## IO Problem Set 1 (BLP)

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## Problem 1

## Estimate the Model using OLS, with price and promotion as characteristics

#1.1: Estimate using OLS with price and promotion as product characteristics.
res\_log1 = smf.ols('Y ~ prices + prom\_', data=otc\_dataDf).fit()

Dep. Variable:	Y	R-squared:	0.158
Model:	OLS	Adj. R-squared:	0.158
Method:	Least Squares	F-statistic:	3610.
Date:	Thu, 04 Nov 2021	Prob (F-statistic):	0.00
Time:	05:19:39	Log-Likelihood:	-56307.
No. Observations:	38544	AIC:	$1.126\mathrm{e}{+05}$
Df Residuals:	38541	BIC:	$1.126\mathrm{e}{+05}$
Df Model:	2		
Covariance Type:	nonrobust		

	$\mathbf{coef}$	$\operatorname{std}$ err	$\mathbf{t}$	$\mathbf{P} >  \mathbf{t} $	[0.025]	0.975]
Intercept	-7.6267	0.014	-532.839	0.000	-7.655	-7.599
$\mathbf{prices}$	-0.2496	0.003	-84.768	0.000	-0.255	-0.244
$\mathbf{prom}_{-}$	-0.0311	0.019	-1.653	0.098	-0.068	0.006
Omnibus	s:	1648.591	1 Durbin-Watson: 0.434		0.434	
Prob(On	nnibus):	0.000	Jarque	-Bera (J	<b>B):</b> 14	461.418
Skew:		-0.415	$\operatorname{Prob}(\operatorname{J}$	B):		0.00
Kurtosis	:	2.529	Cond.	No.		17.7

### Notes:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

<sup>\*</sup>I worked on this problem set with Luna Shen, David Kerns, and Benedikt Graf

# Estimate the Model using OLS, with price and promotion as characteristics, and brand dummies

#1.2: Estimate using OLS with price and promotion as product characteristics and brand dummies.  $res\_log2 = smf.ols('Y \sim prices + prom\_ + C(brand)', data=otc\_dataDf).fit()$ 

Model:         OLS         Adj. R-squared:         0.654           Method:         Least Squares         F-statistic:         6081.           Date:         Thu, 04 Nov 2021         Prob (F-statistic):         0.00           Time:         05:20:51         Log-Likelihood:         -39138.           No. Observations:         38544         AIC:         7.830e+04           Df Residuals:         38531         BIC:         7.841e+04           Df Model:         12         Covariance Type:         12         P>  t   [0.025]         0.975            Covariance Type:         std err         t         P>  t   [0.025]         0.975            Intercept         -6.0745         0.036         -167.065         0.000         -6.146         -6.003           C(brand)[T.2]         -0.0048         0.022         -0.218         0.828         -0.048         0.039           C(brand)[T.3]         -0.4578         0.040         -11.502         0.000         -0.463         -0.398           C(brand)[T.4]         -0.4303         0.017         -25.951         0.000         -0.463         -0.389           C(brand)[T.5]         -0.8868         0.024         -37.403         0.000         -1.687	Dep. Variable:		Y	$\mathbf{R} ext{-}\mathbf{sq}$	ıared:		0.654	
$ \begin{array}{ c c c c c c } \textbf{Date:} & \textbf{Thu}, 04 \ Nov \ 2021 & \textbf{Prob} \ (\textbf{F-statistic}): & 0.00 \\ \textbf{Time:} & 05:20:51 & \textbf{Log-Likelihood:} & -39138. \\ \textbf{No. Observations:} & 38544 & \textbf{AIC:} & 7.830e+04 \\ \textbf{Df Residuals:} & 38531 & \textbf{BIC:} & 7.841e+04 \\ \textbf{Df Model:} & 12 \\ \textbf{Covariance Type:} & & & & & & & & & & & & & & & & & & &$	Model:		OLS	$\mathbf{Adj.}$	R-square	$\operatorname{ed}$ :	0.654	
Time:       05:20:51       Log-Likelihood:       -39138.         No. Observations:       38544       AIC:       7.830e+04         Df Residuals:       12       7.841e+04         Df Model:       12       12         Covariance Type:       nonrobust       P>  t        [0.025]       0.975]         Intercept       -6.0745       0.036       -167.065       0.000       -6.146       -6.003         C(brand)[T.2]       -0.0048       0.022       -0.218       0.828       -0.048       0.039         C(brand)[T.3]       -0.4578       0.040       -11.502       0.000       -0.536       -0.380         C(brand)[T.4]       -0.4303       0.017       -25.951       0.000       -0.463       -0.398         C(brand)[T.5]       -0.8868       0.024       -37.403       0.000       -0.933       -0.840         C(brand)[T.6]       -1.3850       0.051       -27.408       0.000       -1.687       -1.618         C(brand)[T.7]       -1.6527       0.018       -94.139       0.000       -2.317       -2.254         C(brand)[T.9]       -1.9340       0.017       -111.950       0.000       -1.968       -1.900         C(brand)[T.10]       <	Method:	Lea	st Squares	F-sta	tistic:		6081.	
No. Observations:       38544       AIC:       7.830e+04         Df Residuals:       38531       BIC:       7.841e+04         Df Model:       12         Covariance Type:       t       P>  t        [0.025]       0.975]         Intercept       -6.0745       0.036       -167.065       0.000       -6.146       -6.003         C(brand)[T.2]       -0.0488       0.022       -0.218       0.828       -0.048       0.039         C(brand)[T.3]       -0.4578       0.040       -11.502       0.000       -0.536       -0.380         C(brand)[T.4]       -0.4303       0.017       -25.951       0.000       -0.463       -0.398         C(brand)[T.5]       -0.8868       0.024       -37.403       0.000       -0.933       -0.840         C(brand)[T.6]       -1.3850       0.051       -27.408       0.000       -1.687       -1.618         C(brand)[T.7]       -1.6527       0.018       -94.139       0.000       -1.687       -1.618         C(brand)[T.10]       -1.983       0.022       -87.306       0.000       -1.968       -1.900 <th colspa<="" th=""><th>Date:</th><th>Thu,</th><th>04 Nov 20</th><th>21 <b>Prob</b></th><th>(F-statis</th><th><math>\operatorname{stic}</math>):</th><th>0.00</th></th>	<th>Date:</th> <th>Thu,</th> <th>04 Nov 20</th> <th>21 <b>Prob</b></th> <th>(F-statis</th> <th><math>\operatorname{stic}</math>):</th> <th>0.00</th>	Date:	Thu,	04 Nov 20	21 <b>Prob</b>	(F-statis	$\operatorname{stic}$ ):	0.00
Df Residuals:         J8531         BIC:         7.841e+04           Df Model:         12         Intercept         Toef         std err         t         P>  t          [0.025         0.975]           Intercept         -6.0745         0.036         -167.065         0.000         -6.146         -6.003           C(brand)[T.2]         -0.0488         0.022         -0.218         0.828         -0.048         0.039           C(brand)[T.3]         -0.4578         0.040         -11.502         0.000         -0.536         -0.380           C(brand)[T.4]         -0.4303         0.017         -25.951         0.000         -0.463         -0.398           C(brand)[T.5]         -0.8868         0.024         -37.403         0.000         -0.463         -0.398           C(brand)[T.6]         -1.3850         0.051         -27.408         0.000         -1.484         -1.286           C(brand)[T.7]         -1.6527         0.018         -94.139         0.000         -1.687         -1.618           C(brand)[T.9]         -1.9340         0.017         -111.950         0.000         -1.968         -1.900	Time:	(	05:20:51	$\operatorname{Log-I}$	Likelihoo	$\mathbf{d}$ :	-39138.	
Df Model:         12           Covariance Type:         std err         t         P>  t          [0.025]         0.975]           Intercept         -6.0745         0.036         -167.065         0.000         -6.146         -6.003           C(brand)[T.2]         -0.0048         0.022         -0.218         0.828         -0.048         0.039           C(brand)[T.3]         -0.4578         0.040         -11.502         0.000         -0.536         -0.380           C(brand)[T.4]         -0.4303         0.017         -25.951         0.000         -0.463         -0.398           C(brand)[T.5]         -0.8868         0.024         -37.403         0.000         -0.933         -0.840           C(brand)[T.6]         -1.3850         0.051         -27.408         0.000         -1.484         -1.286           C(brand)[T.7]         -1.6527         0.018         -94.139         0.000         -1.687         -1.618           C(brand)[T.8]         -2.2856         0.016         -141.034         0.000         -2.317         -2.254           C(brand)[T.10]         -1.8983         0.022         -87.306         0.000         -1.941         -1.856           C(brand)[T.11]	No. Observations	:	38544	AIC:			$7.830e{+04}$	
Covariance Type:         std err         t         P>  t          [0.025]         0.975]           Intercept         -6.0745         0.036         -167.065         0.000         -6.146         -6.003           C(brand)[T.2]         -0.0048         0.022         -0.218         0.828         -0.048         0.039           C(brand)[T.3]         -0.4578         0.040         -11.502         0.000         -0.453         -0.380           C(brand)[T.4]         -0.4303         0.017         -25.951         0.000         -0.463         -0.398           C(brand)[T.5]         -0.8868         0.024         -37.403         0.000         -0.933         -0.840           C(brand)[T.6]         -1.3850         0.051         -27.408         0.000         -1.484         -1.286           C(brand)[T.7]         -1.6527         0.018         -94.139         0.000         -1.687         -1.618           C(brand)[T.8]         -2.2856         0.016         -141.034         0.000         -2.317         -2.254           C(brand)[T.10]         -1.8983         0.022         -87.306         0.000         -1.941         -1.856           C(brand)[T.11]         -2.1754         0.019         -113.355         0.	Df Residuals:		38531	BIC:			$7.841\mathrm{e}{+04}$	
Intercept         -6.0745         0.036         -167.065         0.000         -6.146         -6.003           C(brand)[T.2]         -0.0048         0.022         -0.218         0.828         -0.048         0.039           C(brand)[T.3]         -0.4578         0.040         -11.502         0.000         -0.536         -0.380           C(brand)[T.4]         -0.4303         0.017         -25.951         0.000         -0.463         -0.398           C(brand)[T.5]         -0.8868         0.024         -37.403         0.000         -0.933         -0.840           C(brand)[T.6]         -1.3850         0.051         -27.408         0.000         -1.484         -1.286           C(brand)[T.7]         -1.6527         0.018         -94.139         0.000         -1.687         -1.618           C(brand)[T.8]         -2.2856         0.016         -141.034         0.000         -2.317         -2.254           C(brand)[T.9]         -1.9340         0.017         -111.950         0.000         -1.968         -1.900           C(brand)[T.10]         -1.8983         0.022         -87.306         0.000         -1.941         -1.856           C(brand)[T.11]         -2.1754         0.019         -113	Df Model:		12					
Intercept         -6.0745         0.036         -167.065         0.000         -6.146         -6.003           C(brand)[T.2]         -0.0048         0.022         -0.218         0.828         -0.048         0.039           C(brand)[T.3]         -0.4578         0.040         -11.502         0.000         -0.536         -0.380           C(brand)[T.4]         -0.4303         0.017         -25.951         0.000         -0.463         -0.398           C(brand)[T.5]         -0.8868         0.024         -37.403         0.000         -0.933         -0.840           C(brand)[T.6]         -1.3850         0.051         -27.408         0.000         -1.484         -1.286           C(brand)[T.7]         -1.6527         0.018         -94.139         0.000         -1.687         -1.618           C(brand)[T.8]         -2.2856         0.016         -141.034         0.000         -2.317         -2.254           C(brand)[T.10]         -1.8983         0.022         -87.306         0.000         -1.941         -1.856           C(brand)[T.11]         -2.1754         0.019         -113.355         0.000         -2.213         -2.138           prices         -0.3412         0.010         -33.864 <th>Covariance Type:</th> <th>ne</th> <th>onrobust</th> <th></th> <th></th> <th></th> <th></th>	Covariance Type:	ne	onrobust					
C(brand)[T.2]         -0.0048         0.022         -0.218         0.828         -0.048         0.039           C(brand)[T.3]         -0.4578         0.040         -11.502         0.000         -0.536         -0.380           C(brand)[T.4]         -0.4303         0.017         -25.951         0.000         -0.463         -0.398           C(brand)[T.5]         -0.8868         0.024         -37.403         0.000         -0.933         -0.840           C(brand)[T.6]         -1.3850         0.051         -27.408         0.000         -1.484         -1.286           C(brand)[T.7]         -1.6527         0.018         -94.139         0.000         -1.687         -1.618           C(brand)[T.8]         -2.2856         0.016         -141.034         0.000         -2.317         -2.254           C(brand)[T.9]         -1.9340         0.017         -111.950         0.000         -1.968         -1.900           C(brand)[T.10]         -1.8983         0.022         -87.306         0.000         -1.941         -1.856           C(brand)[T.11]         -2.1754         0.019         -113.355         0.000         -2.213         -2.138           prices         -0.3412         0.010         -33.864<		$\mathbf{coef}$	$\operatorname{std}$ err	$\mathbf{t}$	$\mathbf{P} >  \mathbf{t} $	[0.025]	0.975]	
C(brand)[T.3]         -0.4578         0.040         -11.502         0.000         -0.536         -0.380           C(brand)[T.4]         -0.4303         0.017         -25.951         0.000         -0.463         -0.398           C(brand)[T.5]         -0.8868         0.024         -37.403         0.000         -0.933         -0.840           C(brand)[T.6]         -1.3850         0.051         -27.408         0.000         -1.484         -1.286           C(brand)[T.7]         -1.6527         0.018         -94.139         0.000         -1.687         -1.618           C(brand)[T.8]         -2.2856         0.016         -141.034         0.000         -2.317         -2.254           C(brand)[T.9]         -1.9340         0.017         -111.950         0.000         -1.968         -1.900           C(brand)[T.10]         -1.8983         0.022         -87.306         0.000         -1.941         -1.856           C(brand)[T.11]         -2.1754         0.019         -113.355         0.000         -2.213         -2.138           prices         -0.3412         0.010         -33.864         0.000         -0.361         -0.321           prom_         0.3294         0.013         26.122	Intercept	-6.0745	0.036	-167.065	0.000	-6.146	-6.003	
C(brand)[T.4]         -0.4303         0.017         -25.951         0.000         -0.463         -0.398           C(brand)[T.5]         -0.8868         0.024         -37.403         0.000         -0.933         -0.840           C(brand)[T.6]         -1.3850         0.051         -27.408         0.000         -1.484         -1.286           C(brand)[T.7]         -1.6527         0.018         -94.139         0.000         -1.687         -1.618           C(brand)[T.8]         -2.2856         0.016         -141.034         0.000         -2.317         -2.254           C(brand)[T.9]         -1.9340         0.017         -111.950         0.000         -1.968         -1.900           C(brand)[T.10]         -1.8983         0.022         -87.306         0.000         -1.941         -1.856           C(brand)[T.11]         -2.1754         0.019         -113.355         0.000         -2.213         -2.138           prices         -0.3412         0.010         -33.864         0.000         -0.361         -0.321           prom_         0.3294         0.013         26.122         0.000         0.305         0.354           Prob(Omnibus):         0.000         Jarque-Bera (JB):	C(brand)[T.2]	-0.0048	0.022	-0.218	0.828	-0.048	0.039	
C(brand)[T.5]         -0.8868         0.024         -37.403         0.000         -0.933         -0.840           C(brand)[T.6]         -1.3850         0.051         -27.408         0.000         -1.484         -1.286           C(brand)[T.7]         -1.6527         0.018         -94.139         0.000         -1.687         -1.618           C(brand)[T.8]         -2.2856         0.016         -141.034         0.000         -2.317         -2.254           C(brand)[T.9]         -1.9340         0.017         -111.950         0.000         -1.968         -1.900           C(brand)[T.10]         -1.8983         0.022         -87.306         0.000         -1.941         -1.856           C(brand)[T.11]         -2.1754         0.019         -113.355         0.000         -2.213         -2.138           prices         -0.3412         0.010         -33.864         0.000         -0.361         -0.321           prom_         0.3294         0.013         26.122         0.000         0.305         0.354           Omnibus:         2773.498         Durbin-Watson:         1.024           Prob(Omnibus):         0.000         Jarque-Bera (JB):         3867.305           Skew:	C(brand)[T.3]	-0.4578	0.040	-11.502	0.000	-0.536	-0.380	
C(brand)[T.6]         -1.3850         0.051         -27.408         0.000         -1.484         -1.286           C(brand)[T.7]         -1.6527         0.018         -94.139         0.000         -1.687         -1.618           C(brand)[T.8]         -2.2856         0.016         -141.034         0.000         -2.317         -2.254           C(brand)[T.9]         -1.9340         0.017         -111.950         0.000         -1.968         -1.900           C(brand)[T.10]         -1.8983         0.022         -87.306         0.000         -1.941         -1.856           C(brand)[T.11]         -2.1754         0.019         -113.355         0.000         -2.213         -2.138           prices         -0.3412         0.010         -33.864         0.000         -0.361         -0.321           prom_         0.3294         0.013         26.122         0.000         0.305         0.354           Omnibus:         2773.498         Durbin-Watson:         1.024           Prob(Omnibus):         0.000         Jarque-Bera (JB):         3867.305           Skew:         -0.618         Prob(JB):         0.00	C(brand)[T.4]	-0.4303	0.017	-25.951	0.000	-0.463	-0.398	
C(brand)[T.7]       -1.6527       0.018       -94.139       0.000       -1.687       -1.618         C(brand)[T.8]       -2.2856       0.016       -141.034       0.000       -2.317       -2.254         C(brand)[T.9]       -1.9340       0.017       -111.950       0.000       -1.968       -1.900         C(brand)[T.10]       -1.8983       0.022       -87.306       0.000       -1.941       -1.856         C(brand)[T.11]       -2.1754       0.019       -113.355       0.000       -2.213       -2.138         prices       -0.3412       0.010       -33.864       0.000       -0.361       -0.321         prom_       0.3294       0.013       26.122       0.000       0.305       0.354         Omnibus:       2773.498       Durbin-Watson:       1.024         Prob(Omnibus):       0.000       Jarque-Bera (JB):       3867.305         Skew:       -0.618       Prob(JB):       0.00	C(brand)[T.5]	-0.8868	0.024	-37.403	0.000	-0.933	-0.840	
C(brand)[T.8]       -2.2856       0.016       -141.034       0.000       -2.317       -2.254         C(brand)[T.9]       -1.9340       0.017       -111.950       0.000       -1.968       -1.900         C(brand)[T.10]       -1.8983       0.022       -87.306       0.000       -1.941       -1.856         C(brand)[T.11]       -2.1754       0.019       -113.355       0.000       -2.213       -2.138         prices       -0.3412       0.010       -33.864       0.000       -0.361       -0.321         prom_       0.3294       0.013       26.122       0.000       0.305       0.354         Omnibus:       2773.498       Durbin-Watson:       1.024         Prob(Omnibus):       0.000       Jarque-Bera (JB):       3867.305         Skew:       -0.618       Prob(JB):       0.00	C(brand)[T.6]	-1.3850	0.051	-27.408	0.000	-1.484	-1.286	
C(brand)[T.9]       -1.9340       0.017       -111.950       0.000       -1.968       -1.900         C(brand)[T.10]       -1.8983       0.022       -87.306       0.000       -1.941       -1.856         C(brand)[T.11]       -2.1754       0.019       -113.355       0.000       -2.213       -2.138         prices       -0.3412       0.010       -33.864       0.000       -0.361       -0.321         prom_       0.3294       0.013       26.122       0.000       0.305       0.354         Omnibus:       2773.498       Durbin-Watson:       1.024         Prob(Omnibus):       0.000       Jarque-Bera (JB):       3867.305         Skew:       -0.618       Prob(JB):       0.00	C(brand)[T.7]	-1.6527	0.018	-94.139	0.000	-1.687	-1.618	
C(brand)[T.10]       -1.8983       0.022       -87.306       0.000       -1.941       -1.856         C(brand)[T.11]       -2.1754       0.019       -113.355       0.000       -2.213       -2.138         prices       -0.3412       0.010       -33.864       0.000       -0.361       -0.321         prom_       0.3294       0.013       26.122       0.000       0.305       0.354         Omnibus:       2773.498       Durbin-Watson:       1.024         Prob(Omnibus):       0.000       Jarque-Bera (JB):       3867.305         Skew:       -0.618       Prob(JB):       0.00	C(brand)[T.8]	-2.2856	0.016	-141.034	0.000	-2.317	-2.254	
C(brand)[T.11]       -2.1754       0.019       -113.355       0.000       -2.213       -2.138         prices       -0.3412       0.010       -33.864       0.000       -0.361       -0.321         prom_       0.3294       0.013       26.122       0.000       0.305       0.354         Omnibus:       2773.498       Durbin-Watson:       1.024         Prob(Omnibus):       0.000       Jarque-Bera (JB):       3867.305         Skew:       -0.618       Prob(JB):       0.00	` / L	-1.9340	0.017		0.000	-1.968	-1.900	
prices         -0.3412         0.010         -33.864         0.000         -0.361         -0.321           prom_         0.3294         0.013         26.122         0.000         0.305         0.354           Omnibus:         2773.498         Durbin-Watson:         1.024           Prob(Omnibus):         0.000         Jarque-Bera (JB):         3867.305           Skew:         -0.618         Prob(JB):         0.00		-1.8983	0.022	-87.306	0.000	-1.941	-1.856	
prom_         0.3294         0.013         26.122         0.000         0.305         0.354           Omnibus:         2773.498         Durbin-Watson:         1.024           Prob(Omnibus):         0.000         Jarque-Bera (JB):         3867.305           Skew:         -0.618         Prob(JB):         0.00	C(brand)[T.11]	-2.1754	0.019	-113.355		-2.213	-2.138	
Omnibus:         2773.498         Durbin-Watson:         1.024           Prob(Omnibus):         0.000         Jarque-Bera (JB):         3867.305           Skew:         -0.618         Prob(JB):         0.00	$\mathbf{prices}$				0.000			
Prob(Omnibus):       0.000       Jarque-Bera (JB):       3867.305         Skew:       -0.618       Prob(JB):       0.00	$\operatorname{prom}_{\_}$	0.3294	0.013	26.122	0.000	0.305	0.354	
Skew: $-0.618$ <b>Prob(JB):</b> $0.00$	Omnibus:	2'	773.498	Durbin-W	atson:	1.0	024	
	Prob(Omnik	ous):	0.000			3867	7.305	
Kurtosis: 3.938 Cond. No. 112.	Skew:		-0.618	` ,		0.	00	
	Kurtosis:		3.938	Cond. No	•	11	12.	

### Notes:

<sup>[1]</sup> Standard Errors assume that the covariance matrix of the errors is correctly specified.

# Estimate the Model using OLS, with price and promotion as characteristics, and store-brand dummies

#1.3. Using OLS with price and promotion as product characteristics and store-brand  $\#(the\ interaction\ of\ brand\ and\ store)\ dummies.$ 

res\_log3 = smf.ols('Y ~ prices + prom\_ + C(brand)\*C(store)', data=otc\_dataDf).fit()

Dep. Variable:	Y	R-squared:	0.722
Model:	OLS	Adj. R-squared:	0.716
Method:	Least Squares	F-statistic:	121.9
Date:	Thu, 04 Nov 2021	Prob (F-statistic):	0.00
Time:	05:21:32	Log-Likelihood:	-34946.
No. Observations:	38544	AIC:	$7.150\mathrm{e}{+04}$
Df Residuals:	37739	BIC:	$7.839e{+04}$
Df Model:	804		
Covariance Type:	nonrobust		
	0 1 1	D       [0.00#	0.0==1

	coei	sta err	τ	$\mathbf{P} >  \mathbf{t} $	[0.025]	0.975]
Intercept	-6.1994	0.093	-66.365	0.000	-6.382	-6.016
prices	-0.3302	0.010	-34.349	0.000	-0.349	-0.311
$\mathbf{prom}_{\_}$	0.3288	0.011	28.619	0.000	0.306	0.351
Omnibus:		4044.934	Durbir	ı-Watsoı	1:	1.268
Prob(Om	nibus).	0.000	Jarque	-Bera (J	(B): 7	222.052
	iiibab).	0.000	9 642 9 643	, <b>–</b> 51 a (8	<i></i>	
Skew:	inibus).	-0.721	Prob(J			0.00

#### Notes:

<sup>[1]</sup> Standard Errors assume that the covariance matrix of the errors is correctly specified.

<sup>[2]</sup> The condition number is large, 4.08e+03. This might indicate that there are strong multicollinearity or other numerical problems. Dummies omitted.

## Estimate the models from parts 1-3 using wholesale cost as an instrument

# OLS with price and promotion as product characteristics, using wholesale cost as instrument wholeSale\_IV1 = iv.IV2SLS.from\_formula('Y ~ 1 + [prices ~ cost\_] + prom\_ ', data=otc\_dataDf).fit()

Dep. Variable:	Y	R-squared:	0.1531
Estimator:	IV-2SLS	Adj. R-squared:	0.1531
No. Observations:	38544	F-statistic:	5255.4
Date:	Thu, Nov 04 2021	P-value (F-stat)	0.0000
Time:	05:25:20	Distribution:	chi2(2)
Cov. Estimator:	$\operatorname{robust}$		

	Parameter	Std. Err.	T-stat	P-value	Lower CI	Upper CI
Intercept	-7.8181	0.0150	-520.30	0.0000	-7.8476	-7.7887
$prom_{\_}$	-0.0068	0.0170	-0.4034	0.6866	-0.0401	0.0264
$\mathbf{prices}$	-0.2066	0.0029	-71.884	0.0000	-0.2122	-0.2009

Endogenous: prices Instruments: cost\_

Robust Covariance (Heteroskedastic)
Debiased: False

## # OLS with price and promotion as product characteristics and brand dummies # using wholesale cost as instrument

wholeSale\_IV2 = iv.IV2SLS.from\_formula('Y ~ 1 + [prices ~ cost\_] + prom\_ + C(brand)', data=otc\_dataDf).

Dep. Variable:	Y	R-squared:	0.6446
Estimator:	IV-2SLS	Adj. R-squared:	0.6445
No. Observations:	38544	F-statistic:	$9.69\mathrm{e}{+04}$
Date:	Thu, Nov 04 2021	P-value (F-stat)	0.0000
Time:	05:26:08	Distribution:	chi2(12)
Cov. Estimator:	$\operatorname{robust}$		

	Parameter	Std. Err.	T-stat	P-value	Lower CI	Upper CI
Intercept	-7.2171	0.0652	-110.69	0.0000	-7.3449	-7.0893
C(brand)[T.2]	-0.5161	0.0309	-16.703	0.0000	-0.5766	-0.4555
C(brand)[T.3]	-1.6627	0.0698	-23.833	0.0000	-1.7994	-1.5260
C(brand)[T.4]	-0.2833	0.0147	-19.314	0.0000	-0.3121	-0.2546
C(brand)[T.5]	-1.4660	0.0358	-40.904	0.0000	-1.5363	-1.3958
C(brand)[T.6]	-2.9699	0.0914	-32.484	0.0000	-3.1491	-2.7907
C(brand)[T.7]	-1.4158	0.0181	-78.185	0.0000	-1.4513	-1.3803
C(brand)[T.8]	-2.3613	0.0137	-172.35	0.0000	-2.3882	-2.3344
C(brand)[T.9]	-2.1365	0.0169	-126.55	0.0000	-2.1696	-2.1034
C(brand)[T.10]	-1.4120	0.0321	-44.036	0.0000	-1.4749	-1.3492
C(brand)[T.11]	-2.5260	0.0283	-89.396	0.0000	-2.5814	-2.4707
prom	0.4307	0.0145	29.801	0.0000	0.4024	0.4590
prices	-0.0081	0.0189	-0.4287	0.6682	-0.0452	0.0290

Endogenous: prices Instruments: cost

Robust Covariance (Heteroskedastic)
Debiased: False

wholeSale\_IV3 = iv.IV2SLS.from\_formula('Y ~ 1 + [prices ~ cost\_] + prom\_ + C(brand)\*C(store)', data=otc

<sup>#</sup> OLS with price and promotion as product characteristics and brand dummies # using wholesale cost as instrument

Dep. Variable:	Y	R-squared:	0.7150
Estimator:	IV-2SLS	Adj. R-squared:	0.7090
No. Observations:	38544	F-statistic:	$1.766\mathrm{e}{+05}$
Date:	Thu, Nov 04 2021	P-value (F-stat)	0.0000
Time:	05:27:37	Distribution:	chi2(804)
Cov. Estimator:	$\operatorname{robust}$		, ,

	Parameter	Std. Err.	T-stat	P-value	Lower CI	Upper CI
Intercept	-7.2138	0.0775	-93.106	0.0000	-7.3657	-7.0620

31.774

-1.9442

0.0000

0.0519

0.3934

-0.0695

0.4451

0.0003

Table 1: IV-2SLS Estimation Summary, dummies suppressed

Endogenous: prices

0.4193

-0.0346

prom

prices

Instruments: cost\_ Robust Covariance (Heteroskedastic) Debiased: False

0.0132

0.0178

Estimate the models from parts 1–3 using the Hausman instrument

Dep. Variable:	Y	R-squared:	0.1578
Estimator:	IV-2SLS	Adj. R-squared:	0.1577
No. Observations:	38544	F-statistic:	9465.0
Date:	Thu, Nov 04 2021	P-value (F-stat)	0.0000
Time:	05:40:33	Distribution:	chi2(2)
Cov. Estimator:	$\operatorname{robust}$		. ,

	Parameter	Std. Err.	T-stat	P-value	Lower CI	Upper CI
Intercept	-7.6143	0.0135	-565.64	0.0000	-7.6407	-7.5879
$\mathbf{prom}_{\_}$	-0.0327	0.0170	-1.9257	0.0541	-0.0660	0.0006
$\mathbf{prices}$	-0.2524	0.0026	-97.062	0.0000	-0.2574	-0.2473

Endogenous: prices

Instruments: pricestore1, pricestore2, pricestore3, pricestore4, pricestore5, pricestore6, pricestore7, pricestore8, pricestore9, pricestore10, pricestore11, pricestore12, pricestore13, pricestore14, pricestore15, pricestore16, pricestore17, pricestore18, pricestore19, pricestore20, pricestore21, pricestore22, pricestore23, pricestore24, pricestore25, pricestore26, pricestore27, pricestore28, pricestore29, pricestore30

Robust Covariance (Heteroskedastic)

Debiased: False

### Mean own-price elasticities from the estimates in models 1–3

These results make sense. As a rule of thumb, the own-price elasticities should be  $\in (-2, -5)$ . The IV estimates using the Hausman instrument are approximately in this range. The OLS estimates are not, indicating that endogeneity is a practical concern in this setting. The estimates with wholesale cost as an instrument are also "too small", indicating that wholesale cost may not be a viable instrument in this context.

Dep. Variable:	Y	R-squared:	0.6511
Estimator:	IV-2SLS	Adj. R-squared:	0.6510
No. Observations:	38544	F-statistic:	$9.529\mathrm{e}{+04}$
Date:	Thu, Nov 04 2021	P-value (F-stat)	0.0000
Time:	05:41:01	Distribution:	chi2(12)
Cov. Estimator:	$\operatorname{robust}$		

_	Parameter	Std. Err.	T-stat	P-value	Lower CI	Upper CI
Intercept	-5.4061	0.0539	-100.33	0.0000	-5.5117	-5.3005
C(product ids)[T.2]	0.2942	0.0259	11.370	0.0000	0.2435	0.3449
C(product ids)[T.3]	0.2471	0.0574	4.3071	0.0000	0.1347	0.3595
C(product ids)[T.4]	-0.5162	0.0140	-36.812	0.0000	-0.5437	-0.4888
$\mathrm{C(product\_ids)[T.5]}$	-0.5479	0.0298	-18.367	0.0000	-0.6064	-0.4894
$\mathrm{C(product\_ids)[T.6]}$	-0.4578	0.0751	-6.0967	0.0000	-0.6050	-0.3107
$\mathrm{C(product\_ids)[T.7]}$	-1.7913	0.0169	-105.81	0.0000	-1.8245	-1.7581
$\mathrm{C(product\_ids)[T.8]}$	-2.2413	0.0143	-156.43	0.0000	-2.2694	-2.2132
${ m C(product\_ids)[T.9]}$	-1.8155	0.0156	-116.73	0.0000	-1.8460	-1.7850
${ m C(product\_ids)[T.10]}$	-2.1827	0.0280	-77.963	0.0000	-2.2376	-2.1279
${ m C(product\_ids)[T.11]}$	-1.9703	0.0231	-85.436	0.0000	-2.0155	-1.9251
$\operatorname{prom}_{\_}$	0.2701	0.0143	18.947	0.0000	0.2421	0.2980
prices	-0.5361	0.0155	-34.507	0.0000	-0.5665	-0.5056

### Endogenous: prices

Instruments: pricestore1, pricestore2, pricestore3, pricestore4, pricestore5, pricestore6, pricestore7, pricestore8, pricestore9, pricestore10, pricestore11, pricestore12, pricestore13, pricestore14, pricestore15, pricestore16, pricestore17, pricestore18, pricestore29, pricestore20, pricestore21, pricestore22, pricestore23, pricestore24, pricestore25, pricestore26, pricestore27, pricestore28, pricestore29, pricestore30

Robust Covariance (Heteroskedastic)

Debiased: False

Dep. Variable:	Y	R-squared:	0.7183
Estimator:	IV-2SLS	Adj. R-squared:	0.7123
No. Observations:	38544	F-statistic:	$1.711\mathrm{e}{+05}$
Date:	Thu, Nov 04 2021	P-value (F-stat)	0.0000
Time:	05:42:30	Distribution:	chi2(804)
Cov. Estimator:	robust		` ′

	Parameter	Std. Err.	T-stat	P-value	Lower CI	Upper CI
Intercept	-5.4606	0.0662	-82.482	0.0000	-5.5903	-5.3308
$\mathbf{prom}_{\_}$	0.2630	0.0130	20.297	0.0000	0.2376	0.2884
prices	-0.5454	0.0138	-39.560	0.0000	-0.5725	-0.5184

Endogenous: prices

Instruments: pricestore1, pricestore2, pricestore3, pricestore4, pricestore5, pricestore6, pricestore7, pricestore8, pricestore9, pricestore10, pricestore11, pricestore12, pricestore13, pricestore14, pricestore15, pricestore16, pricestore17, pricestore18, pricestore29, pricestore20, pricestore21, pricestore22, pricestore23, pricestore24, pricestore25, pricestore26, pricestore27, pricestore28, pricestore29, pricestore30

Robust Covariance (Heteroskedastic) Dummies omitted.

Debiased: False

'	OLS1	OLS2	OLS3	IV4.1	IV4.2	IV4.3	IV5.1	IV5.2	IV5.3
brand									
1	-0.852929	-1.166183	-1.128481	-0.706043	-0.027733	-0.118239	-0.862496	-1.832176	-1.864240
2	-1.232714	-1.685451	-1.630960	-1.020423	-0.040082	-0.170887	-1.246541	-2.647991	-2.694332
3	-1.750607	-2.393550	-2.316167	-1.449128	-0.056921	-0.242681	-1.770243	-3.760477	-3.826287
4	-0.739114	-1.010568	-0.977896	-0.611828	-0.024032	-0.102461	-0.747405	-1.587691	-1.615476
5	-1.283685	-1.755141	-1.698398	-1.062616	-0.041739	-0.177953	-1.298083	-2.757481	-2.805738
6	-2.036190	-2.784018	-2.694011	-1.685529	-0.066207	-0.282271	-2.059029	-4.373936	-4.450483
7	-0.666923	-0.911862	-0.882382	-0.552069	-0.021685	-0.092453	-0.674403	-1.432616	-1.457688
8	-0.900107	-1.230688	-1.190900	-0.745096	-0.029267	-0.124779	-0.910203	-1.933518	-1.967356
9	-0.989782	-1.353297	-1.309545	-0.819327	-0.032183	-0.137210	-1.000884	-2.126149	-2.163357
10	-0.481135	-0.657841	-0.636573	-0.398277	-0.015644	-0.066698	-0.486532	-1.033526	-1.051613
11	-1.109697	-1.517254	-1.468201	-0.918591	-0.036082	-0.153834	-1.122144	-2.383739	-2.425456

### Problem 2

Our results for this section don't make sense, and there are a few indications that we may have errors in our code. Our GMM function reached the maximum number of iterations. It's not clear if we set the tolerance level too low or if it simply failed to converge; if it didn't converge then the estimation procedure is incorrect and our results *shouldn't* make sense.

### Estimate the parameter values using BLP

$\alpha$	eta	$\sigma_{ib}$	$\sigma_I$	$\sigma_I^2$
1.67671625	$\begin{bmatrix} 40.5539681\\ -37.20820459\\ 22.10159763\\ -9.87790967\\ -18.56618279\\ 17.5039916\\ -32.63598696\\ 34.20049778\\ -12.49605257\\ 0.95162148\\ -53.64393846 \end{bmatrix}$	$\begin{bmatrix} 0.35372042 \\ 0.4527695 \\ 0.2383683 \end{bmatrix}$	0.005161	-0.121263

Note that we have one more element of  $\beta$  than we should. When we constructed the dummies, we neglected to exclude one dummy variable, but we were unable to re-run our code before submitting our results. Given more time, we would re-run this step, and we suspect that the coefficients would then make more sense.

### What are the elasticities for store 9 in week 10?

We under-estimated the difficulty of this question. We know that we can calculate this from the first order conditions, and that we need to take a numerical integral over consumers, but we don't know how to do this.

# Back out the marginal costs for store 9 in week 10. How are they different from wholesale costs?

We have code that does this (for part 3) but we were unable to run it before turning in the HW. It should be almost exactly the same procedure as in part 3, but we need to use the random coefficient model's coefficients, and we are running into bugs in the code when we do that.

	store	week	brand	prices	new_prices	price_change
33	9	10	1	3.29	3.235631	-0.054369
34	9	10	2	4.87	4.815631	-0.054369
35	9	10	3	6.38	6.325631	-0.054369
36	9	10	4	2.83	2.797369	-0.032631
37	9	10	5	5.29	5.257369	-0.032631
38	9	10	6	8.39	8.357369	-0.032631
39	9	10	7	2.71	2.694294	-0.015706
40	9	10	8	3.34	3.324294	-0.015706
41	9	10	9	3.97	3.954294	-0.015706
42	9	10	10	1.69	1.671601	-0.018399
43	9	10	11	4.49	4.471601	-0.018399

# How to predict the change in prices after the merger using the random coefficients model?

The procedure for predicting the effects of a merger using estimates from the random coefficients model is exactly the same. When we estimate the logit model, we end up with unrealistic elasticities, and hence unrealistic substitution patterns. The random coefficients model gives us a more reasonable matrix of elasticities, but we use it in the same way. When we want to assess the change of moving from two single-product firms to a multi-product firm, we switch from looking at firms that take FOCs with respect to a single price to a single firm that takes FOCs with respect to two prices (the price of each good that it produces). What does this mean? With a more realistic estimate of substitution patterns, we have a better idea of how consumers will respond to changes in prices. Pre-merger, a firm would be "unwilling" to raise its price because it would lose customers. Now, however, the merged firm may recognize that increasing the price of one of it's products will cause consumers to switch to its other product, so its profit maximizing price may be higher in the merged case than in the pre-merger case. The random coefficients model is giving us a better insight into these actual substitution patterns.