

固定收益证券

路磊

北京大学光华管理学院

课程信息

- 本科生选修课
- 周五上午: 9-12点
- 路磊
 - 办公室: 光华新楼 361
 - 电话: 6276-7227
 - E-mail: <u>leilu@gsm.pku.edu.cn</u>
 - 。 答疑时间: 预约
- 助教: 陈靖
 - E-mail: cjing@pku.eddu.cn

课程概述和目标

- 课程概述: 本课程包括固定收益证券的工具,定价和风险管理。
- 课程目标:通过本课程的学习,学生对固定收益证券市场的基本理论,定价,以及风险管理有一定的了解,能够把理论和实践结合起来。

课程教材

- Fixed Income Securities, 2nd Edition by Bruce Tuckman (John Wiley & Sons, Inc)
- 固定收益分析, Frank Fabozzi (著),张敦力,赵纯祥(译), 东北财经大学出版社,2011年。
- 债券市场,分析和策略,Frank Fabozzi(著),路蒙佳(译),中国人民大学出版社,2010年。



www.chinabond.com.cn

www.bondmarket.com

www.federalreserve.com

www.standardpoors.com

www.bis.org

www.bloomberg.com

课程材料

- 讲义:课前在course.pku.edu.cn上下载讲义,含有大量的案例分析。
- 参考资料: 大量的资料可以从以上网址下载。
- 案例分析: 利用课堂所学知识, 进行案例分析。
- 作业: 有一定数量的作业,难度适中。
- 课程论文:可以是一个实证分析,也可以是一篇关于中国债券市场的论述性报告。
- 教学方式: 教师教授为主,希望同学们积极发言。

课程评估

- 课堂参与和作业完成情况: 30%
- 案例分析(小组形式): 20%
- 课程论文: 50%

课程安排

Tuckman	Topic		
Chapter 1	Introduction to Fixed Income Markets		
Chapter 15			
Notes			
Chapter 3	Bond Analytics		
Chapters 5-6	The Salomon Brothers Bond Squeeze		
Notes			
Chapter 2	Term Structure of Interest Rates		
Chapter 9-14	Interest Rate Models		
Notes			
Notes	Measuring Risk and Reward of bonds with imbedded		
	options		
Notes	Portfolio Management Strategies		
Chapters 15-20	Fixed Income Derivatives		
Notes			
Chapter 21	Mortgage Backed Securities		
Notes			
Chapter 21	CMOs and Asset Backed Securities		
Notes			
Notes	Convertible Bonds		
	Credit Derivatives		
Chapters 7-8	Risk Management/Hedging		
Notes			



Fixed Income Markets

- US Government Securities
 - Treasury Securities
 - Agency Securities
- Municipal Bonds
- Corporate Debt
- Money Markets
- Mortgage-Backed Securities (MBS)
- Asset-Backed Securities (ABS)
- Fixed Income Derivatives

Bonds

- A bond is a contract between the issuer and the purchaser where:
 - The purchaser lends money to the issuer
 - The issuer promises to pay it back with interest
 - In the US, the issuer usually pays interest payments twice per year and pays interest and principal when the bond matures.

Bond Terminology

- Par Value
 - Face value of each bond
- Maturity
 - Date all debt is paid off (e.g., Maturity is 8/15/2019)
 - Also used for time until that date (e.g., maturity is ten years)
- Coupon Rate
 - In the US, Interest Rate is usually paid every six months
 - If coupon rate is 10%, then the owner gets two payments per year of 5% of the par value

Bond Terminology

Price

- Expressed as a percent of par value. Price of 100% referred to as "par."
- Price does not include Accrued Interest

Yield

- Nominal rate used to discount all cash flows of the bond.
- The one period rate is (yield/2)

US Treasury Securities

- Market Size
 - \$13,361,739,911,386.51 (as of 8/23/2010)
 - \$ 8,833,342,442,821.93 in Marketable Securities
- Treasury Bills (Maturity less than one year)
- One payment at maturity Sold at a discount
 - Priced using a discount rate
- Treasury Notes (Maturity of 2,3,5,10 years)
 - Interest paid semiannually, principal repaid at maturity
- Treasury Bonds (Maturity 30 years)
 - Interest paid semiannually, principal repaid at maturity
- Treasury Inflation-Protected Securities (TIPS)
 - Interest paid semiannually, principal repaid at maturity
 - Principal amount grows according to an inflation index
- Treasury Strips
 - One single payment in the future. Priced at a discount to face value.

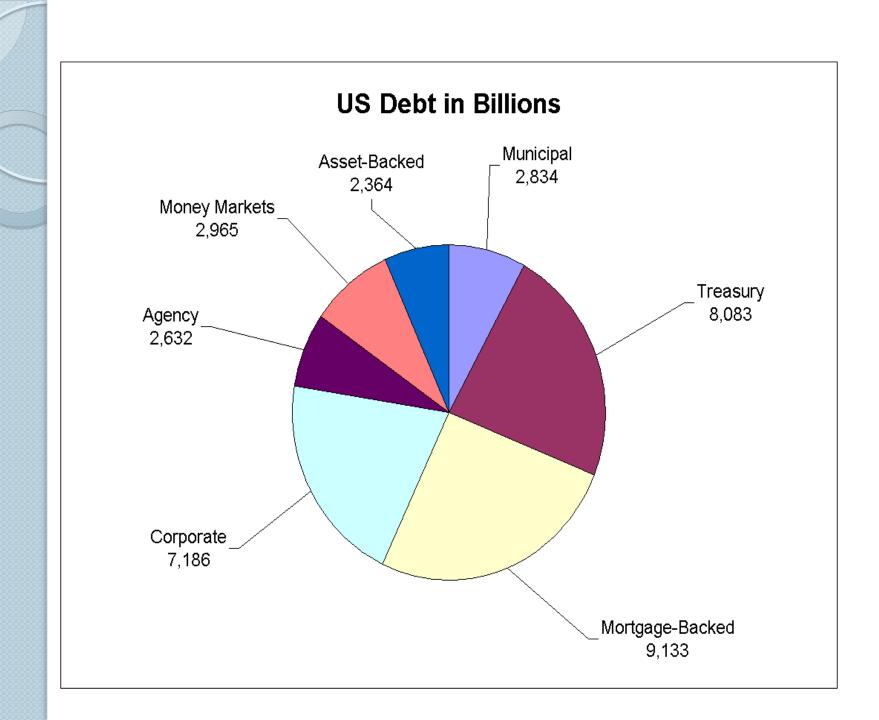
US Public Debt As of 8/23/2010

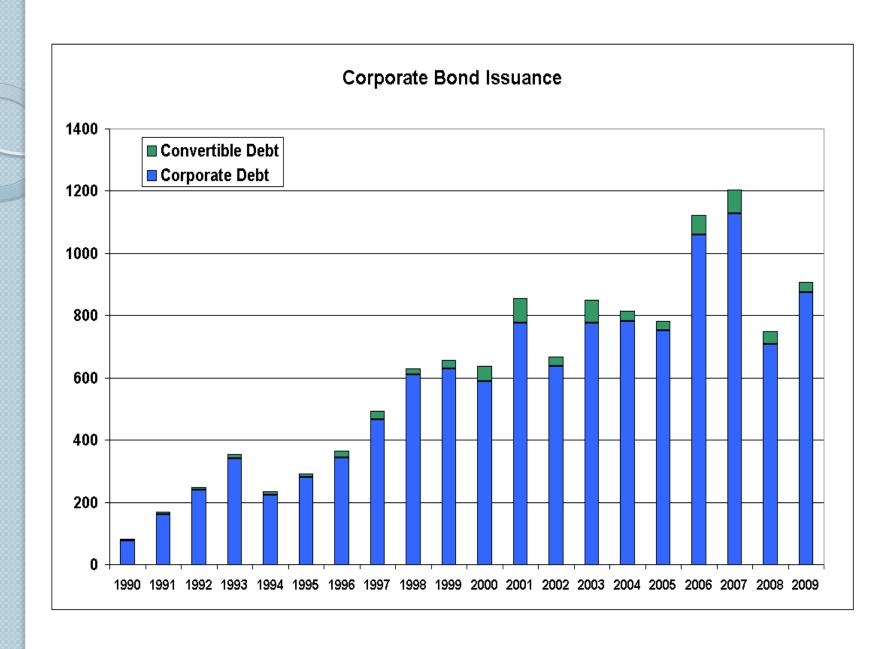
- Total: \$13,361,739,911,386.51
- \$12,327,380,804,696.82 (as of 1/22/2010)
- \$11,896,808,244,570.28 (as of 10/22/2009
- \$11,605,521,079,875.38 (as of 7/23/2009)
- \$10,617,861,263,183.30 (as of 12/30/2008)
- \$9,618,734,657,724.09 (as of 8/26/2008)
- \$8,984,216,518,515.89 (8/30/2007)
- \$8,919,046,678,032.00 as of 7/1/2007
- \$7,777,880,152,594.89 as of 6/1/2005
- \$6,792,556,749,803.50 as of 9/2/2003
- \$6,380,582,269,971.85 as of 1/13/2003
- \$5,574,178,209,886.86 as of 9/30/2000
- Marketable: \$8,833,342,442,821.93
- Non-marketable: \$4,528,397,468,564.58
- In December 2009, the breakdown was:
- T-Bills: \$1,788 B
- T-Notes: \$4,179 B
- T-Bonds: \$715 B
- Inflation: \$568 B

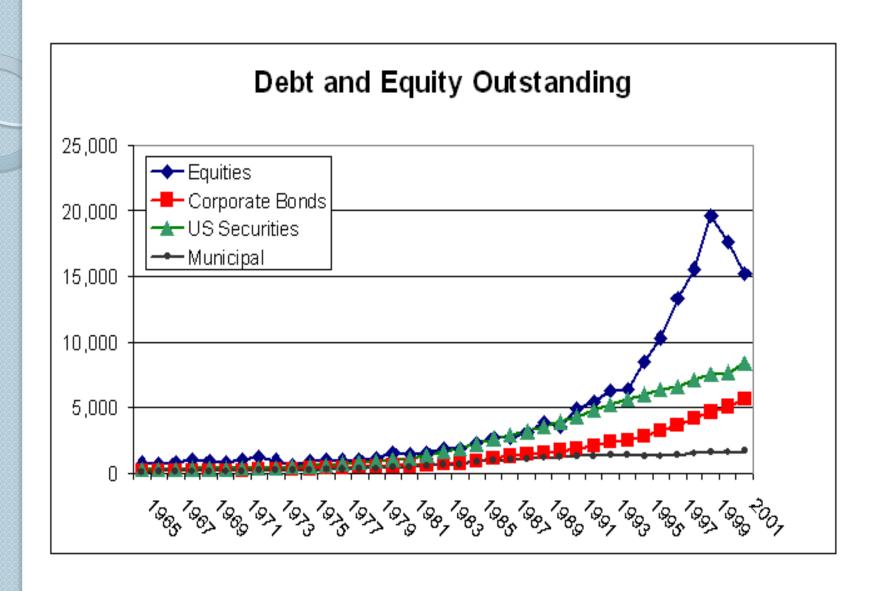
Outstanding US Debt in Billions

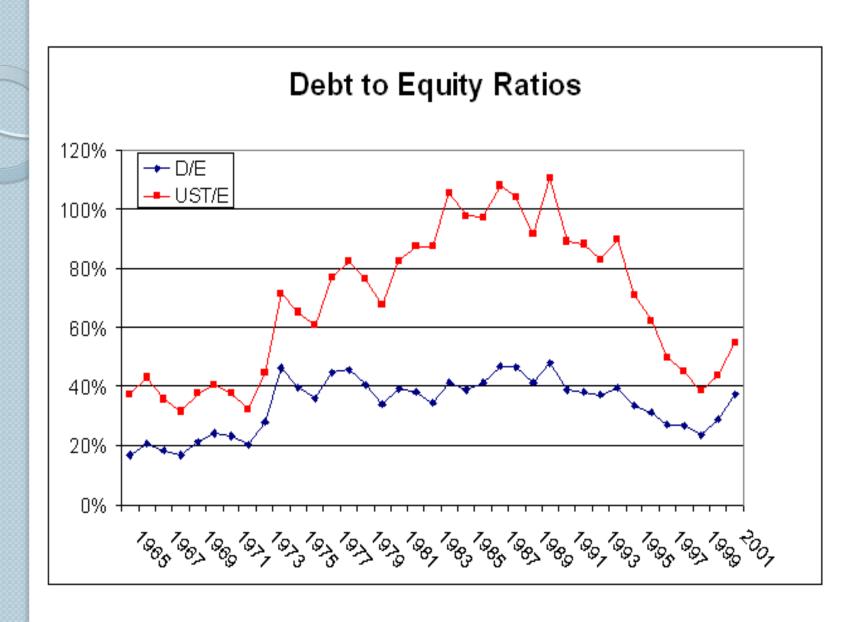
	2010-Q1	2008-Q3	∆ Outstanding
Municipal	2,834	2,639	195
Treasury	8,083	5,716	2,368
Mortgage-Backed	9,133	9,121	12
Corporate	7,186	6,135	1,051
Agency	2,632	3,176	(543)
Money Markets	2,965	3,942	(977)
Asset-Backed	2,364	2,794	(431)
Total	32,036	33,524	(1,488)

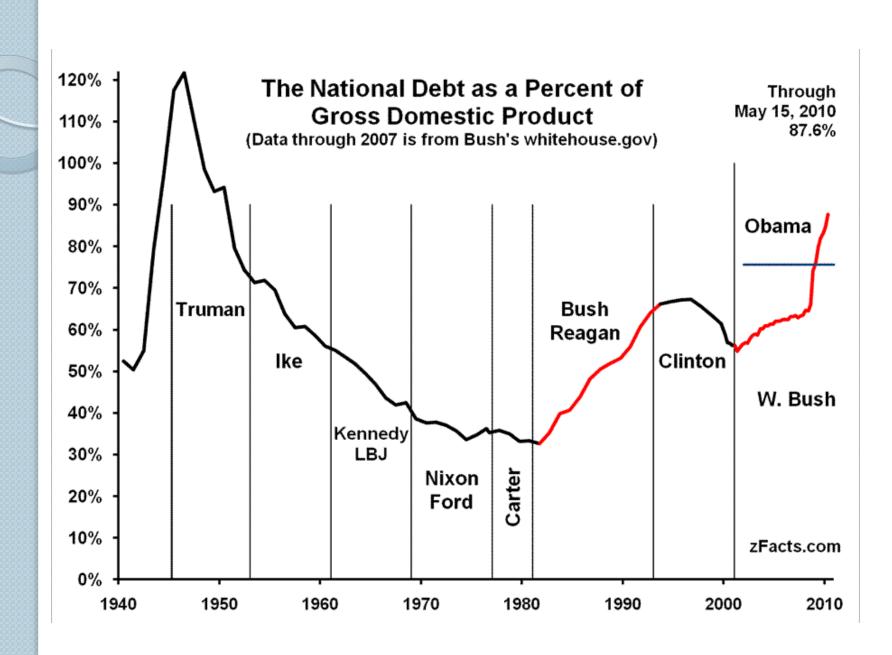
Source: SIFMA











Terminology (US Treasury Securities)

- Bills:
 - Short term.
 - One payment at maturity
- Notes & Bonds:
 - Intermediate-term (Notes), Long-term (Bonds)
 - Interest paid regularly
 - Principal paid at maturity
- On-The-Run (OTR) vs Off-The-Run:
 - OTR most recently issued
 - An Off-the-run ten year bond could be a 30-year bond that was issued about 20 years ago.
 - An On-the-run ten year bond was just issued recently

Bond Yield

• Yield:

- Internal Rate of Return (IRR) that equates present value of cash flows with price plus accrued interest.
- Yield is expressed as a semiannual rate meaning it is expressed as a yearly rate with two compounding periods per year. If Yield = 8%, then effective annual rate is calculated:

$$r = \left(1 + \frac{.08}{2}\right)^2 - 1 = 1.04^2 - 1 = 8.16\%$$

• Bills:

- Short-term Debt. 4-week, 13 week bill, 26 week bill and (possibly discontinued) 52-week bill.
- Sold at auction at a discount to face value.
- Pays face value at maturity.
- Price quoted as a discount rate

- Treasury Notes
 - 2-year, 5-year, 10-year Debt Obligations
 - Sold at Auction
 - Semiannual Interest Payments
 - Principal plus one period of Interest paid at Maturity
 - Price quoted as % of Par or as Yield

- Treasury Bonds
 - 30-year Debt Obligations
 - Discontinued in the late 1990s, but brought back a couple years ago
 - Sold at Auction
 - Semiannual Interest Payments
 - Principal plus Interest paid at Maturity
 - Price quoted as % of Par or as Yield

- Inflation Indexed Notes & Bonds
 - Coupon Rate set at Auction
 - Principal is adjusted for inflation, and is paid at maturity
 - Semiannual payments based on outstanding inflation adjusted principal.
 - Index is the non-seasonally adjusted U.S. City Average All Items All Urban CPI (CPI-U)
 - We won't be valuing inflation indexed bonds in this class

- Features
 - No Credit Risk
 - Liquid Market
 - Prices quoted in 32nds or 64ths
 - 103:12 → 103 12/32% of par
 - 103:12+ → 103 25/64% of par
 - Accrued Interest (AI)
 - d = days from last coupon to settlement
 - D = total days in coupon period
 - C = coupon rate
 - Present Value is Par Amount times (Price plus AI)

$$AI = \left(\frac{d}{D}\right)\left(\frac{C}{2}\right)Par$$

Accrued Interest

- In most finance classes, bonds are always priced using whole periods.
- In this class, the real world (and the WSJ), there is usually less than one whole period until the next coupon.
- The IRS uses the capital gains rate for any changes in capital (price) but charges the ordinary rate on interest.
- Therefore, they want value broken up into the principal portion and interest portion so that they can calculate taxes.

Accrued Interest

- Day Counting:
 - For Government bonds, the number of days since the last coupon was paid and the total number of days in the period are the actual number of days
 - For most other bonds, the calculations use 360 days per year (180 days per half year) and 30 days for each month.
 - This means that for Government bonds, the accrued interest for the following periods different, but for corporate bonds, they are all the same
 - From 2/15-3/15
 - From 3/15-4/15
 - From 4/15-5/15

Treasury Auctions

- Treasury Bills
 - 4-week, 13-week and 26-week bills: Offered each week.
 - **52-week bills:** Were offered every four weeks may have been discontinued.
 - **2-year, 5-year notes:** Issued monthly.
 - **10-Year Notes** Issued February, May, August and November
 - **30-year bond:** Issued February and August
 - Inflation-indexed security (note or bond): January, April, July, and October – depending on maturity.

Auction Process

- Auction is announced.
- "Sealed" Bids are accepted by Phone, Internet or on Paper.
 - Noncompetitive Bids
 - Up to \$1MM (Bills) \$5MM (Other)
 - Security Purchase Guaranteed
 - Competitive Bids
 - Bills Bid Discount rate and Amount
 - Notes & Bonds Bid Yield and Amount
 - Bidding is limited to 35% of the issue per bidder

Auction Process

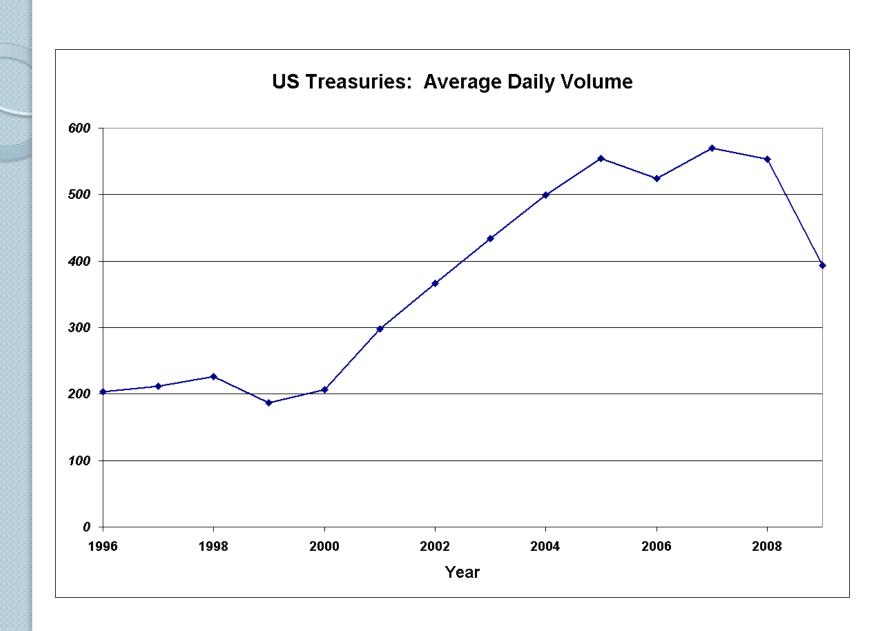
- Coupon Rate is set at the highest accepted bid.
 - All noncompetitive bids are filled at this interest rate.
 - All bids with lower yields are filled at this rate.
 - All bids at this rate share what remains.
 - All bids at a higher yield are rejected.

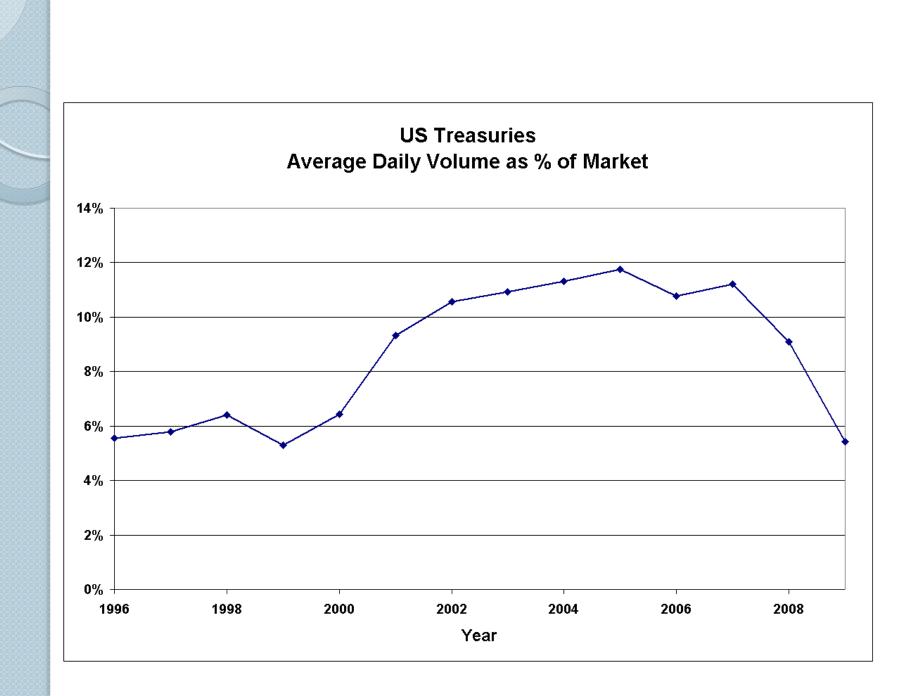
Auction Process: Who Bids?

- Most noncompetitive bids are from individuals
- Competitive bids come from institutions and Primary Issuers
- Primary Dealers:
 - Investment banks that bid for their clients.
 - Prior to 1991, others could only order for their own account
 - Capital Reserves & Volume requirements
- In 1991, Salomon Brothers cornered the market on the two-year note.
 - The fallout from this caused the Treasury to change its rules to make the auction more competitive
 - We will discuss the Salomon Bond Squeeze in the next class

Secondary Market

- Buy or Sell after auction
 - Mainly on-the-run treasuries
- Reasons for high volume
 - rebalancing portfolios
 - corporations with spare funds
 - Interest rate hedgers/speculators





Secondary Market

- OTC (Dealer) Market
 - No Exchange Phones or computers used to place orders
 - Bid and Ask set by Dealers
 - 50/50 trading with customers/other dealers
 - Institutional markets dominate retail

Secondary Market

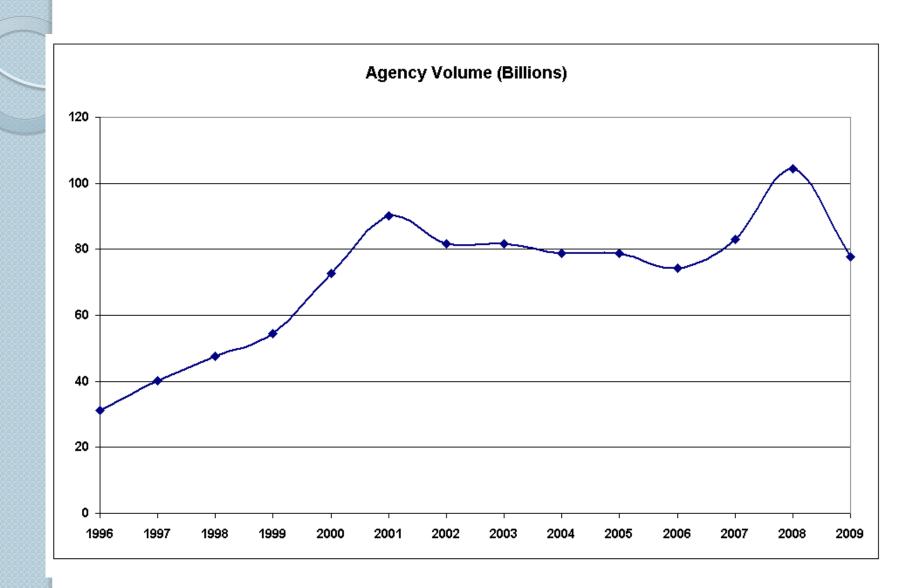
- Trading begins when issue is announced ('When-issued' trading).
- On-the-run most recently issued securities
 - The market for OTR securities is much more active
- Trading concentrated in "when-issued" and on-the-run issues.
- Trades settle on the next business day (T+1)

Treasury Strips

- Coupon bonds can be split into strips.
- Strips (or Zeros) pay principal at maturity, but pay no interest.
- Original strips: TIGRs (Merrill Lynch) Early 1980s
- Priced at a discount
- Arbitrage keeps strips market in line with bond prices

Agency Bonds

- Bonds sold by US Agencies
 - Fed Home Loan Bank
 - Federal Farm Credit
 - Student Loans (SLMA)
 - GNMA
- These bonds use corporate bond conventions for yield and accrued interest
 - These conventions are slightly different from treasuries
- "Full faith and credit" of US
- Trade at slight spread to Treasuries



Corporate Bonds

- Corporations can borrow money through the corporate bond market
- The company pays interest (the coupon) every six months, and pays principal plus interest at maturity.
 - Foreign corporations might not pay semiannually
- There is credit risk (the company could default)
- Many corporate bonds have other features, which we will discuss later in the course.
- Delivery is T+3 (trade date plus three business days)
- Daily Volume About \$15B (2010)

Present Value Review

Financial Principals

- 1. Money is worth more now than in the future.
- 2. Investors demand to be rewarded for taking on risk.
- 3. Two assets that always have the same payoffs have the same price (the *Law of One Price*)

Present Values

- The price of a financial asset will be tied to (at least) two things:
 - Time until you get the money
 - Risk associated with how much you get
- Let's start off by considering the value of a future payment when there is no risk to the amount that you will receive

Present Value

- Notation
 - V_0 Value Today
 - V_n Value after n periods
 - n Number of Periods
 - r Effective Periodic Rate
 - R Nominal Interest Rate (APR)
 - *m* Number of Compounding Periods/Year
 - t Number of Years
 - APR *Effective* Annual Rate (compounded rate)

One Year - One Period

• If there is one compounding period of a year, then:

$$APR = r = R = \frac{V_1}{V_0} - 1$$

Multi-Period Effective Annual Rate

$$APR = (1+r)^m - 1 = \left(1 + \frac{R}{m}\right)^m - 1$$

Compounding Example

Using the following formula and R = 6%,

$$r = \left(1 + \frac{R}{m}\right)^m - 1$$
 we get:

	Nominal Rate	Periods	Periodic Rate	Effective Rate
Yearly	6%	1	6.00%	6.000000%
Semiannual	6%	2	3.00%	6.090000%
Quarterly	6%	4	1.50%	6.136355%
Monthly	6%	12	0.50%	6.167781%
Daily	6%	365	0.01644%	6.183131%
Hourly	6%	8,760	0.00068%	6.183633%
Every Second	6%	525,600	0.0000114%	6.183654%
Continuous	6%	N/A	N/A	6.183655%

Continuous Compounding

$$APR = \lim_{m \to \infty} \left(1 + \frac{R}{m} \right)^m - 1 = e^R - 1$$

Note: We will not do very much with continuous compounding until we talk about FI Derivatives

Future Value

• Invest V_0 for one period:

$$V_1 = V_0 (1+r)$$

• Invest for 2 periods

$$V_2 = V_1 (1+r) = V_0 (1+r)^2$$

• Invest for *n* periods

$$V_n = V_0 (1+r)^n$$

Present Value

• Use algebra to define Present Value in terms of Future Value

$$V_0 = V_n / (1+r)^n$$

Present Value

- What do we need
 - Value of future cash flow
 - Number of periods until that flow is received
 - Periodic Interest Rate

Multiple Cash Flows

- Suppose you have two cash flows, F_1 and F_2 . Then the present value of those flows is equal to the sum of the present values.
- In general:

$$PV(F_1,...,F_k) = \sum_{j=1}^k PV(F_k)$$

Perpetuities & Annuities

Perpetuity: A fixed payment is made each period forever

• Annuity: A fixed payment is made each period for a specific number of periods.

PV of a Perpetuity

- C = Amount Paid each period
- r = Periodic Interest Rate

$$PV = \frac{C}{r}$$

- Where does this come from?
 - Do you remember geometric series from Calculus?

Perpetuities

$$V = \sum_{k=1}^{\infty} \frac{C}{(1+r)^k}$$

$$V = \frac{C}{(1+r)} + \sum_{k=2}^{\infty} \frac{C}{(1+r)^k}$$

$$V = \frac{C}{(1+r)} + \frac{1}{(1+r)} \sum_{k=1}^{\infty} \frac{C}{(1+r)^k}$$

$$V = \frac{C}{(1+r)} + \frac{1}{(1+r)} V$$

$$V\left(\frac{r}{(1+r)}\right) = \frac{C}{(1+r)}$$

$$V = \left(\frac{C}{(1+r)}\right) \left(\frac{(1+r)}{r}\right) = \frac{C}{r}$$

The good news: You don't need to know this.

I just wanted you toknow that there is a reason why this formula works

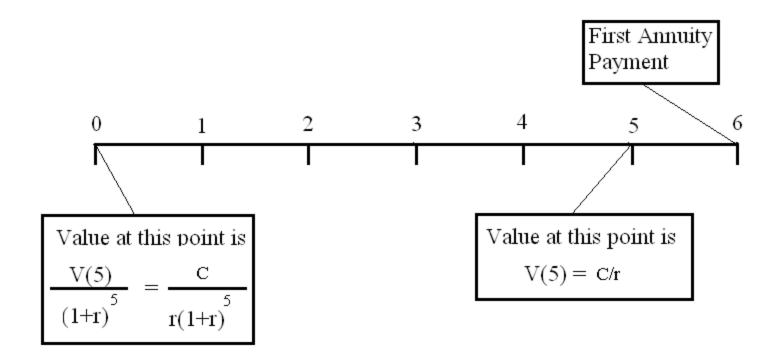
Value of a Perpetuity That Starts in the Future

- What is the value of a perpetuity that starts paying in period (n+1) (time t_{n+1})
- We know that the value at time t_n is
- So we need to discount this back to the present. The PV of a perpetuity that starts paying in period (n+1) is

$$PV = \frac{1}{(1+r)^n} \frac{C}{r} = \frac{C}{r \cdot (1+r)^n}$$

Value of a Perpetuity That Starts in the Future

• Consider this time line:



Annuity

- An annuity pays a fixed amount, C, for a predetermined number of periods.
- An *n*-period annuity pays C for *n* periods.
- The present value is:

$$PV = \sum_{k=1}^{n} \frac{C}{(1+r)^k}$$

- This is easy to calculate if *n* is small, but difficult if it is large
- But there is a better formula

Annuity

- An annuity can be thought of as a perpetuity that starts now minus a perpetuity that starts in period (n+1).
- Therefore, its value must be equal to the value of a perpetuity that starts in period 1 minus the value of a perpetuity that starts in period (n+1)

PV of Annuity

• Assume C is paid for *n* period.

$$PV = \frac{C}{r} - \frac{C}{r(1+r)^n}$$

Growing Perpetuities

- A growing perpetuity is an asset that pays in every period with the payment growing over time at some rate *g*.
 - The cash flows look like C, C(1+g), $C(1+g)^2$, ...
- How do we find the present value of a growing perpetuity.
- The present value is:

$$PV = \sum_{k=1}^{\infty} \frac{C(1+g)^{k-1}}{(1+r)^k} = \frac{C}{r-g}$$

Present Value Summary

Assume that r is the one period interest rate:

The present value of a cashflow C that is paid after n periods is :

$$PV(C) = \frac{C}{\left(1+r\right)^n}$$

The present value of a perpetuity that pays C in every period is:

$$PV = \frac{C}{r}$$

The present value of a growing perpetuity that pays C in the first period and grows at g is:

$$PV = \frac{C}{r - g}$$

The present value of a perpetuity that pays C starting in period (n+1) is:

$$PV = \frac{C}{r \cdot (1+r)^n}$$

The present value of an anuity that pays C for n periods is :

$$PV = \frac{C}{r} - \frac{C}{r \cdot (1+r)^n}$$

Money Markets

- Money Market instruments are a collection of short term debt obligations including:
 - T-Bills
 - Commercial paper
 - Repurchase Agreements
 - Federal Funds
 - Banker's Acceptances
 - Eurodollar Deposits & CDs

Treasury Bills

- All the safety of T-Bonds
- Maturity 3 mo, 6 mo, 1 year (discontinued)
- No coupons or accrued interest
- Auctioned by Treasury
- Market size \$1,788 B (2009-Q3)
- Priced by Discount Rate:

$$P = Par - Par \times Discount \times \frac{\text{Daysto maturity}}{360}$$

Fed Funds Market

- Fed Funds The Fed requires banks to deposit reserves.
 No interest paid
- Fed Funds Market Banks with excess reserves lend reserves to those who need it at Fed Funds rate.
- Interest Paid = Principal×days×Rate/360
- Commercial Banks are largest investors
- Very short-term usually overnight

Fed Funds Market

- Fed sets policy with target rate
- Risks are small
 - Short-term maturities
 - High quality borrowers
- Rates tied to Repo Market, since banks can borrow there to raise cash for reserves.
- Billions of Dollars traded per Day
 - 2/3 from Commercial Banks
 - 1/3 from Broker/Dealers

Commercial Paper

- Corporate Debt
 - Short term (up to 270 days) due to SEC registration rules
 - Less than 90 days: larger market (can be used as collateral with Fed)
 - Often roll over debt to pay back
 - Alternative to bank loans
 - High quality firms (Many financial companies)
- Market size \$1,066B (7/2010)
 - Less than half of 2007 levels
 - Source SIFMA

Commercial Paper

- Default Risk minimal
 - One default from 1971-1988
 - Three in 1989, Four in 1990
 - Lehman Brothers defaulted on CP in 9/2008
 - Rated by Moody's, S&P, Fitch
 - Risk is that Company cannot pay
- Dealer Placed or Directly Placed
- Priced by Discount Rate (like T-Bills)

Commercial Paper

- Light trading in secondary market
- Bought by MM Mutual Funds, trusts, companies with short term surplus
- How do they differ from T-Bills
 - Pay higher rate
 - Credit risk
 - State & local taxes on interest
 - Less liquid

Eurodollar Deposits

- Eurodollars are dollar-denominated deposits in banks outside the US
- Multinational companies use Eurodollars to simplify transactions.
- Major banks use Eurodollar market to raise short-term funds
- Rate charged is marginal cost-of-funds
 - Negotiated by major banks many in London. The average rate sets LIBOR
- LIBOR
 - London Inter-Bank Offer Rate

Eurodollar Deposits

- Dealers match buyers & sellers
- There is some credit risk, especially for longer maturities
- LIBOR is often used as a benchmark for risky floating rate debt.
- Note: US Banks sell CDs in a similar manner

Repurchase Agreements The Repo Market

- Market for short-term collateralized borrowing and lending
- Used by financial institutions & Government
 - \$3.8 Trillion (9/2009) 42% decrease from 2008
- What is a repo agreement?
 - One party agrees to buy security at a set date (today or tomorrow) and sell it back the next day. The effect? One party lends money for one day using security as collateral.
 - Borrow funds Repo
 - Borrow Collateral Reverse Repo

Repo Market

- Liquid market for many securities
- Most Repos are Treasuries, though others can be used.
- The lender of funds has unrestricted use of the collateral
- Rates reported like Fed Funds market
- Highly desirable collateral gets low rates are On Special
 - Rates determined demand does the 1st party really need the security or does the 2nd party really need money?
- On-the-run treasuries are often on special (short interest is high)

Repo Market

Haircuts

- The one borrowing money can't borrow against the total value. The amount of 'reserve' is called a haircut
- Haircuts are greater when there is more price risk
 - Note when you borrow for a house or car, you can't borrow the total value.
- Credit risk (counterparty risk) is low
 - Goes both ways.
 - The party who lends money is at risk if the price falls and counterparty defaults. The haircut helps.
 - The party who borrows money is at risk if the price rises and counterparty defaults. The haircut hurts.

Repo Market

Participants

- Dealers (cover shorts, finance positions), Do both & capture spread
- Thrifts, Banks sell collateral (raise short-term funds)
- Federal Reserve (implements policy by buying or selling to set rates)

• Determinants of Repo Rate

- Issue Quality
- Term (maturity) of Repo
- Delivery Requirements
- Availability of requirements
- Fed Policy

Repurchase Agreement (Repo) Market Haircuts during the Crisis*

Asset Class**	July '07 Pre-Crisis	Late July- August	Q3 2007	Q4 2007	Q1 2008	Q2 2008	Q2> Current*
Corporates A-AA rated	0%	0%	0%	0%	0%	0%	0%
Corporates BBB rated	0%	0%	0%	0%	0%	0-5%	0-5%
Corporates < BBB- rated	0%	0%	0%	0%	0%	0-5%	0-5%
ABS AA-AA *	0%	2-5%	3-7%	5-10%	10-15%	15-20%	20-25%
ABS BBB-AA	0%	3-7%	5-10%	10-15%	15-20%	20-25%	20-30%+
ABS < BBB	0-2%	5-10%	10-15%	15-20%	20-25%	No financing	No financing
CLO, Other AA-AAA	0%	2-5%	3-7%	5-10%	10-15%	15-20%	15-25%
CLO, Other BBB-AA	0%	3-7%	5-10%	10-15%	15-20%	20-25%	20-30%
CLO, Other < BBB	0-2%	5-10%	10-15%	15-20%	20-25%	No financing	No financing
CMO, Other AA-AAA	0%	3-7%	4-8%	5-10%+	15-20%	20-25%	20-30%+
CMO, Other BBB-AA	0%	5-10%	5-10%+	15-20%	20-25%	20-25%	No financing
CMO, Other < BBB	0-2%	5-10%	10-20%	20-25%	No financing	No financing	No financing
CDO AA-AAA	0%	3-7%	5-10%	10-20%	15-20%	15-20%	15-20%
CDO BBB-AA	0%	5-10%	10-15%	15-25%	20-30%	25-30%	No financing
CDO < BBB	0-2%	10%+	15-20%	25-30%	No financing	No financing	No financing

Source: Repo trader.

^{*} As of September 15, 2008.