### The Marginal Efficiency of Active Search

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### **Motivation**

- Consider non-employed workers willing to accept a job... (as in CPS)
  - ► Active non-employed: e.g., contacts an employer about a position
  - ► Passive non-employed: e.g., waits for an employer to contact them Key margin for participation, UI, etc.
- During a recession,
  - Fraction of non-employed engaged in active search increases
  - Active search of the active non-employed increases
  - Active-passive ratio in job-finding probabilities decreases

Consistent with decline in premium from active search

- Cyclicality of active-passive ratio not driven by cyclical heterogeneity
- Instead, symptomatic of "crowding-out" of active search

### Motivation, cont'd

- ► Theory à la DMP typically abstracts from OLF & passive non-empl.
- But OLF and "passive non-empl." important for labor market flows...
  - ▶ 1/2 of new hires from non-employment come from OLF
  - Passive non-employed improve fit of matching function
  - ► OLF → U flows generate recessionary increase in unemployment
- Contemporary literature incorporates non-participation into DMP
  - e.g. Krusell et al (2017), Faberman et al (2022)
- ► Key restriction: active and passive search as perfect substitutes
  - Implies constant active-passive ratio of job-finding probabilities
  - Goes back to Blanchard and Diamond (1990)
- Restriction violated by recessionary decline in active-passive ratio
  - Workhorse models preclude crowding-out of active search

### What I do

- Document crowding-out of active search during recessions:
  - More active searchers among non-employed who want work
  - But active-passive ratio in job-finding rates falls

Not driven by cyclical composition

- Show formally: violation of perfect substitution
- Rejection of DMP w/ active & passive as perfect subst's
- ► Incorporate diminishing marginal efficiency of active search into three-state DMP, test/estimate, and explore implications:
  - 1. Active search less important during a recession
  - 2. Bailey-Chetty formula prescribes recessionary increase in UI
  - 3. Decentralized allocation not efficient under Hosios condition

# A general model

### Goal

#### Write down labor supply block of DMP model:

- Extensive and intensive margins of active search
- ▶ Procyclical opportunity cost of employment ⇒ countercyclical search
- Job-finding probabilities depend on search efficiency
- Search efficiency is a composite of active and passive search
- Derive theoretical restriction relating
  - Active-passive ratio in job-finding probabilities
  - Average quantity of active search
- ► Then take restriction to data

### Setting

- Representative family à la Andolfatto (1995) and Merz (1996)
  - Unit measure of workers indexed by i within each family
  - ▶  $ne_t$  workers are non-employed,  $1 ne_t$  are employed Perfect consumption insurance within family
- Concave utility over consumption
- Workers must sacrifice leisure to work or search
- Contacts generated through CRS matching function m<sub>t</sub>
- $\triangleright$  Large measure of firms post  $v_t$  vacancies search
- Search of non-employed can be passive and/or active

### Active and passive search

- Non-employed inelastically provide one unit of passive search
- Non-employed workers choose  $s_{A,i,t}$  units of active search, subject to
  - Fixed costs,  $\varsigma_{i,t} \sim \Gamma$  drawn *iid* w/ probability  $\lambda$
  - ightharpoonup Convex costs,  $c(s_{A,i,t})$
- Flexible to different notions of active search:
  - ▶ Intensive & extensive margin:  $s_{A,i,t} \in \mathbb{R}_+$  (FMST 2022)
  - **Extensive margin only:**  $S_{A,i,t} \in \{0,1\}$  (KMRS 2017)
- $\triangleright$  CRS matching function  $m_t$  over search efficiency and vacancies
- Search efficiency is composite of active and passive search

### Matching function and job-finding probabilities

 $\triangleright$  Job-finding rate,  $f_{i,t}$ 

$$f_{i,t} = \mathbf{s}_{i,t} \cdot \left(\frac{m_t(\mathbf{s}_t, \mathbf{v}_t)}{\mathbf{s}_t}\right) \tag{*}$$

 $\triangleright$  Search efficiency,  $s_{i,t}$ 

$$\mathbf{S}_{i,t} = \omega \cdot \mathbf{S}_{A,i,t} + (1 - \omega) \cdot \mathbf{1} \tag{**}$$

Aggregate active search, s<sub>A,t</sub>

$$\mathbf{s}_{A,t} = \int_{i} \mathbf{s}_{A,i,t} d\Gamma^{u}_{t}$$

Aggregate search efficiency, s<sub>t</sub>

$$\mathbf{s}_t = \omega \cdot \mathbf{s}_{A,t} + (\mathbf{1} - \omega) \cdot n\mathbf{e}_t$$

Fraction of non-employed engaged in active search,  $\Gamma_t^u(\bar{\zeta}_t)$ 

$$\Gamma_t^u(\bar{\zeta}_t) \equiv \int \mathbb{I}\{s_A(x,\varsigma) > 0\} d\Gamma_t^u(x,\varsigma)$$

### Problem of the unemployed

$$egin{aligned} U_{i,t} &= \max_{oldsymbol{S_{A,i,t}}} \left\{ rac{1}{\mu_t} \left( \psi - arsigma_{i,t} \cdot \mathbb{I} \left\{ oldsymbol{S_{A,i,t}} > 0 
ight\} - \chi \cdot rac{oldsymbol{S_{A,i,t}}^{1+\kappa}}{1+\kappa} 
ight) 
ight. \ &+ \mathbb{E}_{t+1|t} \left\{ igwedge_{t,t+1} \cdot \left( f_{i,t} U_{i,t+1} + (1-f_{i,t}) V_{i,t+1} 
ight) 
ight\} 
ight. \ & \qquad \qquad \text{with} \ f_{i,t} &= \left( \omega \cdot oldsymbol{S_{A,i,t}} + (1-\omega) 
ight) \end{aligned}$$

- $V_{i,t}$  ( $U_{i,t}$ ) is consumption-equivalent value of (un)employment
- ► Flow value of leisure  $\psi$  and search cost normalized by marginal utility of consumption  $\mu_t$ , with  $\Lambda_{t,t+1} \equiv \beta \cdot (\mu_{t+1}/\mu_t)$

### Solution

$$\frac{\chi}{\mu_t} \left( \mathbf{s}_{A,i,t}^* \right)^{\kappa} = \mathbb{E}_{t+1|t} \left\{ \Lambda_{t,t+1} \cdot \omega \cdot \mathbf{f}_t \left[ \mathbf{V}_{i,t+1} - \mathbf{U}_{i,t+1} \right] \right\} \quad \text{if } \varsigma_{it} \leq \zeta_t(\mathbf{x}_i)$$

where

$$\boldsymbol{\zeta}_{t}(\boldsymbol{x}_{i}) = \left(\omega \cdot \boldsymbol{s}_{A,i,t}^{*} \cdot \boldsymbol{f}_{t}\right) \cdot \mathbb{E}_{t+1|t} \left\{ \boldsymbol{\Lambda}_{t+1,t} \left[\boldsymbol{V}_{i,t+1} - \boldsymbol{U}_{i,t+1}\right] \right\} - \frac{1}{\mu_{t}} \left[ \chi \left( \frac{\left(\boldsymbol{s}_{A,i,t}^{*}\right)^{1+\kappa}}{1+\kappa} \right) \right]$$

- ightharpoonup MC = MB when net value of active search is positive
- $\triangleright$  Active search ( $s_{A,i,t}$  &  $\zeta_t$ ) can be
  - ightharpoonup Procyclical, from  $f_t$  (substitution effect)
  - $\triangleright$  Countercyclical, from  $\mu_t$  (income effect)

Income effect dominates.

### Restriction: active-passive ratio and average active search

► Restriction in active-passive ratio:  $\bar{f}_{A,t}/\bar{f}_{P,t}$  and  $\bar{s}_A^*$ 

$$\frac{\overline{f}_{A,t}}{\overline{f}_{P,t}} - 1 = \frac{\left(\omega \cdot \overline{s}_{A,t}^* + (1-\omega)\right) \left(\frac{m_t(s_t, v_t)}{s_t}\right)}{\left(1 - \omega\right) \left(\frac{m_t(s_t, v_t)}{s_t}\right)} - 1 = \left(\frac{\omega}{1 - \omega}\right) \cdot \overline{s}_{A,t}^*$$

from eqn's (\*) and (\*\*)

- ▶ Unit elasticity in  $\bar{s}_{A,t}^*$  all other quantities drop out!
  - Match efficiency differenced out
  - ▶ Unobserved heterogeneity of non-employed enters through  $\bar{s}_{A,t}^*$
  - ▶ Where is  $\Gamma_t^u(\bar{\zeta}_t)$ ? (Fraction of non-employed actively searching)
- ▶ Similar restr'n appears in KMRS (2017, AER) & FMST (2022, ECTA) & ...

# the data

Bringing the restriction to

### CPS, 1996-2019

- Starting in 1994, CPS records following for jobless respondents:
  - Whether the respondent would be willing to accept a job
  - ▶ Whether the worker is engaged in nine methods of active search
  - ► If # search methods = 0, why no active search?

Consistent monthly merges available 1996+

- Non-employed worker willing to accept a job is
  - Active searcher if # search methods > 0
  - ► Passive searcher: if # search methods = 0 & "able" to accept work
- Time spent searching near linear in # of search methods (Mukoyama, Patterson, and Sahin 2018) ⇒ measure of search effort
- Note: exclude temporary-layoff for practical and conceptual reasons

### The active and passive non-employed

	Active	Passive	A-NE	Avg. # of
	non-employed	non-employed	$\overline{A}$ - $\overline{NE}$ + $\overline{P}$ - $\overline{NE}$	search methods
mean(x)	4.9	1.3	0.79	1.85
std(x)/std(Y)	11.0	5.7	1.50	2.65
corr(x, Y)	-0.89	-0.70	-0.75	-0.64

Note: Data from CPS, 1996-2019. A-NE and P-NE refer to active and passive non-employed Y indicates quarterly GDP. For second and third row, series are taken as (1) quarterly averages of seasonally adjusted monthly series, (2) logged, then (3) HP-filtered with smoothing parameter of 1600

- Both frac. searching & # of search methods is countercyclical
- See also Osberg (1993), Shimer (2004), Faberman and Kudlyak (2016),
   Elsby, Hobijn and Sahin (2015), Mukoyama, Patterson, and Sahin (2018)

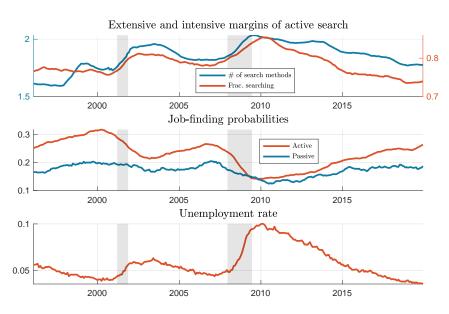
### Job-finding rates of the active and passive non-employed

	$ extit{A-NE}  ightarrow  extit{E}$	$ extit{P-NE}  ightarrow  extit{E}$	A-P
	probability	probability	ratio
mean(x)	0.23	0.17	1/1.32
std(x)/std(Y)	8.67	8.87	9.53
corr(x, Y)	0.85	0.32	0.48

Note: Data from CPS, 1996-2019. A-NE and P-NE refer to active and passive non-employed, "A-P ratio" refers to active-passive ratio of job-finding probabilities, Y indicates quarterly GDP. For second and third row, series are taken as (1) quarterly averages of seasonally adjusted monthly series, (2) logged, then (3) HP-filtered with smoothing parameter of 1600

- Mildy procyclical job-finding probability of passive non-employed
- Highly procyclical job-finding probability of active non-employed
- ► Thus, procyclical active-passive ratio in job-finding probabilities

### Search and job-finding probabilities



### Testing the restriction

Recall restriction:

$$\log\left(\frac{\overline{f}_{A,t}}{\overline{f}_{P,t}}-1\right) = \log\left(\frac{\omega}{1-\omega}\right) + 1 \cdot \log \overline{s}_{A,t}^*$$

Theory predicts unit elasticity

- ▶ Estimated elasticity from data: -5.85 (SE= 0.873)
- Robust to:
  - Inclusion of time trend, cyclical indicator
  - Restricting active searchers to low duration of unemployment
  - ► Controls for cyclical composition along observable dimensions ...
  - ightharpoonup Time-varying  $\omega$  (introduces upward bias into estimated elasticity)
- Rejection of DMP with active and passive as perfect substitutes



# An unrestricted

**CES** search aggregator

### CES aggregator for search effort

▶ Aggregate search effort  $s_t$  given by CES aggregator over  $s_{A,t}$  and  $s_{P,t}$ 

$$\mathbf{s}_t = \left(\omega \left(\mathbf{z}_t \cdot \mathbf{s}_{A,t}\right)^{\rho} + (1-\omega)\mathbf{s}_{P,t}^{\rho}\right)^{\frac{1}{\rho}}$$

w/ exogenous zt

Aggregate active & passive search satisfy

$$\mathbf{s}_{A,t} = \int \mathbf{s}_{A,i,t} d\Gamma^u_t = (\Gamma^u_t(\bar{\zeta}_t)ne_t) \cdot \bar{\mathbf{s}}^*_{A,t}, \quad \mathbf{s}_{P,t} = \int d\Gamma^u_t = ne_t$$

 $\blacktriangleright$   $ME_{A,t}$  and  $ME_{P,t}$  are marginal efficiencies of active and passive search

$$ME_{A,t} = \frac{\partial \mathbf{s}_t}{\partial \mathbf{s}_{A,t}} = \omega \cdot \mathbf{z}_t^{\rho} \cdot \left(\frac{\mathbf{s}_t}{\mathbf{s}_{A,t}}\right)^{1-\rho}, \quad ME_{P,t} = \frac{\partial \mathbf{s}_t}{\partial \mathbf{s}_{P,t}} = (1-\omega) \cdot \left(\frac{\mathbf{s}_t}{\mathbf{s}_{P,t}}\right)^{1-\rho}$$

### Returns to search

▶ The job-finding probability  $f_{i,t}$  of a worker with search efficiency  $s_{i,t}$  is

$$f_{i,t} = \mathbf{s}_{i,t} \cdot \left( \frac{m_t(\mathbf{s}_t, \mathbf{v}_t)}{\mathbf{s}_t} \right)$$

▶ The search efficiency  $s_{i,t}$  of a worker supplying  $s_{A,i,t}$ 

$$s_{i,t} = ME_{A,t} \cdot s_{A,i,t} + ME_{P,t} \cdot 1$$

by linear homogeneity of the CES search aggregator

▶ Nests prior case when  $\rho = 1 \& z_t = 1$ :

$$s_{i,t} = \omega \cdot s_{A,i,t} + (1 - \omega) \cdot 1$$

### Restriction from theory, redux

▶ Relative job-finding probabilities, active vs. passive search

$$\frac{\overline{f}_{A,t}}{\overline{f}_{P,t}} - 1 = \frac{\left(ME_{A,t} \cdot \overline{s}_{A,t}^* + ME_{P,t}\right) \left(\frac{m_t(s_t, v_t)}{s_t}\right)}{ME_{P,t} \left(\frac{m_t(s_t, v_t)}{s_t}\right)} - 1$$

$$= Z_t^{\rho} \cdot \left(\frac{\omega}{1 - \omega}\right) \left(\frac{1}{\Gamma_t^{U}(\xi_t)\overline{s}_{A,t}^*}\right)^{1 - \rho} \cdot \overline{s}_{A,t}^*$$

► Thus,

$$\log\left(\frac{\overline{f}_{A,t}}{\overline{f}_{P,t}}-1\right) = \rho \cdot \log Z_t + \log\left(\frac{\omega}{1-\omega}\right) + (\rho-1) \cdot \log \Gamma_t^u(\zeta_t) + \rho \cdot \log \overline{S}_{A,t}^*$$

**Proof.** Return to data: test restriction in  $\rho$ , estimate  $\omega$  and  $\rho$ 

### Regression estimates

	(1)	(2)	(3)	(4)	(5)	(6)
$eta_{Frac}$	-4.785** (2.0448)	-4.118*** (0.4892)	-8.142*** (1.6186)	-0.381 (2.5928)	-2.986*** (0.6375)	-4.211* (2.2981)
$eta_{\#}$	-2.727** (1.1464)	-3.118*** (0.4892)	_	-2.884** (1.1334)	-1.986*** (0.6375)	_
$eta_{0}$	0.705 (0.8636)	0.995*** (0.2773)	-1.052** (0.4448)	2.233* (1.1453)	1.201*** (0.3315)	0.281 (0.8902)
Additional controls	Time trend		Time trend + unempl. rate			
Constrain $\beta_{Frac} + 1 = \beta_{\#}$ ?	No	Yes	_	No	Yes	_
F-test	$p(\beta_{Frac} + 1 = \beta_{\#})$	$p(\rho = 1)$	$p(\rho = 1)$	$p(\beta_{Frac} + 1 = \beta_{\#})$	$p(\rho=1)$	$p(\rho=1)$
	= 0.719	= 0.000	= 0.000	= 0.297	= 0.000	= 0.070
N	264	264	264	264	264	264
Implied $\rho$		-3.118	-9.142		-1.986	-5.211
Implied $\omega$	_	0.730	0.259	_	0.769	0.570

Note: CPS, 1996-20019

### Regression estimates, Pt. 1

	(1)	(2)	(3)
$eta_{Frac}$	-4.785** (2.0448)	-4.118*** (0.4892)	-8.142*** (1.6186)
$eta_{\#}$	-2.727** (1.1464)	-3.118*** (0.4892)	_
$eta_{f 0}$	0.705 (0.8636)	0.995*** (0.2773)	-1.052** (0.4448)
Additional controls	Time trend		
Constrain $\beta_{Frac} + 1 = \beta_{\#}$ ?	No	Yes	_
F-test	$p(\beta_{Frac} + 1 = \beta_{\#})$	p( ho=1)	$p(\rho=1)$
	= 0.719	= 0.000	= 0.000
N	264	264	264
Implied $\rho$	_	-3.118	-9.142
Implied $\omega$	_	0.730	0.259

### Regression estimates, Pt. 2

	(4)	(5)	(6)	
$eta_{Frac}$	-0.381	-2.986*** (0.0375)	-4.211*	
$eta_{\#}$	(2.5928) -2.884**	(0.6375) -1.986***	(2.2981)	
$eta_0$	(1.1334) 2.233*	(0.6375) 1.201***	0.281	
P0	(1.1453)	(0.3315)	(0.8902)	
Additional controls	Time trend + unempl. rate			
Constrain $\beta_{Frac} + 1 = \beta_{\#}$ ?	No	Yes	_	
F-test	$p(\beta_{Frac} + 1 = \beta_{\#})$	p( ho=1)	p( ho=1)	
	= 0.297	= 0.000	= 0.070	
N	264	264	264	
Implied $ ho$	_	-1.986	-5.211	
Implied $\omega$		0.769	0.570	

### Quick takeaway

$$\log\left(\frac{\overline{f}_t^A}{\overline{f}_t^P} - 1\right) = \rho \cdot \log z_t + \log\left(\frac{\omega}{1 - \omega}\right) + (\rho - 1) \cdot \log \Gamma_t^u(\xi_t) + \rho \cdot \log \overline{s}_t^{A,*}$$

- **Reject** restriction  $\rho = 1$  (i.e., existing framework)
- ► Fail to reject restriction  $\beta_{Frac} + 1 = \beta_{\#}$  (i.e., unrestricted framework)
- ► Elasticity of substitution  $\frac{1}{1-\rho}$  is 1/4 (int. + ext.) or 1/10 (ext. only)
- Quick interpretation (more later):
  - For the worker: active search as a strategic substitute
  - ► For the firm: stable ratio of hires from referrals to outside applications

Application 1:
The marginal efficiency of active search over the business cycle

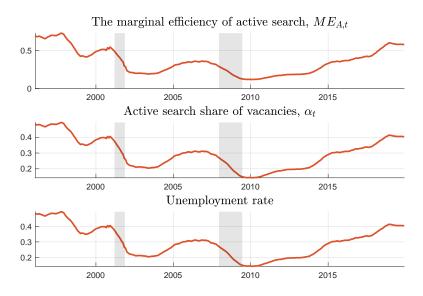
### What is a CES search aggregator?

► Equivalence: separate submarkets for active and passive search

$$m_t(s_t, v_t) = m_t \left( \frac{\textit{ME}_{\textit{A},t} \cdot s_{\textit{A},t}, \alpha_t \cdot v_t}{s_t} \right) + m_t \left( \frac{\textit{ME}_{\textit{P},t} \cdot s_{\textit{P},t}, (1 - \alpha_t) \cdot v_t}{s_t} \right)$$
with  $\alpha_t = \frac{\textit{ME}_{\textit{A},t} \cdot s_{\textit{A},t}}{s_t} = \frac{s_{\textit{A},t}^{\rho}}{s_{\textit{A},t}^{\rho} + s_{\textit{P},t}^{\rho}}, \quad \rho \leq 1$ 

- (Obtains through constant returns)
- ▶ Vacancy share of active search  $\alpha_t$  analogous to factor share
  - $ho < 0 \Rightarrow \alpha_t$  decreasing in  $(s_{A,t}/s_{P,t})$
  - ► Countercyclical  $(s_{A,t}/s_{P,t})$   $\Rightarrow$  Procyclical  $\alpha_t$
- $\blacktriangleright$  ME<sub>A,t</sub> and  $\alpha_t$  both fall during recessions

### Backing out the marginal efficiency of active search



## Application 2:

**Baily-Chetty Formula** 

### Appl. 2) Baily-Chetty Formula

Optimal UI described by Baily-Chetty formula:

$$\frac{d \log u}{d \log R} = \underbrace{\left(\frac{U'(c^u)}{U'(c^e)} - 1\right)}_{\text{decreasing in } R}$$
(BC)

where u is unemployment and R is the replacement rate

- ▶ Landais et al. (2018): if wages are perfectly rigid (+ other conditions), (BC) describes optimal replacement rate R
- ▶ Micro-elasticity  $\frac{d \log u}{d \log R}$  typically taken as constant  $\Rightarrow R$  constant
- ▶ But  $\frac{d \log u}{d \log R}$  is proportional to the marginal efficiency of active search...

### Appl. 2) Baily-Chetty Formula, cont'd

Write micro-elasticity as

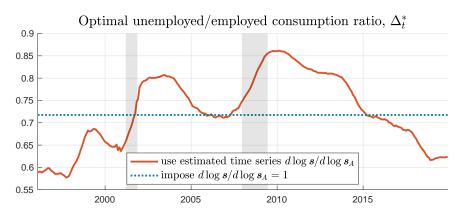
$$\frac{d \log u}{d \log R} = \frac{d \log u}{d \log f} \cdot \frac{d \log f}{d \log R}$$

$$\approx -(1 - \tilde{u}) \cdot \frac{d \log f}{d \log s} \cdot \frac{d \log s}{d \log s_A} \cdot \frac{d \log s_A}{d \log R}$$

$$= -(1 - \tilde{u}) \cdot \sigma \cdot \left[\omega \cdot \left(\frac{s_A}{s}\right)^{\rho}\right] \cdot \frac{d \log s_A}{d \log R}$$

- Note,  $\rho$  < 0, so the elasticity is not constant!
- Next, (i) take avg.  $-\frac{d \log f}{d \log R}$  to be equal to 0.42 (Katz and Meyer, 1990), (ii) compute average  $\frac{d \log s}{d \log s_A}$ , and (iii) solve for  $\frac{d \log s_A}{d \log R}$
- ► Use to obtain time series for  $\frac{d \log u}{d \log R}$

### Appl. 2) Baily-Chetty Formula, cont'd



- ▶ Define unemployed/employed consumption ratio:  $\Delta_t = (c_t^u/c_t^e) 1$
- Assume  $U(c) = \log c$ . Then, (BC)  $\Rightarrow \Delta_t^* = (1 + \frac{d \log u}{d \log R})^{-1}$
- $ightharpoonup \Delta_t^*$  higher during recessions due to marginal efficiency of active search

### **Application 3:**

Failure of Hosios condition

### Appl. 3) Failure of Hosios condition

$$U_{i} = \max_{s_{A,i}} \left\{ \frac{1}{\mu} \left( \psi - \varsigma_{i} \cdot \mathbb{I} \left\{ s_{A,i} > 0 \right\} - \chi \cdot \frac{s_{A,i}^{1+\kappa}}{1+\kappa} \right) + \beta \mathbb{E} \left\{ f_{i}U'_{i} + (1-f_{i})V'_{i} \mid \varsigma \right\} \right\}$$
with  $f_{i} = (ME_{A} \cdot s_{A,i} + ME_{P})$ 

- $\triangleright$  Congestion externality: searchers fail to internalize how  $s_{A,i}$  affects f
- ► Here: searchers also fail to internalize how  $S_{A,i}$  affects  $ME_A$  and  $ME_P$
- $ightharpoonup s_{A,i}^* \uparrow \Rightarrow ME_A \downarrow \text{ and } ME_P \uparrow$

### Appl. 3) Failure of Hosios condition, cont'd

Optimal search, worker's problem:

$$\mathbf{c}'\left(\mathbf{s}_{\mathsf{A},i}^*\right) = \beta \mathbb{E}_i \left\{ \mathbf{M} \mathbf{E}_{\mathsf{A}} \cdot \mathbf{f}(\theta) \cdot \psi_i' \right\}$$

where  $\psi_i$  is the marginal value to the HH of having agent i employed

Optimal search, Planner's problem:

$$c'\left(\mathbf{s}_{A,i}^{SP}\right) = \beta \mathbb{E}_{i} \left\{ M \mathbf{E}_{A}^{SP} \cdot f(\theta^{SP}) \cdot \psi_{i}^{SP,\prime} + \underbrace{\frac{\partial M \mathbf{E}_{A}^{SP}}{\partial \mathbf{s}_{A}} \cdot cov(\mathbf{s}_{A,i}^{SP,\prime}, \psi_{i}^{SP,\prime})}_{<0} \right\}$$

where  $\psi_i^{SP}$  is the marginal social value of having agent i employed

► CE=SP only under constant marginal efficiency of active search, ME<sub>A</sub>

# Conclusion

#### Conclusion

- Crowding-out of active search: during recession,
  - Active search goes up
  - ► Active-passive ratio in job-finding probabilities goes down Inconsistent with perfect substitutability of active and passive search
- Novel implications from three-state DMP w/ imperfect subst.
- Reinforces importance of participation margin for understanding unemployment dynamics and policy

## Extra slides

#### Time spent searching (MPS 2018)

198

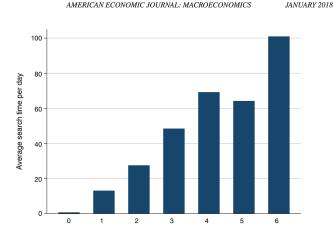


Figure 1. The Average Minutes (per day) Spent on Job Search Activities by the Number of Search Methods

Notes: Each bin reflects the average search time in minutes per day by the number of search methods that the individual reports using in the previous month. Data is pooled from 2003–2014 and observations are weighted by the individual sample weight.

#### Definitions of job search (MPS 2018)

#### TABLE 2—DEFINITIONS OF JOB SEARCH METHODS IN CPS AND ATUS

Contacting an employer directly or having a job interview

Contacting a public employment agency

Contacting a private employment agency

Contacting friends or relatives

Contacting a school or university employment center

Checking union or professional registers

Sending out resumes or filling out applications

Placing or answering advertisements

Other means of active job search

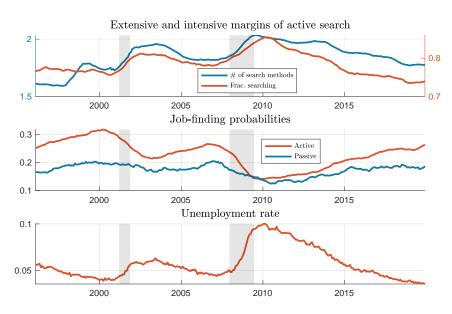
Reading about job openings that are posted in newspapers or on the internet

Attending job training program or course

Other means of passive job search

Note: The first nine are active, the last three are passive.

#### Search and job-finding probabilities



### Elasticity of active-passive ratio in job-finding probabilities

Dependent va	riable: Log acti	ve-passive ratio	o in
in job-find	ling probabilitie	es (minus one)	
	(1)	(2)	(3)
Log # of search methods		-5.017***	-2.977***
	(0.8729)	(0.9411)	(0.9620)
Additional controls	None	e Time trend	Time trend
			+ unempl. rate
$ ho(eta_\#=0)$	0.000	0.000	0.003
$p(\beta_{\#}=1)$	0.000	0.000	0.000
N	264	264	264

#### Elasticity of the active-passive ratio: duration dependence

Dependent variable: Log active-passive ratio in			
in job-finding probabilities (minus one)			
	(1)	(2)	(3)
Log # of search methods	-2.410***	-2.259***	-2.431***
	(0.5178)	(0.6372)	(0.7242)
Additional controls	None	Time trend	Time trend
	None		+ unempl. rate
$p(\beta_{\#}=0)$	0.000	0.001	0.001
$p(\beta_{\#}=1)$	0.000	0.000	0.000
N	287	287	287
CPS 1996-2019			

#### Cyclical composition: groups

- 1. Gender
  - a) Female
  - b) Male
- 2. Race
  - a) Black
  - b) White
  - c) Other non-white
- 3. Age
  - a) 16-24
  - b) 25-55
  - c) 56-64
  - d) 64+
- 4. Martial status (male/female)
  - a) Married
  - b) Previously married
  - c) Never married

- 5. Education
  - a) Less than high school
  - diploma (or equivalent)
  - b) High school diploma
  - (or equivalent)
  - c) Some college
  - d) BA/ Four years of college
  - e) BA+/ More than four years of college
- 6. Region
  - a) Northeast
  - b) Midwest
  - c) South
  - d) West

#### Elasticity of active-passive ratio: cyclical composition

Dependent variable: Log active-passive ratio in in job-finding probabilities (minus one)			
	None	Time trend	Time trend + unempl. rate
		1. Gender	
Log # of search methods	-6.447*** (0.9040)	-5.760*** (1.0593)	-3.004*** (0.9476)
$p(\beta_{\log \#} = 1)$	0.000	0.000	0.000
N	266	266	266
		2. Race	
Log # of search methods	-6.150*** (0.7947)	-5.355*** (0.9732)	-3.439*** (1.0255)
$p(\beta_{\log \#} = 1)$	0.000	0.000	0.000
N	265	265	265
		3. Age	
Log # of search methods	-6.211*** (0.8260)	-4.998*** (0.9519)	-2.117*** (0.7850)
$p(\beta_{\log \#} = 1)$	0.000	0.000	0.000
N	267	267	267

Dependent variable: Log active-passive ratio in in job-finding probabilities (minus one)			
	None	Time trend	Time trend + unempl. rate
	4. Martial status (by gender)		
Log # of search methods	-6.126*** (0.7903)	-5.465*** (0.9173)	-2.520*** (0.8010)
$p(\beta_{\log \#} = 1)$	0.000	0.000	0.000
N	265	265	265
		5. Educatio	n
Log # of search methods	-5.744***	-4.961***	-3.458***
	(0.9564)	(1.0153)	(1.1548)
$p(\beta_{\log \#} = 1)$	0.000	0.000	0.000
N	223	223	223
		6. Region	
Log # of search methods	-5.870***	-4.910***	-2.659***
	(0.8166)	(0.9365)	(0.9044)
$p(\beta_{\log \#} = 1)$	0.000	0.000	0.000
N	265	265	265

#### Random marginal efficiency of active search

Assume that the true DGP is

$$\log\left(\frac{\overline{f}_t^A}{\overline{f}_t^P} - 1\right) = \log\left(\frac{\omega_t}{1 - \omega_t}\right) + 1 \cdot \log \overline{s}_{i,t}^{A,*} + \varepsilon_t$$

with

$$\omega_t = \omega + \mathbf{v}_t, \quad \mathbf{v}_t \& \varepsilon_t \text{ iid}$$

► Then,

$$\begin{split} \tilde{\beta}_{\#} &= \frac{\textit{cov}\left(\log \bar{s}_{t}^{\textit{A},*}, \log\left(\frac{\bar{t}_{t}^{\textit{A}}}{\bar{t}_{t}^{\textit{P}}} - 1\right)\right)}{\textit{var}\left(\log \bar{s}_{t}^{\textit{A},*}, \log\left(\frac{\omega_{t}}{1 - \omega_{t}}\right)\right)} \\ &> 1 \end{split}$$

#### When is active search most effective?

- Question: is job-finding probability increasing in active search effort?
  - Not an obvious question given evidence from aggregate data!
- ► Next, look at individual-level data and introduce
  - Time fixed effects
  - Rich individual controls
- Will show that when aggregate active search is high,
  - Active search effort is less effective
  - Penalty from purely passive search is lower

Suggestive of crowding-out via diminishing returns

#### When is active search most effective? (cont'd)

Dependent variable: Indicator for
moving to employment in subsequent period

	(1)	(2)	(3)
$S_{\hat{l},t}^{A}$	0.006*** (0.0003)	-0.002*** (0.0004)	0.028*** (0.0048)
$oldsymbol{\mathcal{S}}_{i,t}^{A}  imes  ext{relative quantity}$ of active search in aggr.	-	-	-0.003*** (0.0005)
$\mathbb{I}\{\boldsymbol{s}_{i,t}^{A}\neq0\}$	_	0.040*** (0.0013)	0.202*** (0.0125)
$\mathbb{I}\{\boldsymbol{s}_{i,t}^{A} \neq \boldsymbol{0}\} \times \text{relative quantity}$ of active search in aggr.	-	-	-0.016*** (0.0012)
N	865,079	865,079	865,079
Time fixed effects?	Yes	Yes	Yes
Region fixed effects?	Yes	Yes	Yes

Note: Sample of active and passive non-employed, 1996-2019. Includes controls for education, gender, race, marital status, a quartic for age, and fixed-effects for time and region.