.g. the mean; Peng & Chen, 2014) or as the magnitude of the relation between one dichotomous factor and one dependent variable (American Educational Research Association, 2006). Both definitions refers to as the most famous families of measures of effect sizes [Rosenthal_1994]: respectively the d-family and the r-family.

Very often, the contribution of the measures of effect size is overestimated.

First, benchmarks about what should be a small, medium or large effect size might
have contribued at seeing the effect size as a measure of the importance or the relevance of
an effect in real life, but it is not (Stout & Ruble, 1995). The effect size is only a
mathematical indicator of the magnitude of a difference, which depends on the way a
variable is converted into numerical indicator. In order to assess the meaningfulness of en
effect, we should be able to relate this effect with behaviors/meaningful consequences in the
real world (Andersen, McCullagh, & Wilson, 2007). For example, let us imagine a sample of
students in serious school failure who are randomly divided into two groups: an experimental
group following a training program and a control group. At the end of the training, students
in the experimental group have on average significantly higher scores on a test than students
in the control group, and the difference is large (e.g. 30 percents). Does it mean that
students in the experimental condition will be able to pass to the next grade and to continue

normal schooling? Whether the computed magnitude of difference is an important,
meaningful change in everyday life refers to another construct: the clinical significance
(Bothe & Richardson, 2011). [I DON'T LIKE THE WORD "CLINICAL" BECAUSE IT'S
NOT GENERAL ENOUGH.A MEANINGFUL SIGNIFICANCE COULD BE SOCIAL,
PERSONAL, CLINICAL, PROFESIONNAL... ANY IDEA OF A MORE GENERAL
WORD?]. It refers to the interpretation of treatment outcomes and is neither statistical nor
mathematical, it is related to underlying theory that posits an empirical hypothesis. In other

words, the relation between practical and clinical significance is more a theoretical argument

Second, in the context of the comparison of two groups based on their means, it should not replace the null hypothesis testing. Statistical testing allows the researcher to determine whether the oberved departure from H0 occured by chance or not (Stout & Ruble, 1995) while effect size estimators allow to assess the practical signficance of an effect, and as reminds Fan (2001) "a practically meaningful outcome may also have occured by chance, and consequently, is not trustworthy". For this reason, the use of confidence intervals around the effect size estimate is highly recommended (Bothe & Richardson, 2011).

Different goals of measures of effect sizes

Robust measures

- Properties of a good effect size estimator
- 97 Unbiasedness.

than a statistical one.

- 98 Consistency.
- 99 Efficiency.
- Interpretability. Interpretability is not a very clear concept to me. Reading about

2 Simulations

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