



Chapter 8

Profit Maximization and Supply Behavior



Profit Maximization

- A basic assumption for firm's rational behavior
- Do firms really maximize profits?
- The agency problem for CEOs
- The presence of not-for-profit organizations (hospitals and universities)
- Alchian's survival test theory: a strong argument for profit maximization as an approximation

Economic Profit

- A firm uses inputs $j = 1, \dots, m$ to make products $i = 1, \dots, n$.
- Output levels are y_1, \dots, y_n .
- Input levels are x_1, \dots, x_m .
- Product prices are p_1, \dots, p_n .
- Input prices are w_1, \dots, w_m .



Perfectly Competitive Markets

- Price Taking
 - The individual firm sells a very small share of the total market output and, therefore, cannot influence market price
 - Each firm takes market price as given – ***price taker***
 - The individual consumer buys too small a share of industry output to have any impact on market price

The Competitive Firm

- The competitive firm **takes** all output prices p_1, \dots, p_n and all input prices w_1, \dots, w_m as given constants.

Economic Profit

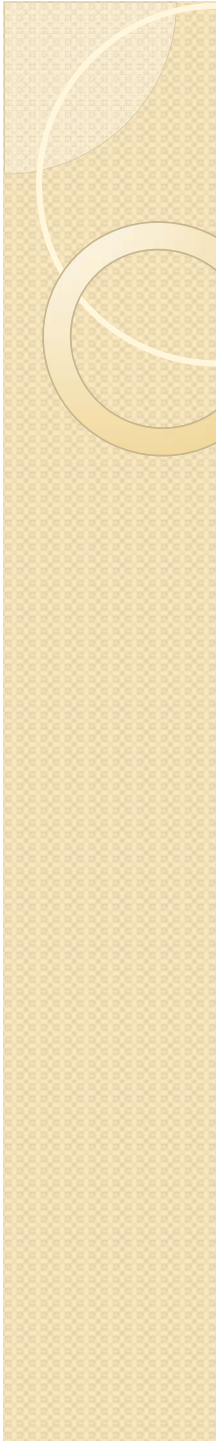
- The economic profit generated by the production plan $(x_1, \dots, x_m, y_1, \dots, y_n)$ is

$$\Pi = p_1 y_1 + \dots + p_n y_n - w_1 x_1 - \dots - w_m x_m.$$

Economic Profit

- How do we value a firm?
- Suppose the firm's stream of periodic economic profits is $\Pi_0, \Pi_1, \Pi_2, \dots$ and r is the rate of interest.
- Then the present-value of the firm's economic profit stream is

$$PV = \Pi_0 + \frac{\Pi_1}{1+r} + \frac{\Pi_2}{(1+r)^2} + \dots$$



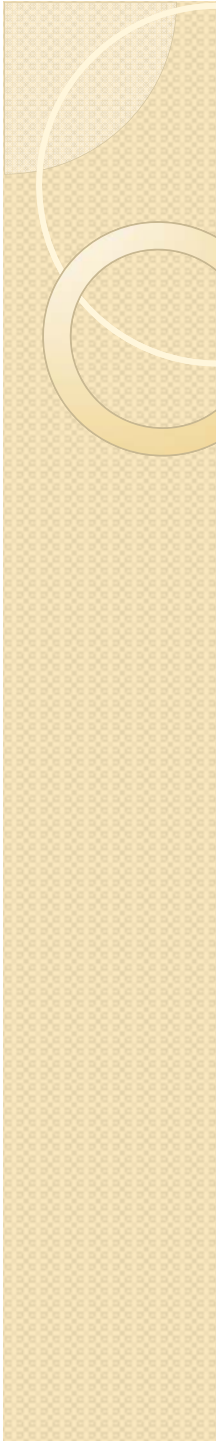
Marginal Revenue, Marginal Cost, and Profit Maximization

- We can study profit maximizing output for any firm, whether perfectly competitive or not
 - Profit (π) = Total Revenue - Total Cost
 - If q is output of the firm, then total revenue is price of the good times quantity
 - Total Revenue (R) = Pq

Marginal Revenue, Marginal Cost, and Profit Maximization

- Costs of production depends on output
 - Total Cost (C) = $C(q)$
- Profit for the firm, π , is difference between revenue and costs

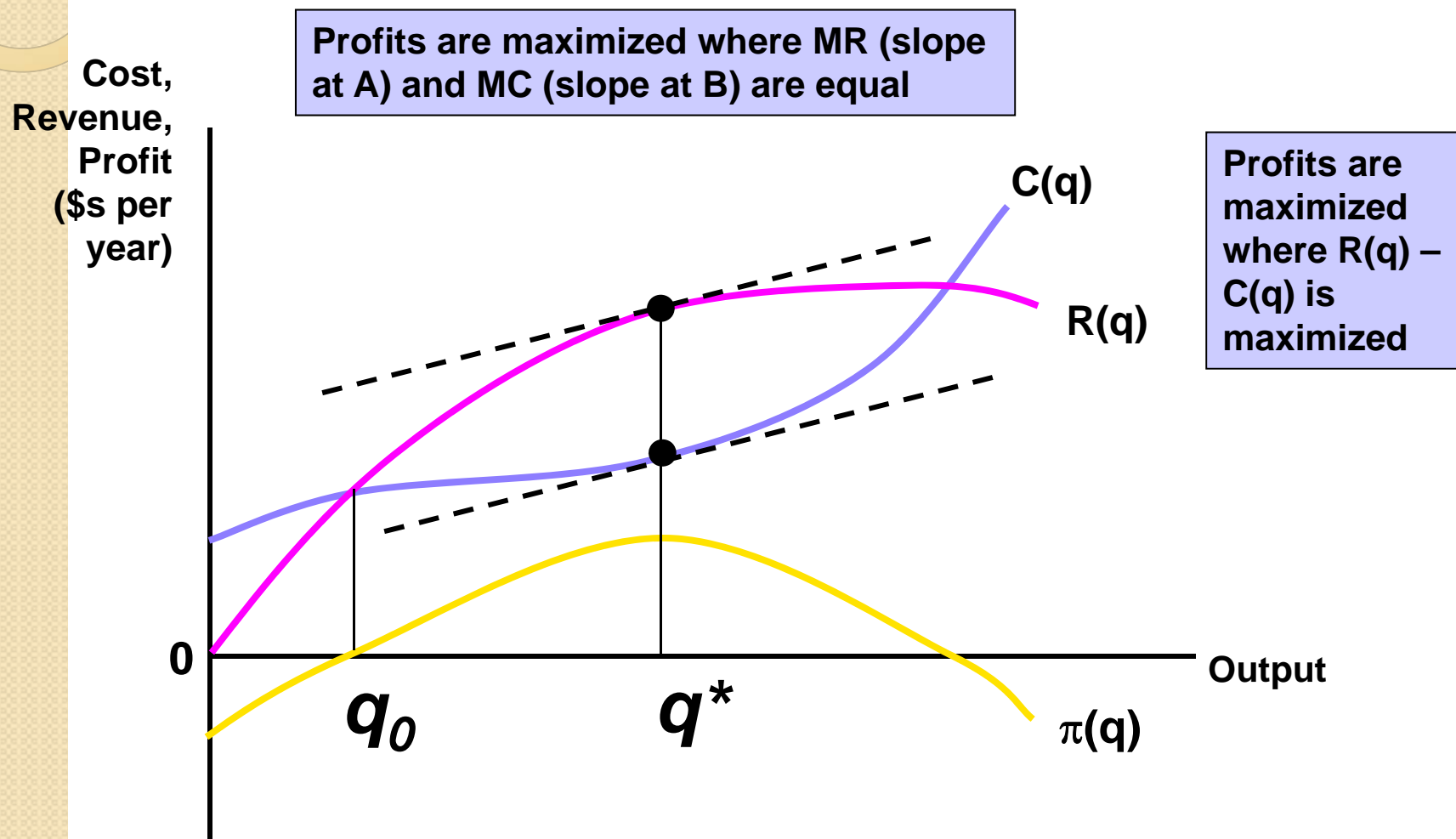
$$\pi(q) = R(q) - C(q)$$



Marginal Revenue, Marginal Cost, and Profit Maximization

- Firm selects output to maximize the difference between revenue and cost
- We can graph the total revenue and total cost curves to show maximizing profits for the firm
- Distance between revenues and costs show profits

Profit Maximization



Marginal Revenue, Marginal Cost, and Profit Maximization

- Profit is maximized at the point at which an additional increment to output leaves profit unchanged

$$\pi(q) = R(q) - C(q)$$

$$\frac{d\pi}{dq} = \frac{dR}{dq} - \frac{dC}{dq} = 0$$

$$= MR - MC = 0$$

$$MR = MC$$



New Assignment

- Problem Set 2
- Due day: November 15
- Lectures for chapters 7, 8, and 9 have been placed in my public folder



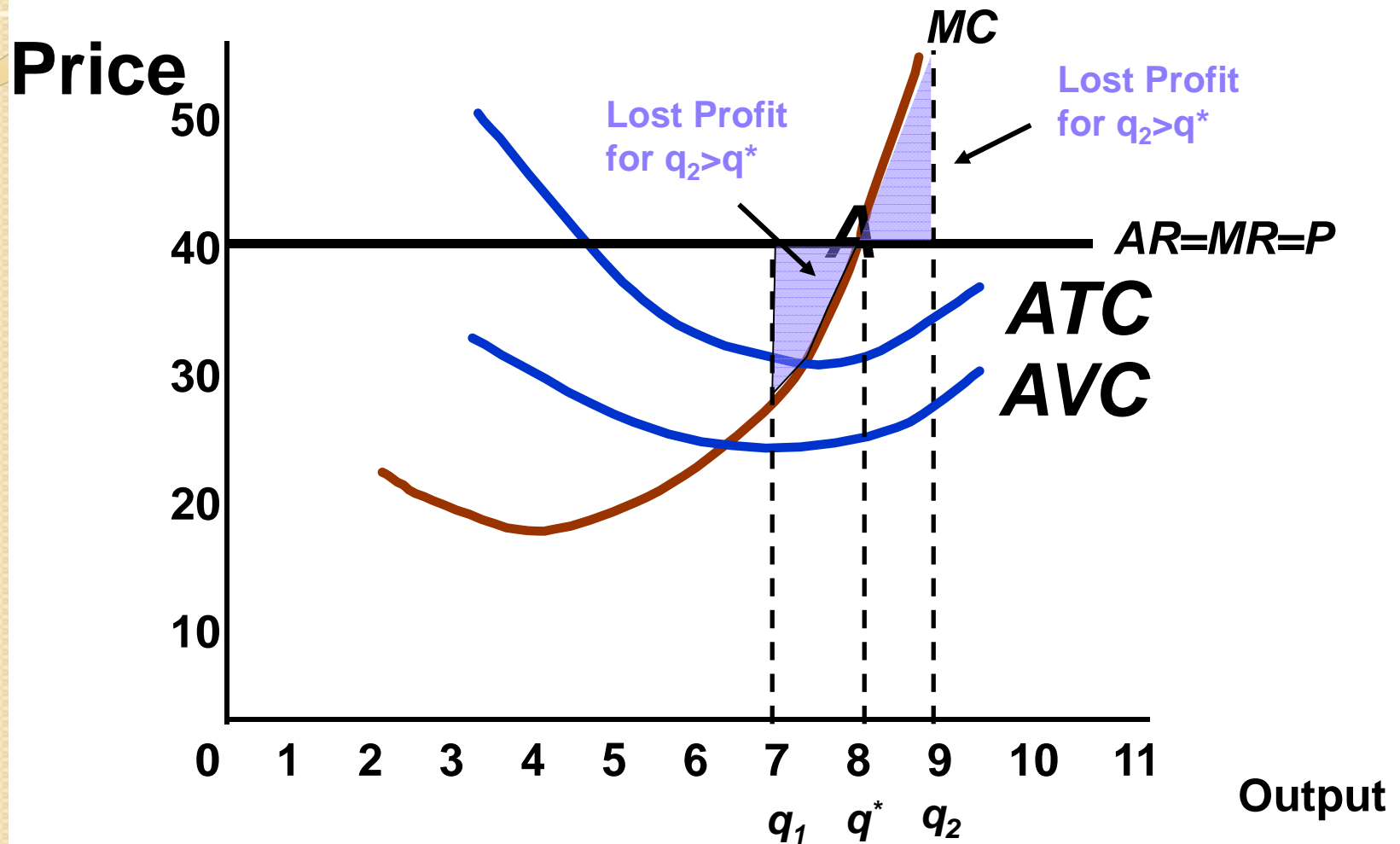
Choosing Output: Short Run

- We will combine revenue and costs with demand to determine profit maximizing output decisions
- In the short run, capital is fixed and firm must choose levels of variable inputs to maximize profits
- We can look at the graph of MR, MC, ATC and AVC to determine profits

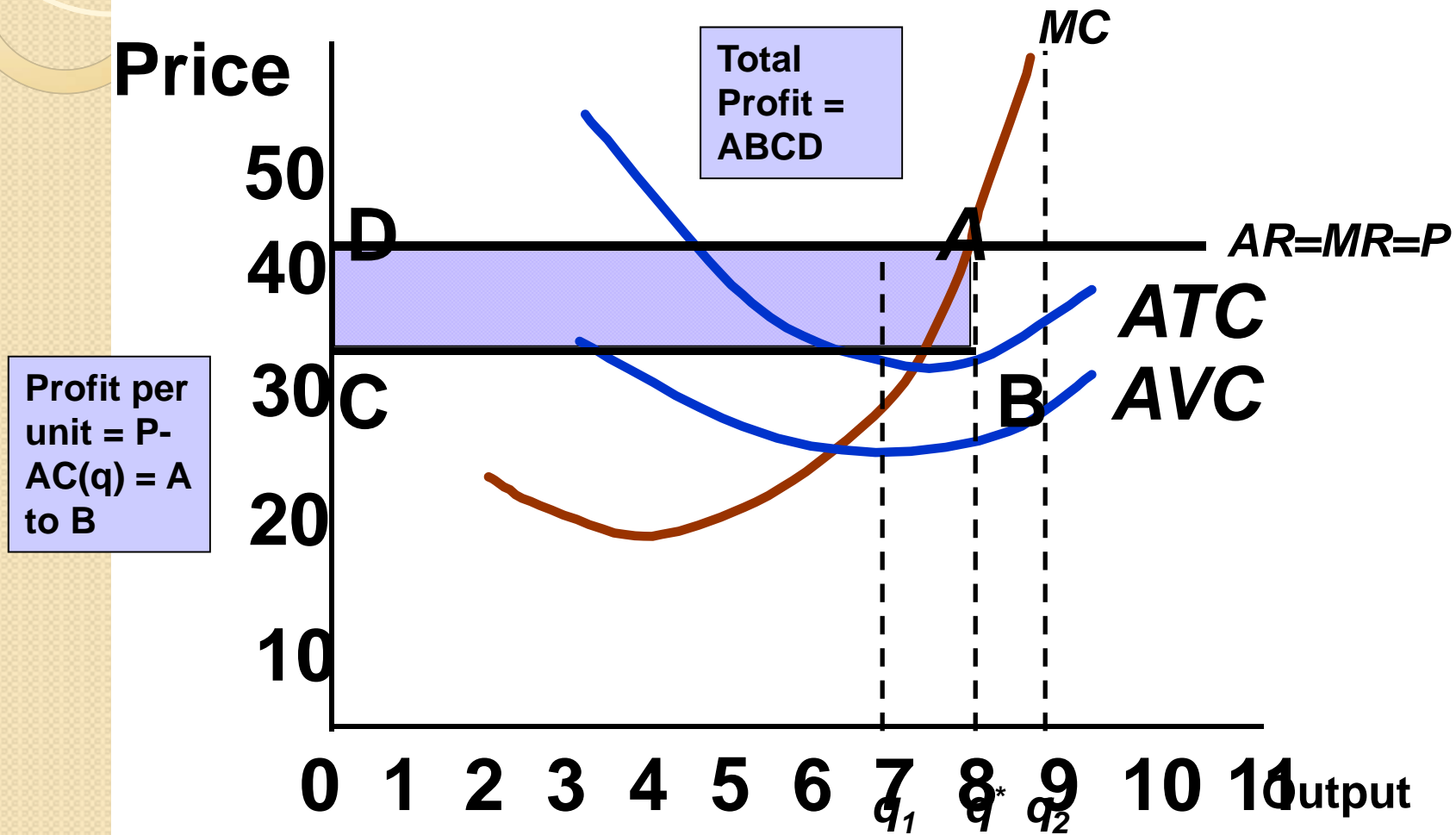
Choosing Output: Short Run

- The point where $MR = MC$, the profit maximizing output is chosen
 - $MR = MC$ at quantity, q^* , of 8
 - At a quantity less than 8, $MR > MC$, so more profit can be gained by increasing output
 - At a quantity greater than 8, $MC > MR$, increasing output will decrease profits

A Competitive Firm



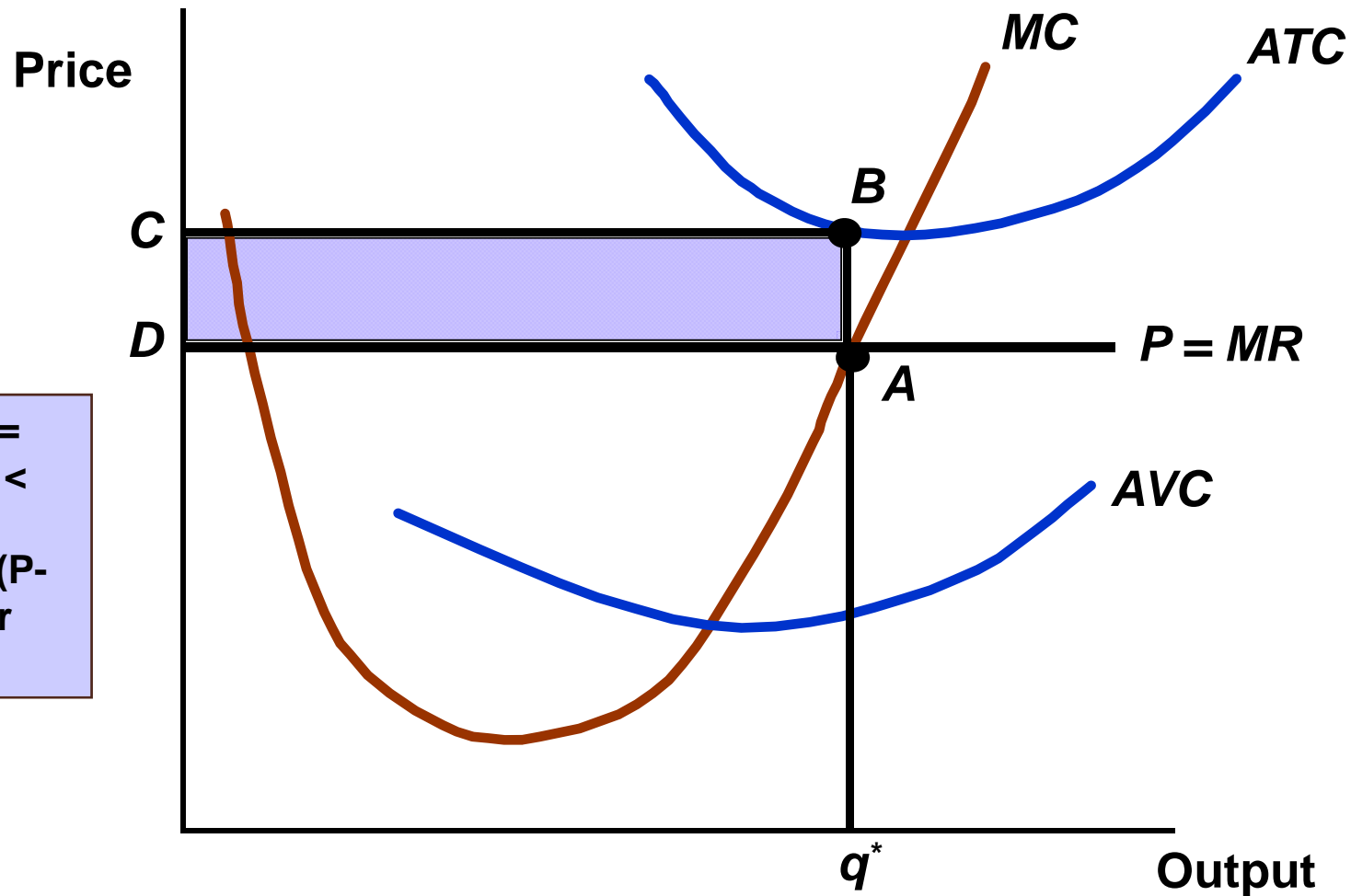
A Competitive Firm – Positive Profits



The Competitive Firm

- A firm does not have to make profits
- It is possible a firm will incur losses if the $P < AC$ for the profit maximizing quantity
 - Still measured by profit per unit times quantity
 - Profit per unit is negative ($P - AC < 0$)

A Competitive Firm – Losses



At q^* : $MR = MC$ and $P < ATC$
Losses = $(P - AC) \times q^*$ or **ABCD**



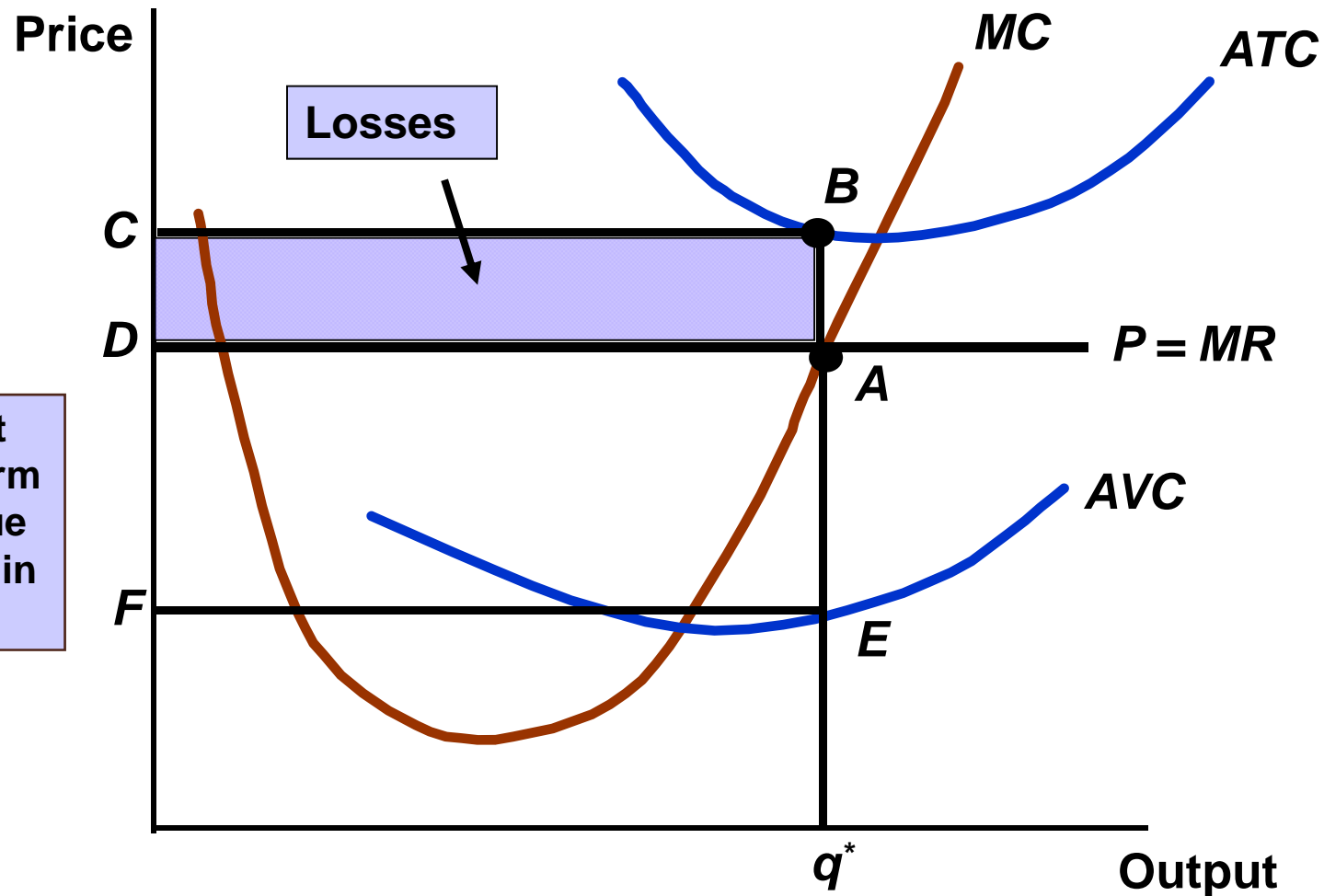
Short Run Production

- Why would a firm produce at a loss?
 - Might think price will increase in near future
 - Shutting down and starting up could be costly
- Firm has two choices in short run
 - Continue producing
 - Shut down temporarily
 - Will compare profitability of both choices

Short Run Production

- When should the firm shut down?
 - If $AVC < P < ATC$, the firm should continue producing in the short run
 - Can cover all of its variable costs and some of its fixed costs
 - If $AVC > P < ATC$, the firm should shut down
 - Cannot cover its variable costs or any of its fixed costs

A Competitive Firm – Losses



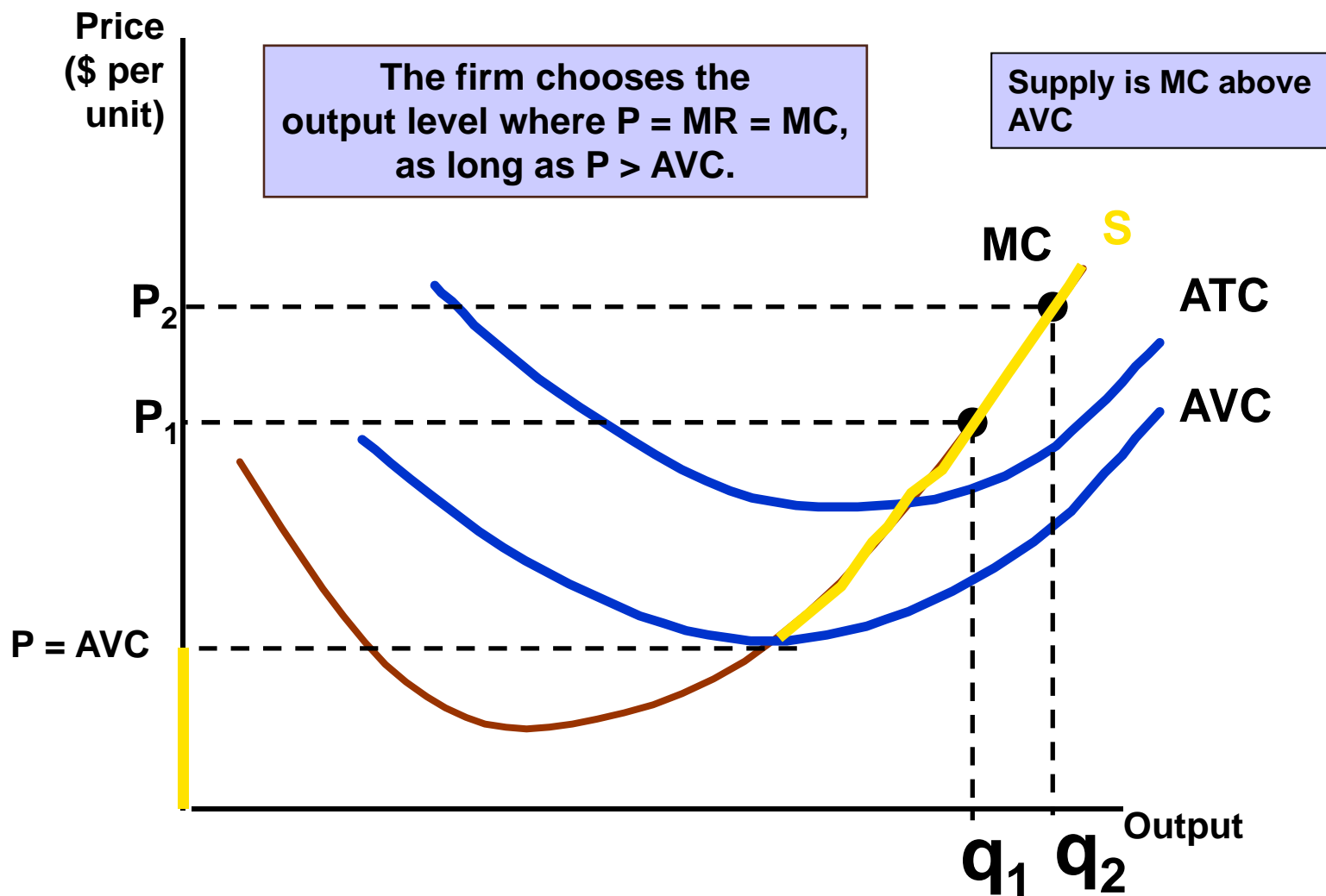
$P < ATC$ but
 $> AVC$ so firm
will continue
to produce in
short run



Competitive Firm – Short Run Supply

- Supply curve tells how much output will be produced at different prices
- Competitive firms determine quantity to produce where $P = MC$
 - Firm shuts down when $P < AVC$
- Competitive firms' supply curve is portion of the marginal cost curve above the AVC curve

A Competitive Firm's Short-Run Supply Curve





A Competitive Firm's Short-Run Supply Curve

- Supply is upward sloping due to diminishing returns
- Higher price compensates the firm for the higher cost of additional output and increases total profit because it applies to all units

Derivation of the Supply Curve

$$\text{Max } \pi(q) = pq - C(q)$$

$$\text{s.t. } \pi \geq -F \Rightarrow p \geq AVC$$

$$d\pi / dp = p - C'(q) = 0 \Rightarrow p = C'(q)$$

$$dp / dq = C''(q) > 0$$



Announcement

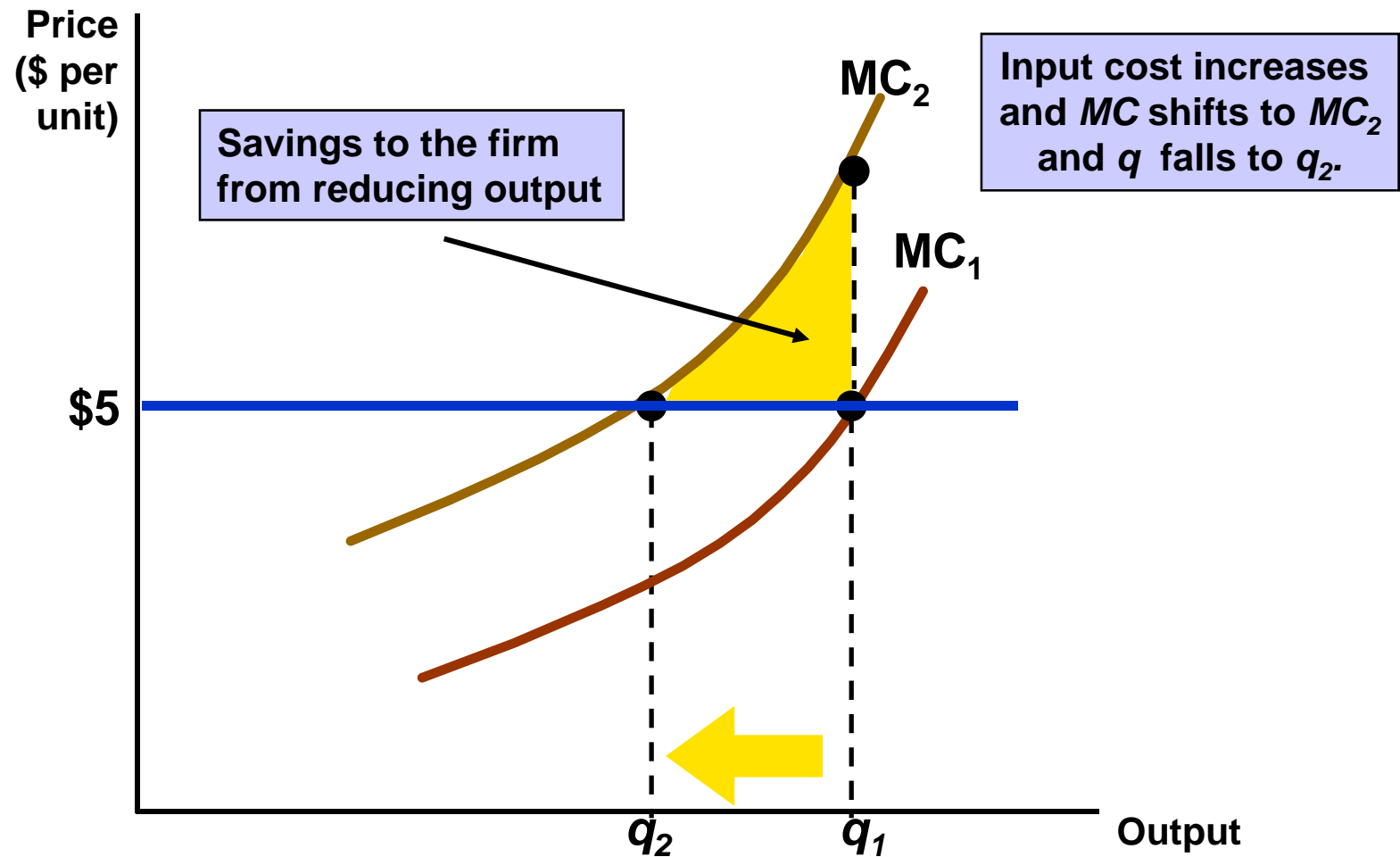
- Problem Set 2: Due on Nov 12



A Competitive Firm's Short-Run Supply Curve

- Over time, prices of product and inputs can change
- How does the firm's output change in response to a change in the price of an input?
 - We can show an increase in marginal costs and the change in the firm's output decisions

The Response of a Firm to a Change in Input Price

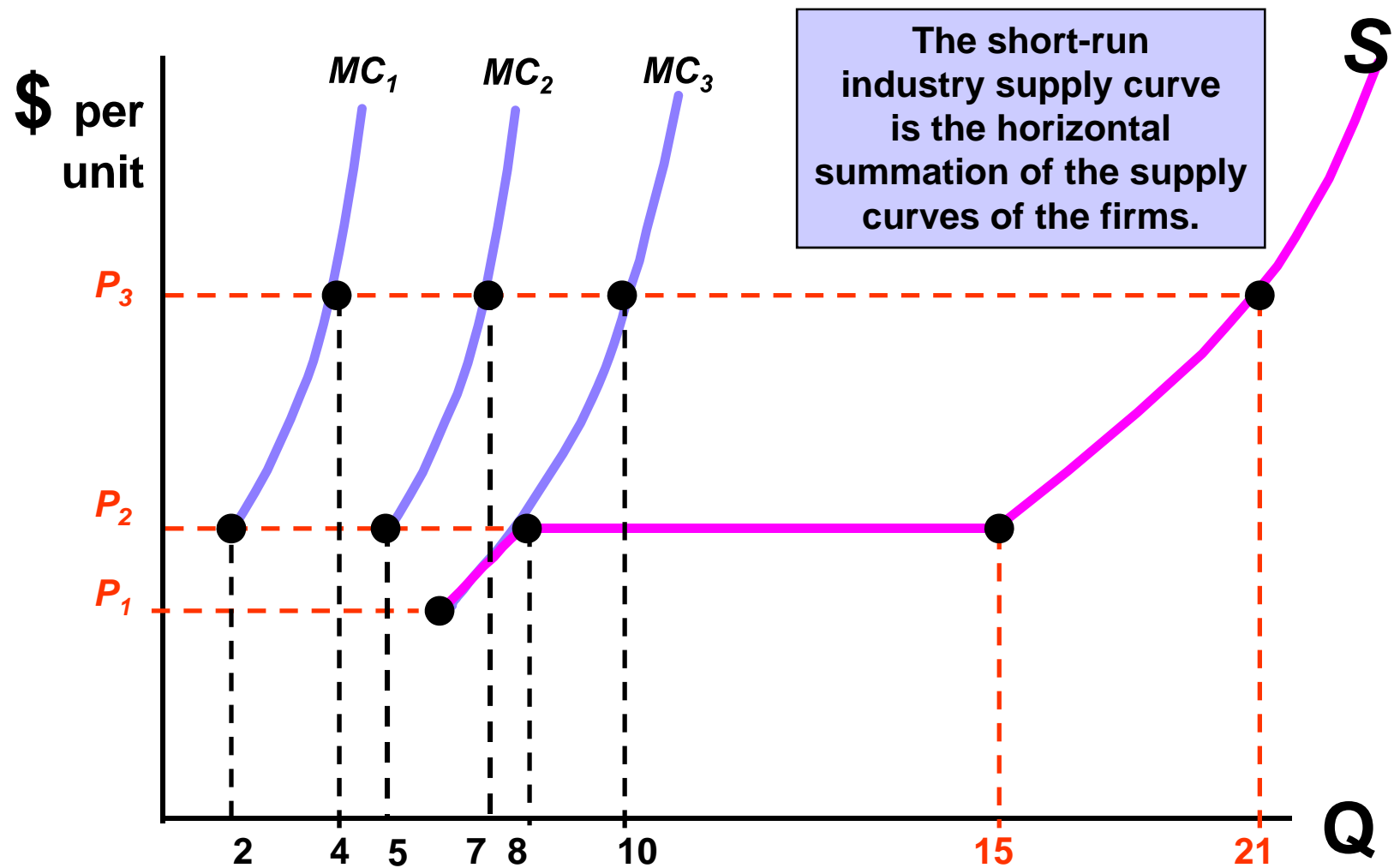




Short-Run Market Supply Curve

- Shows the amount of product the whole market will produce at given prices
- Is the sum of all the individual producers in the market
- We can show graphically how we can sum the supply curves of individual producers

Industry Supply in the Short Run



Elasticity of Market Supply

- Elasticity of Market Supply
 - Measures the sensitivity of industry output to market price
 - The percentage change in quantity supplied, Q , in response to 1-percent change in price

$$E_s = (\Delta Q / Q) / (\Delta P / P)$$



Elasticity of Market Supply

- When MC increases rapidly in response to increases in output, elasticity is low
- When MC increases slowly, supply is relatively elastic
- **Perfectly inelastic** short-run supply arises when the industry's plant and equipment are so fully utilized that new plants must be built to achieve greater output
- **Perfectly elastic** short-run supply arises when marginal costs are constant



Announcements

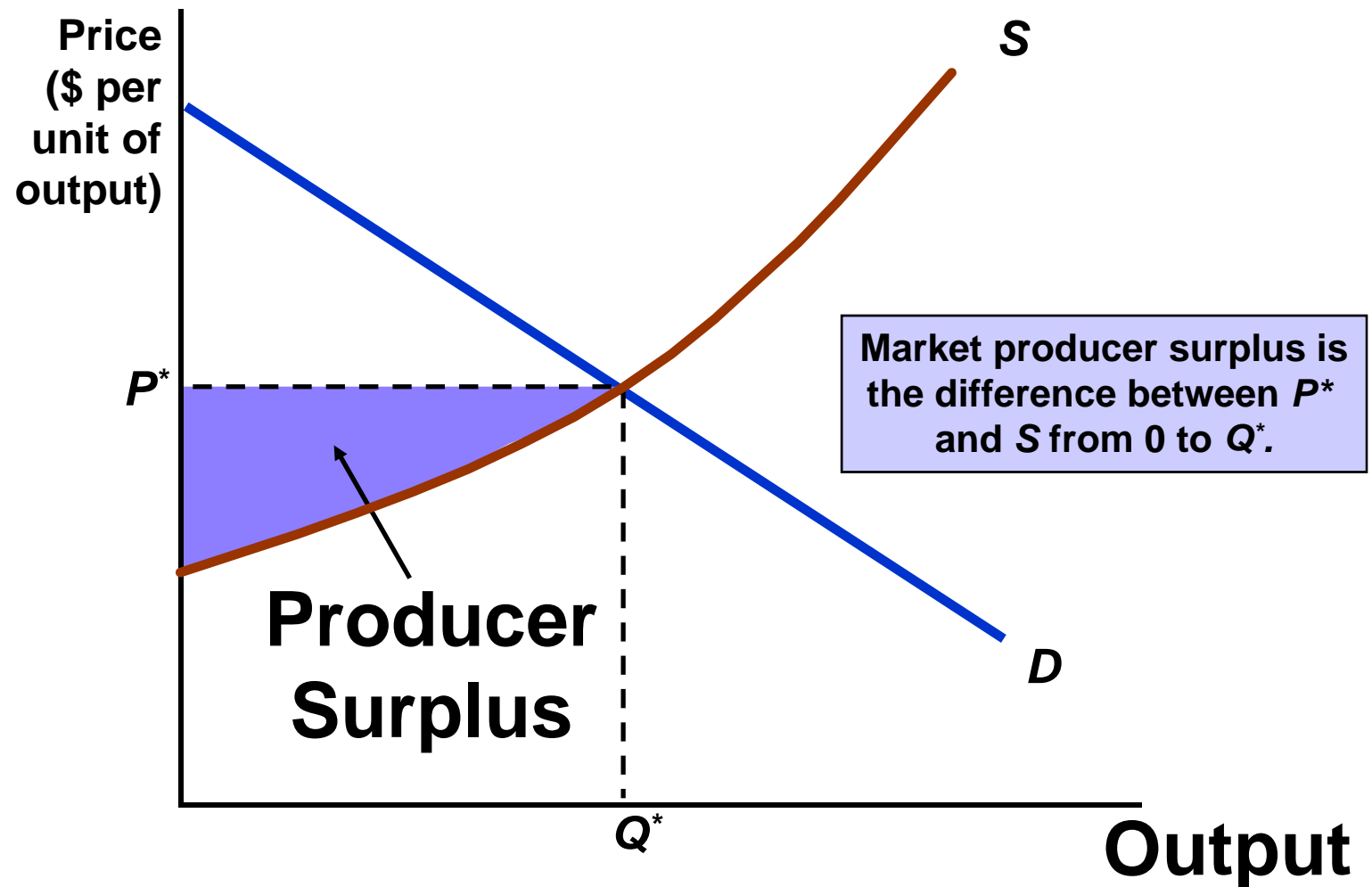
- Problem Set 2 has been assigned;
- Due Day: Nov. 14, 2011
- Chapters 8-9 have been uploaded



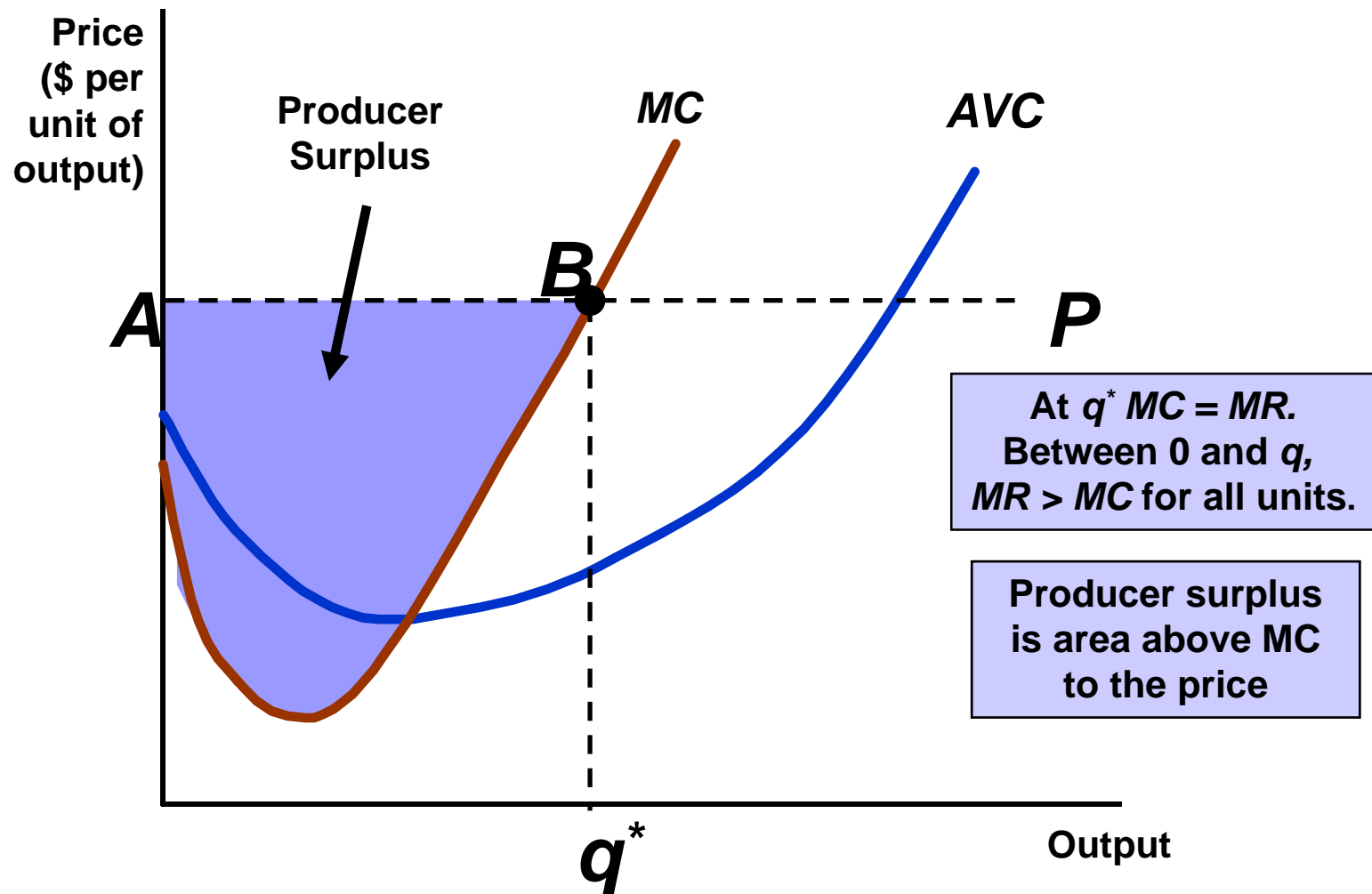
Producer Surplus in the Short Run

- Price is greater than MC on all but the last unit of output
- Therefore, surplus is earned on all but the last unit
- The **producer surplus** is the sum over all units produced of the difference between the market price of the good and the marginal cost of production
- Area above supply curve to the market price

Producer Surplus for a Market



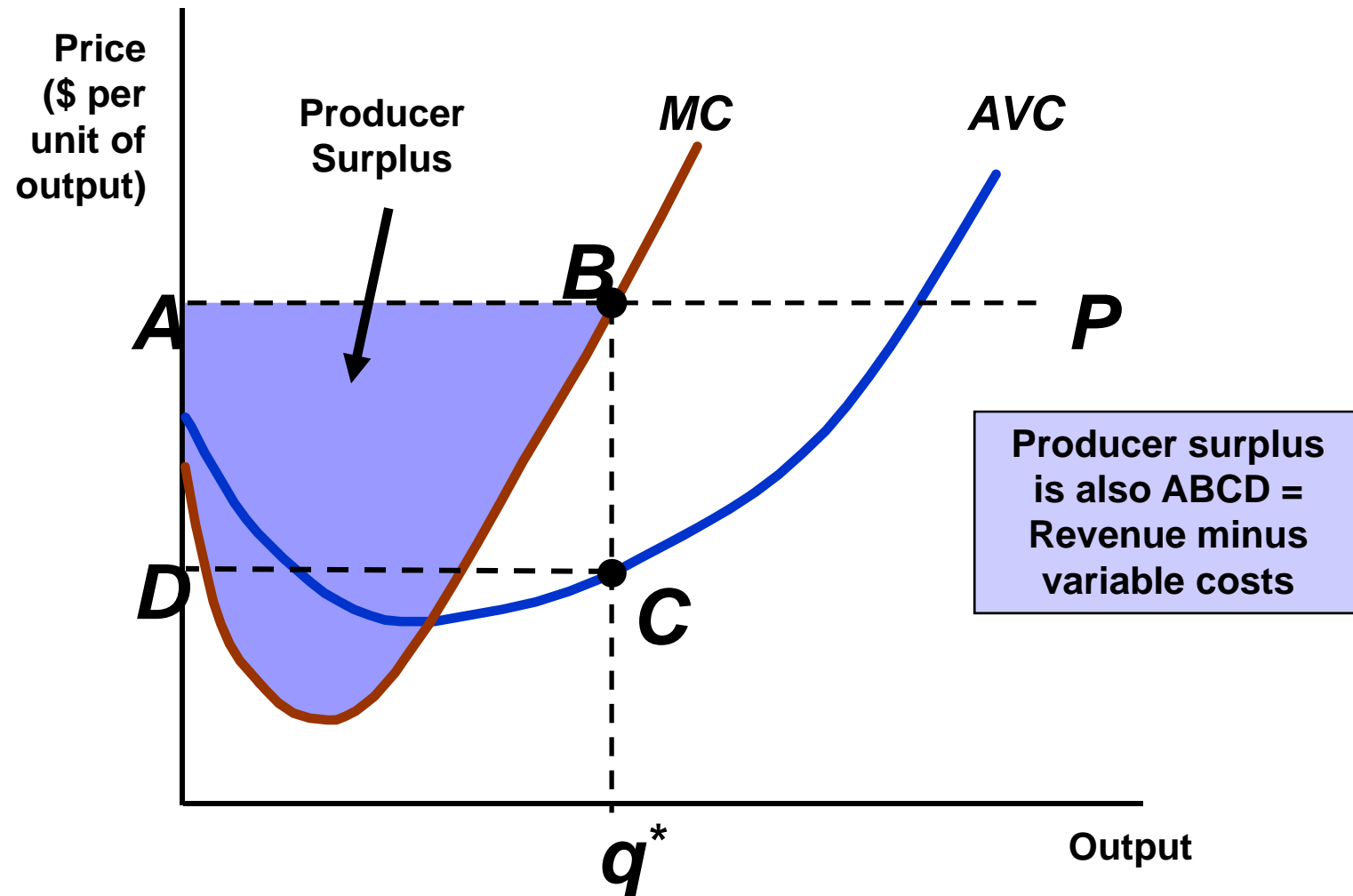
Producer Surplus for a Firm



The Short-Run Market Supply Curve

- Sum of MC from 0 to q^* , it is the sum of the total variable cost of producing q^*
- Producer Surplus can be defined as the difference between the firm's revenue and its total variable cost
- We can show this graphically by the rectangle ABCD
 - Revenue ($0ABq^*$) minus variable cost ($0DCq^*$)

Producer Surplus for a Firm



Producer Surplus Versus Profit

- Profit is revenue minus total cost (not just variable cost)
- When fixed cost is positive, producer surplus is greater than profit

$$\text{Producer Surplus} = \text{PS} = R - \text{VC}$$

$$\text{Profit} = \pi = R - \text{VC} - \text{FC}$$



Producer Surplus Versus Profit

- Costs of production determine magnitude of producer surplus
 - Higher cost firms have less producer surplus
 - Lower cost firms have more producer surplus
 - Adding up surplus for all producers in the market given total market producer surplus
 - Area below market price and above supply curve

Profit Max: Another Look

- Suppose the firm is in a short-run circumstance in which $\mathbf{x}_2 \equiv \tilde{\mathbf{x}}_2$.
- Its short-run production function is $y = f(\mathbf{x}_1, \tilde{\mathbf{x}}_2)$.
- The firm's fixed cost is $\mathbf{FC} = \mathbf{w}_2 \tilde{\mathbf{x}}_2$ and its profit function is

$$\Pi = \mathbf{p}y - \mathbf{w}_1 \mathbf{x}_1 - \mathbf{w}_2 \tilde{\mathbf{x}}_2.$$

Short-Run Iso-Profit Lines

- A $\$ \Pi$ iso-profit line contains all the production plans that provide a profit level $\$ \Pi$.
- A $\$ \Pi$ iso-profit line's equation is

$$\Pi \equiv py - w_1x_1 - w_2\tilde{x}_2.$$

Short-Run Iso-Profit Lines

- A $\$ \Pi$ iso-profit line contains all the production plans that yield a profit level of $\$ \Pi$.
- The equation of a $\$ \Pi$ iso-profit line is

- $\Pi \equiv py - w_1x_1 - w_2\tilde{x}_2$.
i.e.

$$y = \frac{w_1}{p}x_1 + \frac{\Pi + w_2\tilde{x}_2}{p}.$$

Short-Run Iso-Profit Lines

$$y = \frac{w_1}{p} x_1 + \frac{\Pi + w_2 \tilde{x}_2}{p}$$

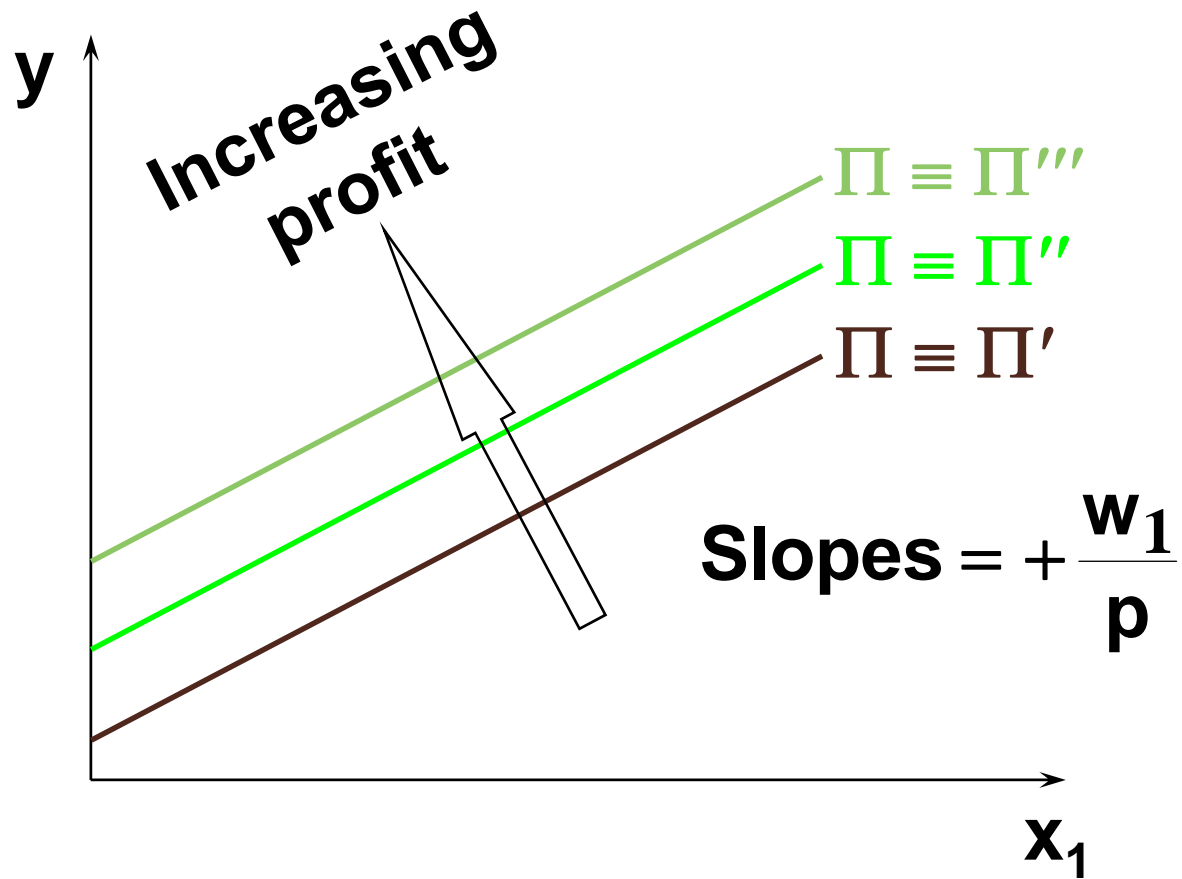
has a slope of

$$\frac{w_1}{p}$$

and a vertical intercept of

$$\frac{\Pi + w_2 \tilde{x}_2}{p}.$$

Short-Run Iso-Profit Lines





Short-Run Profit-Maximization

- The firm's problem is to locate the production plan that attains the highest possible iso-profit line, given the firm's constraint on choices of production plans.
- Q: What is this constraint?

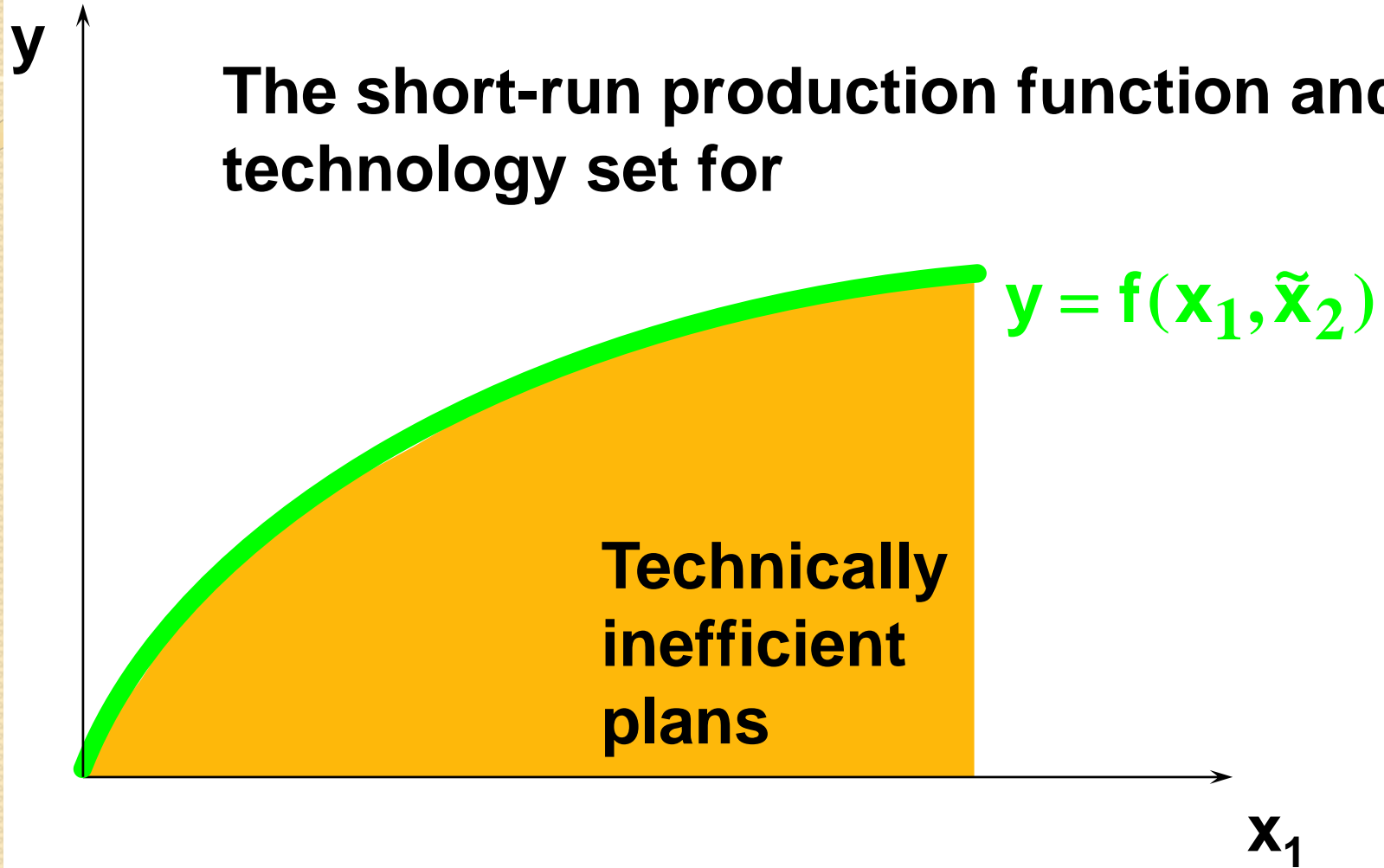


Short-Run Profit-Maximization

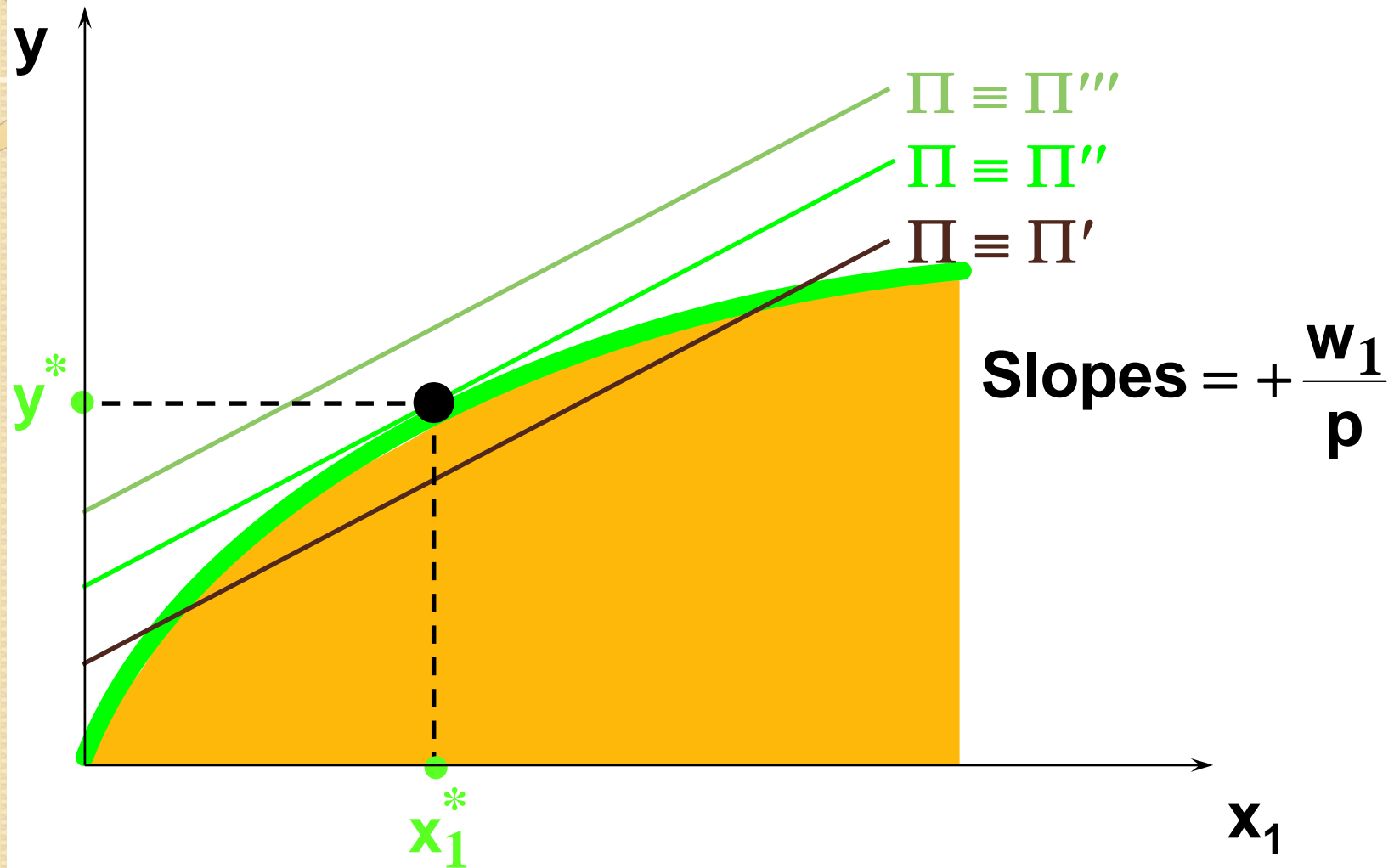
- The firm's problem is to locate the production plan that attains the highest possible iso-profit line, given the firm's constraint on choices of production plans.
- Q: What is this constraint?
- A: The production function.

Short-Run Profit-Maximization

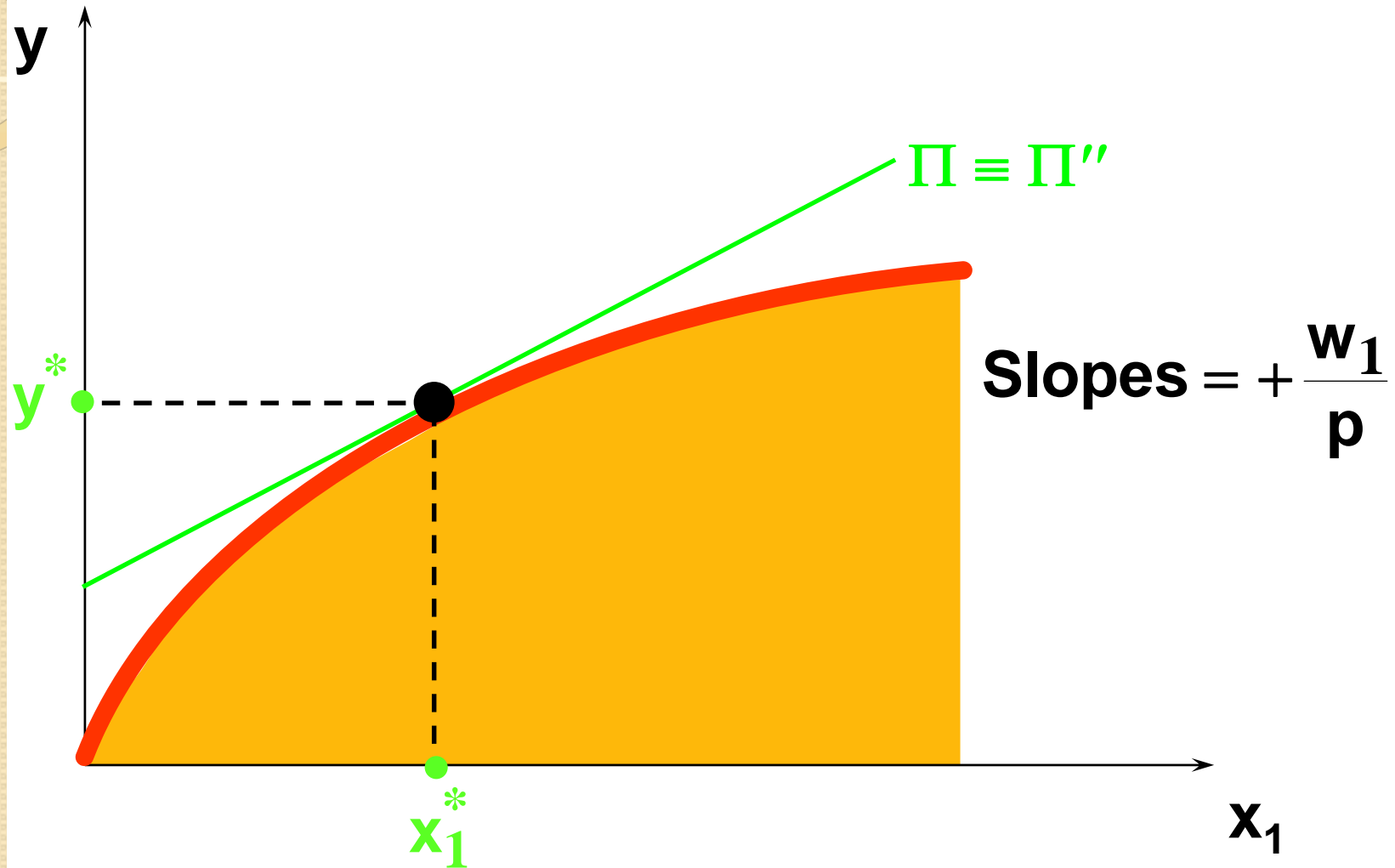
The short-run production function and technology set for



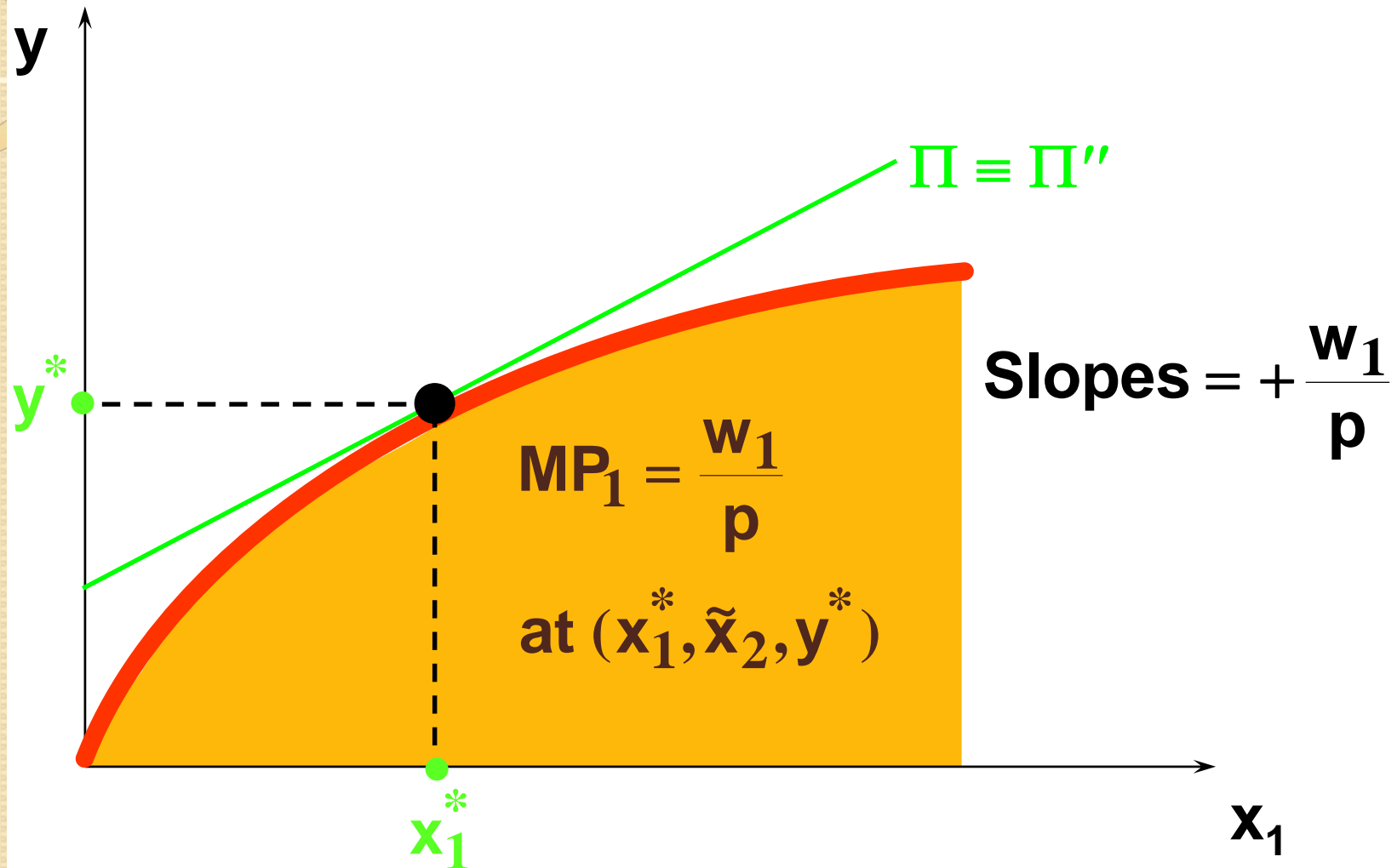
Short-Run Profit-Maximization



Short-Run Profit-Maximization



Short-Run Profit-Maximization



Short-Run Profit-Maximization

$$\mathbf{MP_1 = \frac{w_1}{p} \Leftrightarrow p \times MP_1 = w_1}$$

$\mathbf{p \times MP_1}$ is the marginal revenue product of input 1, the rate at which revenue increases with the amount used of input 1.

If $\mathbf{p \times MP_1 > w_1}$ then profit increases with x_1 .

If $\mathbf{p \times MP_1 < w_1}$ then profit decreases with x_1 .

Profit Max: A Mathematical Approach

$$\text{Max } \Pi = py - w_1x_1 - w_2 \bar{x}_2$$

$$\text{s.t. } y = f(x_1, x_2)$$

$$\Rightarrow \text{Max } \Pi = pf(x_1, x_2) - w_1x_1 - w_2 \bar{x}_2$$

$$\Rightarrow p \frac{\partial f}{\partial x_1} = w_1 \quad \text{or} \quad \frac{\partial f}{\partial x_1} = w_1 / p$$

Comparative Statics of Short-Run Profit-Maximization

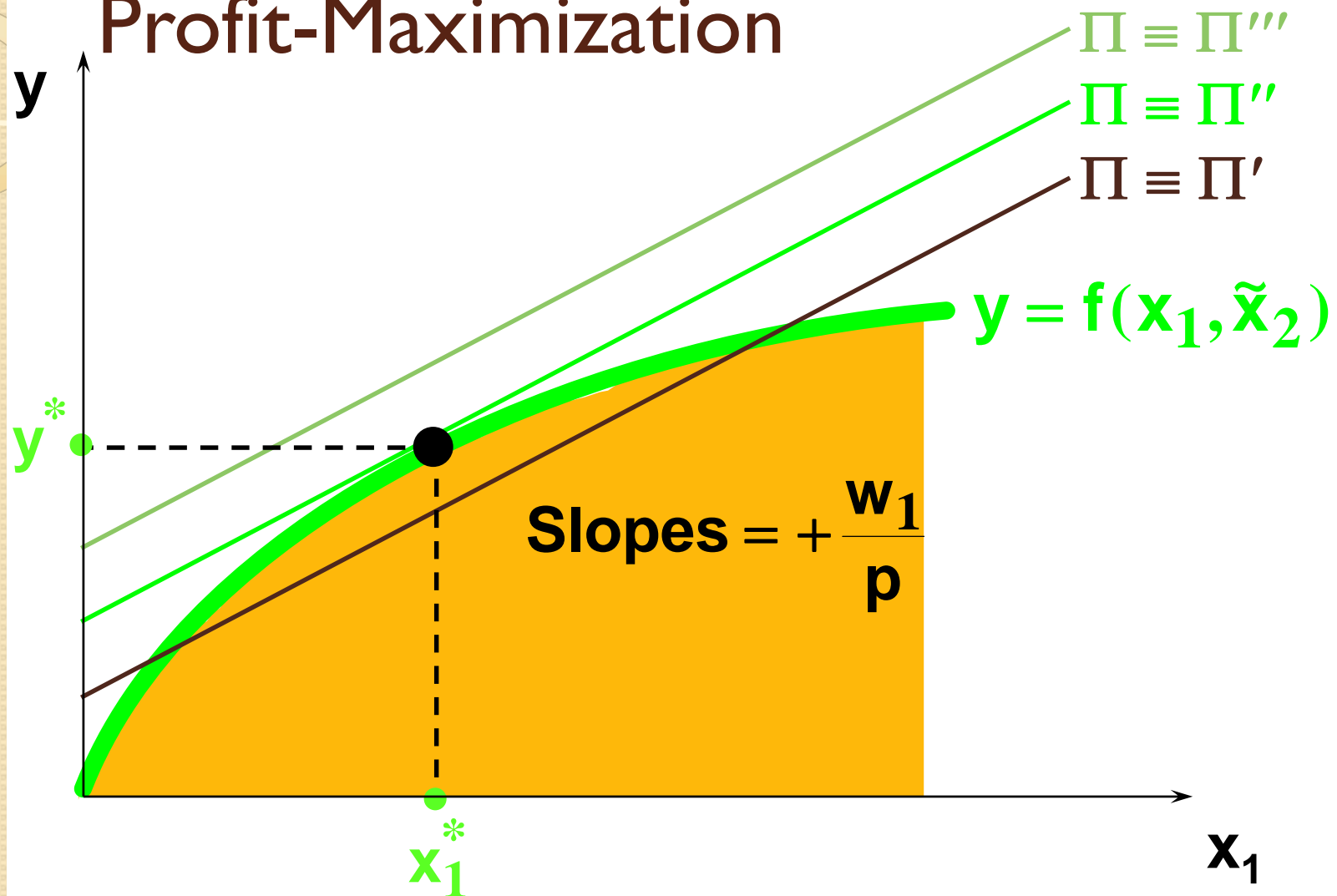
The equation of a short-run iso-profit line is

$$y = \frac{w_1}{p} x_1 + \frac{\Pi + w_2 \tilde{x}_2}{p}$$

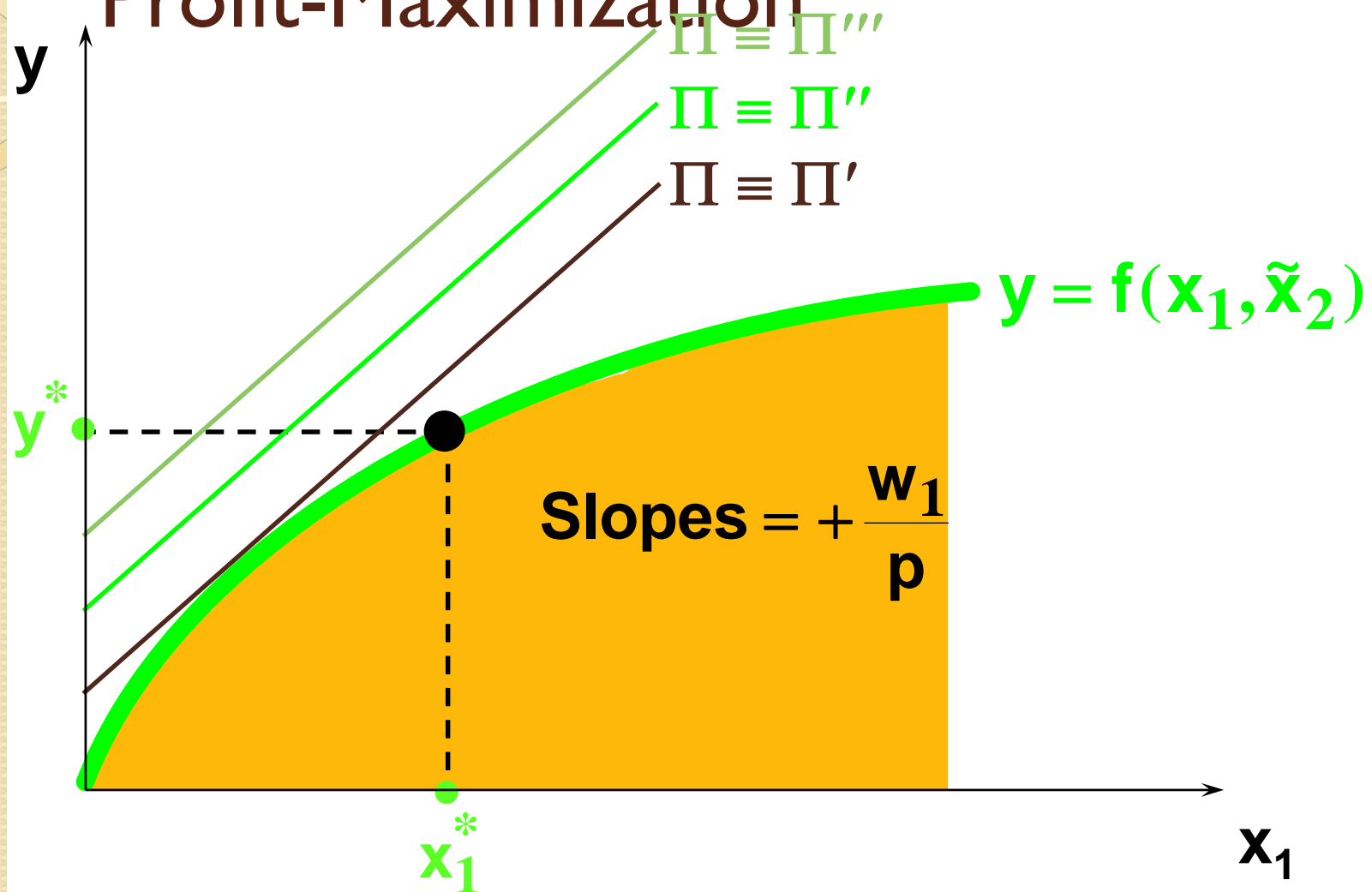
so an increase in w_1 causes

- an increase in the slope, and
- no change to the vertical intercept.

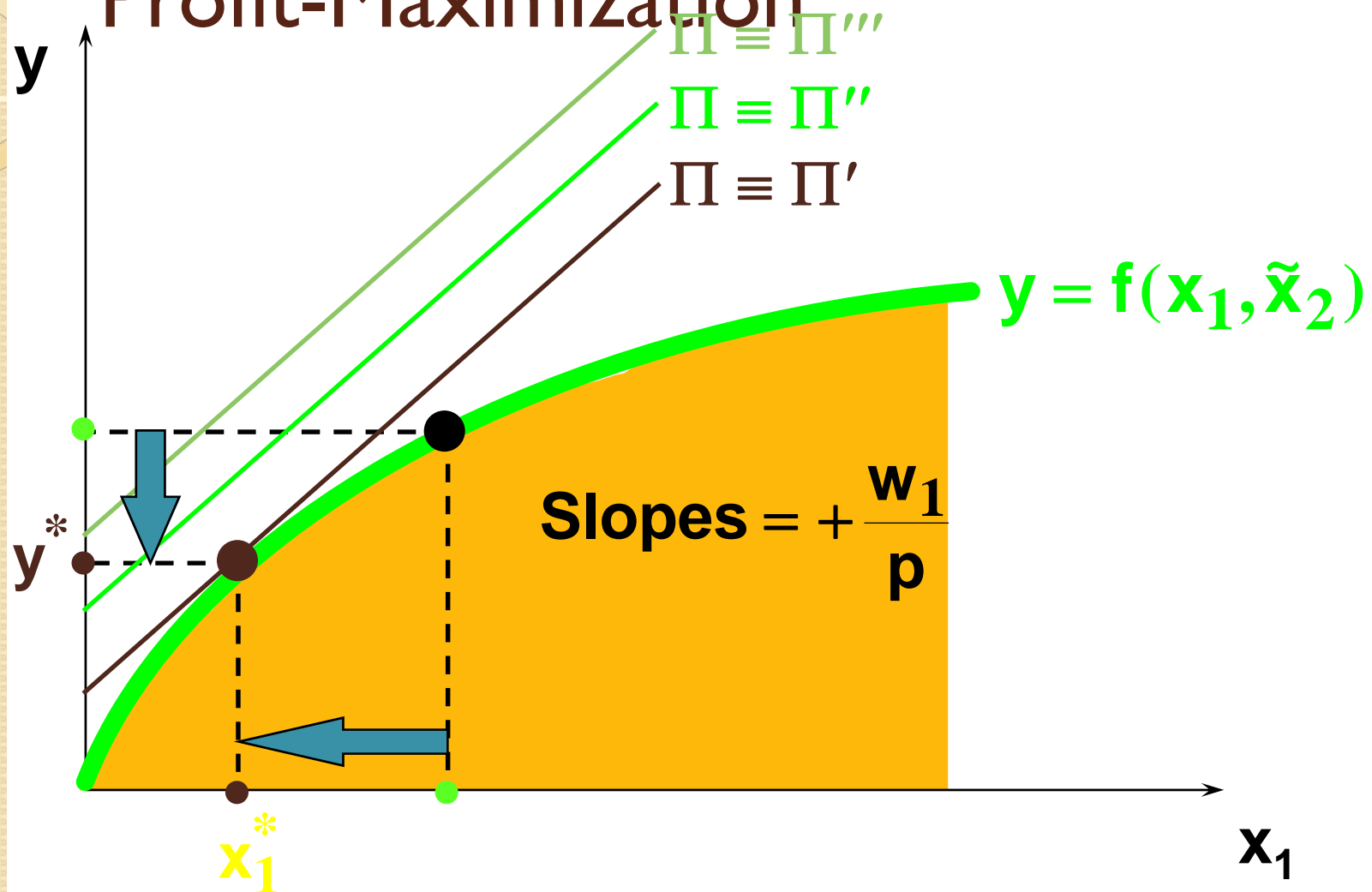
Comparative Statics of Short-Run Profit-Maximization



Comparative Statics of Short-Run Profit-Maximization



Comparative Statics of Short-Run Profit-Maximization





Comparative Statics of Short-Run Profit-Maximization

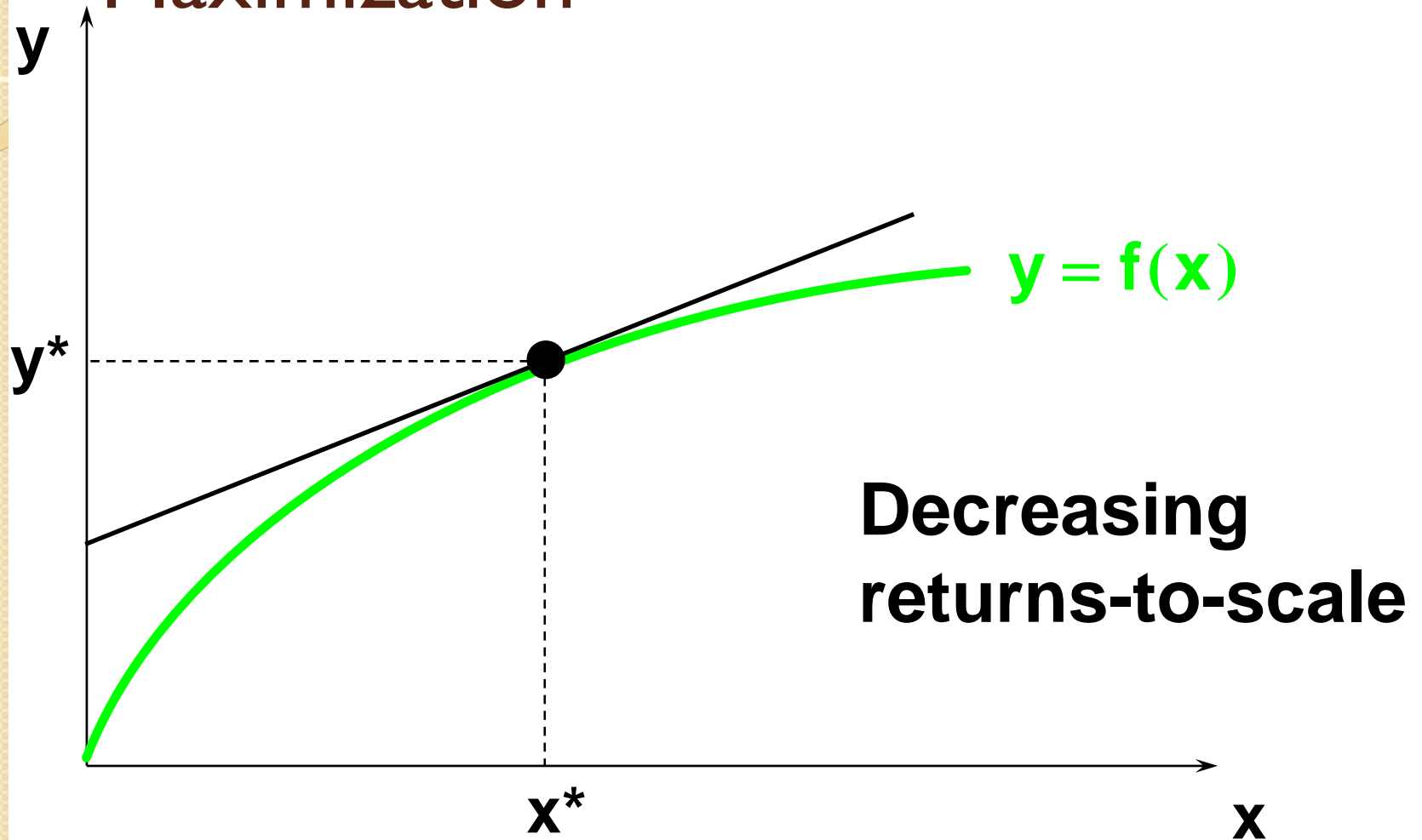
- An increase in w_1 , the price of the firm's variable input, causes
 - a decrease in the firm's output level (the firm's supply curve shifts inward), and
 - a decrease in the level of the firm's variable input (the firm's demand curve for its variable input slopes downward).



Returns-to-Scale and Profit-Maximization

- If a competitive firm's technology exhibits decreasing returns-to-scale then the firm has a single long-run profit-maximizing production plan.

Returns-to Scale and Profit-Maximization

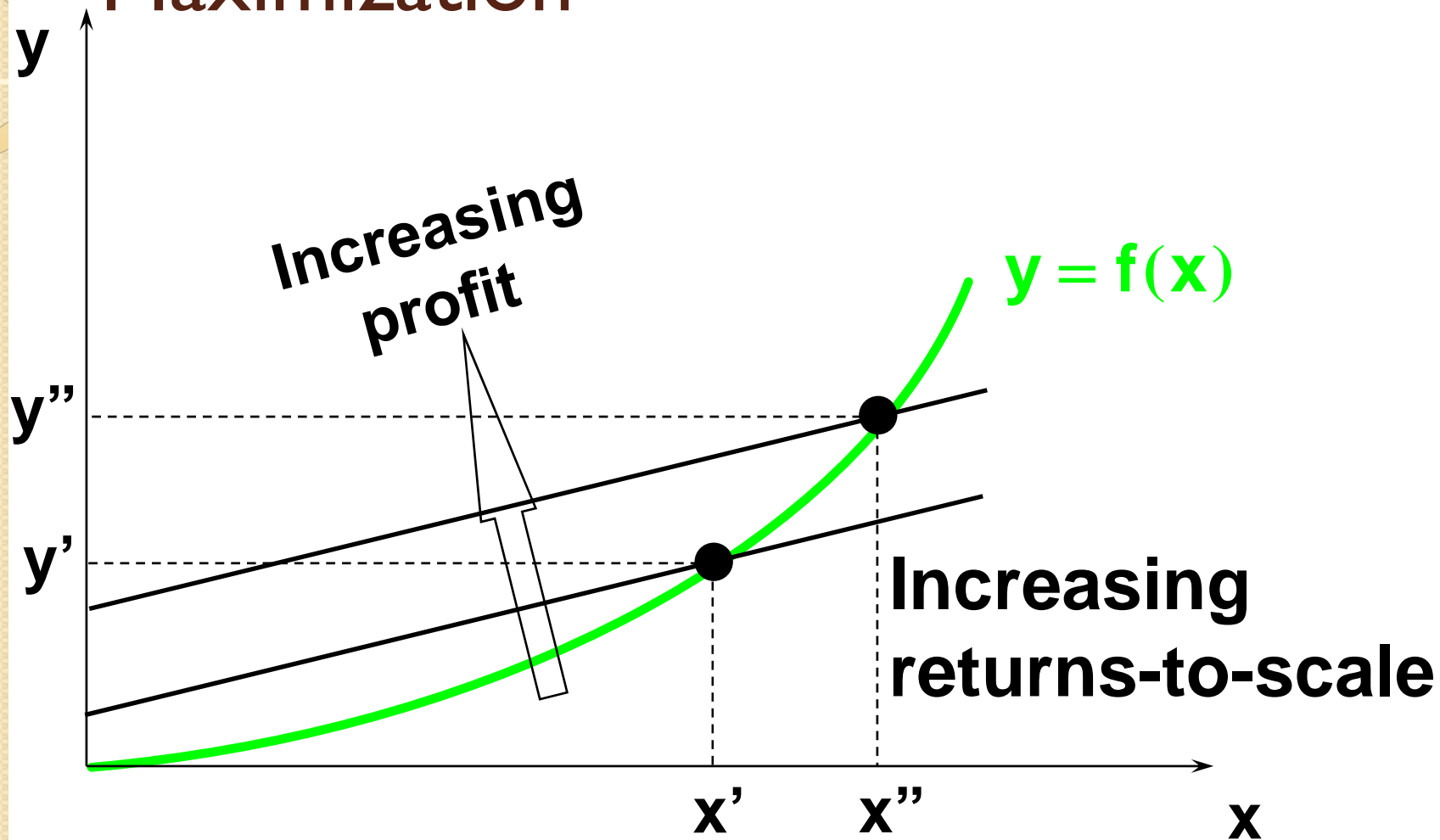




Returns-to-Scale and Profit-Maximization

- If a competitive firm's technology exhibits increasing returns-to-scale then the firm does not have a profit-maximizing plan.

Returns-to Scale and Profit-Maximization





Returns-to-Scale and Profit-Maximization

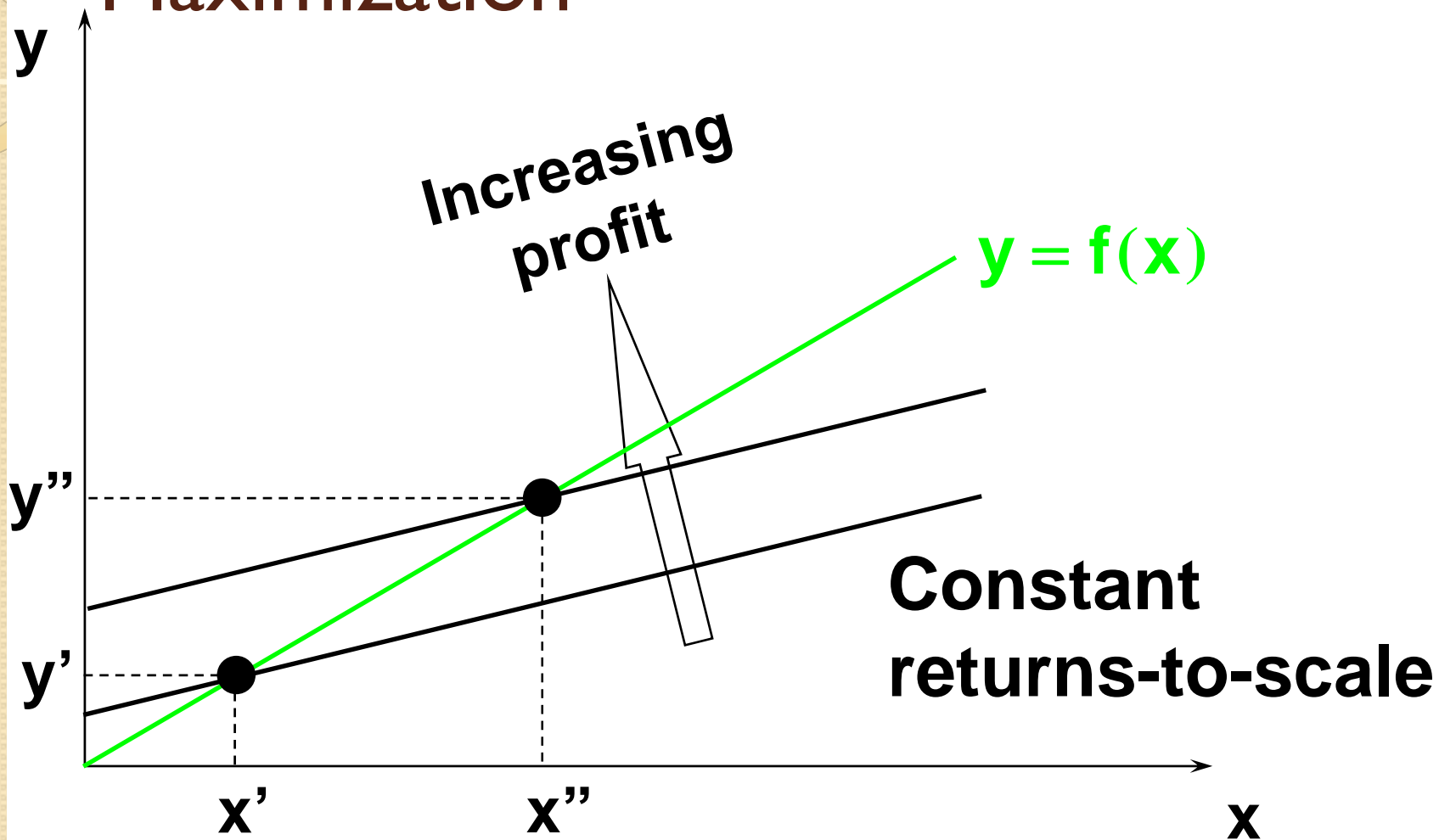
- So an increasing returns-to-scale technology is inconsistent with firms being perfectly competitive.



Returns-to-Scale and Profit-Maximization

- What if the competitive firm's technology exhibits constant returns-to-scale?

Returns-to Scale and Profit-Maximization





Returns-to Scale and Profit-Maximization

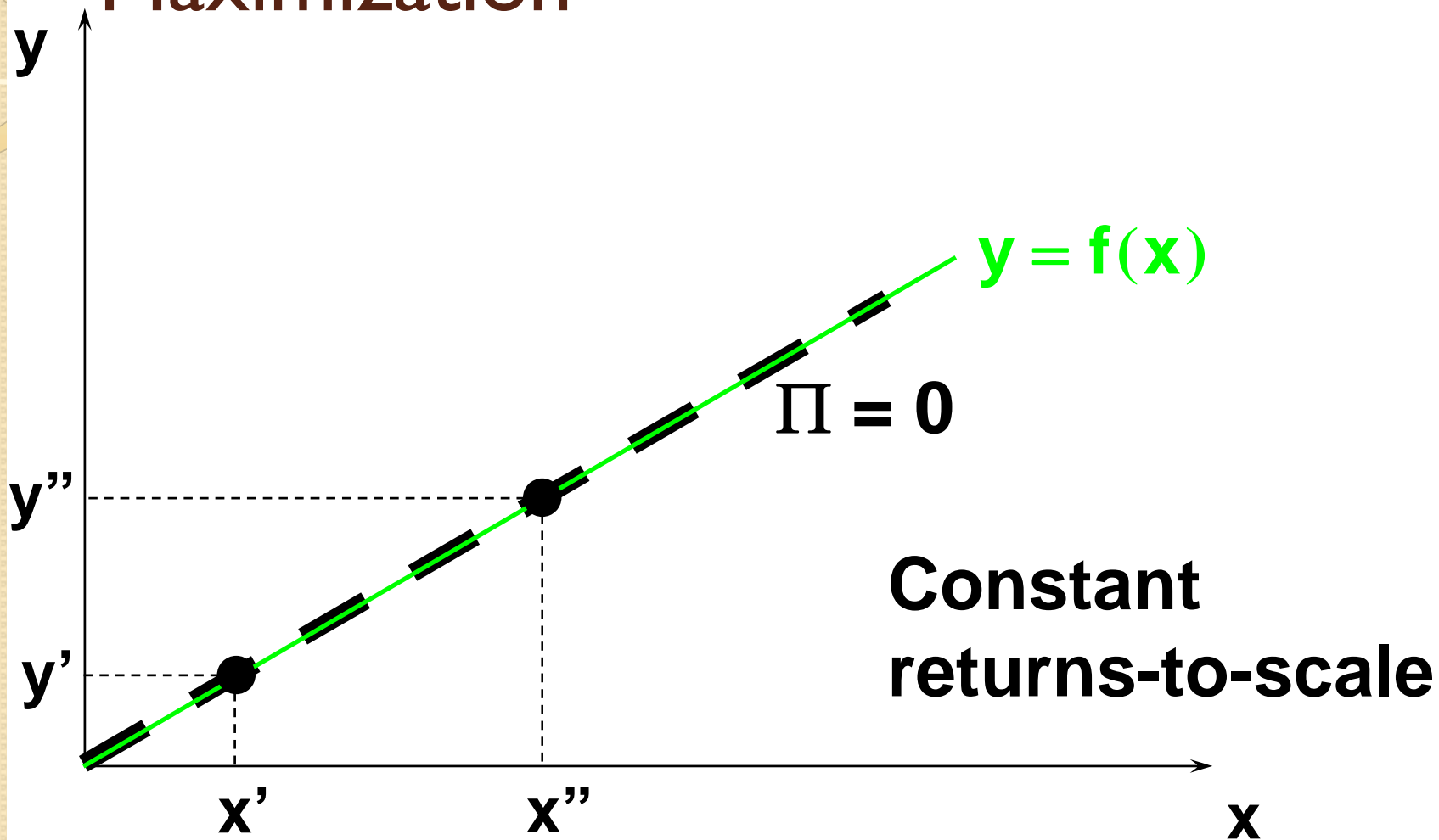
- So if any production plan earns a positive profit, the firm can double up all inputs to produce twice the original output and earn twice the original profit.



Returns-to Scale and Profit-Maximization

- Therefore, when a firm's technology exhibits constant returns-to-scale, earning a positive economic profit is inconsistent with firms being perfectly competitive.
- Hence constant returns-to-scale requires that competitive firms earn economic profits of zero.

Returns-to Scale and Profit-Maximization





Long-Run Competitive Equilibrium

- For long run equilibrium, firms must have no desire to enter or leave the industry
- We can relate economic profit to the incentive to enter and exit the market
- Need to relate accounting profit to economic profit



Long-Run Competitive Equilibrium

- Accounting profit
 - Difference between firm's revenues and direct costs
- Economic profit
 - Difference between firm's revenues and direct and indirect costs
 - Takes into account opportunity costs and entrepreneur ability



Long-Run Competitive Equilibrium

- Zero-Profit

- A firm is earning a normal return on its investment
- Doing as well as it could by investing its money elsewhere
- Normal return is firm's opportunity cost of using money to buy capital instead of investing elsewhere
- Competitive market long run equilibrium

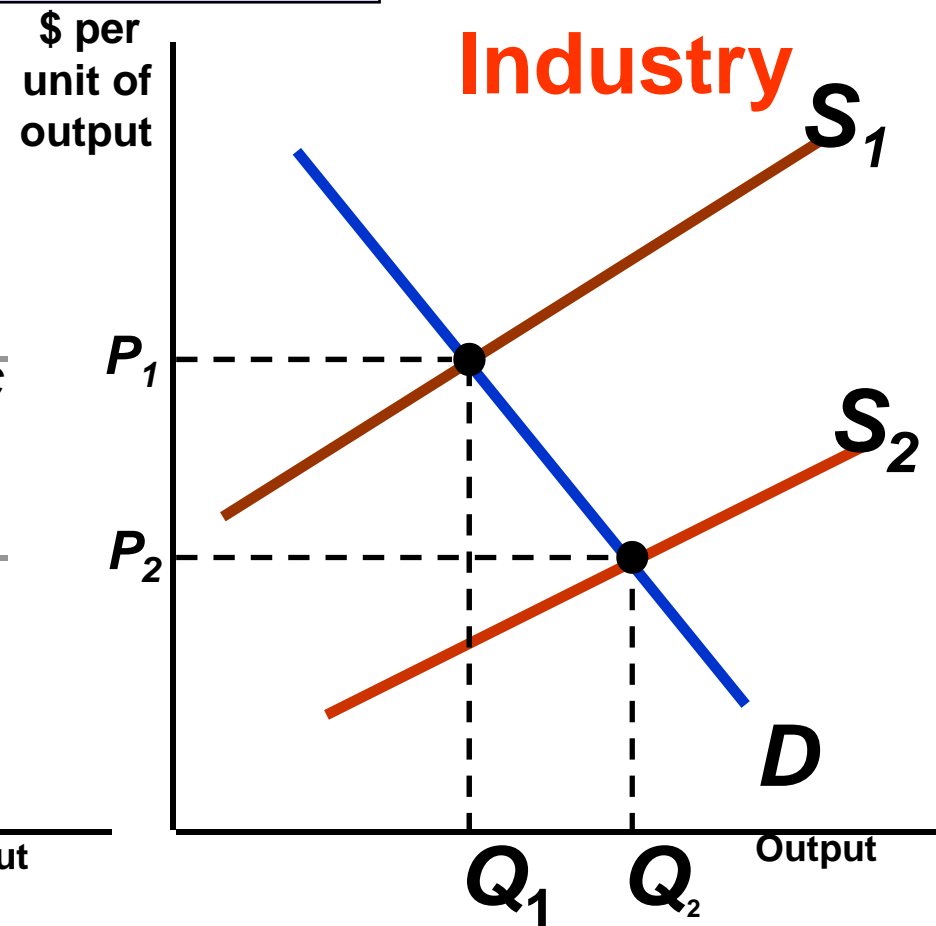
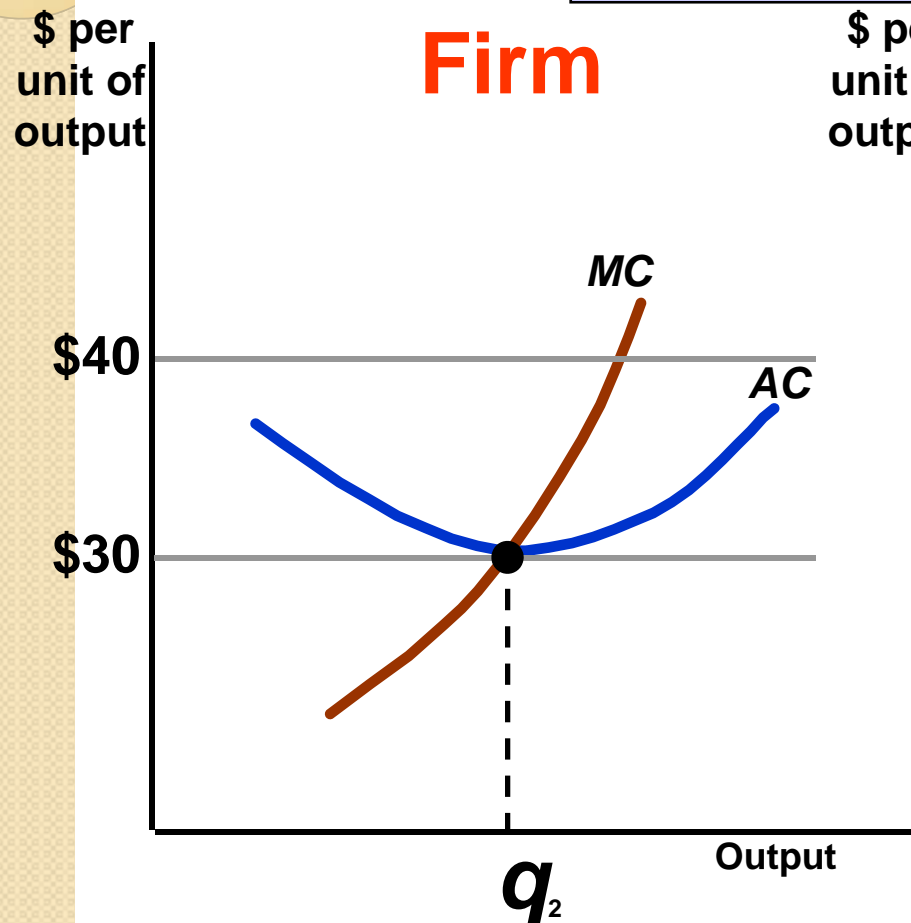


Long-Run Competitive Equilibrium

- Entry and Exit
 - The long-run response to short-run profits is to increase output and profits
 - Profits will attract other producers
 - More producers increase industry supply, which lowers the market price
 - This continues until there are no more profits to be gained in the market – zero economic profits

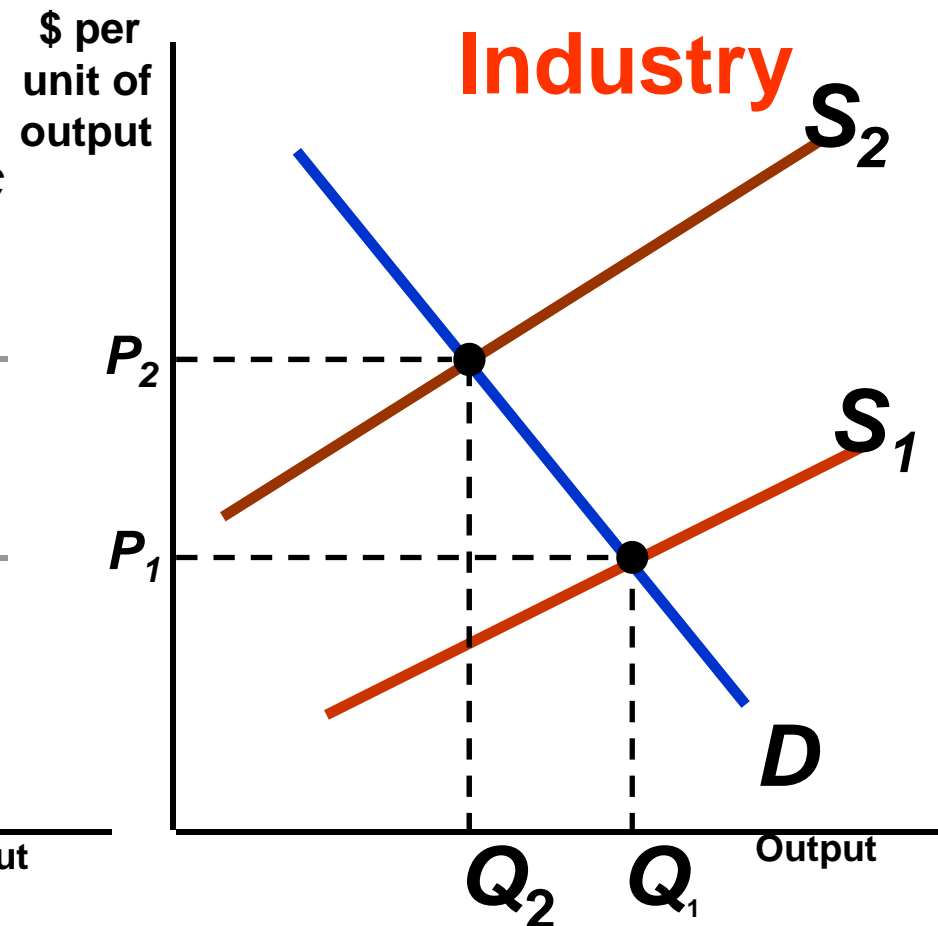
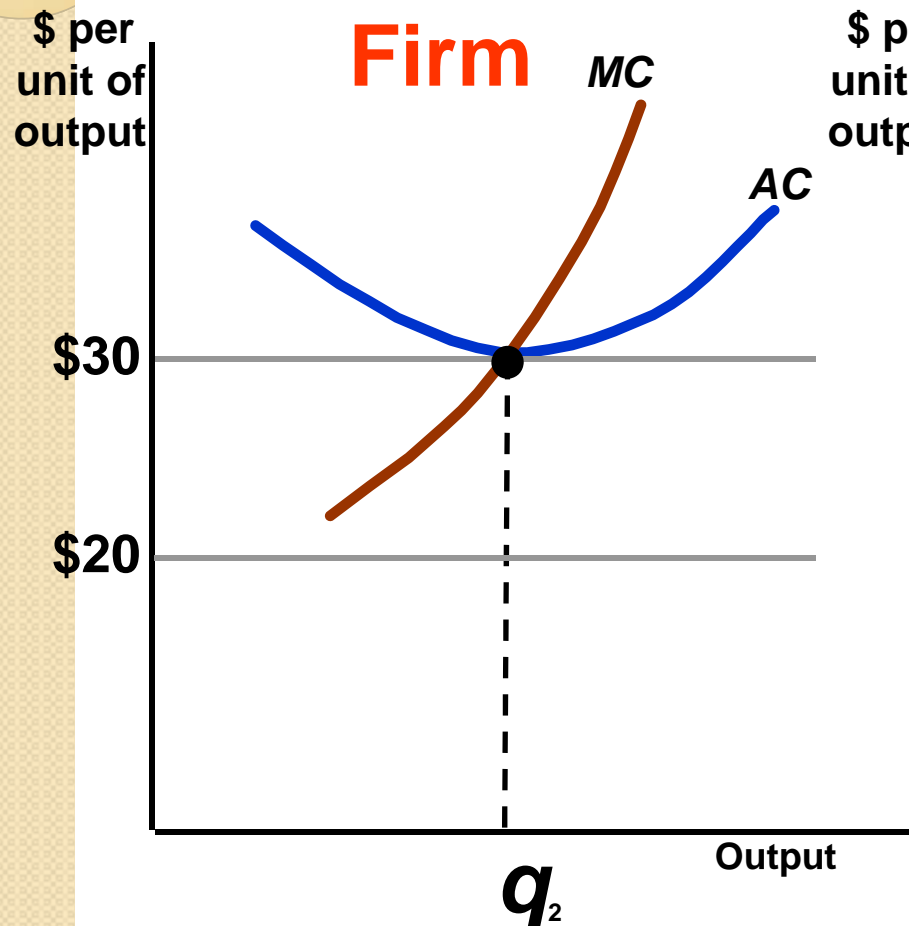
Long-Run Competitive Equilibrium – Profits

- Profit attracts firms
- Supply increases until profit = 0



Long-Run Competitive Equilibrium – Losses

- Losses cause firms to leave
- Supply decreases until profit = 0



Long-Run Competitive Equilibrium

1. All firms in industry are maximizing profits
 - $MR = MC$
2. No firm has incentive to enter or exit industry
 - Earning zero economic profits
3. Market is in equilibrium
 - $Q_D = Q_S$



The Industry's Long-Run Supply Curve

- The shape of the long-run supply curve depends on the extent to which changes in industry output affect the prices the firms must pay for inputs



The Industry's Long-Run Supply Curve

- Assume
 - All firms have access to the available production technology
 - Output is increased by using more inputs, not by invention



The Industry's Long-Run Supply Curve

- To analyze long-run industry supply, will need to distinguish between three different types of industries
 1. Constant-Cost
 2. Increasing-Cost
 3. Decreasing-Cost

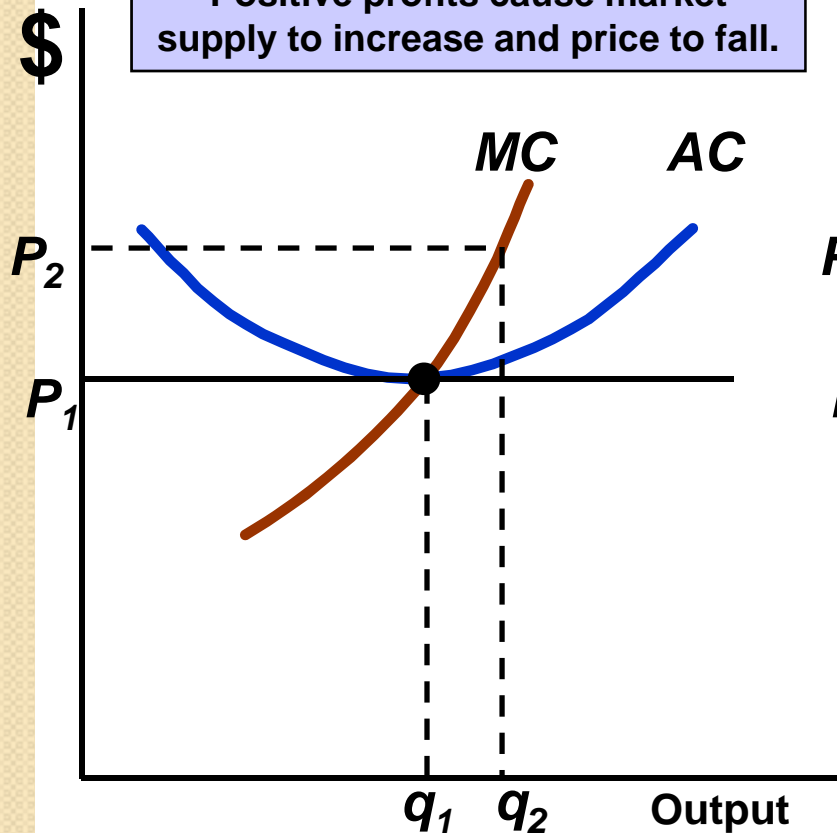


Constant-Cost Industry

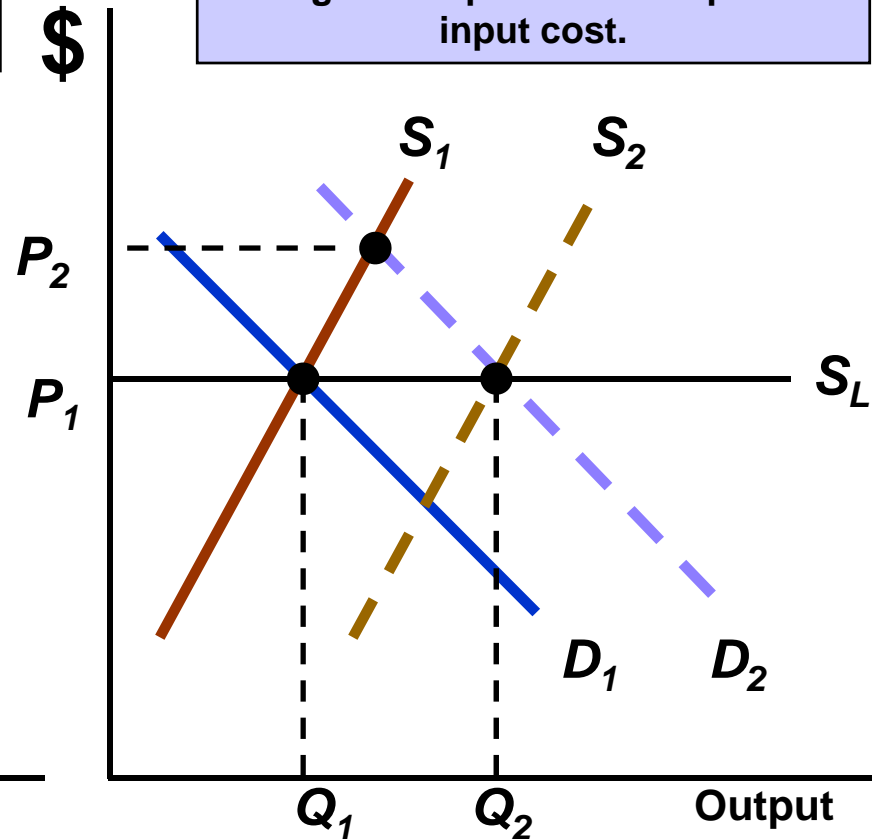
- Industry whose long-run supply curve is horizontal
- Prices of inputs do not change as firms enter or exit
 - Firms' cost curves do not change
- Assume a firm is initially in equilibrium
 - Demand increases, causing price to increase
 - Individual firms increase supply
 - Causes firms to earn positive profits in short run
 - Supply increases, causing market price to decrease
 - Long run equilibrium – zero economic profits

Constant-Cost Industry

Increase in demand increases market price and firm output. Positive profits cause market supply to increase and price to fall.



Q_1 increases to Q_2 . Long-run supply = S_L = LRAC. Change in output has no impact on input cost.





Long-Run Supply in a Constant-Cost Industry

- In a constant-cost industry, the long-run supply is a horizontal line at a price that is equal to the minimum average cost of production



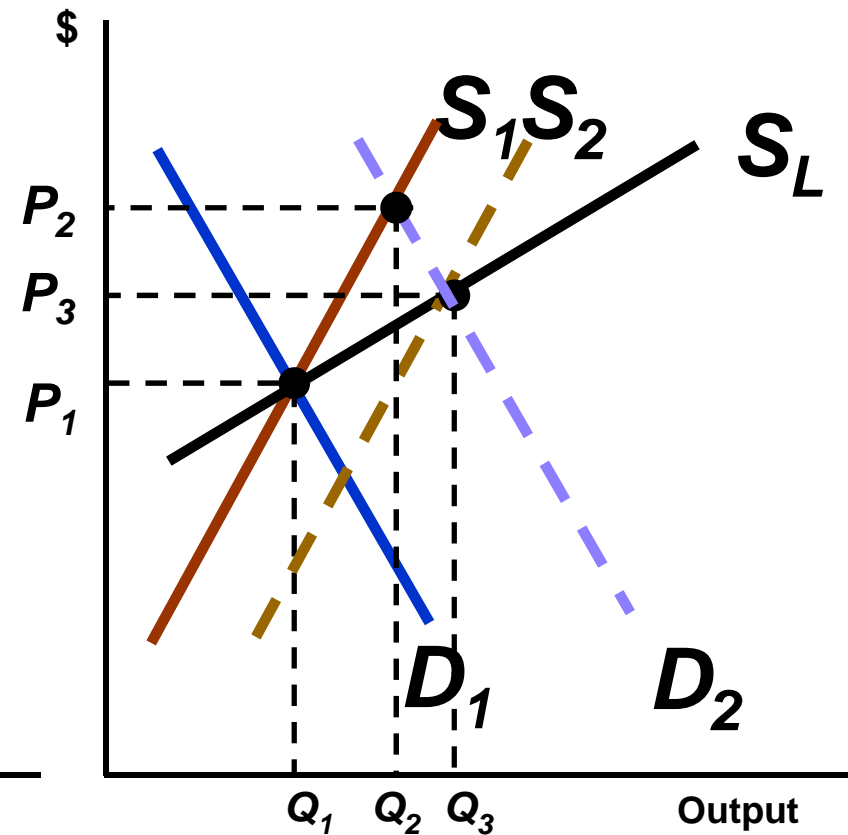
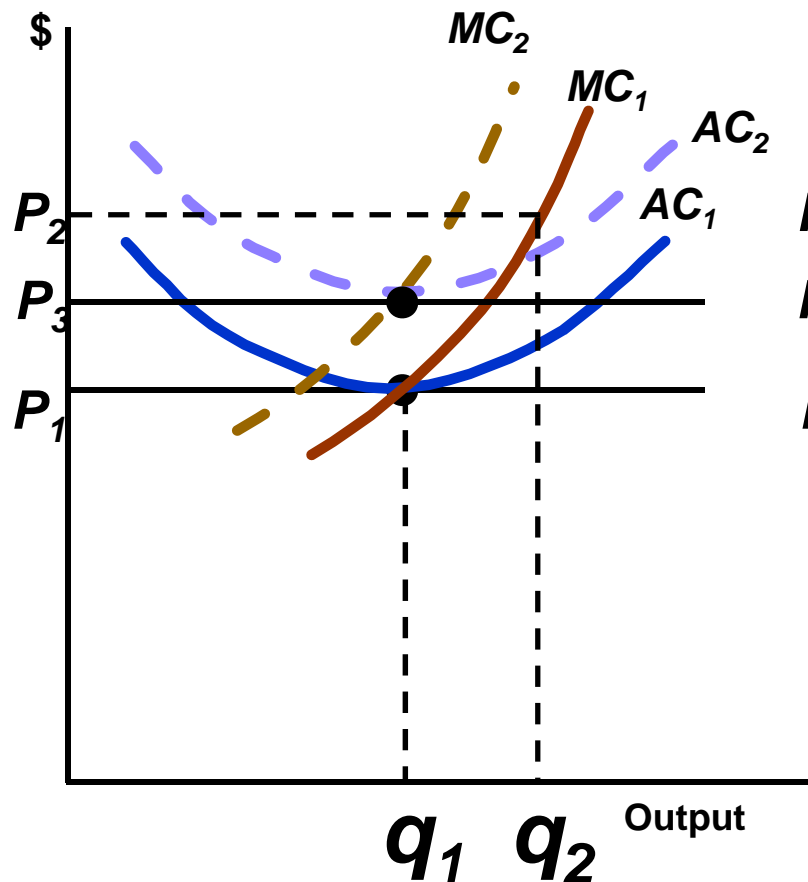
Increasing-Cost Industry

- Prices of some or all inputs rises as production is expanded when demand of inputs increases
- When demand increases, causing prices to increase and production to increase
 - Firms enter the market increasing demand for inputs
 - Costs increase, causing an upward shift in supply curves (congestion, shortage, and so on)
 - Market supply increases but not as much

Long-Run Supply in an Increasing-Cost Industry

Due to the increase in input prices, long-run equilibrium occurs at a higher price.

Long Run Supply is upward Sloping





Long-Run Supply in an Increasing-Cost Industry

- In an increasing-cost industry, long-run supply curve is upward sloping
- More output is produced, but only at the higher price needed to compete for the increased input costs

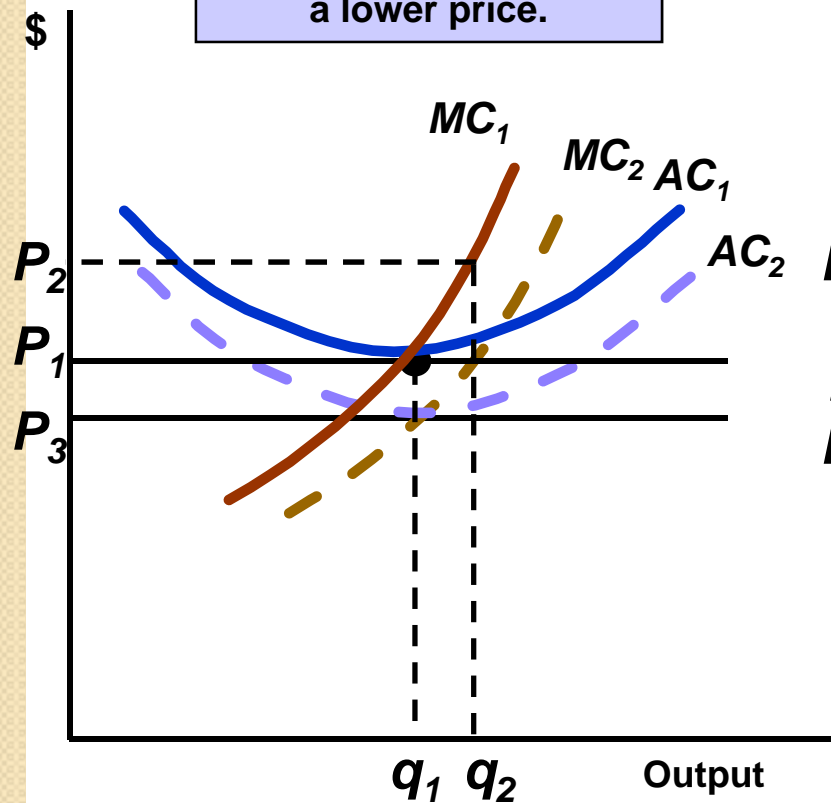


Decreasing-Cost Industry

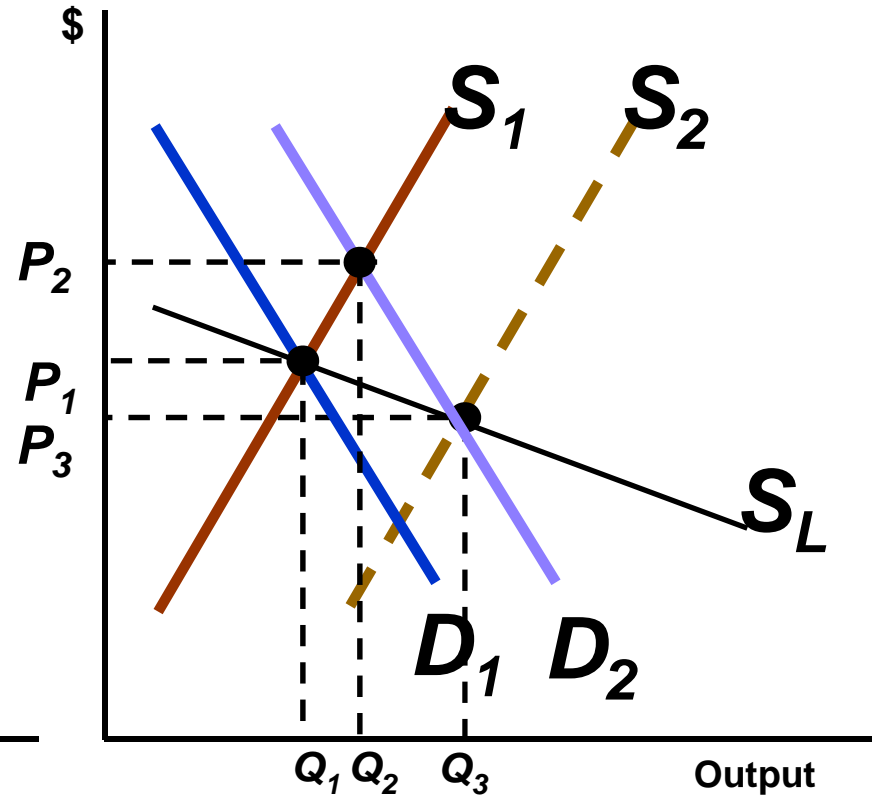
- Industry whose long-run supply curve is downward sloping
- Increase in demand causes production to increase
 - Increase in size allows firm to take advantage of size to get inputs cheaper
 - Increased production may lead to better efficiencies or quantity discounts
 - Costs shift down and market price falls

Long-Run Supply in a Decreasing-Cost Industry

Due to the decrease in input prices, long-run equilibrium occurs at a lower price.



Long Run Supply is Downward Sloping

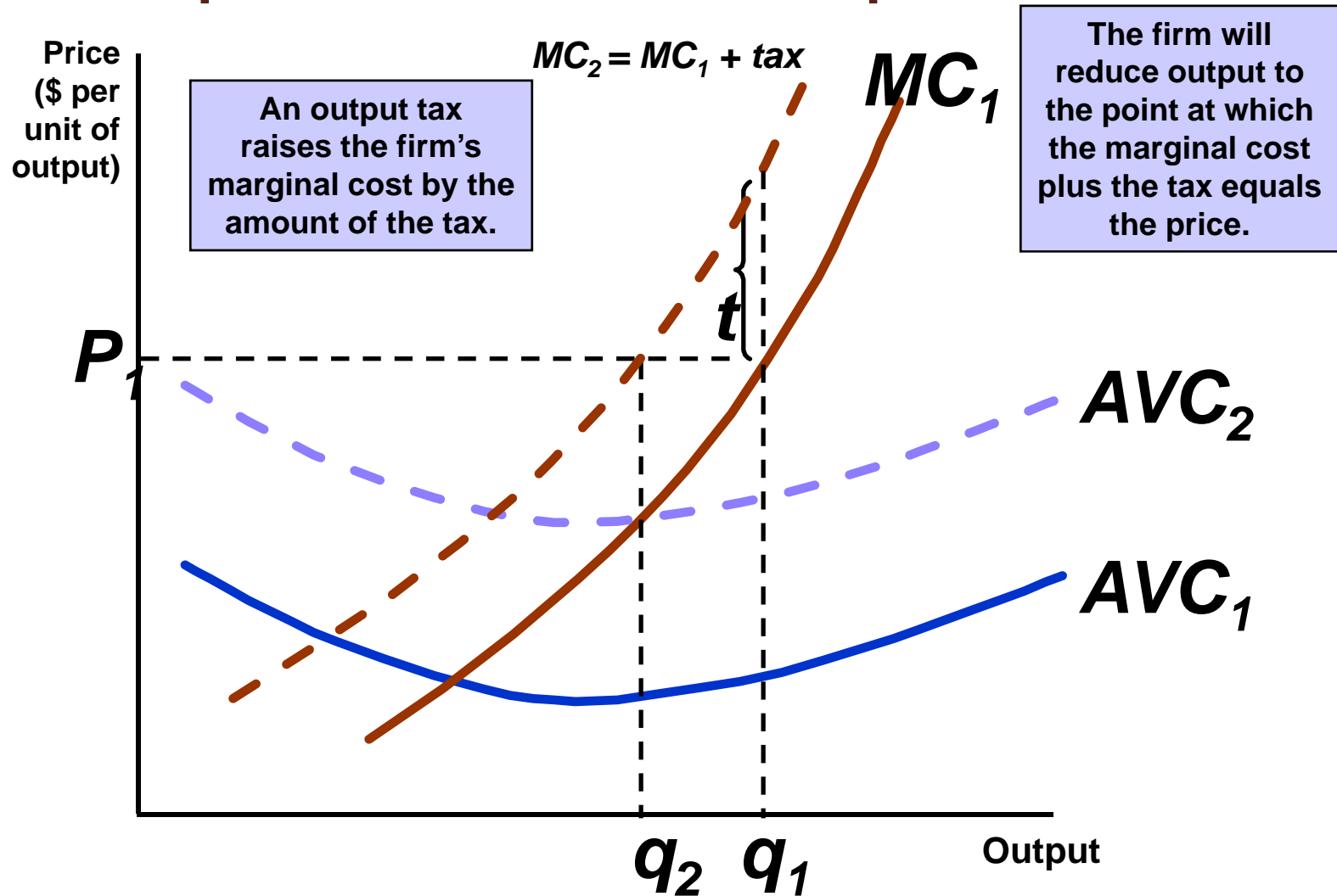




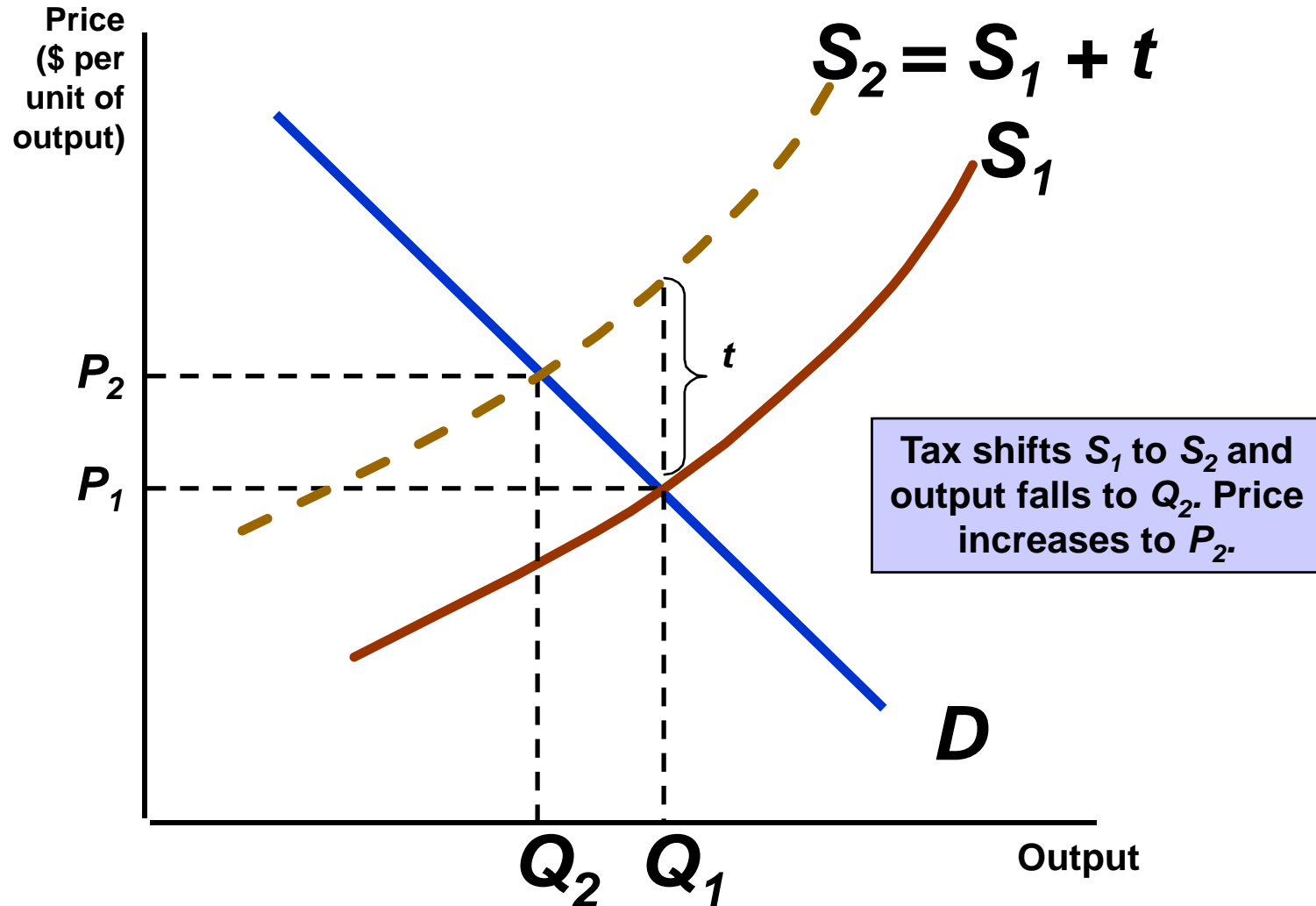
Short-Run Implications for Taxation

- The Effects of a Tax
 - We will consider how a firm responds to a tax on its output
 - The tax impact on the in industry supply curve in the short run

Effect of an Output Tax on a Competitive Firm's Output



Effect of an Output Tax on Industry Output

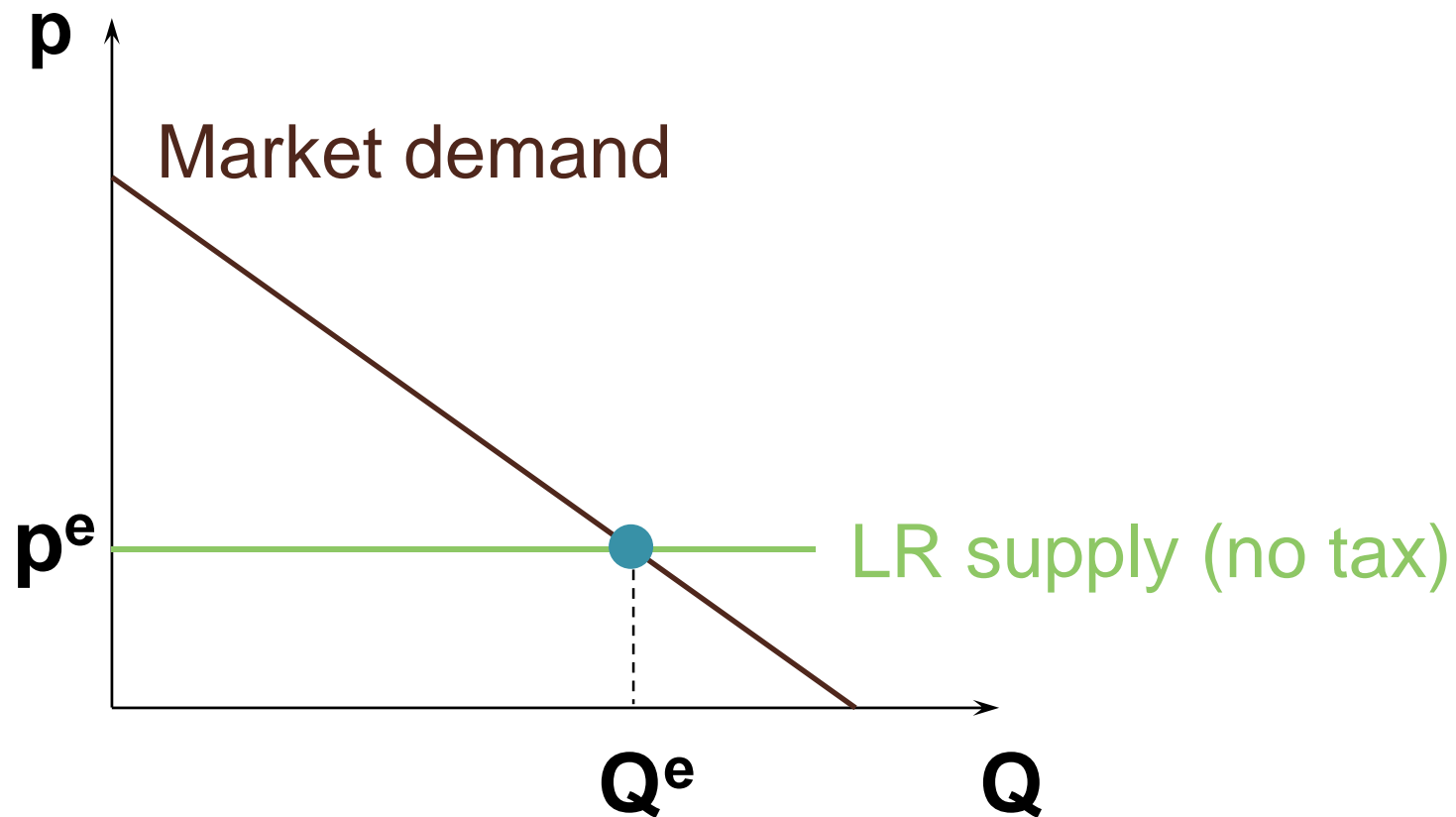




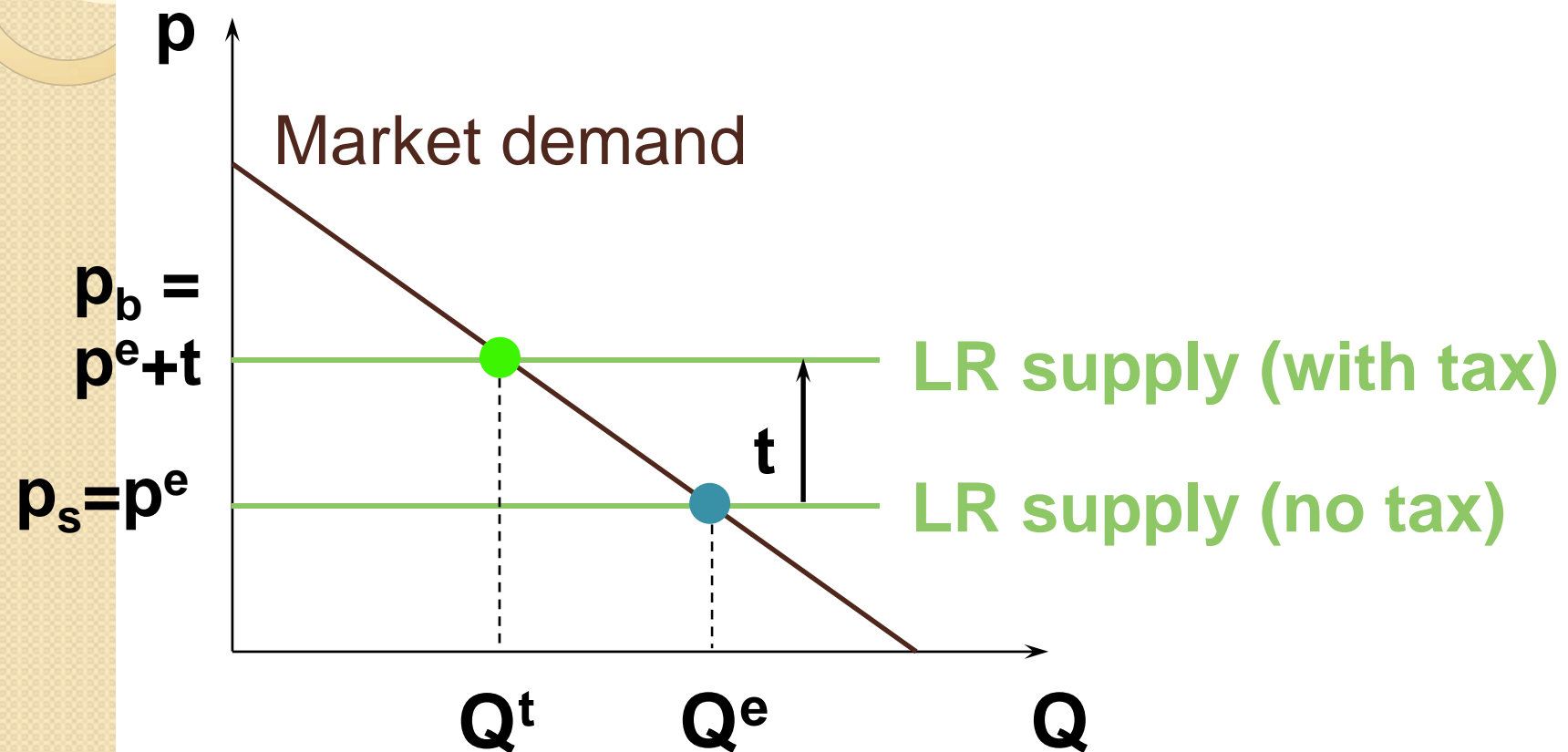
Long-Run Implications for Taxation

- In a short-run equilibrium, the burden of a sales or an excise tax is typically shared by both buyers and sellers, tax incidence of the tax depending upon the own-price elasticities of demand and supply.
- Q: Is this true in a long-run market equilibrium?

Long-Run Implications for Taxation

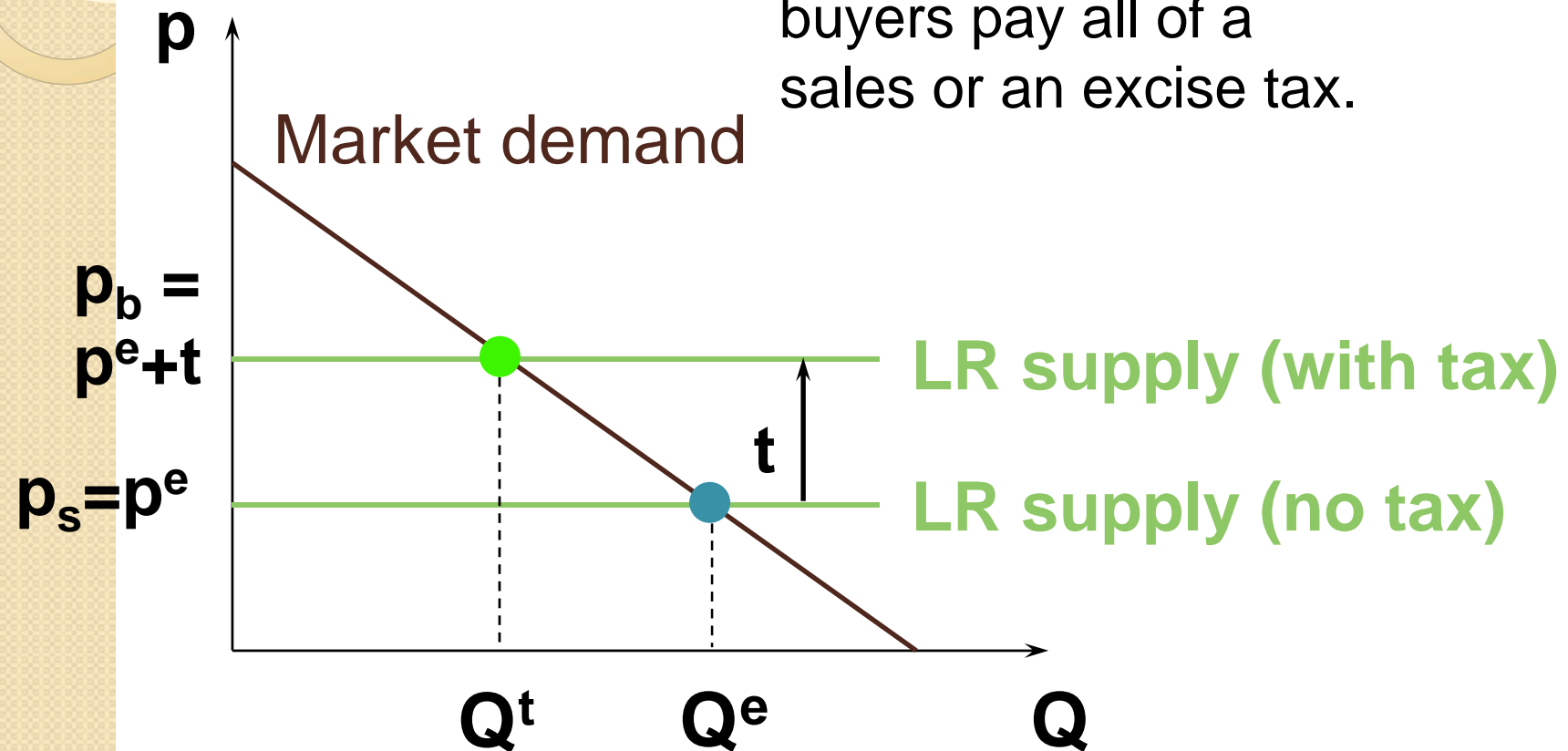


Long-Run Implications for Taxation



Long-Run Implications for Taxation

In the long-run the buyers pay all of a sales or an excise tax.





Fixed Inputs and Economic Rent

- There may be some fixed factor(s) even in the long run
- E.g., the taxi-cab industry has a barrier to entry even though there are lots of cabs competing with each other.
- Cigarette production licensing is a barrier to entry into a competitive industry.
- Other examples of fixed inputs: land, natural resources, talents, or govt. regulation (licensing)



Fixed Inputs and Economic Rent

- Q: When there is a barrier to entry, will not the firms already in the industry make positive economic profits?



Fixed Inputs and Economic Rent

- Q: When there is a barrier to entry, will not the firms already in the industry make positive economic profits?
- A: No. Each firm in the industry makes a zero economic profit. Why?

Fixed Inputs and Economic Rent

- Think of a firm that needs an operating license -- the license is a fixed input that is rented but not owned by the firm
- If the firm makes a positive economic profit then another firm can offer the license owner a higher price for it
- In this way, all firms' economic profits are competed away, to zero



Fixed Inputs and Economic Rent

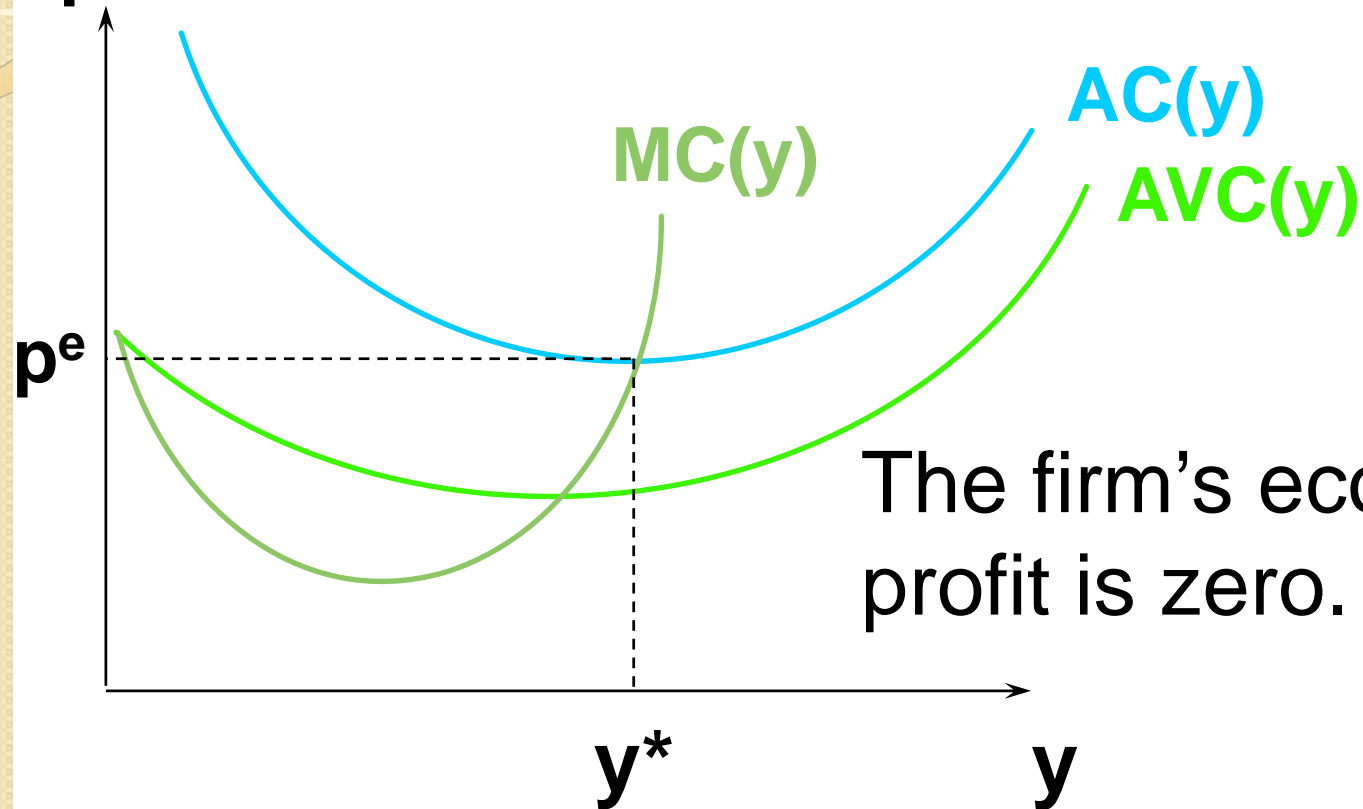
- So in the long-run equilibrium, each firm makes a zero economic profit and each firm's fixed cost is its payment for its operating license
- If the opportunity cost of the input (rent) is not taken into consideration, it may appear that economic profits exist in the long run

Fixed Inputs and Economic Rent

- An input (e.g. an operating license) that is fixed in the long-run causes a long-run fixed cost, F .
- Long-run total cost, $c(y) = F + c_v(y)$.
- And long-run average total cost,
 $AC(y) = AFC(y) + AVC(y)$.
- In the long-run equilibrium, what will be the value of F ?

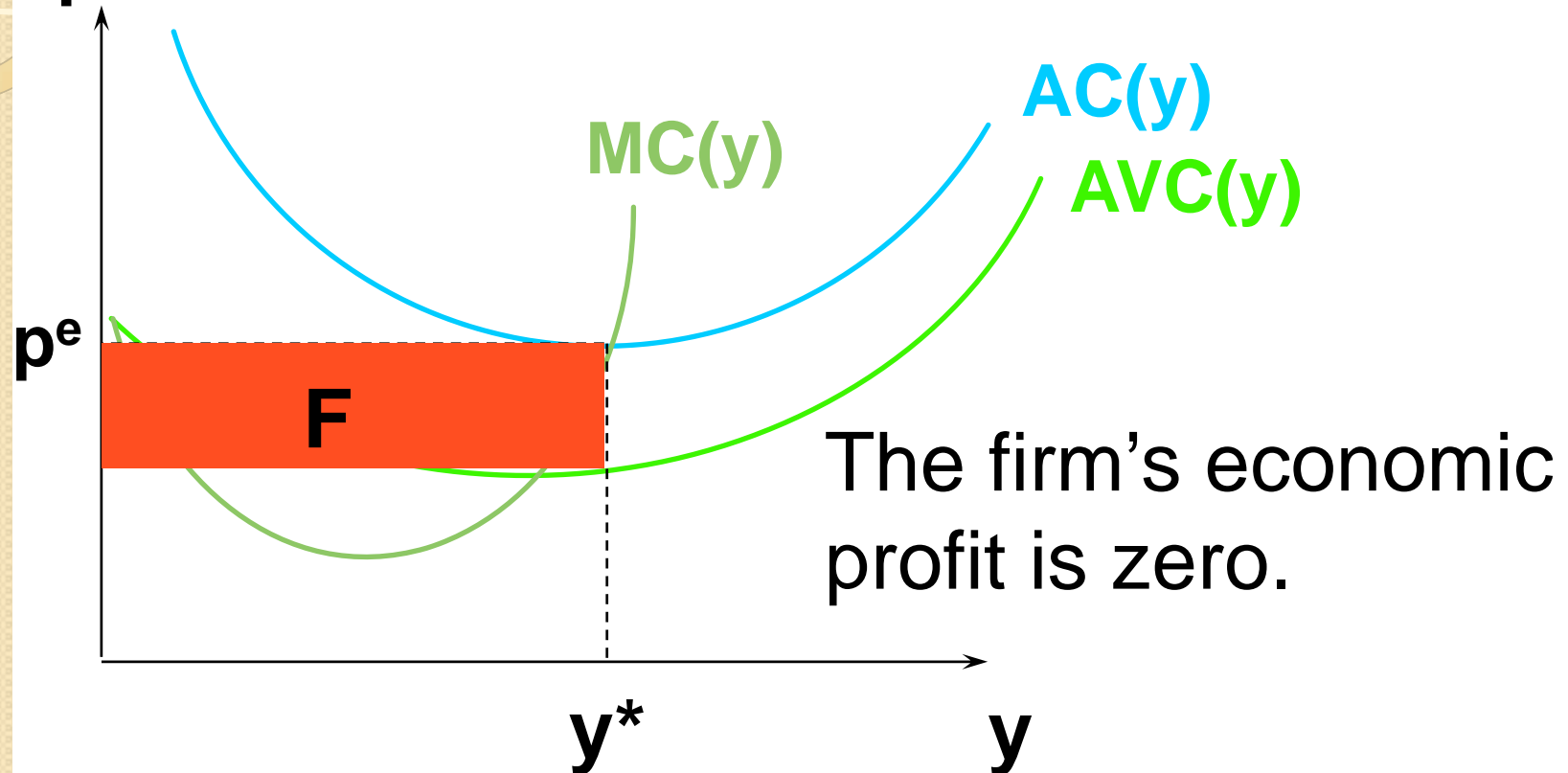
Fixed Inputs and Economic Rent

\$/output unit



Fixed Inputs and Economic Rent

\$/output unit



F is the payment to the owner of the fixed input (the license).

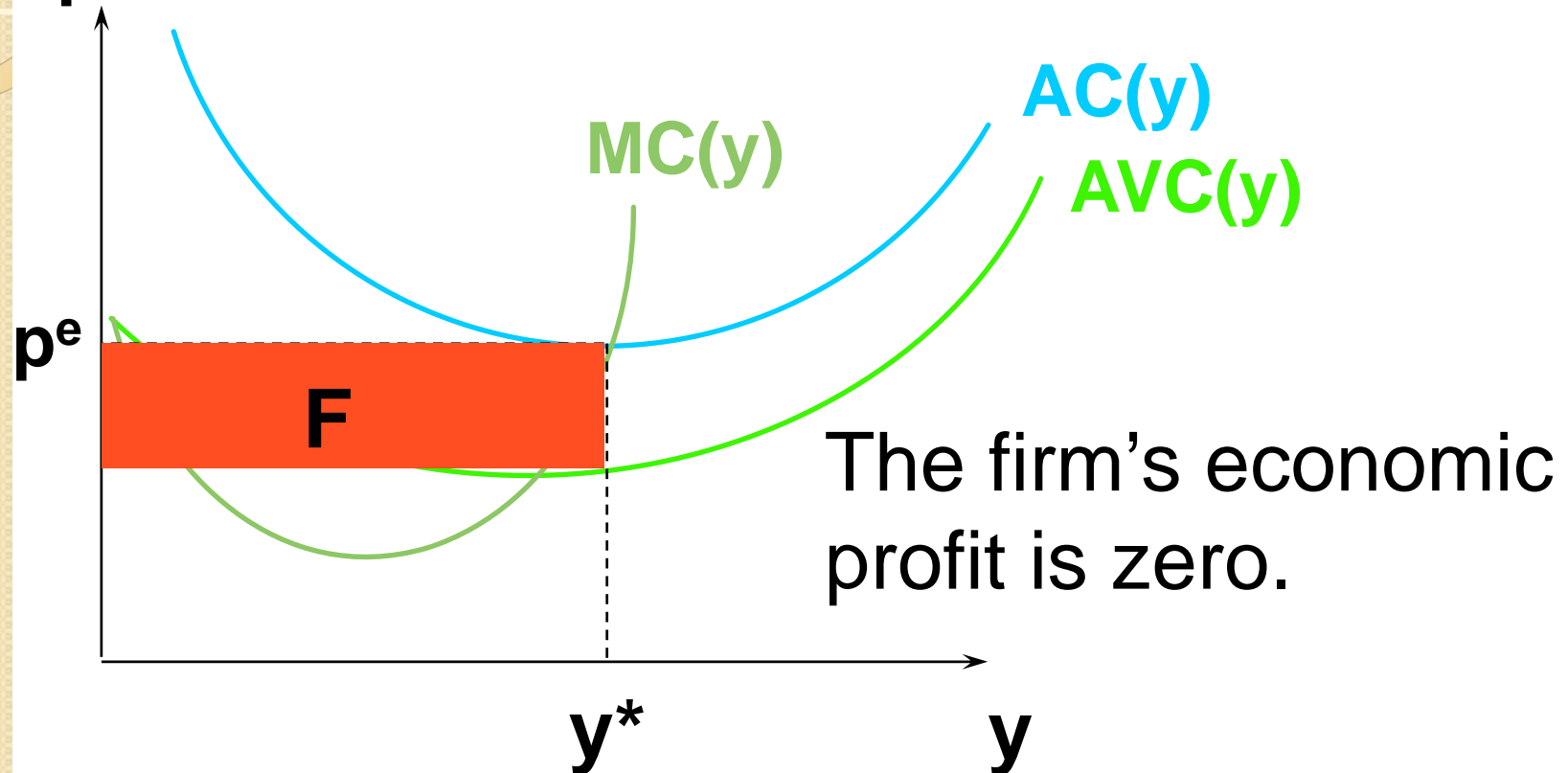


Fixed Inputs and Economic Rent

- Economic rent is the payment for an input that is in excess of the minimum payment required to have that input supplied.
- Each license essentially costs zero to supply, so the long-run economic rent paid to the license owner is the firm's long-run fixed cost.

Fixed Inputs and Economic Rent

\$/output unit



F is the payment to the owner of the fixed input (the license); F = economic rent.

The Implication of Economic Rent

- The equilibrium rent for the fixed input will be whatever it takes to drive profits to zero
- $P^*y^* - C_v(y^*) - \text{rent} = 0$
- $\text{Rent} = P^*y^* - C_v(y^*)$
- ***It is the equilibrium price that determines rent, not the reverse***
- Note that y^* is determined by $p^* = MC(y^*)$ which has nothing to do with rent



Land and Housing Prices

- Many scholars claim that China's high housing prices are due to the high fees levied on the land
- The implication of this claim is that China's housing prices will go down if the government reduces land prices
- Is it true?
- The shops in the airport sell products at the higher price than elsewhere. Shop owners say it is because of high rent in the airport. True or not?



Rent-Seeking

- Restrictions on entry or fixed input creates sizable rents
- This leads to so-called ***rent seeking*** activities
- Efforts directed at keeping or acquiring claims to factors fixed in supply
- These efforts represent a *pure deadweight loss* since no more output is produced and they simply grab rents



Chapter 9

Market Equilibrium



Topics to be Discussed

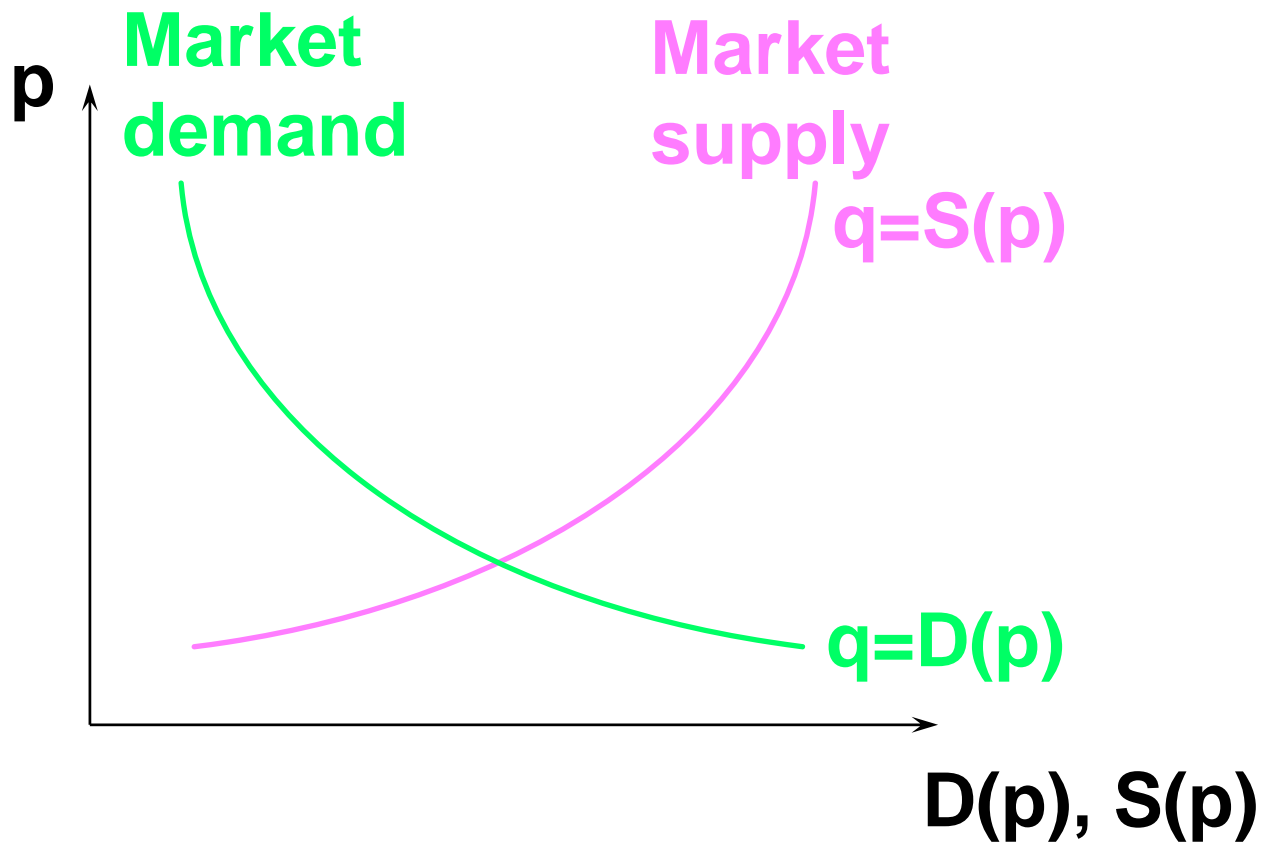
- Market equilibrium
- Quantity tax and equilibrium
- Tax incidence
- Deadweight loss



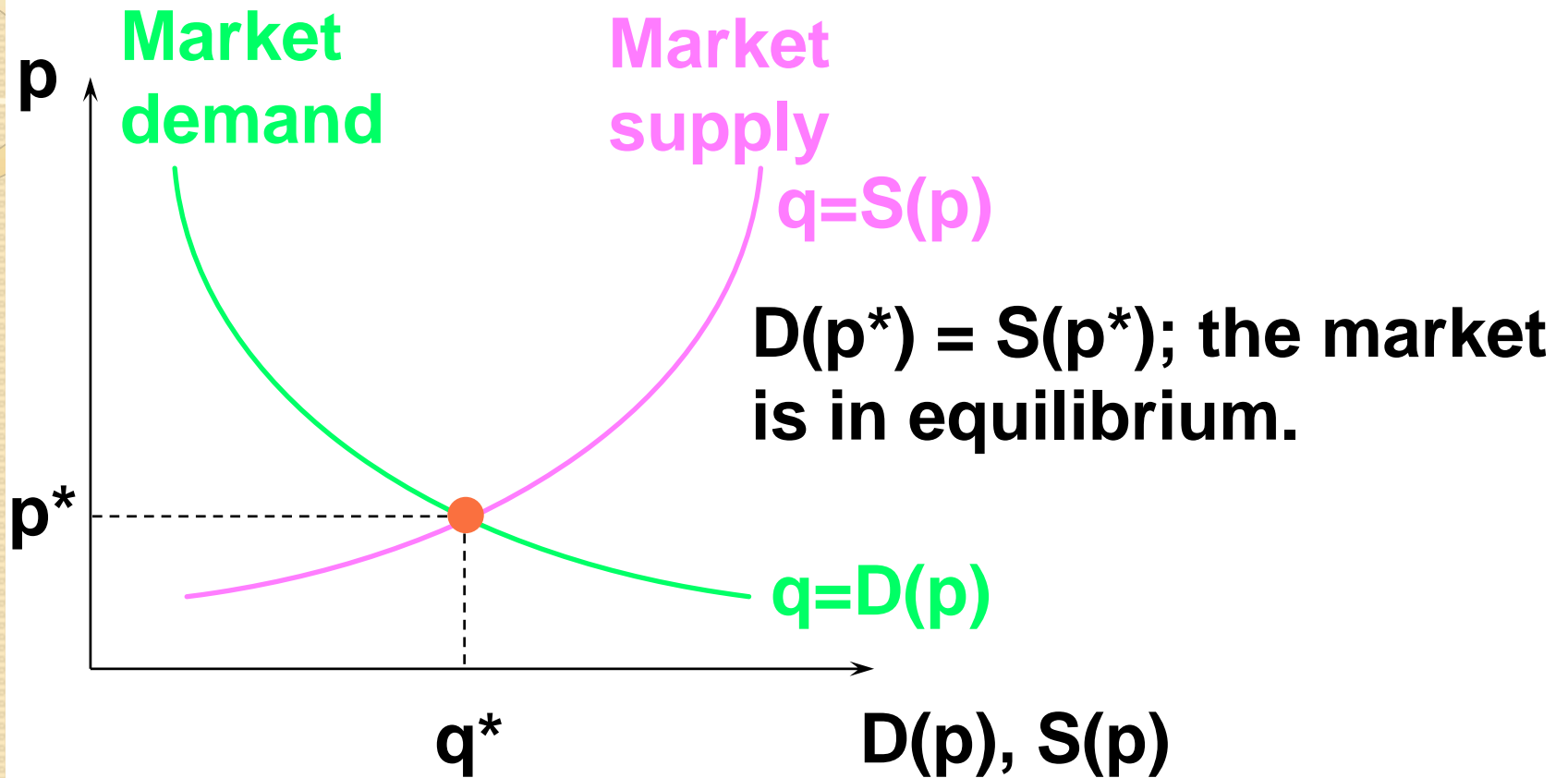
Market Equilibrium

- A market is in **equilibrium** when total quantity demanded by buyers equals total quantity supplied by sellers.
- Also called “market is cleared”

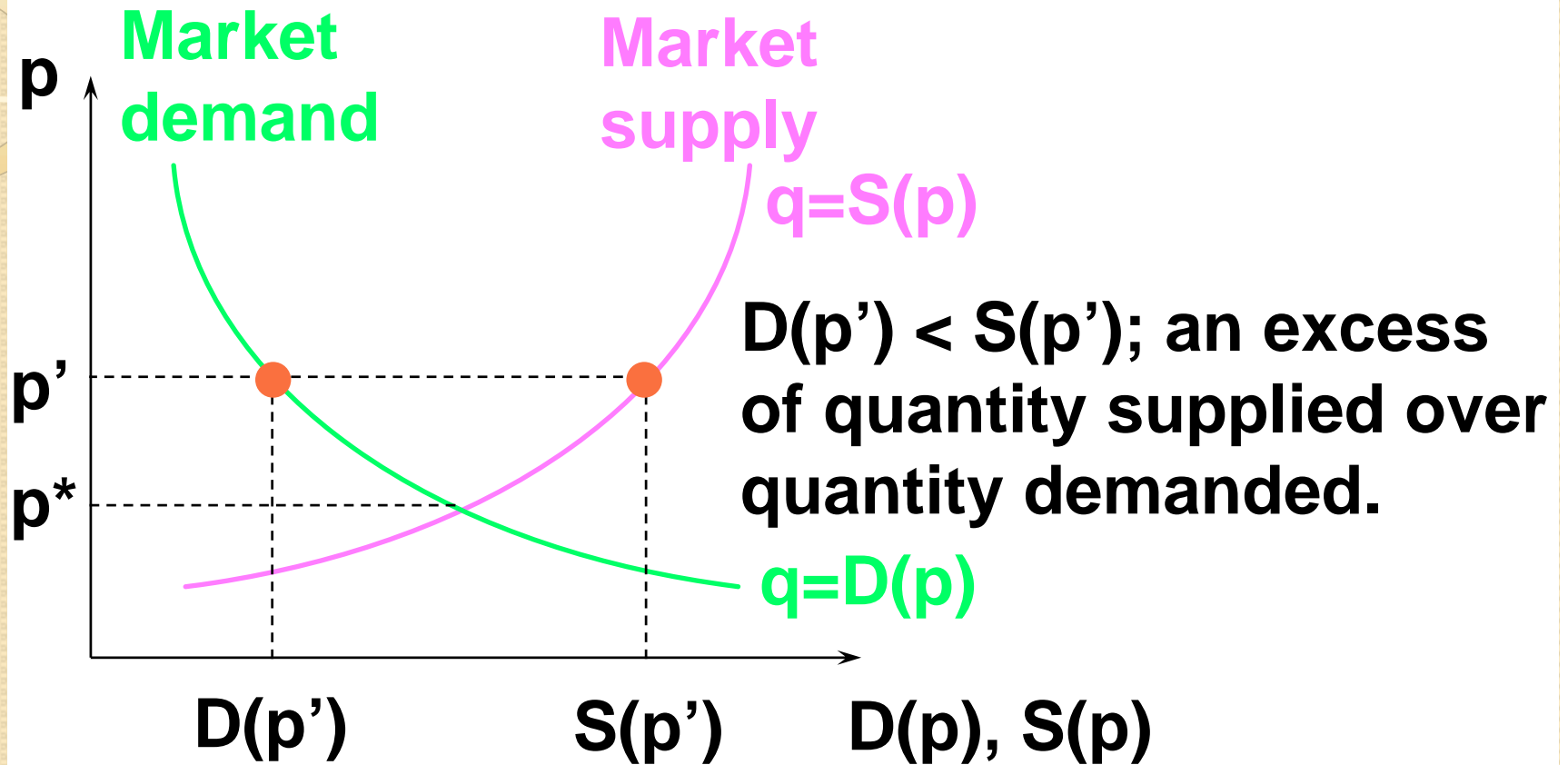
Market Equilibrium



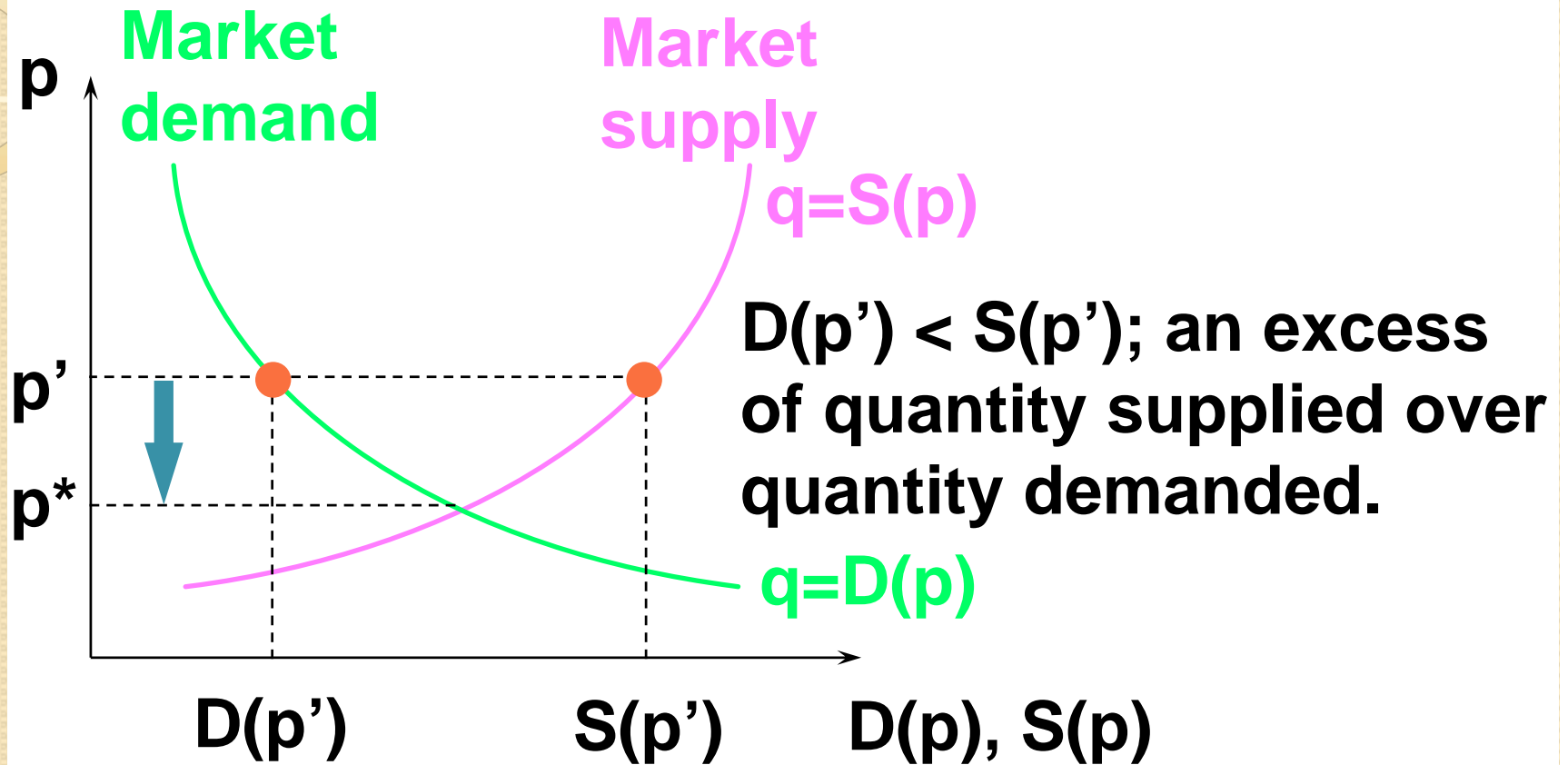
Market Equilibrium



Market Equilibrium

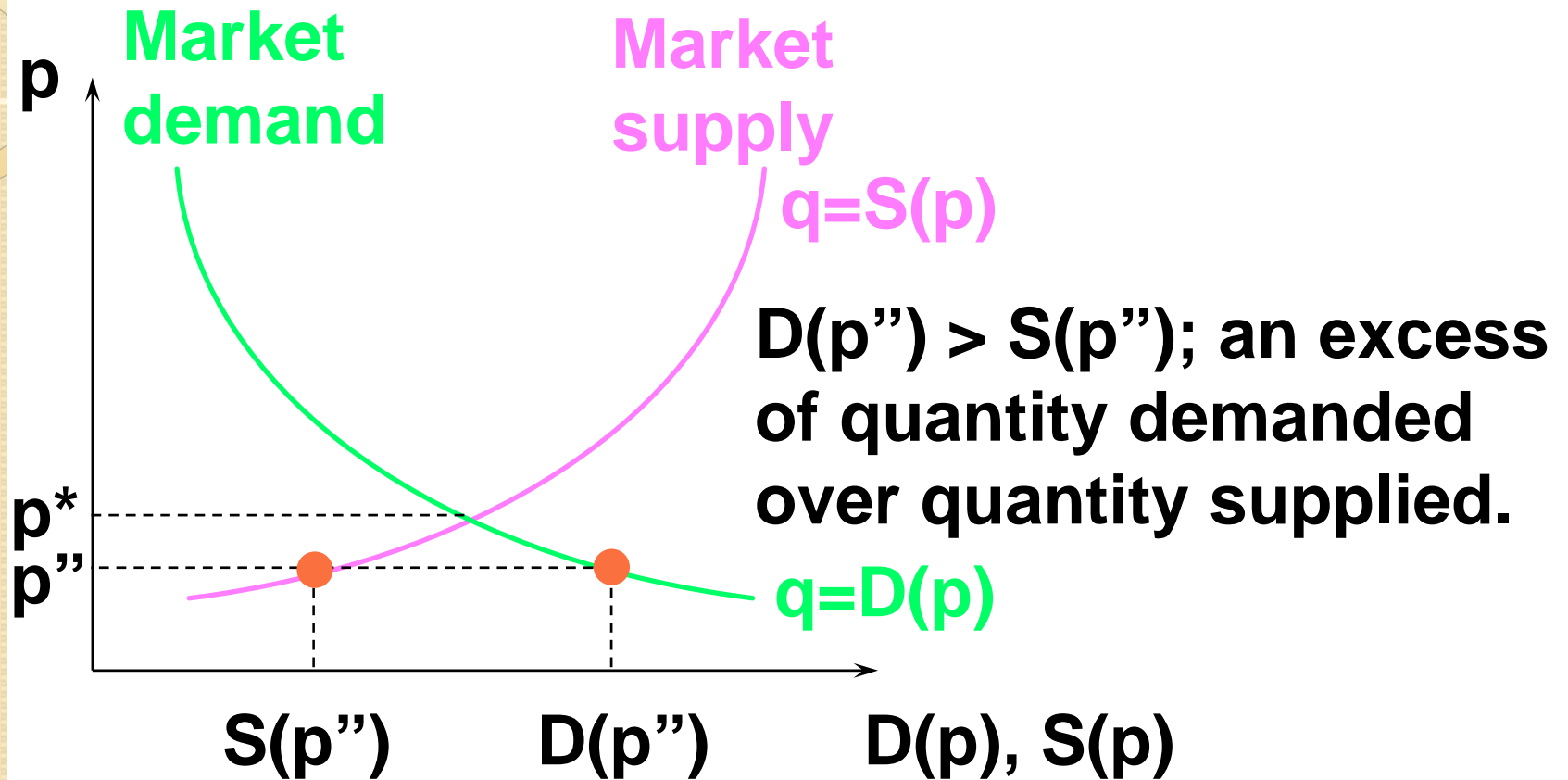


Market Equilibrium

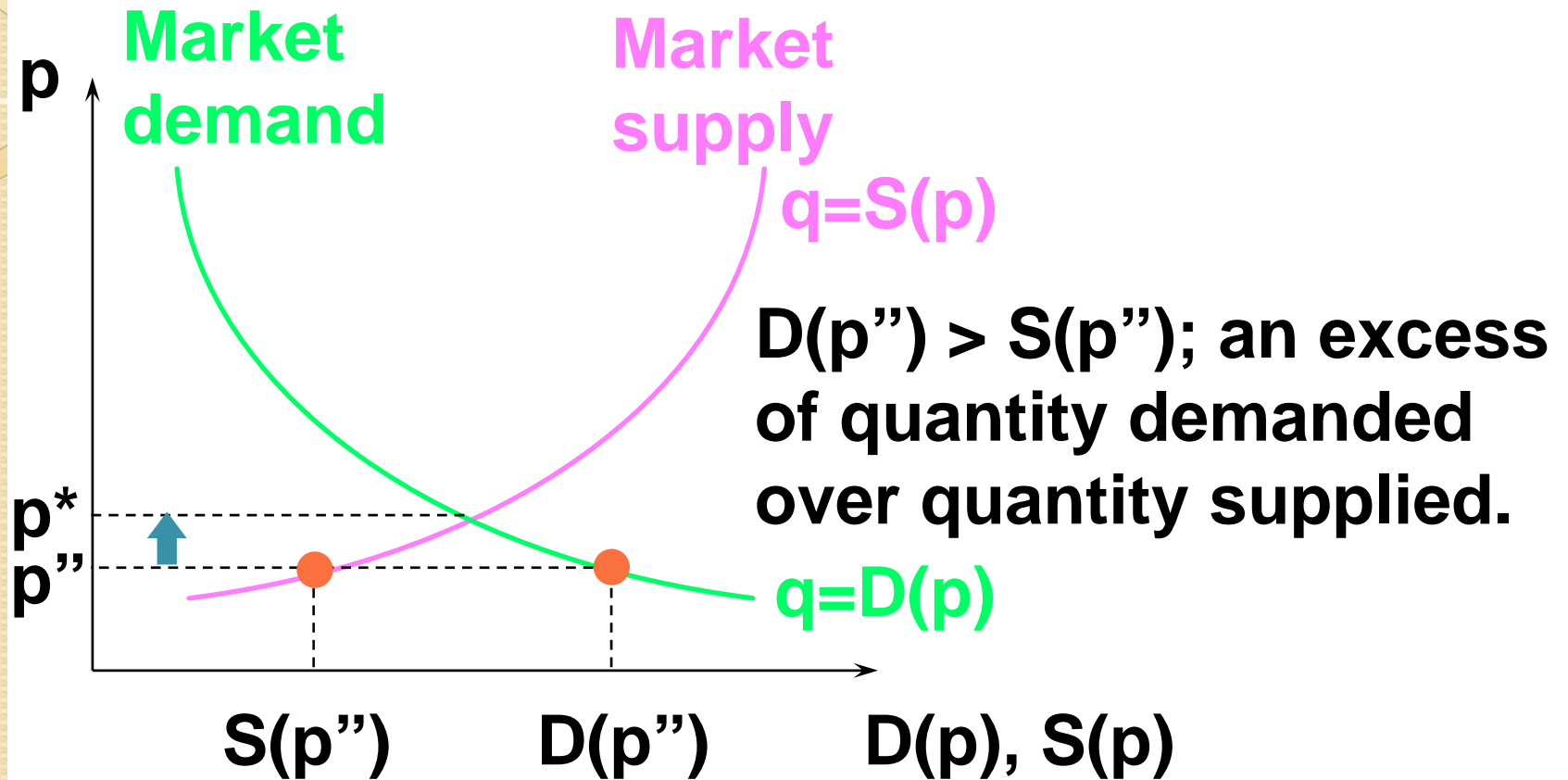


Market price must fall towards p^* .

Market Equilibrium



Market Equilibrium



Market price must rise towards p^* .

Market Equilibrium

- We can calculate the market equilibrium price and quantity using $D(p)=S(p)$
- Can we calculate the market equilibrium using the inverse market demand and supply curves?
- Yes, it is the same calculation
- $P_d(q)=P_s(q)$.

Market Equilibrium

$$q = D(p) = a - bp \Leftrightarrow p = \frac{a - q}{b} = D^{-1}(q),$$

the equation of the inverse market demand curve. And

$$q = S(p) = c + dp \Leftrightarrow p = \frac{-c + q}{d} = S^{-1}(q),$$

the equation of the inverse market supply curve.

Market Equilibrium

$D^{-1}(q),$
 $S^{-1}(q)$

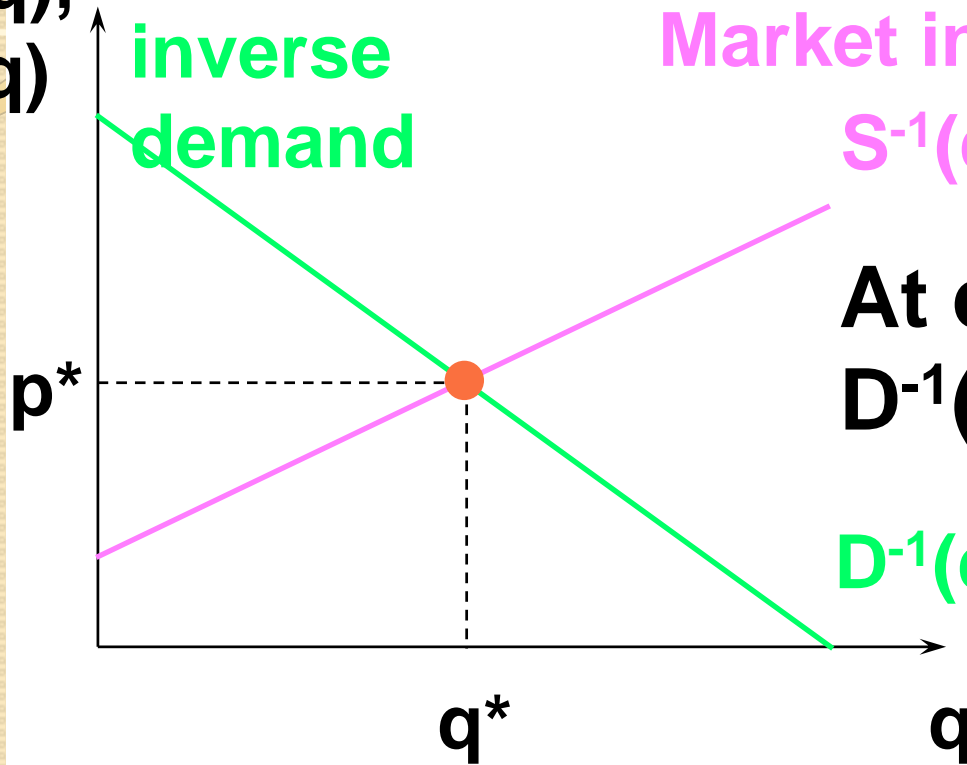
Market
inverse
demand

Market inverse supply

$$S^{-1}(q) = (-c+q)/d$$

At equilibrium,
 $D^{-1}(q^*) = S^{-1}(q^*)$.

$$D^{-1}(q) = (a-q)/b$$





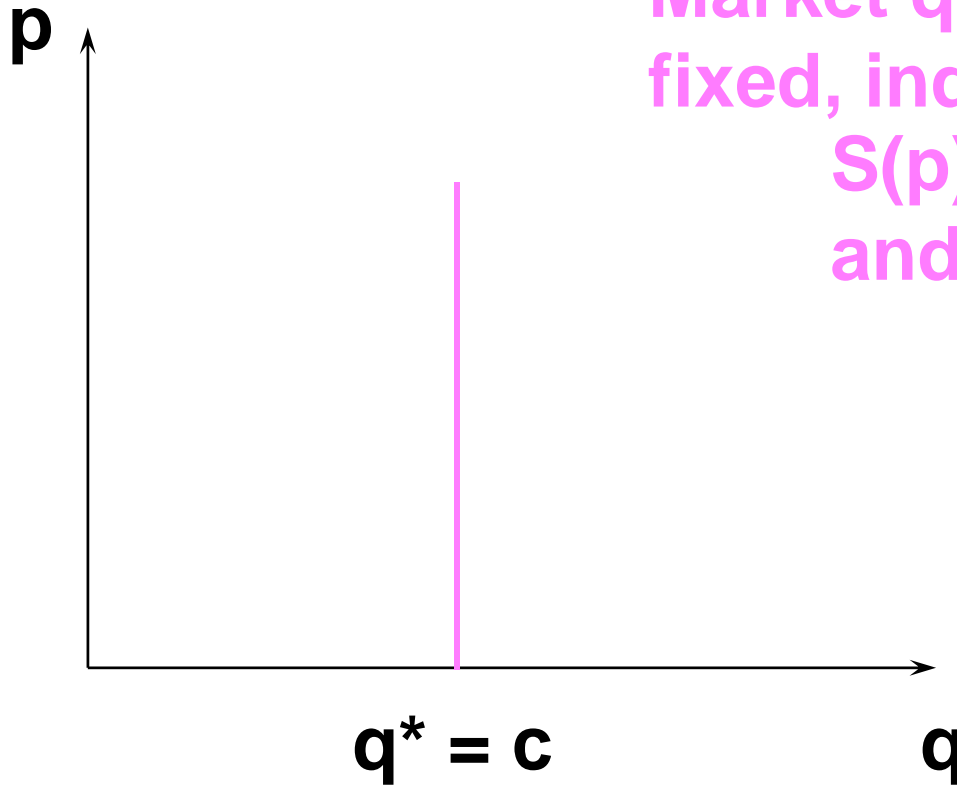
Market Equilibrium

- Two special cases:
 - quantity supplied is fixed, independent of the market price, and
 - quantity supplied is extremely sensitive to the market price.

Market Equilibrium

Market quantity supplied is fixed, independent of price.

$S(p) = c + dp$, so $d=0$
and $S(p) \equiv c$.

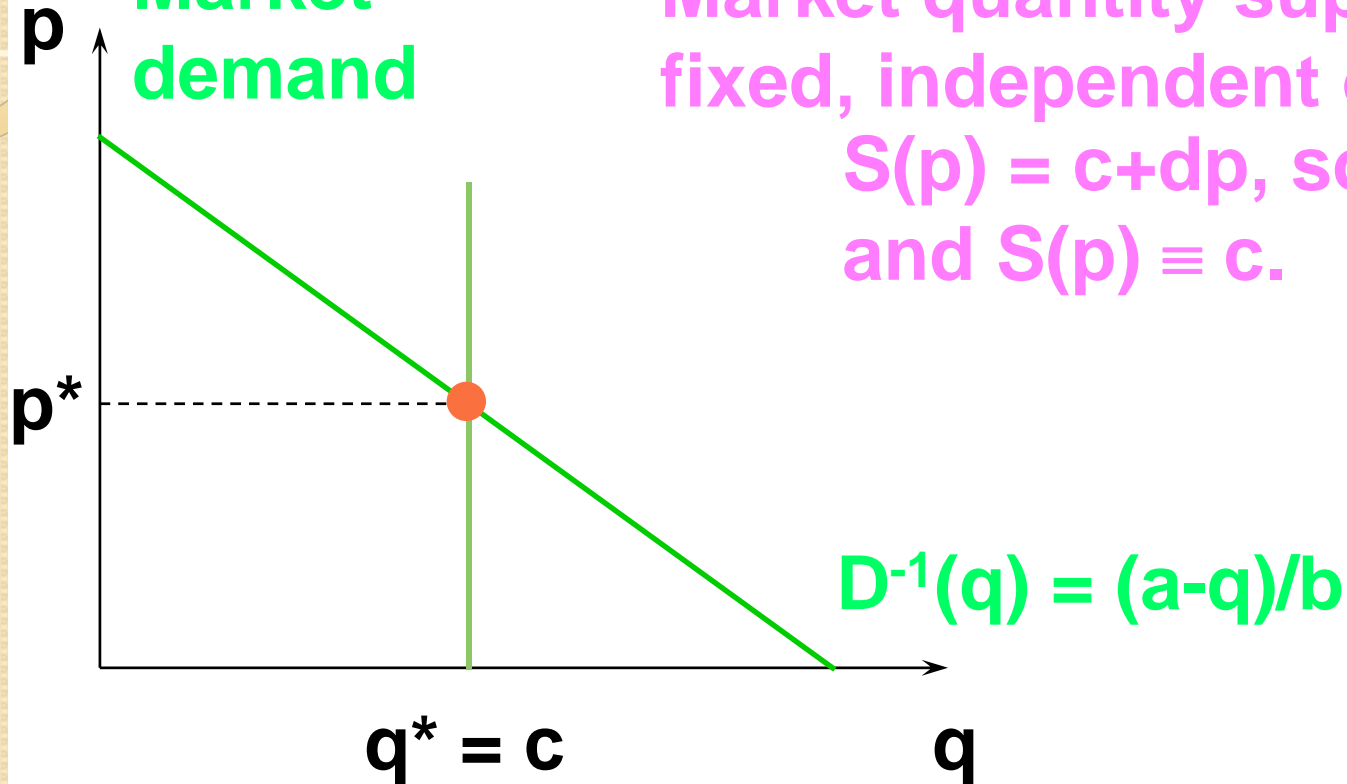


Market Equilibrium

Market
demand

Market quantity supplied is
fixed, independent of price.

$S(p) = c + dp$, so $d=0$
and $S(p) \equiv c$.



Market Equilibrium

Market
demand

Market quantity supplied is
fixed, independent of price.

$S(p) = c + dp$, so $d=0$
and $S(p) \equiv c$.

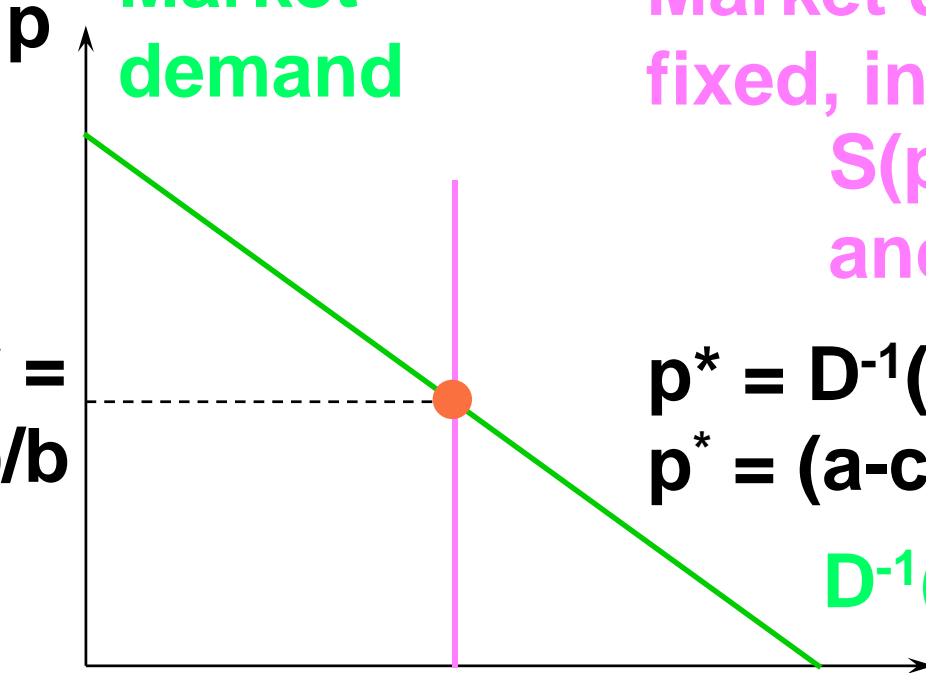
$$p^* = (a-c)/b$$

$p^* = D^{-1}(q^*)$; that is,
 $p^* = (a-c)/b$.

$$D^{-1}(q) = (a-q)/b$$

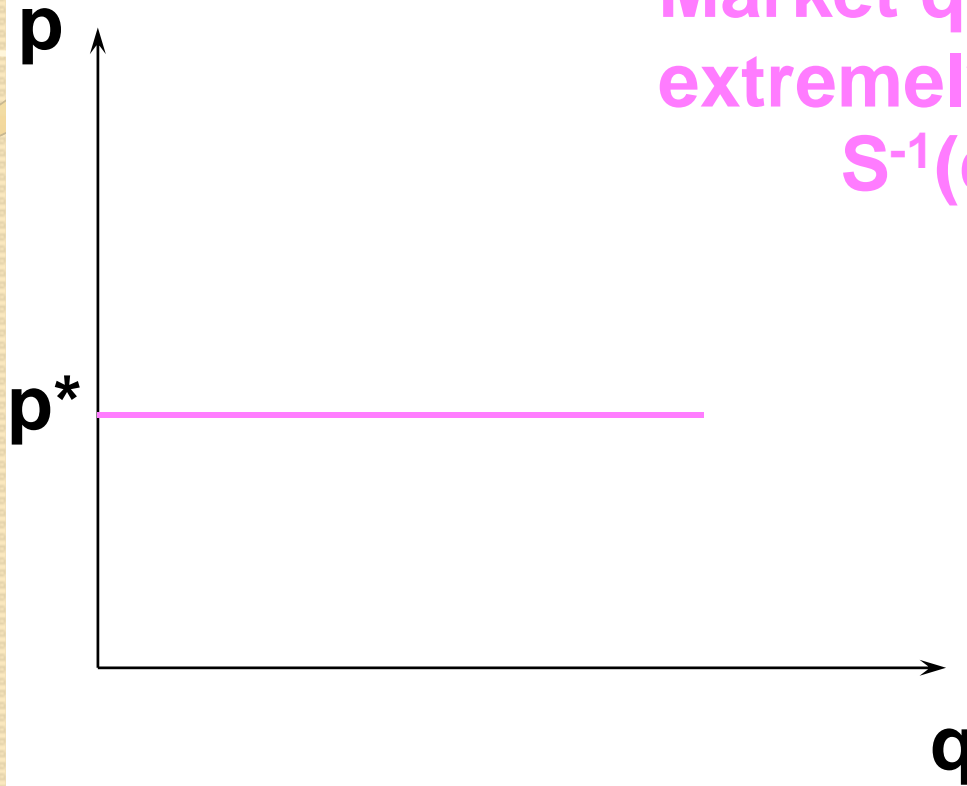
$$q^* = c$$

q



Market Equilibrium

Market quantity supplied is
extremely sensitive to price.
 $S^{-1}(q) = p^*$.

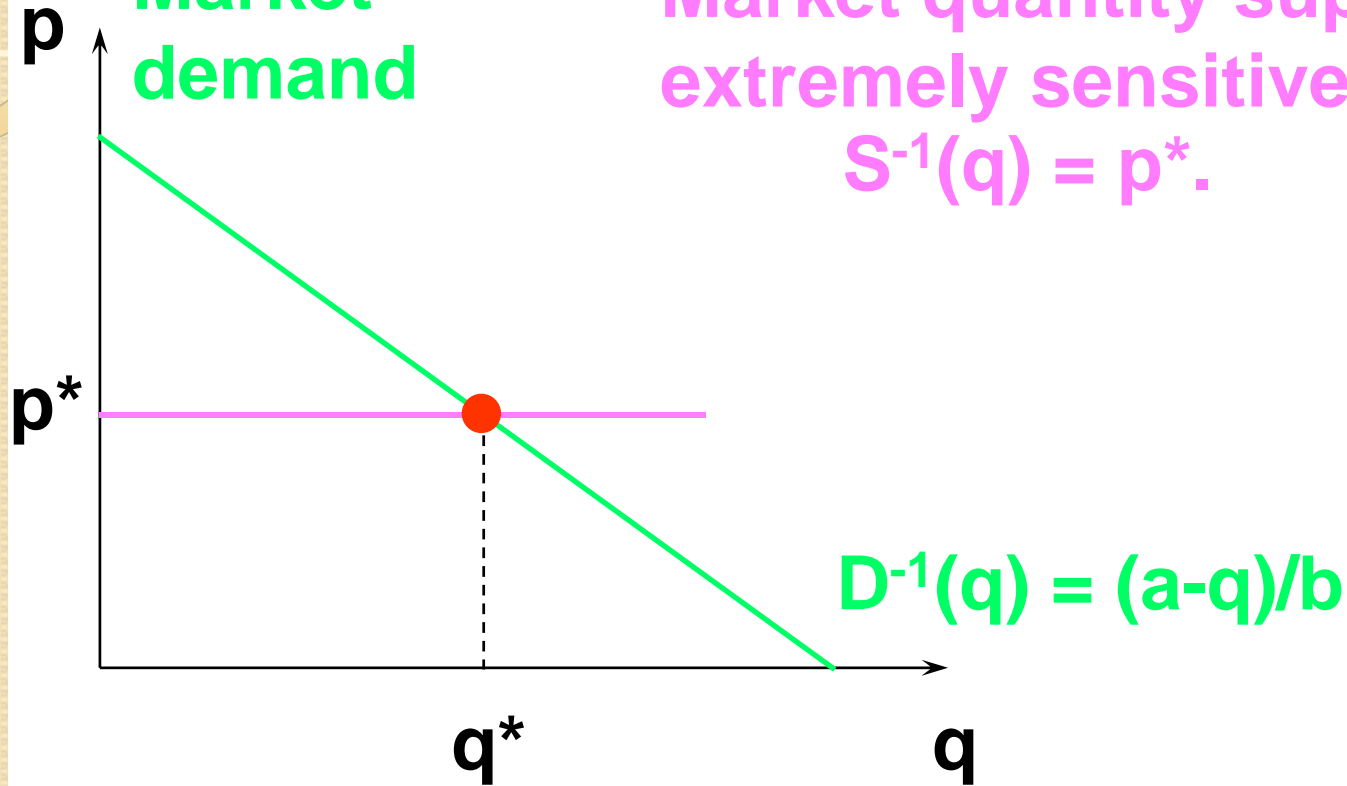


Market Equilibrium

Market
demand

Market quantity supplied is
extremely sensitive to price.

$$S^{-1}(q) = p^*.$$





Comparative Statics

- Shifting demand curves
 - Income
 - Price of other products
- Shifting supply curves
 - Technology
- Taxes



Quantity Taxes

- A quantity tax levied at a rate of $\$t$ is a tax of $\$t$ paid on each unit traded.
- If the tax is levied on sellers then it is an **excise tax**.
- If the tax is levied on buyers then it is a **sales tax**.



Quantity Taxes

- What is the effect of a quantity tax on a market's equilibrium?
- How are prices affected?
- How is the quantity traded affected?
- Who pays the tax?
- How are gains-to-trade altered?

Quantity Taxes

- A tax rate t makes the price paid by buyers, p_b , higher by t from the price received by sellers, p_s .

$$p_b - p_s = t$$

Quantity Taxes

- Even with a tax the market must clear.
- I.e. quantity demanded by buyers at price p_b must equal quantity supplied by sellers at price p_s .

$$D(p_b) = S(p_s)$$

Quantity Taxes

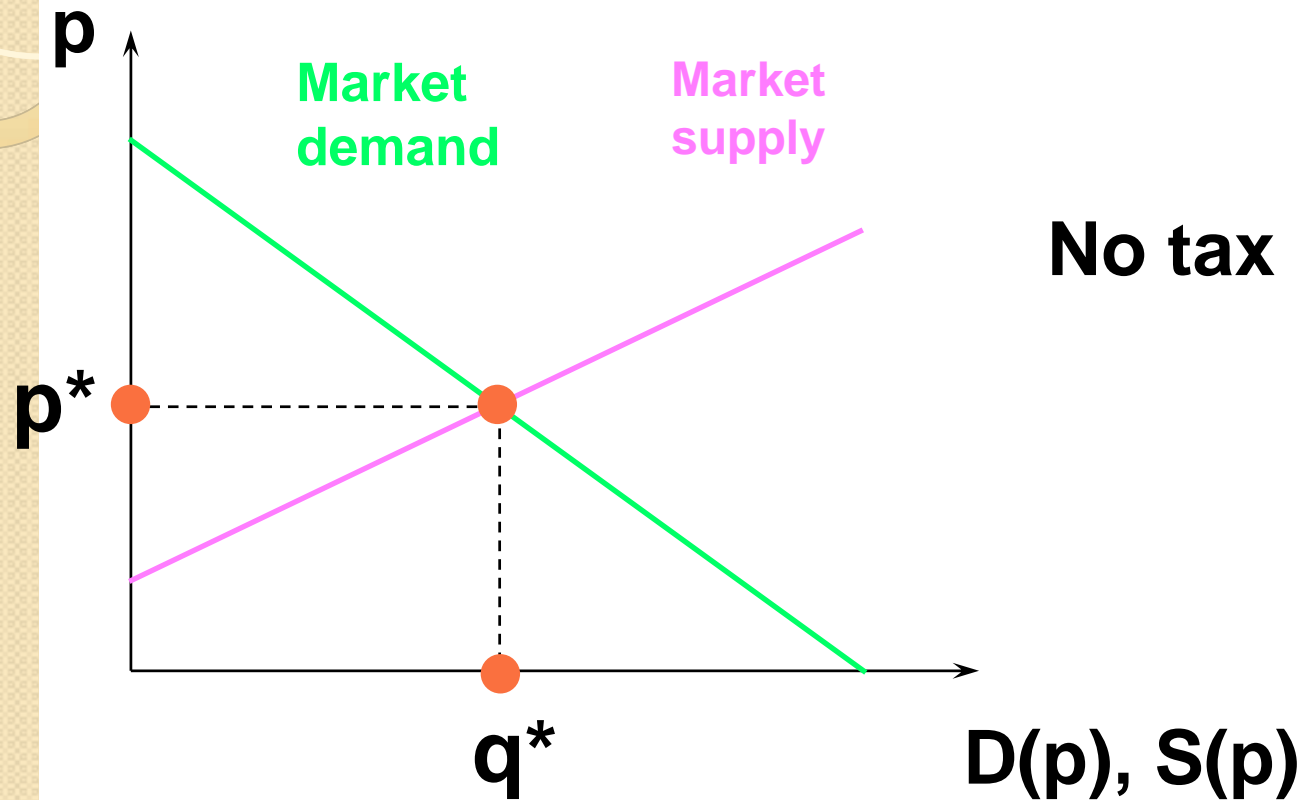
$$p_b - p_s = t \quad \text{and} \quad D(p_b) = S(p_s)$$

describe the market's equilibrium.

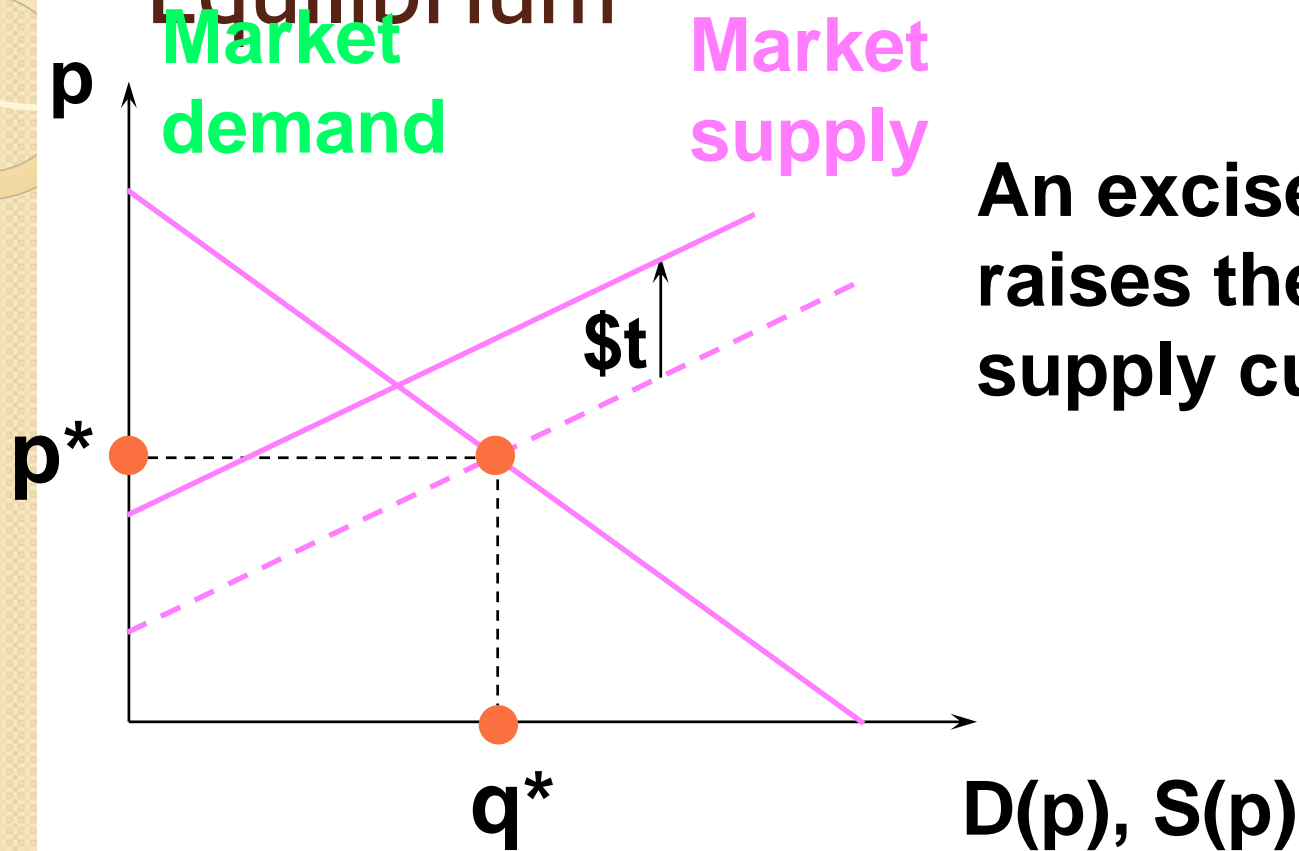
Notice that these two conditions apply no matter if the tax is levied on sellers or on buyers.

Hence, a sales tax rate t has the same effect as an excise tax rate t .

Quantity Taxes & Market Equilibrium

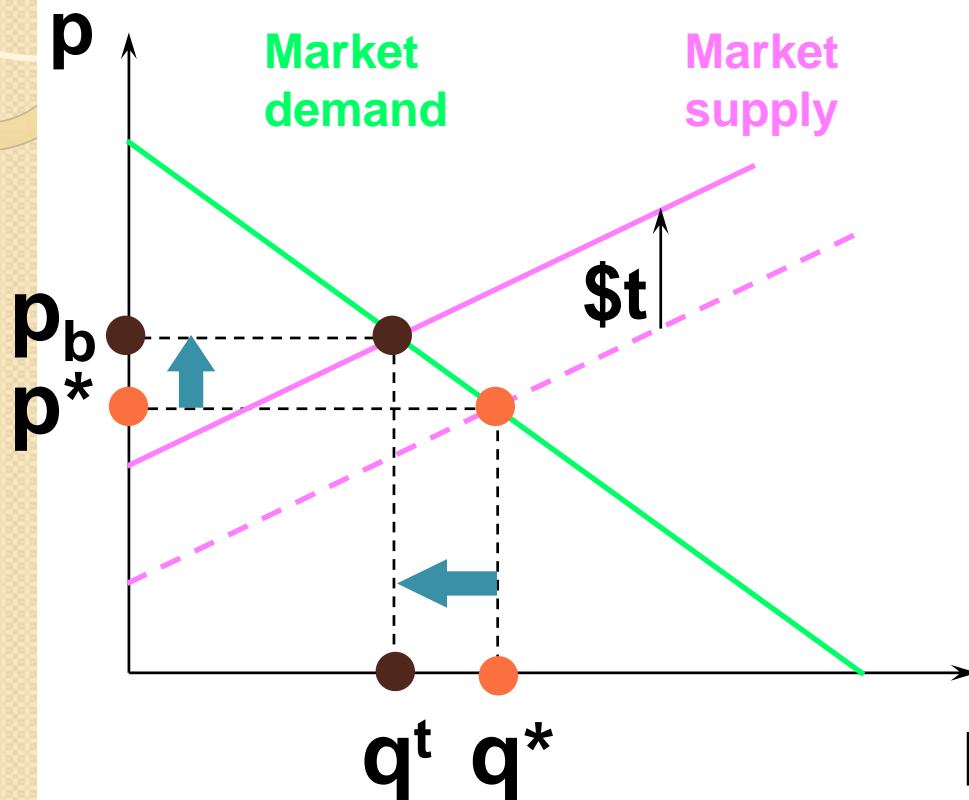


Quantity Taxes & Market Equilibrium



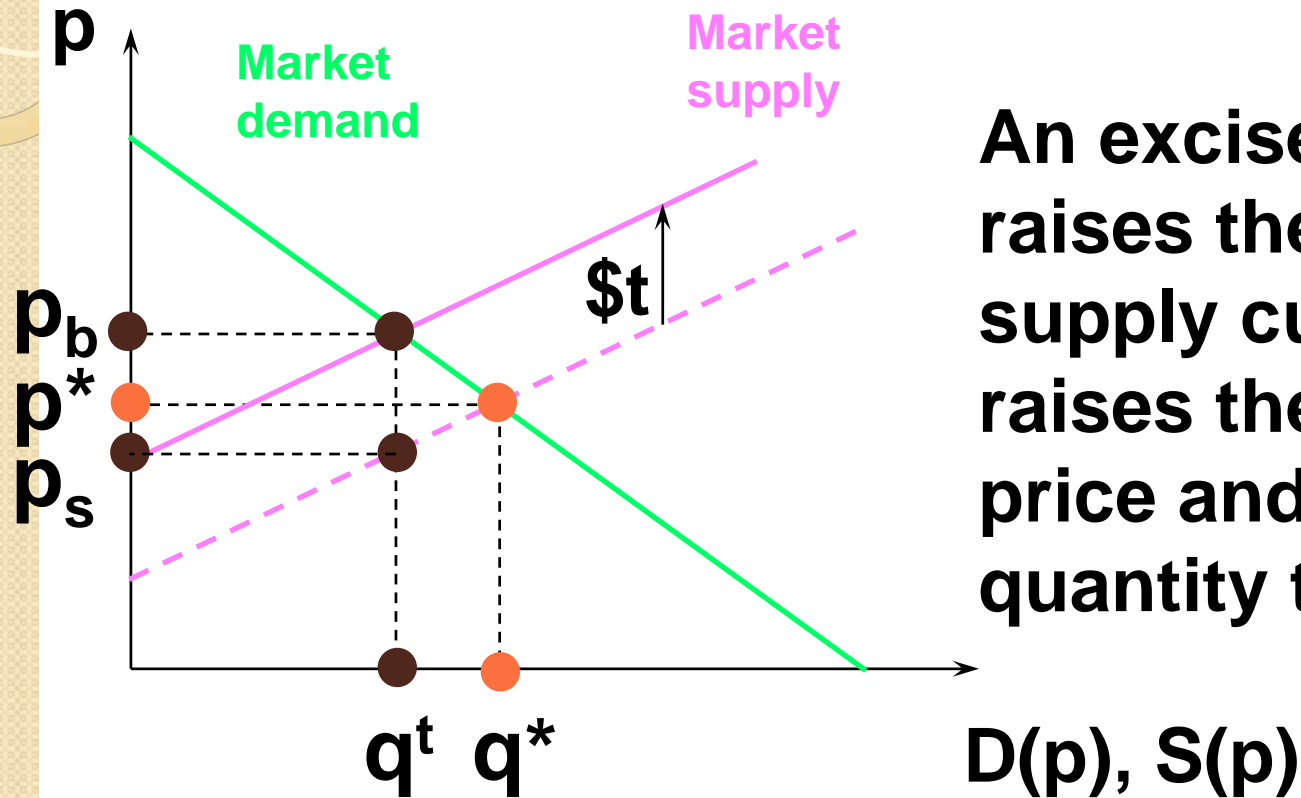
An excise tax raises the market supply curve by $\$t$

Quantity Taxes & Market Equilibrium



An excise tax raises the market supply curve by $\$t$, raises the buyers' price and lowers the quantity traded.

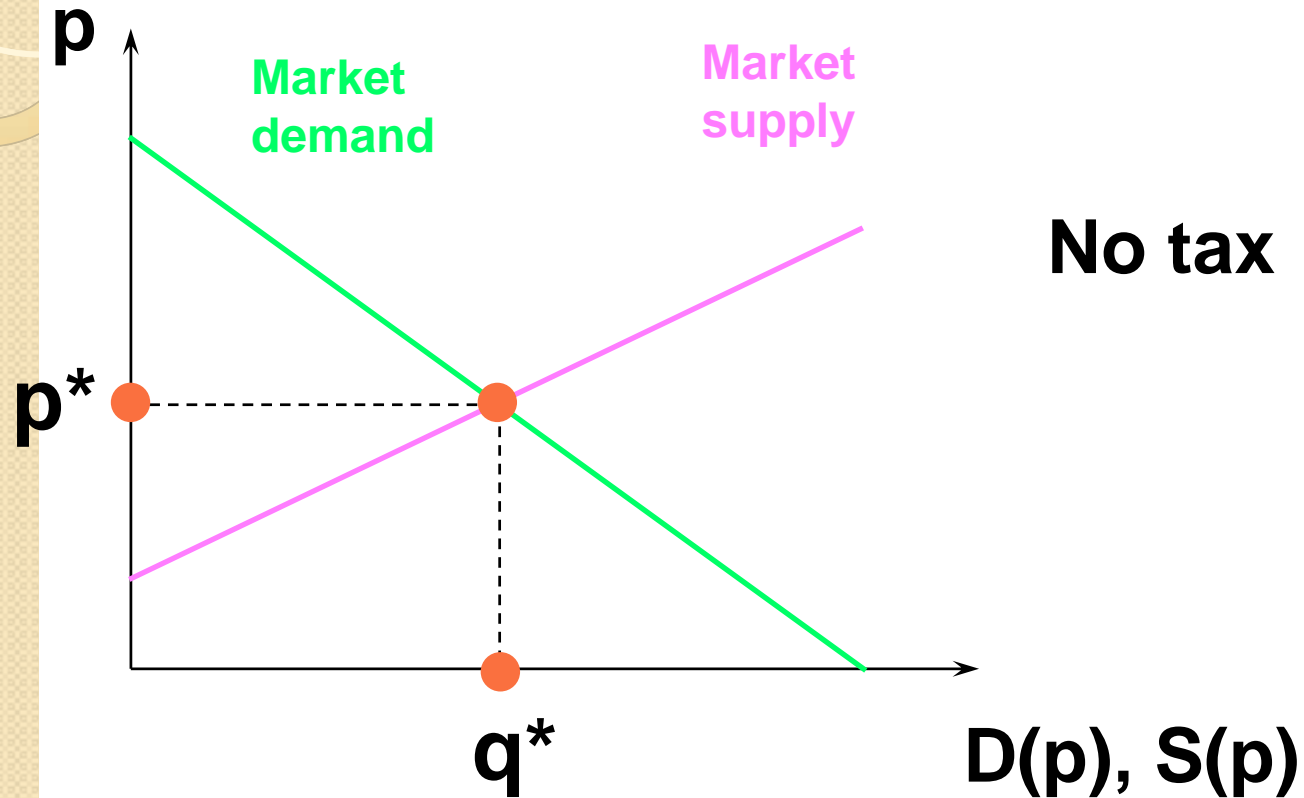
Quantity Taxes & Market Equilibrium



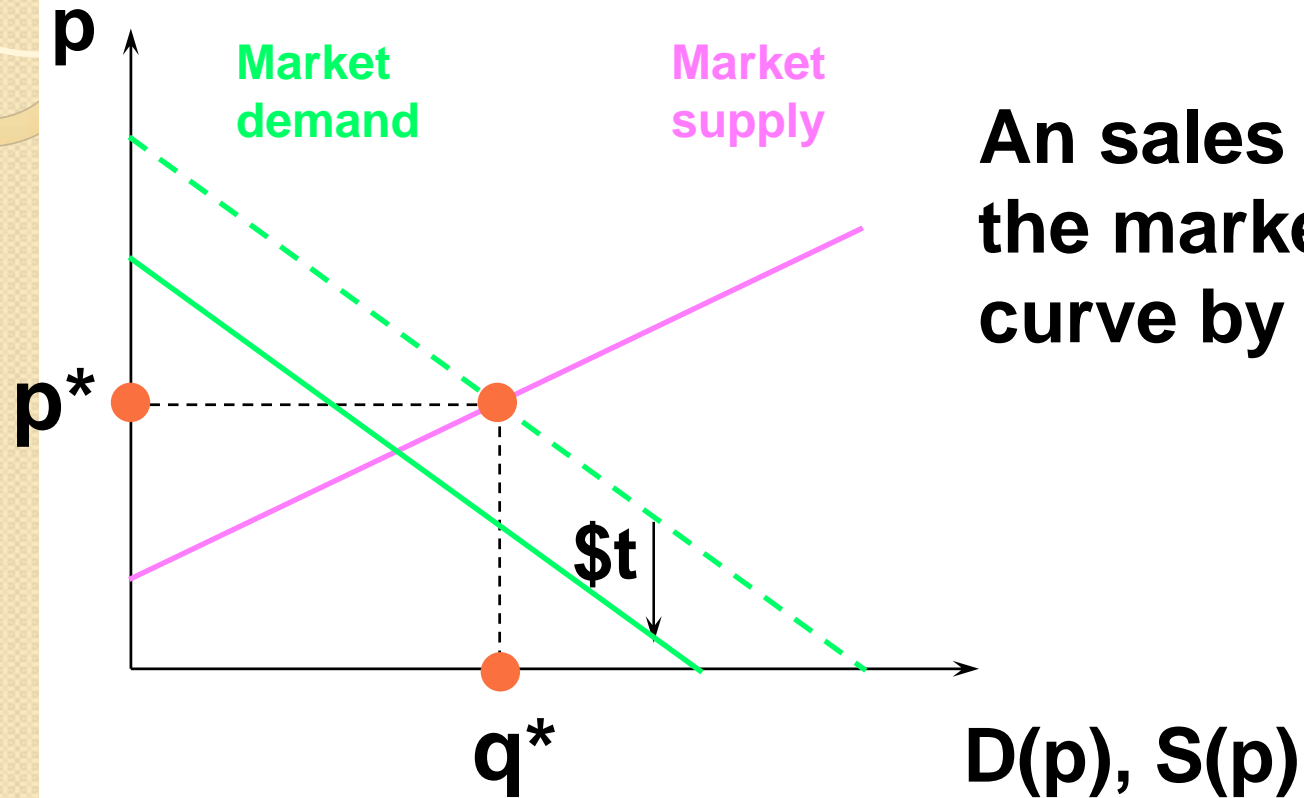
An excise tax raises the market supply curve by $\$t$, raises the buyers' price and lowers the quantity traded.

And sellers receive only $p_s = p_b - t$.

Quantity Taxes & Market Equilibrium

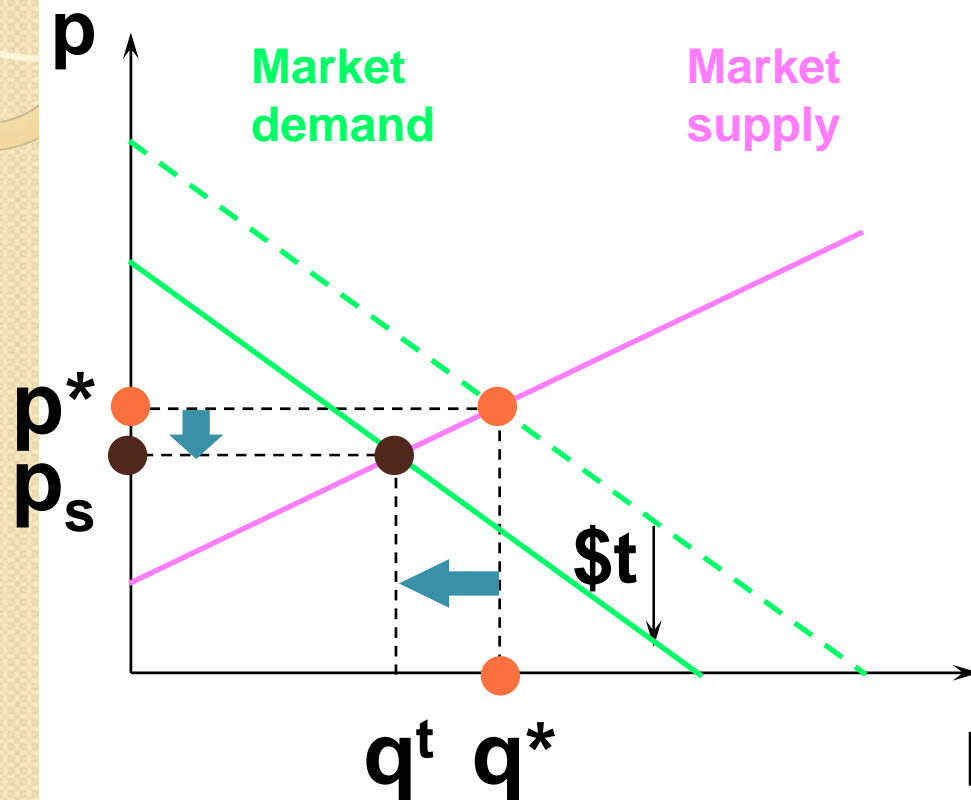


Quantity Taxes & Market Equilibrium



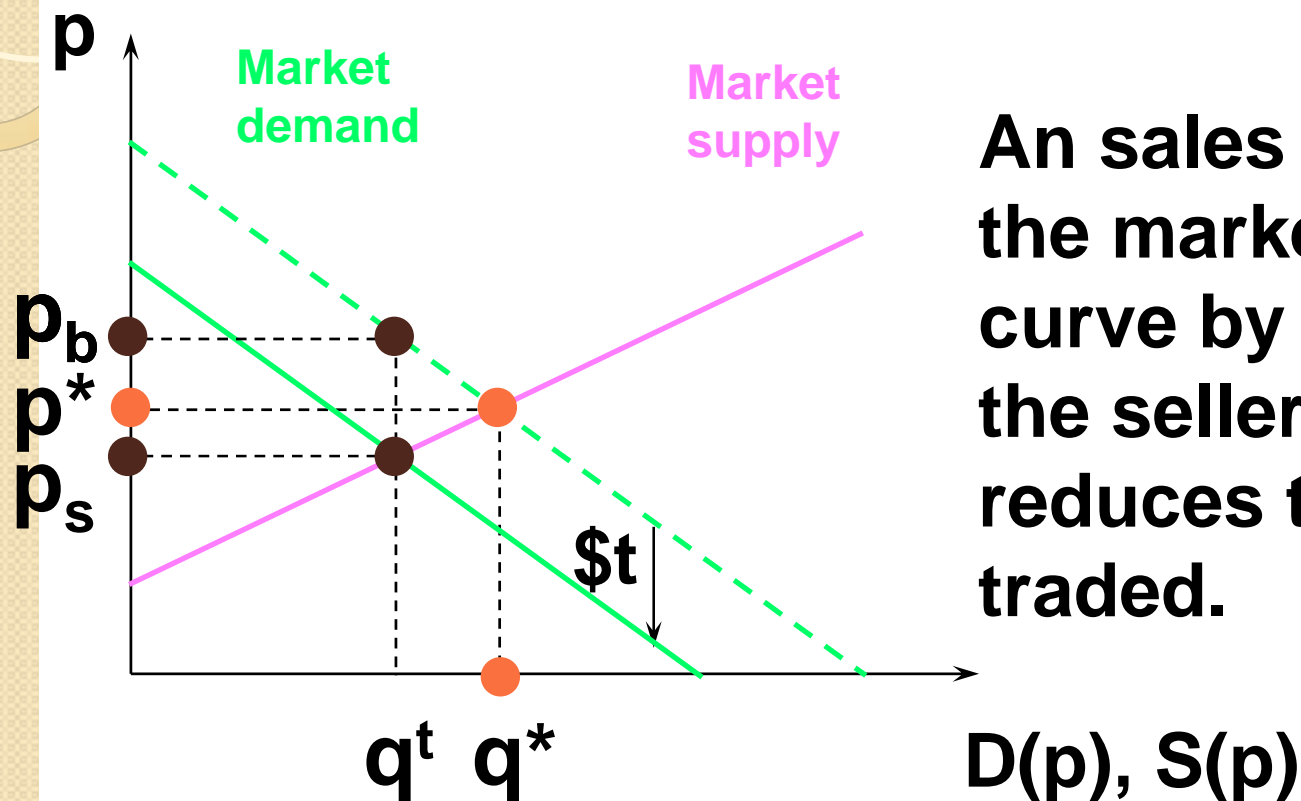
An sales tax lowers the market demand curve by $\$t$

Quantity Taxes & Market Equilibrium



An sales tax lowers the market demand curve by $\$t$, lowers the sellers' price and reduces the quantity traded.

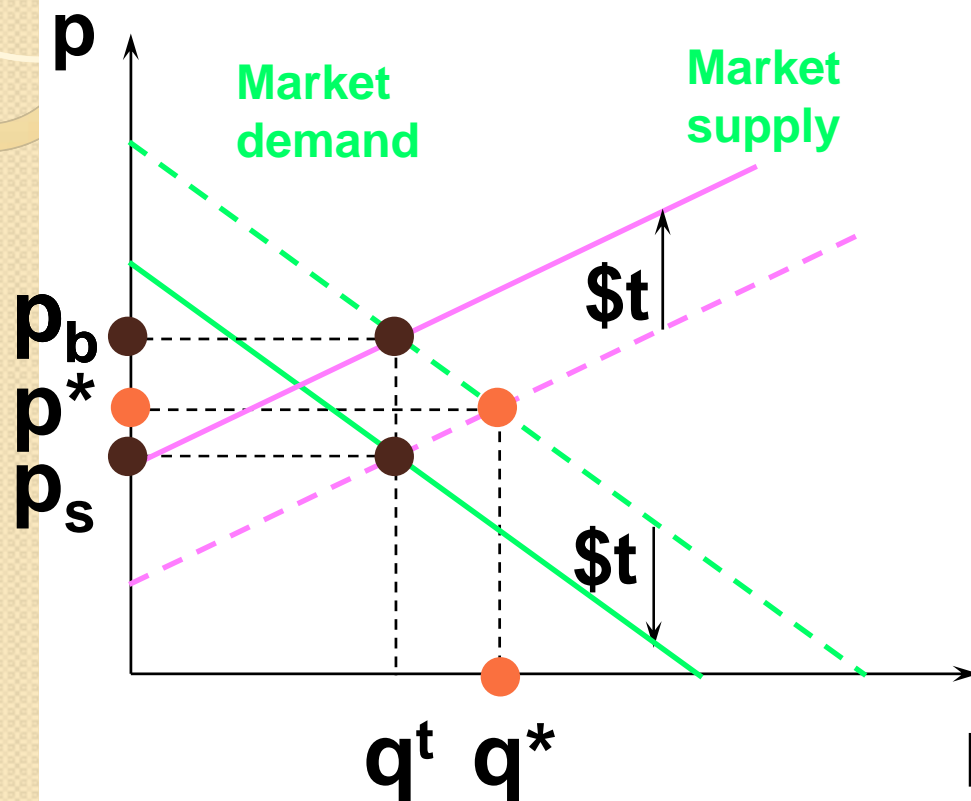
Quantity Taxes & Market Equilibrium



An sales tax lowers the market demand curve by $\$t$, lowers the sellers' price and reduces the quantity traded.

And buyers pay $p_b = p_s + t$.

Quantity Taxes & Market Equilibrium



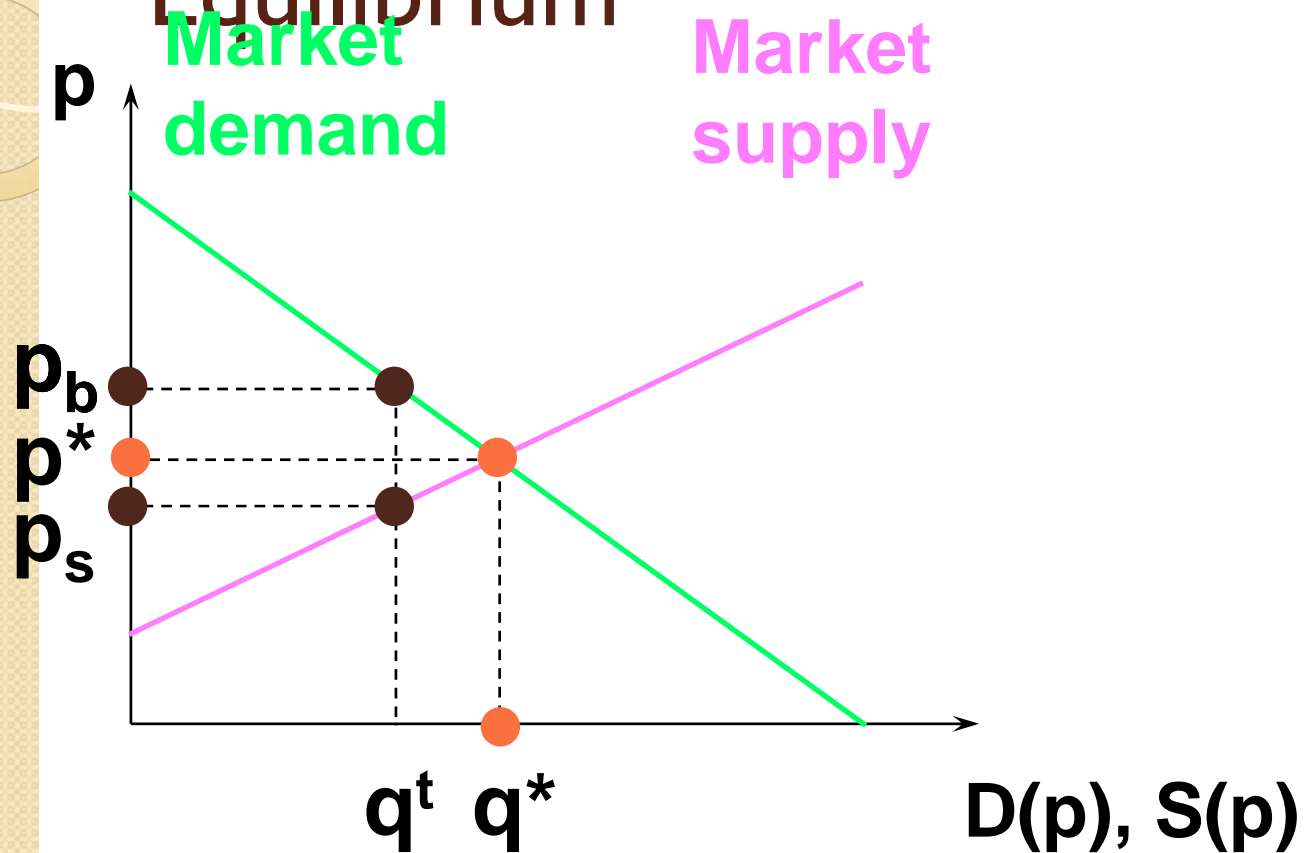
A sales tax levied at rate t has the same effects on the market's equilibrium as does an excise tax levied at rate t .



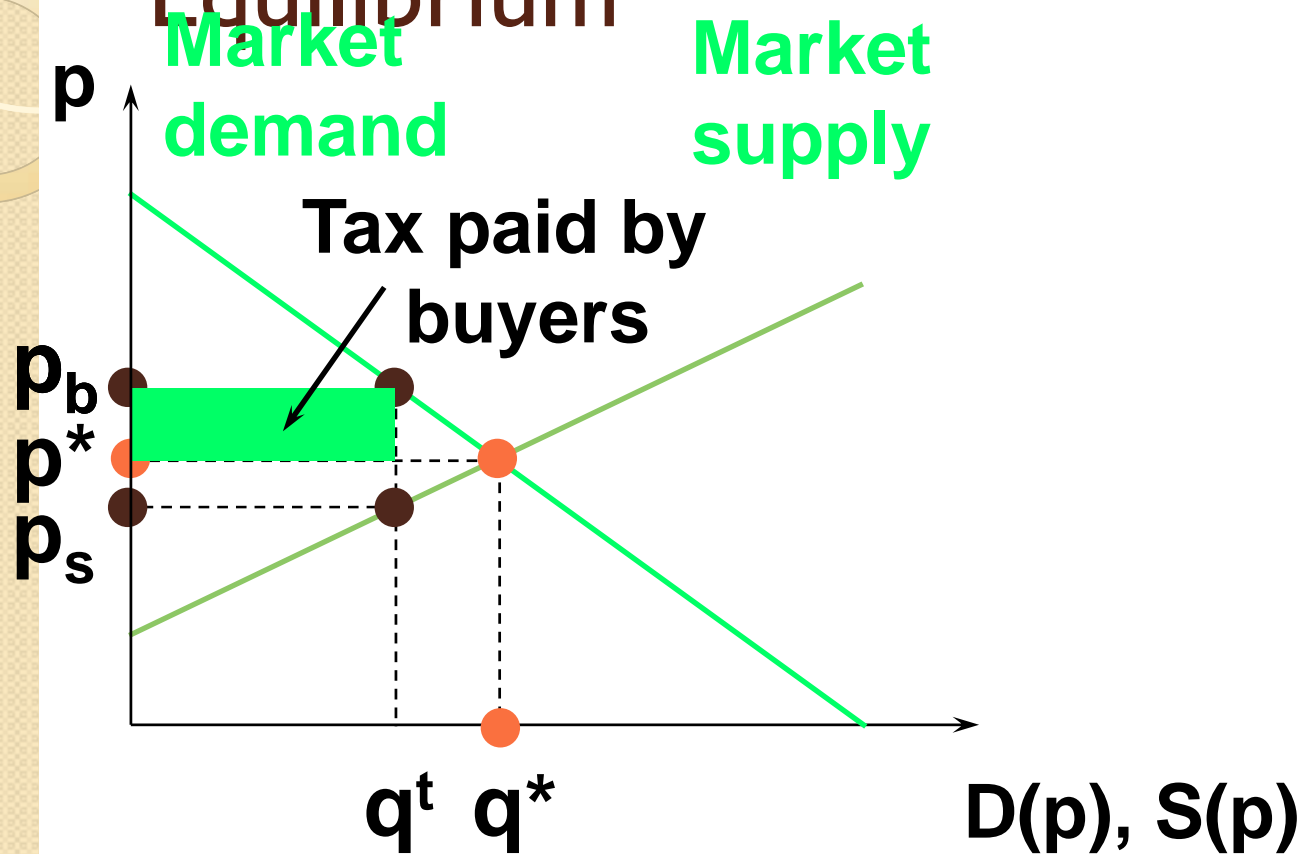
Quantity Taxes & Market Equilibrium

- Who pays the tax of $\$t$ per unit traded?
- The division of the $\$t$ between buyers and sellers is the **incidence** of the tax
- The incidence of a quantity tax depends upon the own-price elasticities of demand and supply

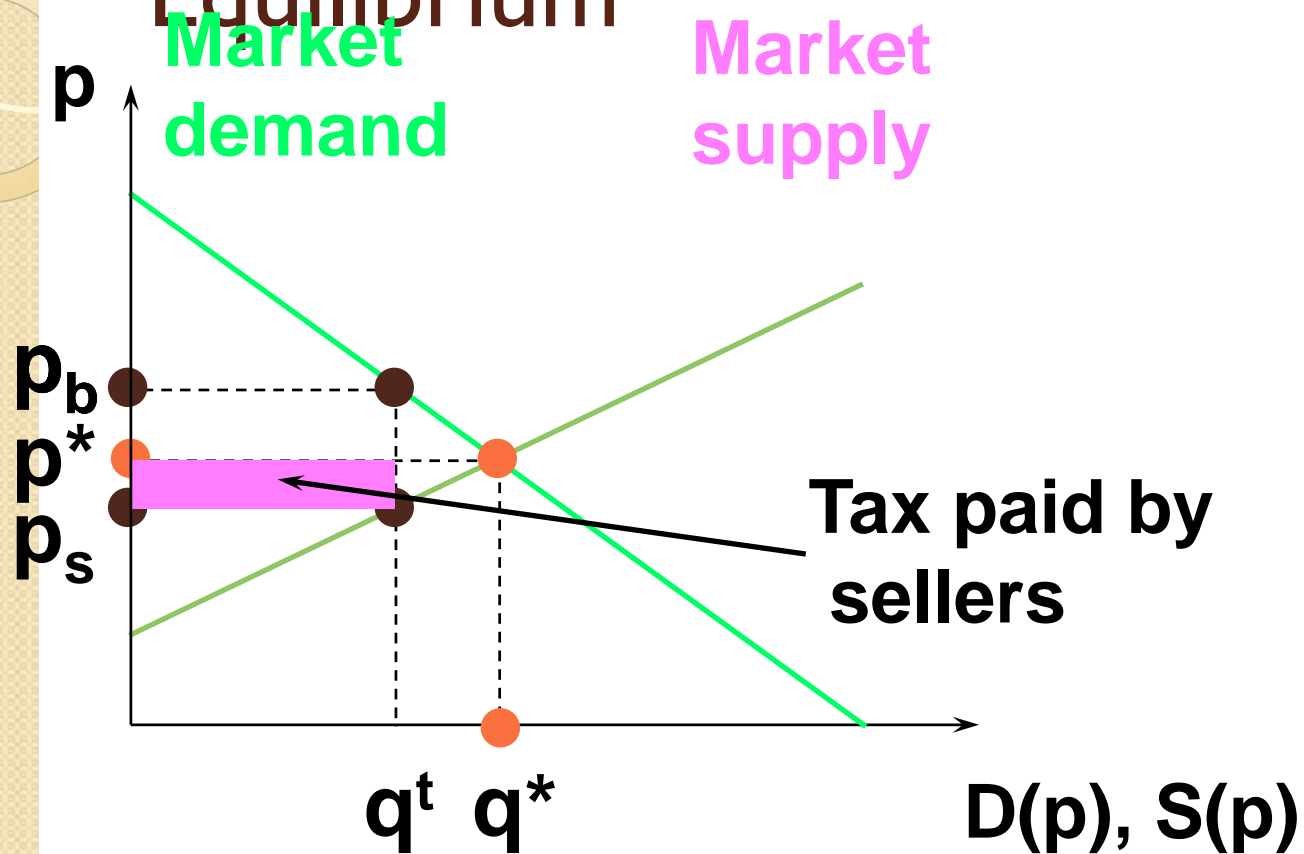
Quantity Taxes & Market Equilibrium



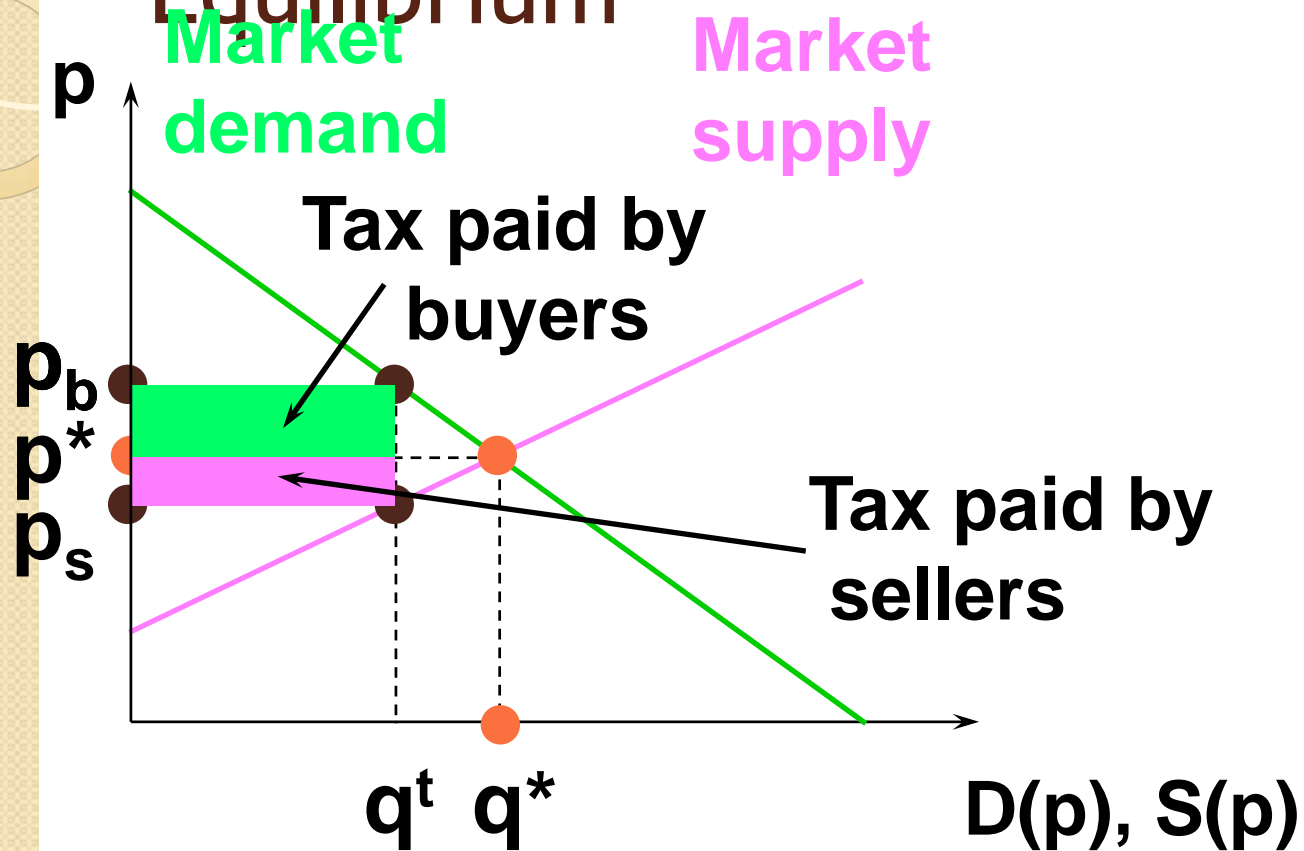
Quantity Taxes & Market Equilibrium



Quantity Taxes & Market Equilibrium



Quantity Taxes & Market Equilibrium

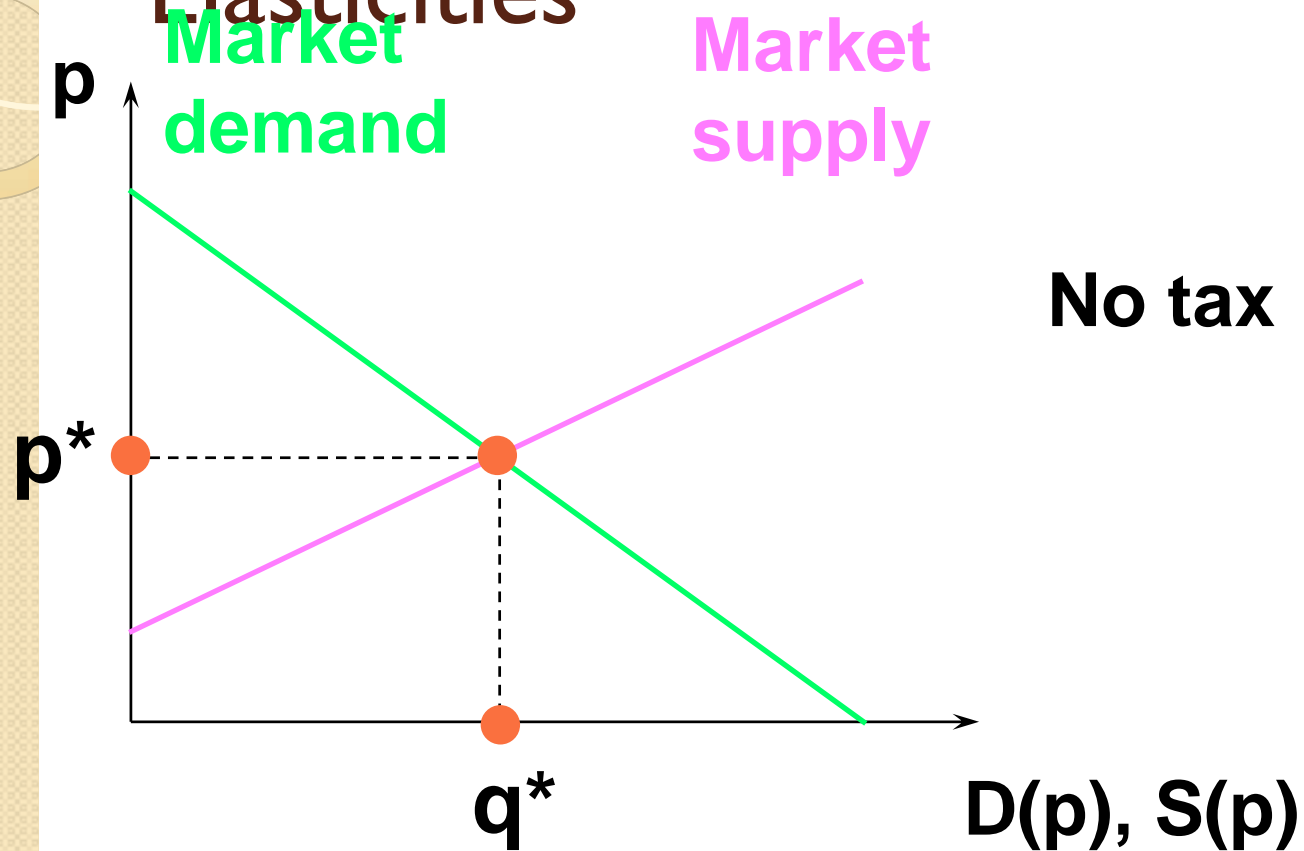




Deadweight Loss and Own-Price Elasticities

- A quantity tax imposed on a competitive market reduces the quantity traded and so reduces gains-to-trade (*i.e.* the sum of Consumers' and Producers' Surpluses).
- The lost total surplus is the tax's deadweight loss, or excess burden.

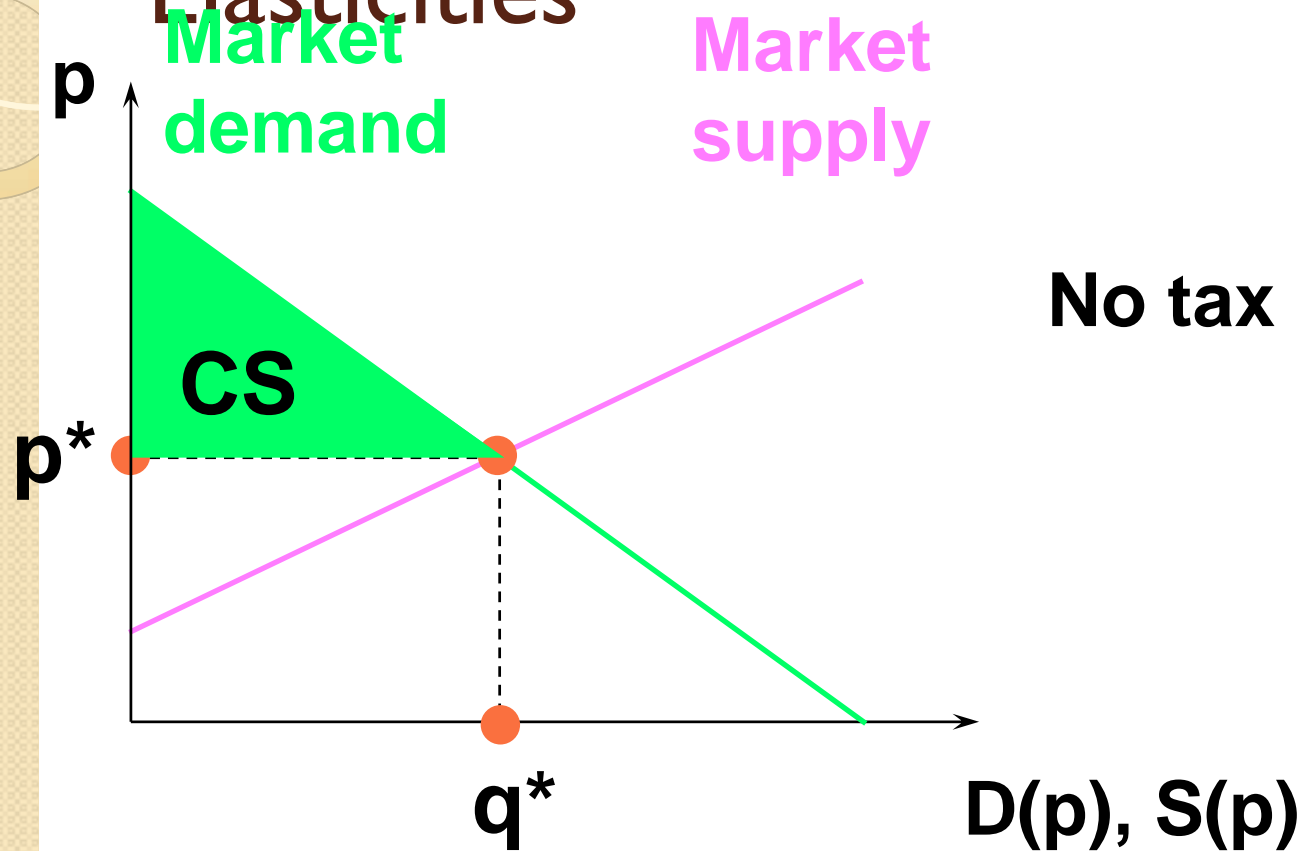
Deadweight Loss and Own-Price Elasticities



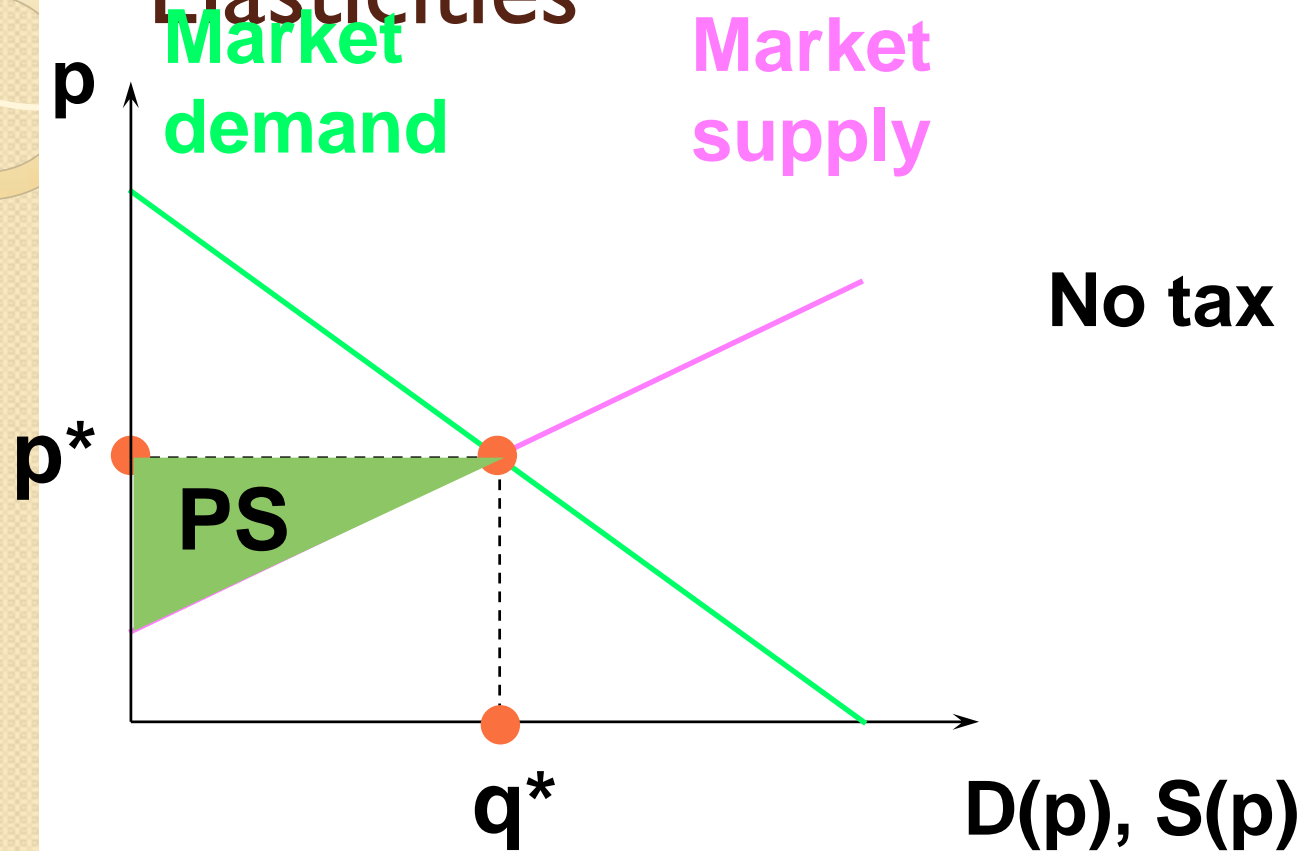
Pareto Efficiency

- At the market equilibrium q^* we have a Pareto efficient outcome: at q^* , the willingness to pay for an extra unit is just equal to the willingness to supply an extra unit at that price
- Q^* maximizes the social welfare (CS+PS)

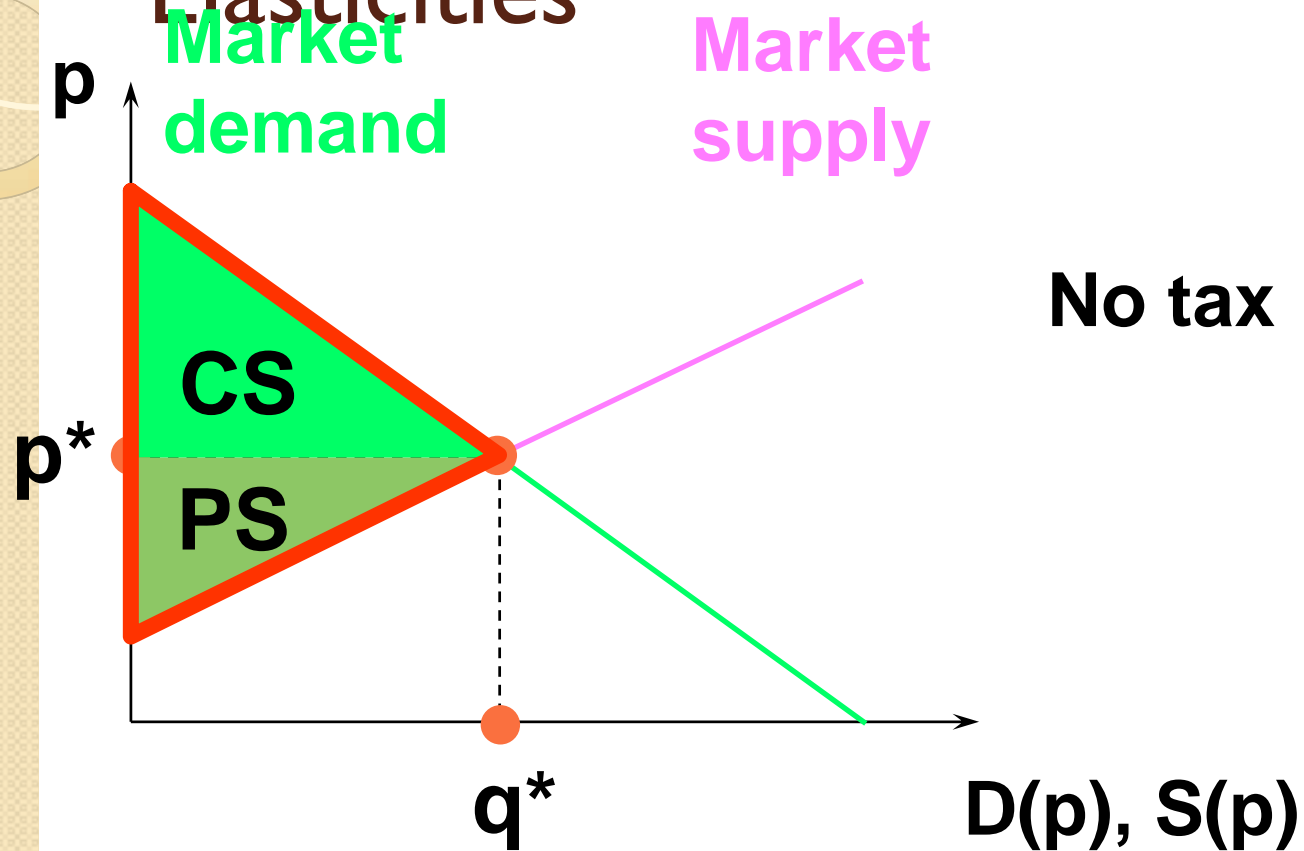
Deadweight Loss and Own-Price Elasticities



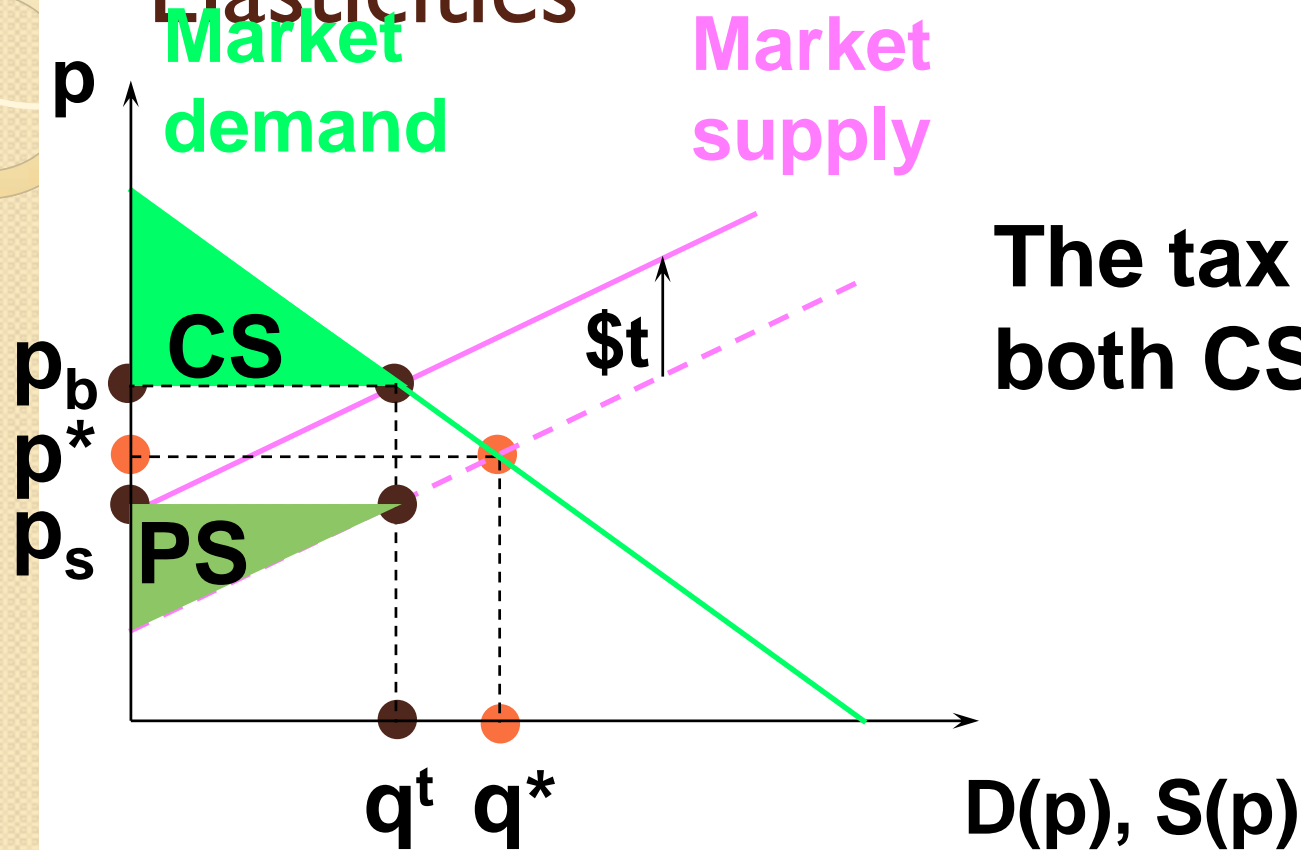
Deadweight Loss and Own-Price Elasticities



Deadweight Loss and Own-Price Elasticities

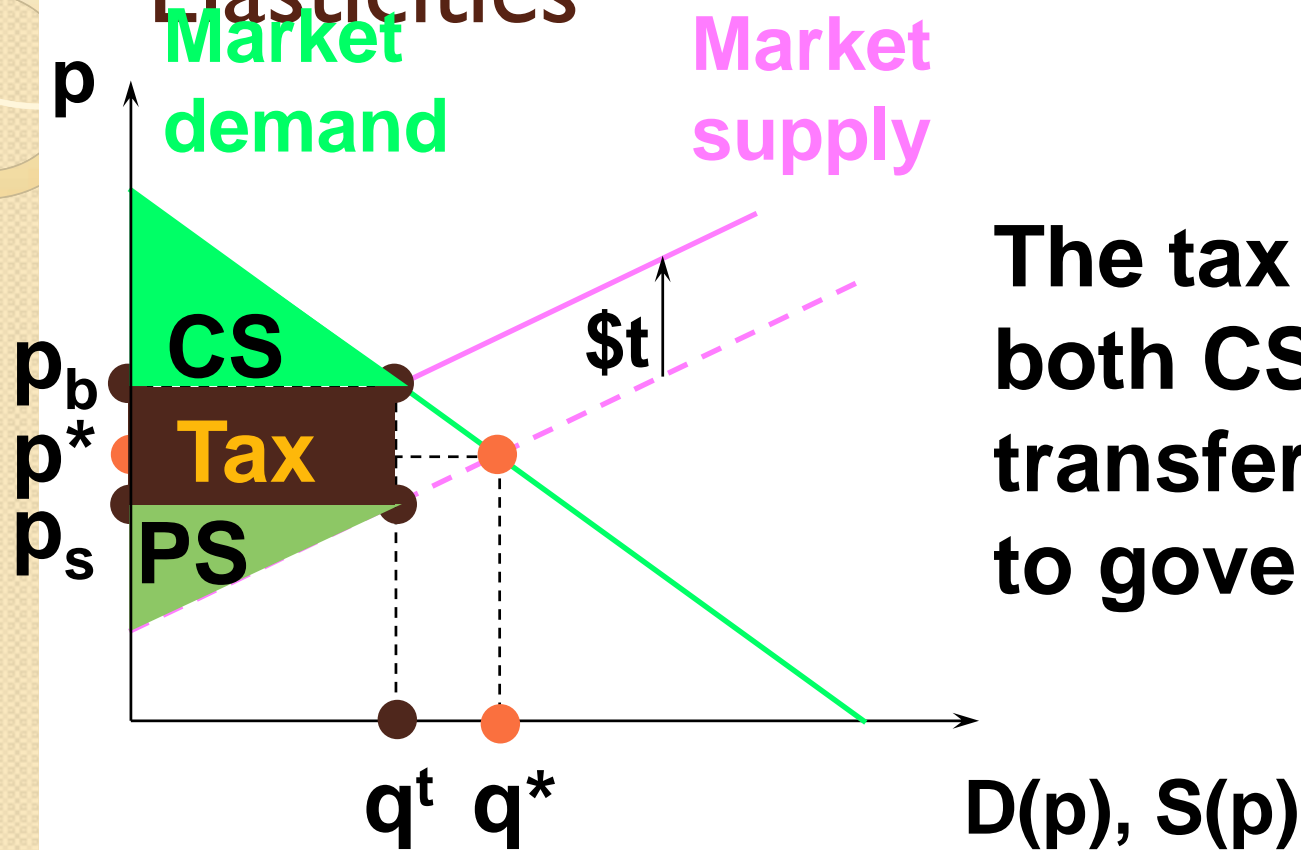


Deadweight Loss and Own-Price Elasticities



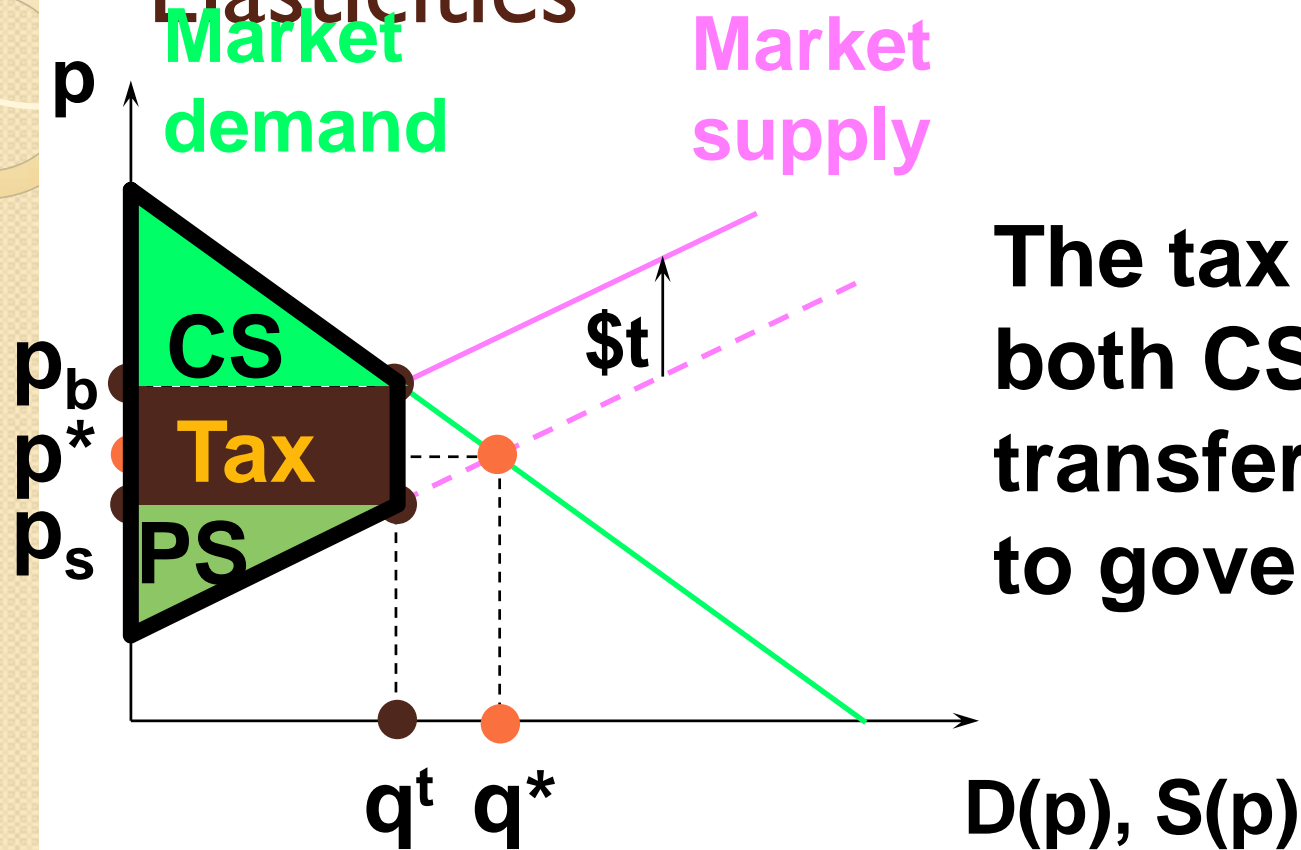
The tax reduces both CS and PS

Deadweight Loss and Own-Price Elasticities



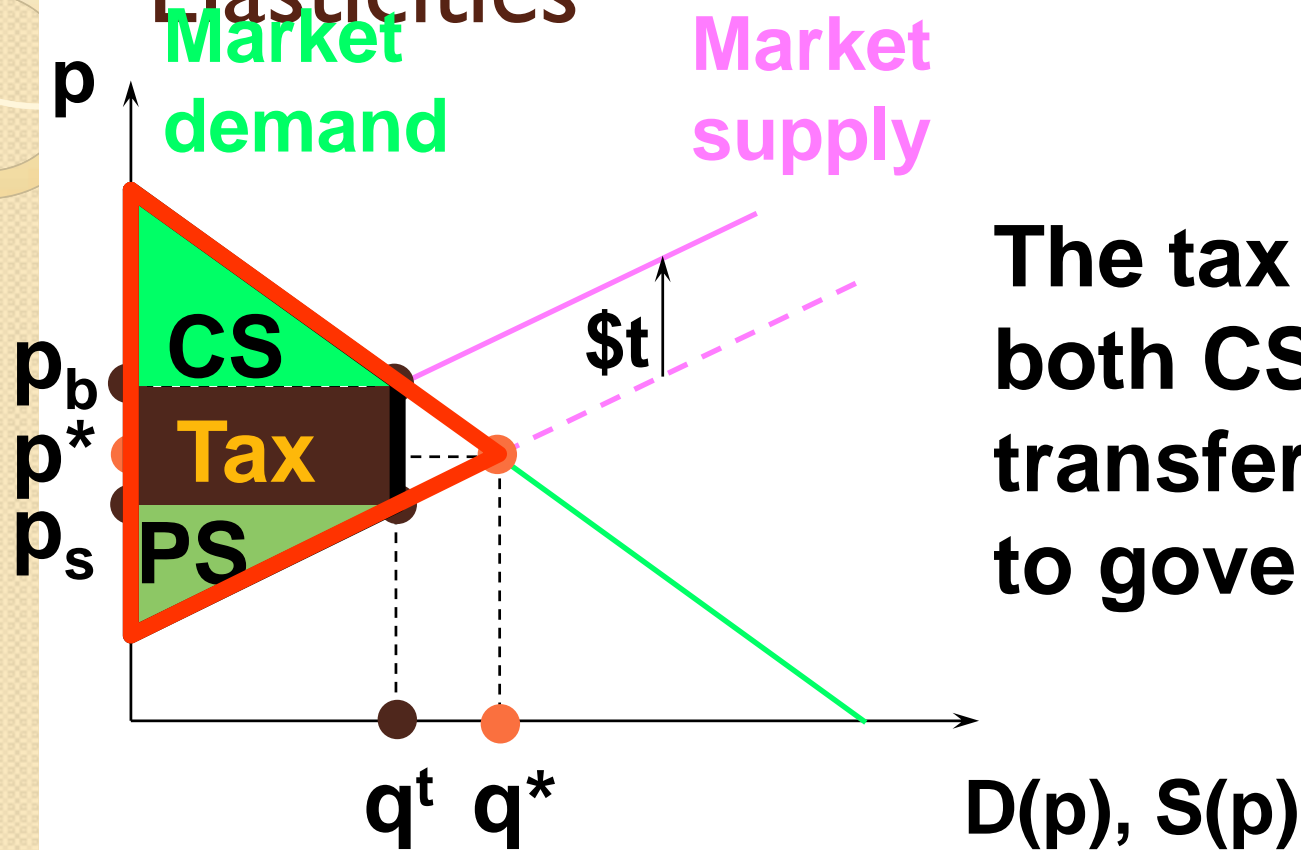
The tax reduces both CS and PS, transfers surplus to government

Deadweight Loss and Own-Price Elasticities



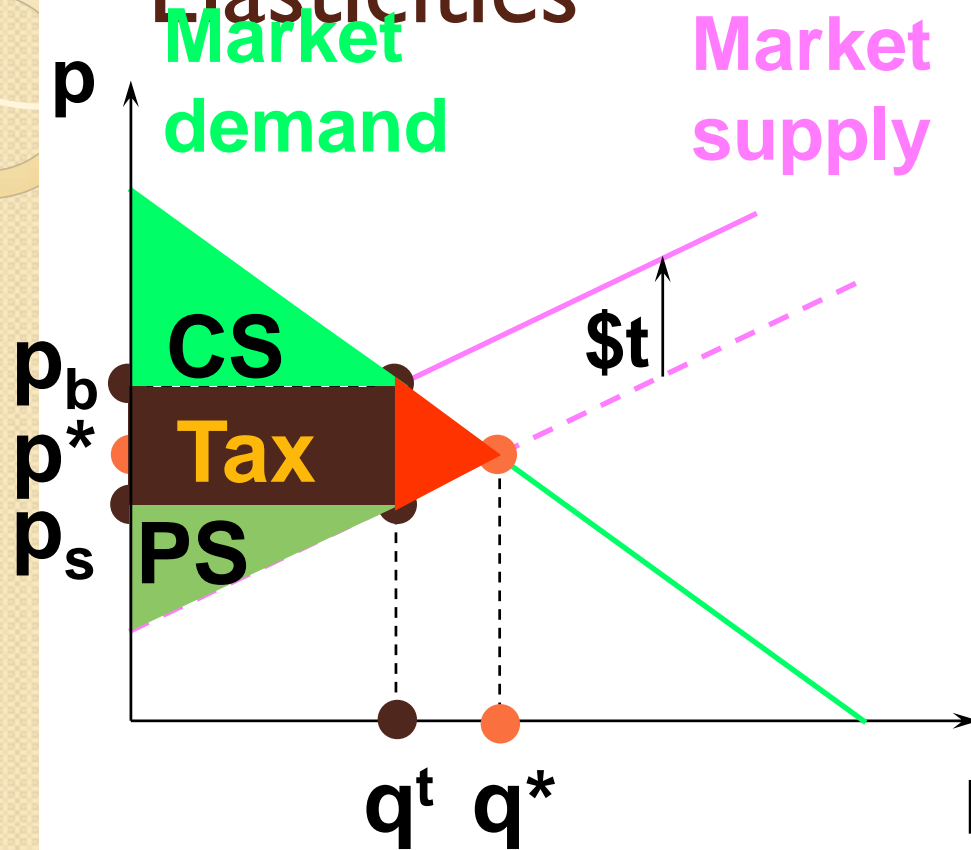
The tax reduces both CS and PS, transfers surplus to government

Deadweight Loss and Own-Price Elasticities



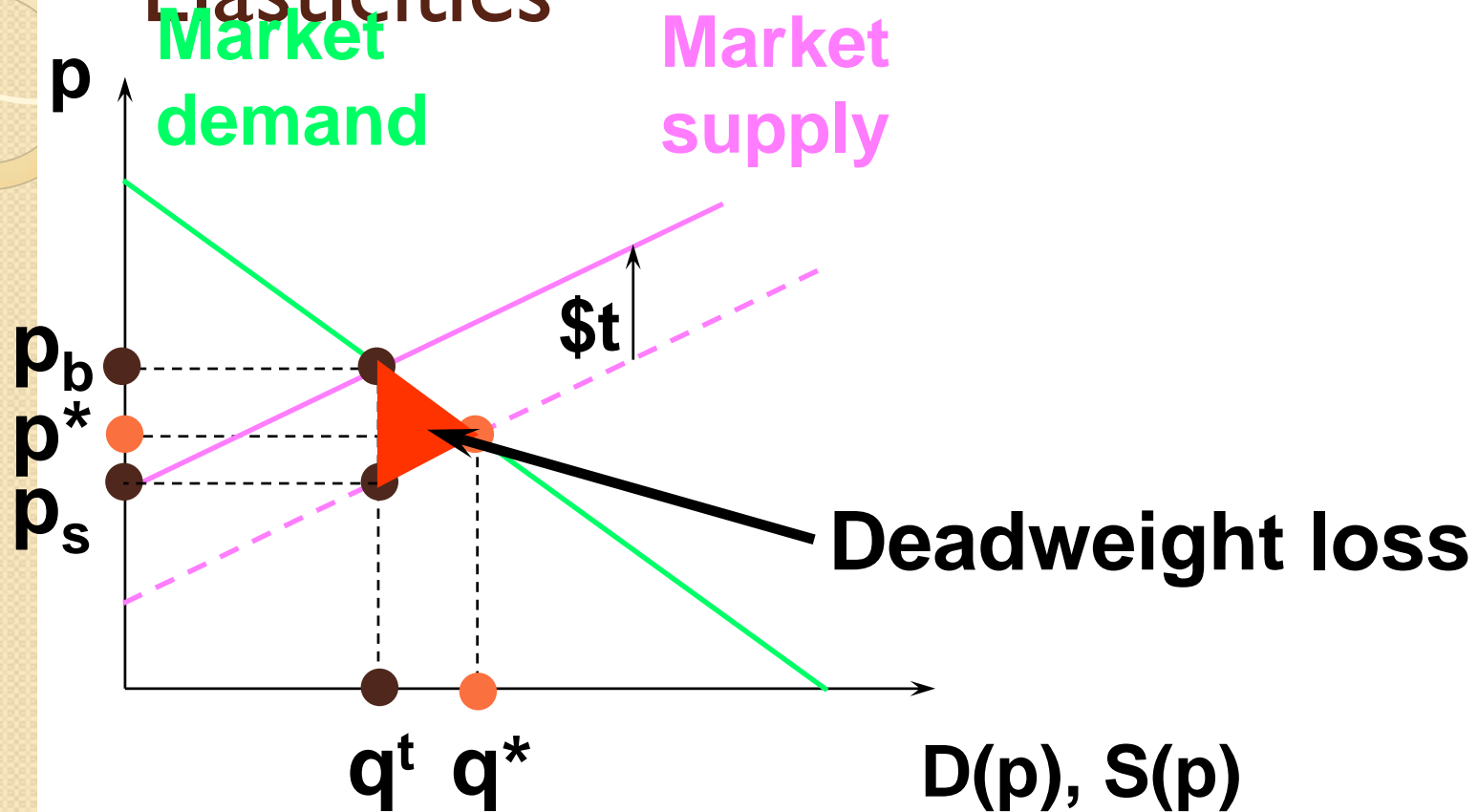
The tax reduces both CS and PS, transfers surplus to government

Deadweight Loss and Own-Price Elasticities

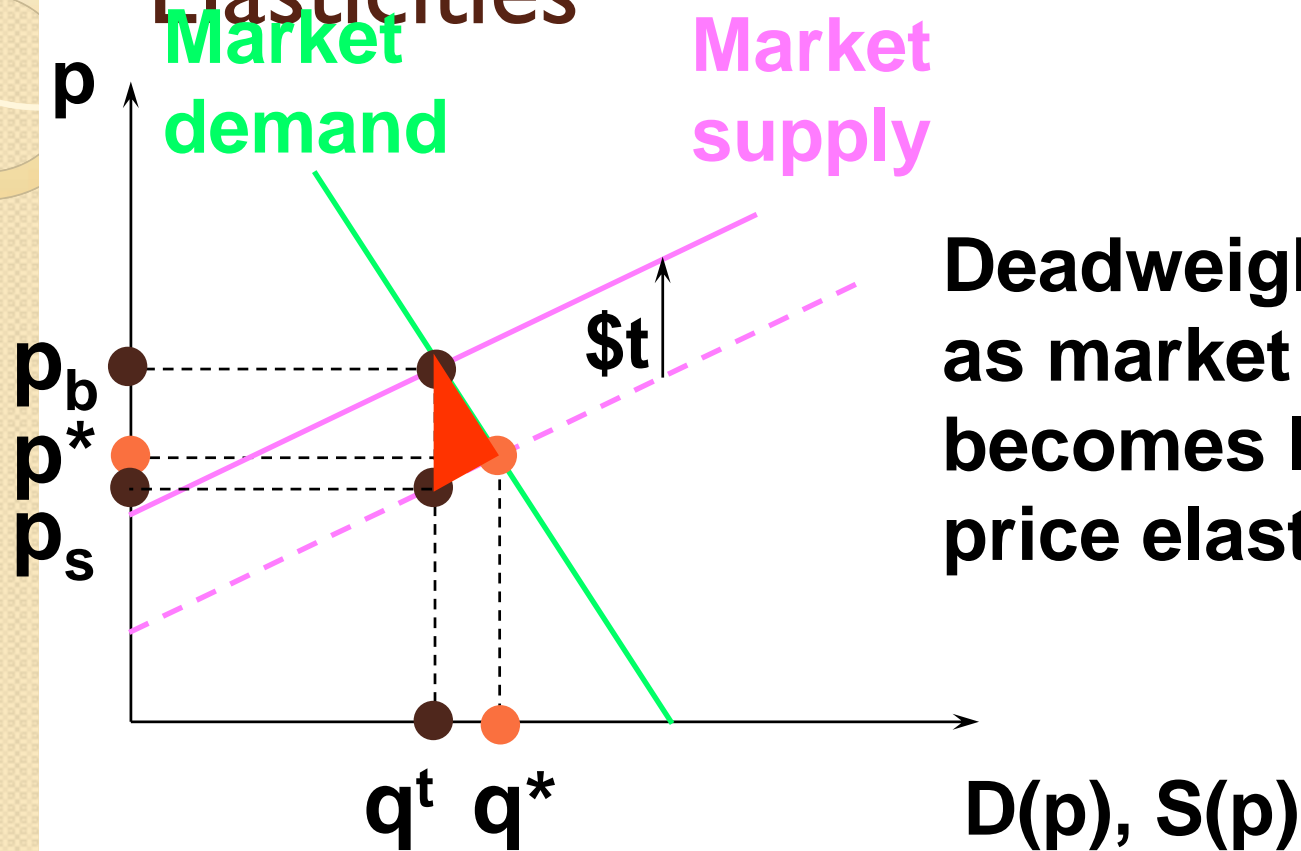


The tax reduces both CS and PS, transfers surplus to government, and lowers total surplus.

Deadweight Loss and Own-Price Elasticities

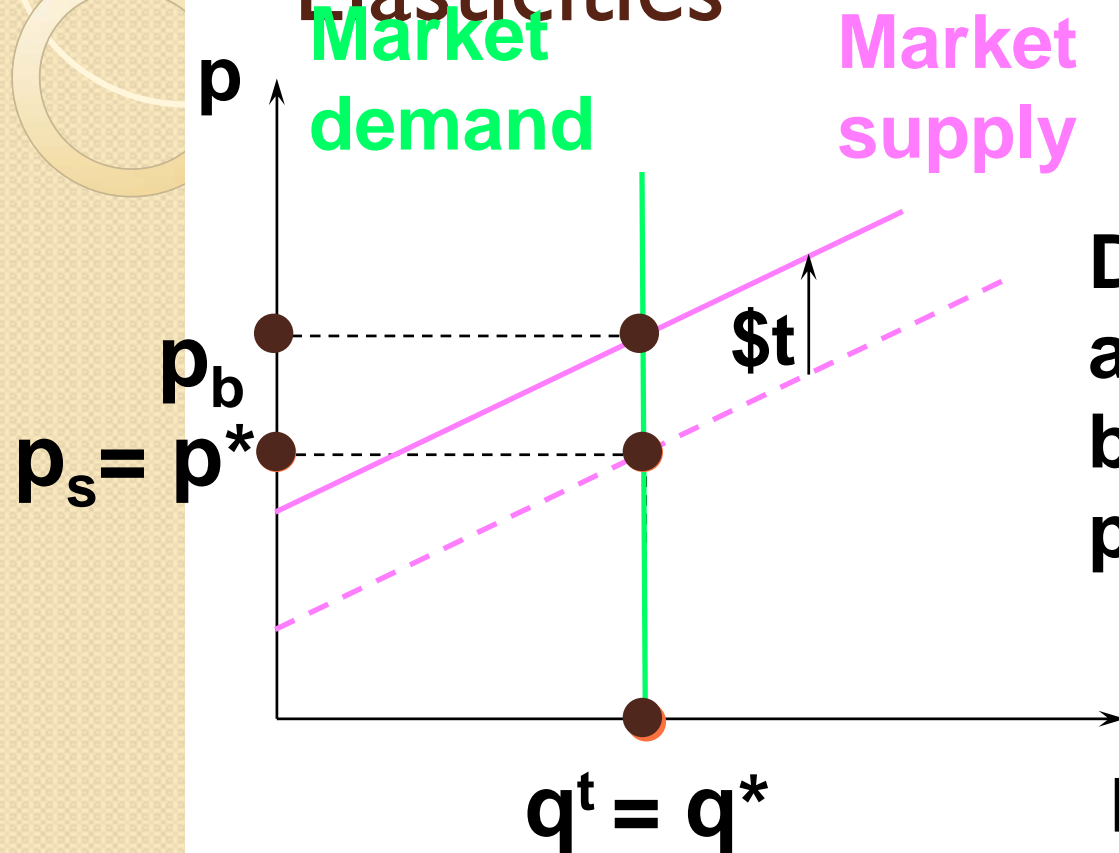


Deadweight Loss and Own-Price Elasticities



Deadweight loss falls as market demand becomes less own-price elastic.

Deadweight Loss and Own-Price Elasticities



Deadweight loss falls as market demand becomes less own-price elastic.

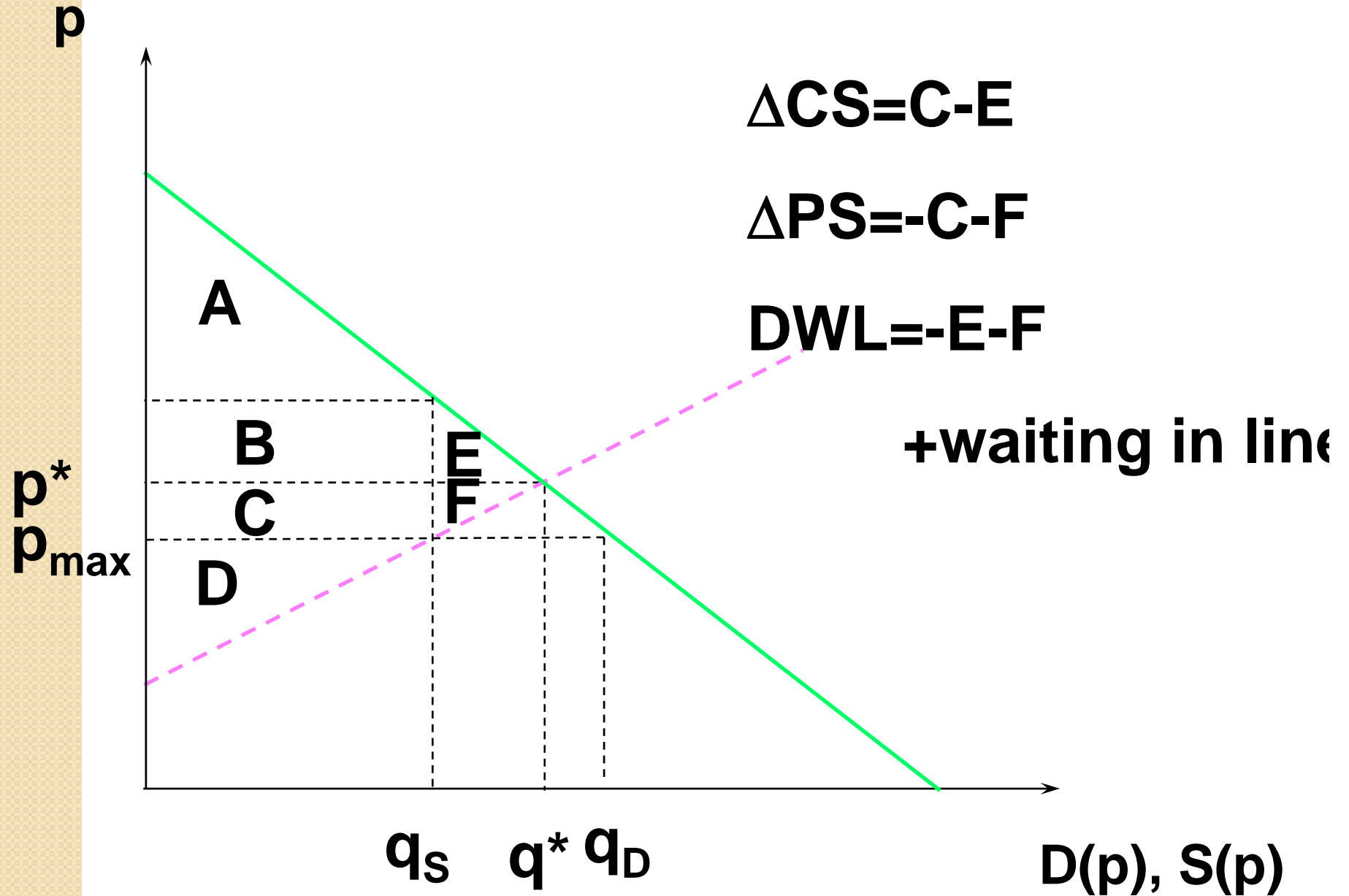
When $\varepsilon_D = 0$, the tax causes no deadweight loss.



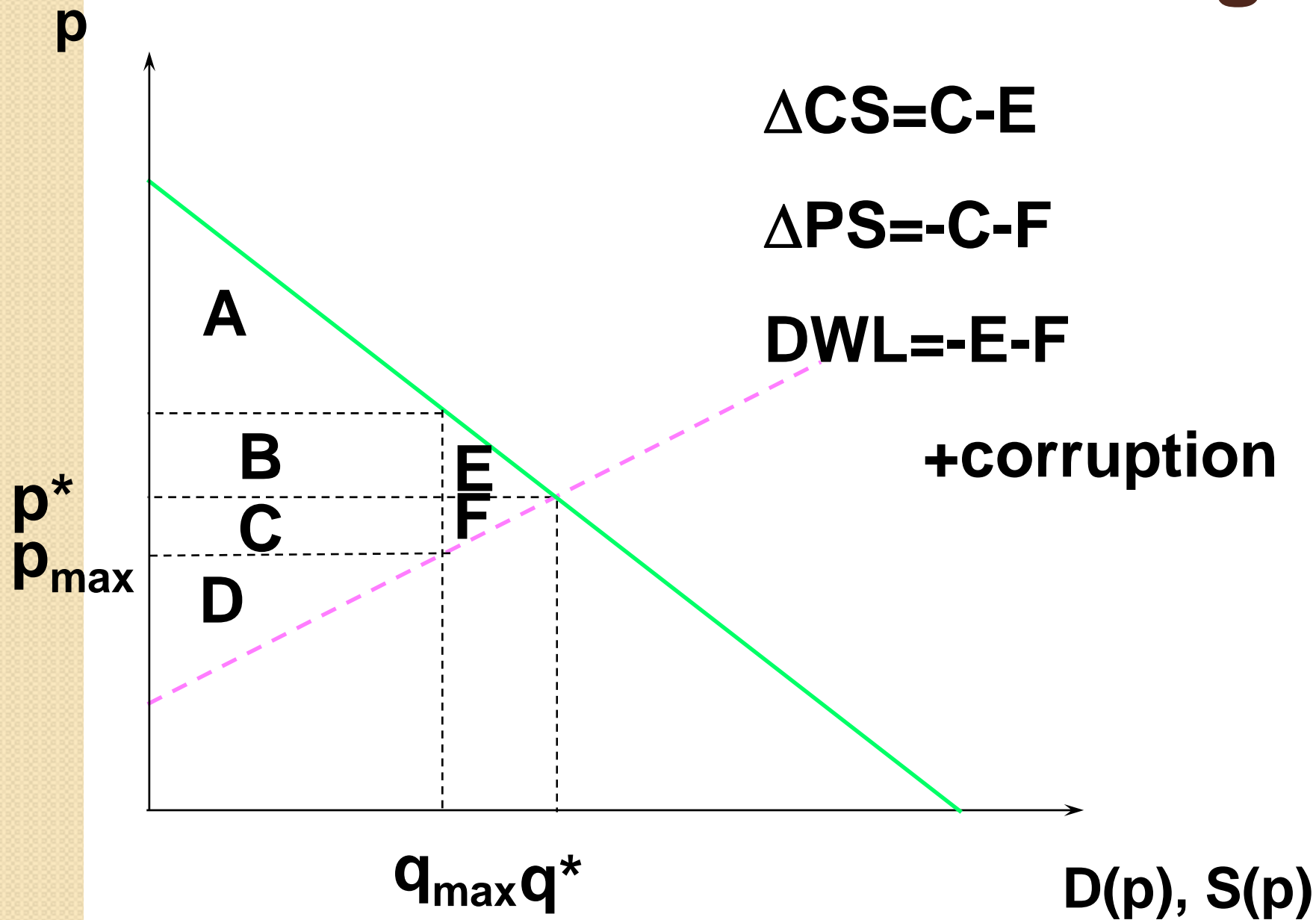
Deadweight Loss and Own-Price Elasticities

- Deadweight loss due to a quantity tax rises as either market demand or market supply becomes more own-price elastic.
- If either $\varepsilon_D = 0$ or $\varepsilon_S = 0$ then the deadweight loss is zero.

Price control



Price control with rationing



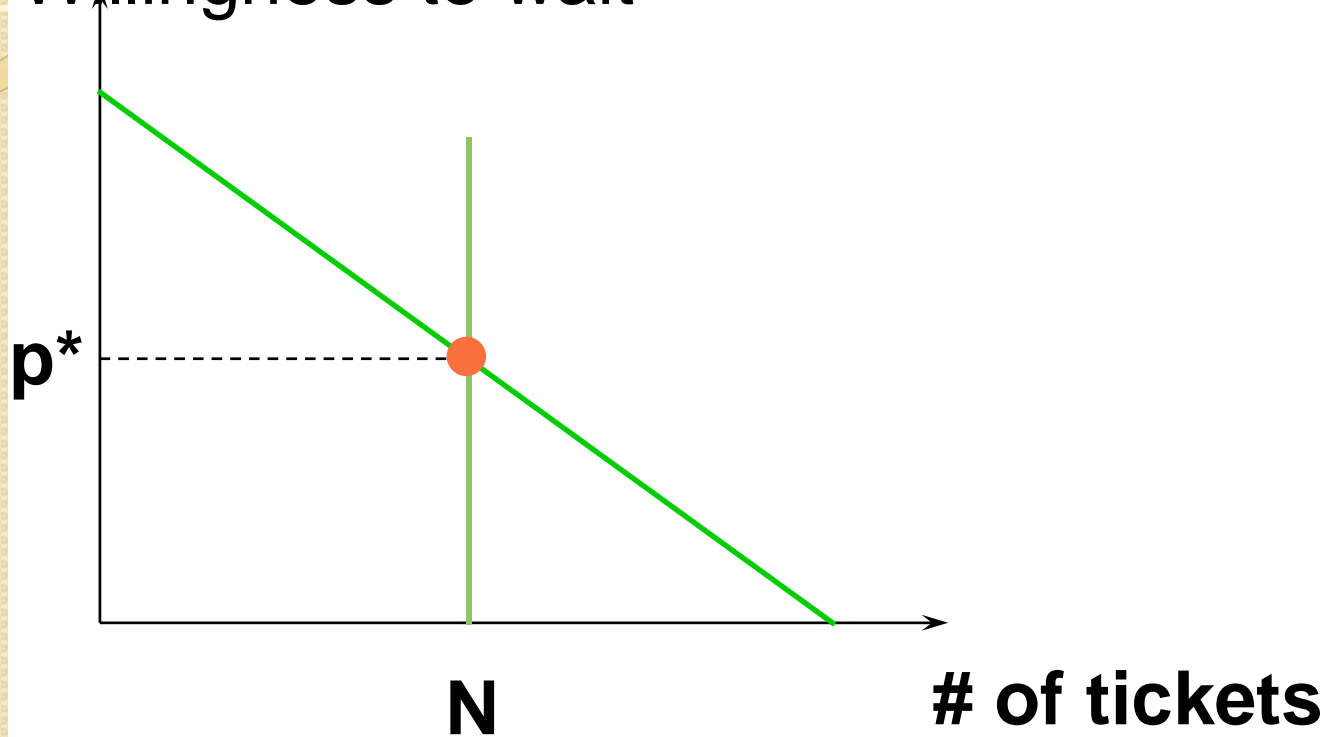


Application: Waiting in Line

- Waiting in line is an alternative (non-market) way of allocating scarce resources
- Is it efficient compared to market mechanism?
- Suppose there is a championship basketball game and tickets are free but limited
- The tickets will be distributed according to the principle of “first-come-first served”
- Willingness to pay vs. willingness to wait

Waiting in Line

Willingness to wait





Why is it so different?

- Waiting time is a private cost and provides no benefits to suppliers
- Waiting time is a pure deadweight loss
- Allocation by waiting time will leave room for ***gain from trade***
- Market price measures both private cost and social benefit
- Market mechanism assures that scarce resources are allocated to most-productive uses