# DaiglePredictionofSocialSecurity.R

#### daigle chris

Sat Dec 8 16:13:22 2018

Chris Daigle Prediction of Social Security Awards

```
# Prepare workspace ####
rm(list = ls())
knitr::opts_chunk$set(message = FALSE)
library(tseries)
library(quantmod)
## Loading required package: xts
## Loading required package: zoo
## Attaching package: 'zoo'
## The following objects are masked from 'package:base':
##
       as.Date, as.Date.numeric
## Loading required package: TTR
## Version 0.4-0 included new data defaults. See ?getSymbols.
library(data.table)
##
## Attaching package: 'data.table'
## The following objects are masked from 'package:xts':
##
##
       first, last
library(leaps)
library(plm)
## Loading required package: Formula
## Attaching package: 'plm'
## The following object is masked from 'package:data.table':
##
##
       between
library(class)
setwd('~/Git/MachineLearningAndBigDataWithR/Data')
dataName <- 'assembled.csv'</pre>
df <- read.csv(dataName, stringsAsFactors = FALSE)</pre>
# Summarize and clean data ####
# head(df)
df \leftarrow df[-1]
# head(df)
# str(df)
```

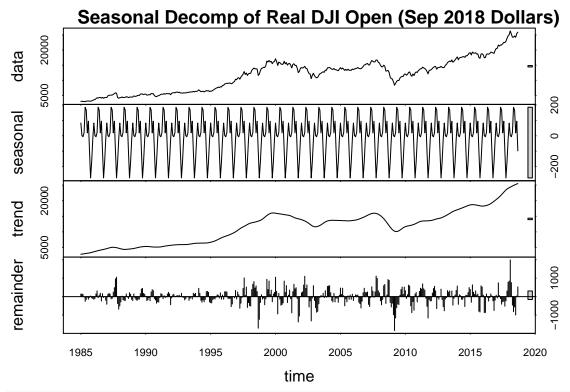
```
# Variable Manipulation ####
# Set dates
df$date <- as.Date(df$date, "%Y-%m-%d")
# Functions to clean data #
spaceless <- function(x) {</pre>
 x <- gsub(" ", ".", x)
}
commaless <- function(x) {</pre>
 x <- gsub(",", "", x)
}
dollarless <- function(x) {</pre>
 x <- gsub("\\$", "", x)
# Loops to apply functions #
for (i in 15:20) {
 df[, i] <- commaless(df[, i])</pre>
for (i in 15:20) {
 df[, i] <- dollarless(df[, i])</pre>
# Loop to transform variable types #
for (i in 15:20) {
 df[, i] <- as.numeric(df[, i])</pre>
# Names with Index ####
# 1 date
                            : Date
# 2 DJIopen
                            : num
# 3 DJIhigh
                            : num
# 4 DJIlow
                            : num
                            : num
# 5 DJIclose
# 6 DJIadjClose
                            : num
# 7 DJIvolume
                             : num
# 8 SPopen
                             : num
# 9 SPhigh
                            : num
# 10 SPlow
                             : num
# 11 SPclose
                              : num
# 12 SPadjClose
                             : num
# 13 SPvolume
                             : num
# 14 fedFundRate
                             : num
# 15 totalSSRetired
                              : num
# 16 averageSSRetiredPay : num
# 17 totalMaleSSRetired : num
# 18 averageMaleSSRetiredPay : num
# 19 totalFemaleSSRetired : num
# 20 averageFemaleSSRetiredPay: num
# 21 cpi
```

```
# Order Change #
df <- df[, c(1, 15, 17, 19, 21, 14, 7, 13, 2:6, 8:12, 16, 18, 20)]
# 1 date
                           : Date
# 2 totalSSRetired
                           : num
# 3 totalMaleSSRetired
                           : num
# 4 totalFemaleSSRetired : num
# 5 cpi
                           : num
# 6 fedFundRate
                            : num
# 7 DJIvolume
# 8 SPvolume
                           : num
# 9 DJIopen
                           : num
# 10 DJIhigh
                             : num
# 11 DJIlow
                             : num
# 12 DJIclose
                            : num
# 13 DJIadjClose
                            : num
# 14 SPopen
                             : num
# 15 SPhigh
                             : num
# 16 SPlow
                            : num
# 17 SPclose
                            : num
# 18 SPadjClose
                             : num
# 19 averageSSRetiredPay : num
# 20 averageMaleSSRetiredPay : num
# 21 averageFemaleSSRetiredPay: num
# Variable Creation ####
# CPI Inflator
latestDate <- tail(df\$date, n = 1)
baseCpi <- df$cpi[df$date == latestDate]</pre>
df$inflator <- baseCpi / df$cpi</pre>
df \leftarrow df[, c(1:6, 22, 7:21)]
realNames <-
  paste('real',
        colnames(df[, 10:22]),
        sep = "")
df[, realNames] <- df$inflator * df[10:22]</pre>
# Differences #
diffNames <-
  paste('diff',
        c(colnames(df[10:22]),
         paste('Real',
                colnames(df[10:22]),
                sep = "")),
        sep = "")
df[, diffNames] <- rep(NA, nrow(df))</pre>
for (i in 36:61) {
  df[, i][2:nrow(df)] <- diff(df[, i - 26], lag = 1)
```

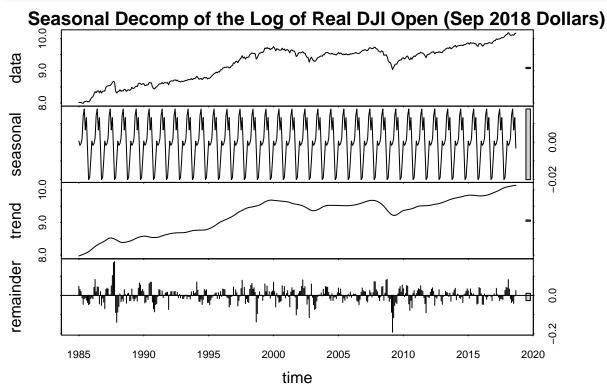
```
diffTargetNames <-</pre>
  paste('diff',
        c(colnames(df[2:4])),
        sep = "")
df[, diffTargetNames] <- rep(NA, nrow(df))</pre>
for (i in 62:64) {
  df[, i][2:nrow(df)] <- diff(df[, i - 60], lag = 1)</pre>
# Positive Indicator #
posNames <-
  paste('pos',
        c(colnames(df[10:22]),
          paste('Real',
                 colnames(df[10:22]),
                 sep = "")),
        sep = "")
df[, posNames] <- rep(0, nrow(df))</pre>
for (i in 65:90) {
  df[, i][df[, i - 20] > 0] <- 1
}
posTargetNames <-
  paste('pos',
        c(colnames(df[2:4])),
        sep = "")
df[, posTargetNames] <- rep(0, nrow(df))</pre>
for (i in 91:93) {
  df[, i][df[, i - 29] > 0] <- 1
# Percent Changes #
percChangeNames <-
  paste('percChange',
        c(colnames(df[10:22]),
          paste('Real', colnames(df[10:22]), sep = "")),
        sep = "")
df[, percChangeNames] <- rep(NA, nrow(df))</pre>
for (i in 94:119) {
  df[, i] <- Delt(df[, i - 84])</pre>
}
for (i in 94:119) {
  df[, i] <- as.numeric(df[, i])</pre>
percChangeTargetNames <-</pre>
  paste('percChange',
        c(colnames(df[2:4])),
        sep = "")
df[, percChangeTargetNames] <- rep(NA, nrow(df))</pre>
for (i in 120:122) {
  df[, i] <- Delt(df[, i - 118])</pre>
```

```
for (i in 120:122) {
 df[, i] <- as.numeric(df[, i])</pre>
# Place all target variables - totalRetired* - together
df <- df[, c(1:4, 62:64, 91:93, 120:122, 5:61, 65:90, 94:119)]
df1 <- df[complete.cases(df), ]</pre>
# Timeseries Evaluation ####
realDJIOpen <-
 ts(
    df$realDJIopen,
    start = c(1985, 1),
    end = c(2018, 9),
    frequency = 12
percRealDJIOpen <-
 ts(
    df1$percChangeRealDJIopen,
    start = c(1985, 2),
    end = c(2018, 9),
    frequency = 12
realSPOpen <-
  ts(
    df$realSPopen,
    start = c(1985, 1),
    end = c(2018, 9),
    frequency = 12
percRealSPOpen <-
  ts(
    df1$percChangeRealSPopen,
    start = c(1985, 2),
    end = c(2018, 9),
    frequency = 12
fedFund <-
 ts(
    df$fedFundRate,
    start = c(1985, 1),
    end = c(2018, 9),
    frequency = 12
totalRetired <-
  ts(
    df$totalSSRetired,
    start = c(1985, 1),
    end = c(2018, 9),
   frequency = 12
```

```
plot(stl(realDJIOpen, s.window = "period"), lwd = 1)
title(main = 'Seasonal Decomp of Real DJI Open (Sep 2018 Dollars)')
```

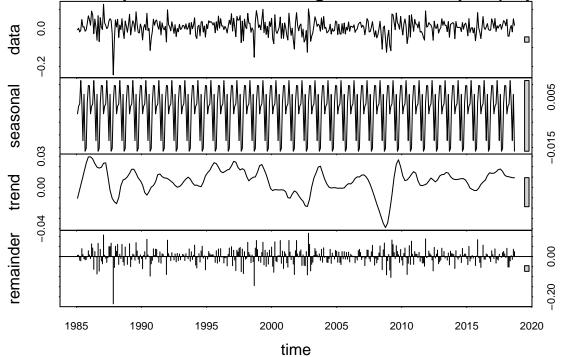


plot(stl(log(realDJIOpen), s.window = "period"), lwd = 1)
title(main = 'Seasonal Decomp of the Log of Real DJI Open (Sep 2018 Dollars)')

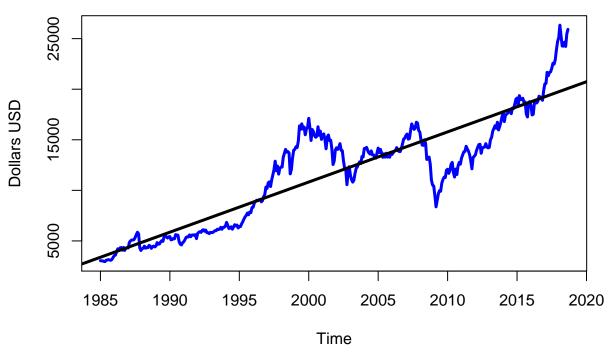


```
plot(stl(percRealDJIOpen, s.window = "period"), lwd = 1)
title(main = 'Seasonal Decomp of the Percent Change of Real DJI Open (Sep 2018 Dollars)')
```

#### easonal Decomp of the Percent Change of Real DJI Open (Sep 2018 Dc

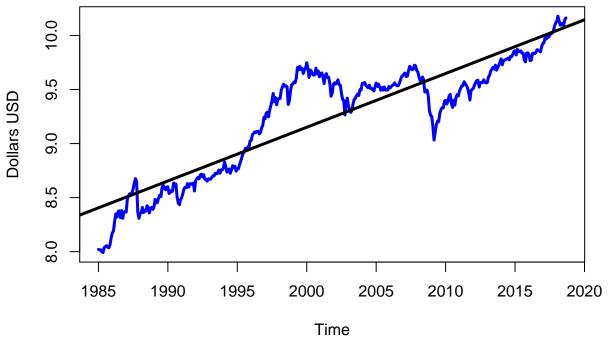


# Real DJI Open (Sep 2018 Dollars)

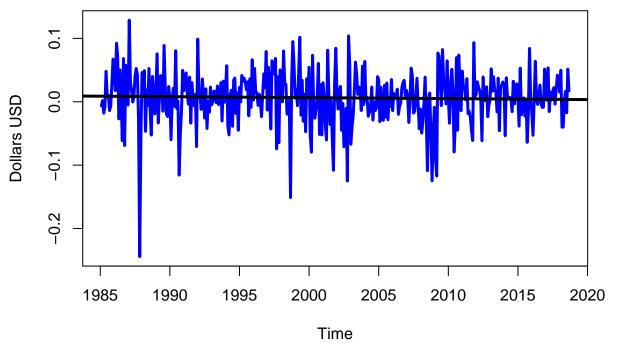


```
plot(log(realDJIOpen),
        col = 'blue',
        lwd = 3,
        ylab = 'Dollars USD')
abline(reg = lm(log(realDJIOpen) ~ time(log(realDJIOpen))), lwd = 3)
title(main = 'Log of Real DJI Open (Sep 2018 Dollars)')
```

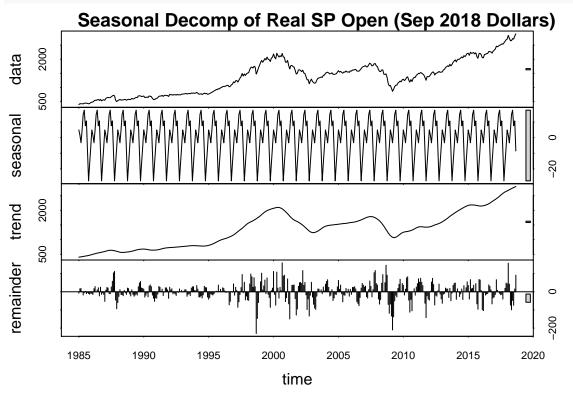
# Log of Real DJI Open (Sep 2018 Dollars)



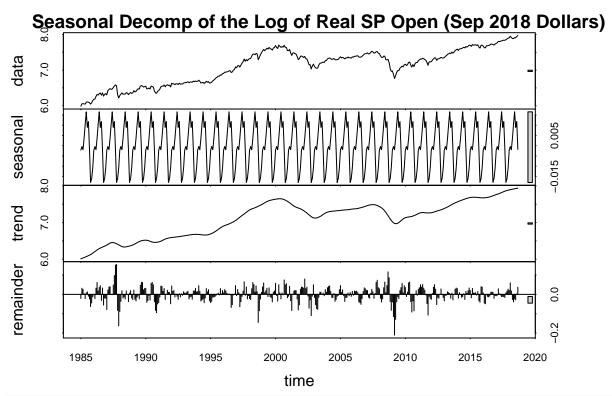
#### Percent Change of Real DJI Open (Sep 2018 USD)



plot(stl(realSPOpen, s.window = "period"), lwd = 1)
title(main = 'Seasonal Decomp of Real SP Open (Sep 2018 Dollars)')

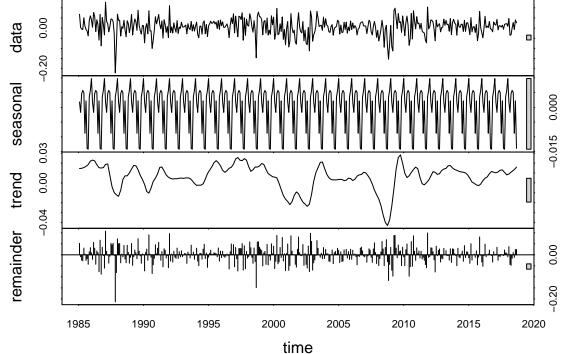


plot(stl(log(realSPOpen), s.window = "period"), lwd = 1)
title(main = 'Seasonal Decomp of the Log of Real SP Open (Sep 2018 Dollars)')



```
plot(stl(percRealSPOpen, s.window = "period"), lwd = 1)
title(main = 'Seasonal Decomp of the Percent Change of Real SP Open (Sep 2018 Dollars)')
```

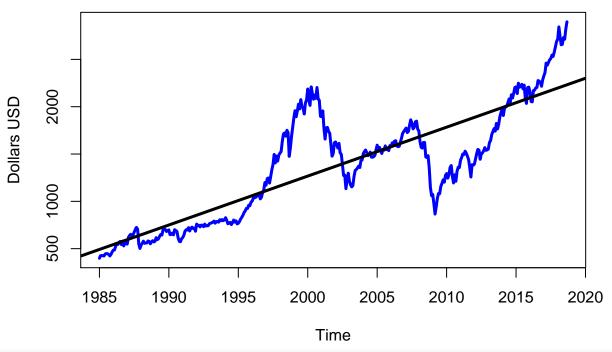




```
plot(realSPOpen,
     col = 'blue',
     lwd = 3,
```

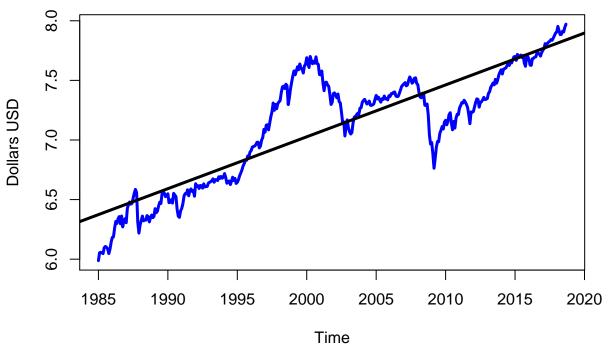
```
ylab = 'Dollars USD')
abline(reg = lm(realSPOpen ~ time(realSPOpen)), lwd = 3)
title(main = 'Real SP Open (Sep 2018 Dollars)')
```

#### Real SP Open (Sep 2018 Dollars)

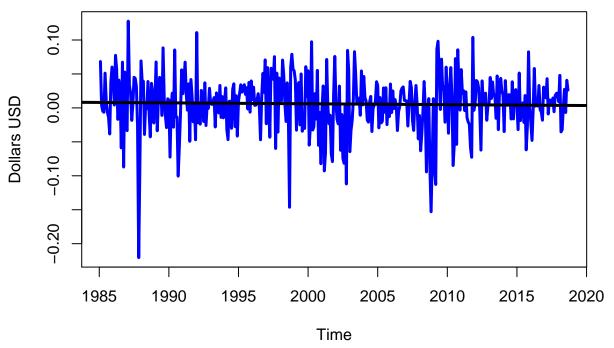


```
plot(log(realSPOpen),
        col = 'blue',
        lwd = 3,
        ylab = 'Dollars USD')
abline(reg = lm(log(realSPOpen) ~ time(log(realSPOpen))), lwd = 3)
title(main = 'Log of Real SP Open (Sep 2018 Dollars)')
```

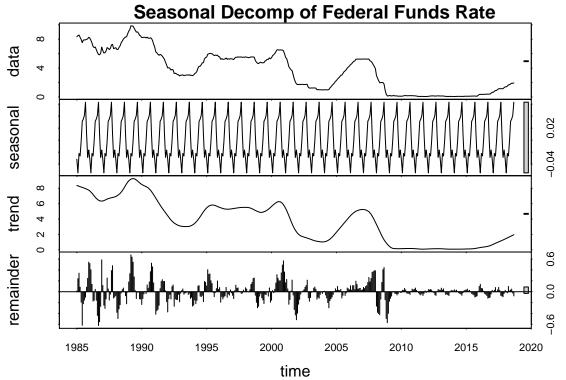
# Log of Real SP Open (Sep 2018 Dollars)



### Percent Change of Real SP Open (Sep 2018 USD)



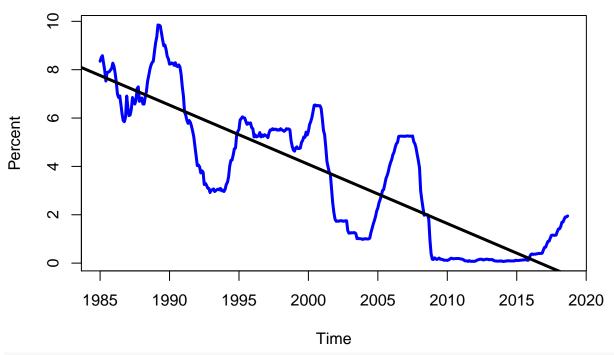
plot(stl(fedFund, s.window = "period"), lwd = 1)
title(main = 'Seasonal Decomp of Federal Funds Rate')



```
plot(fedFund,
    col = 'blue',
    lwd = 3,
```

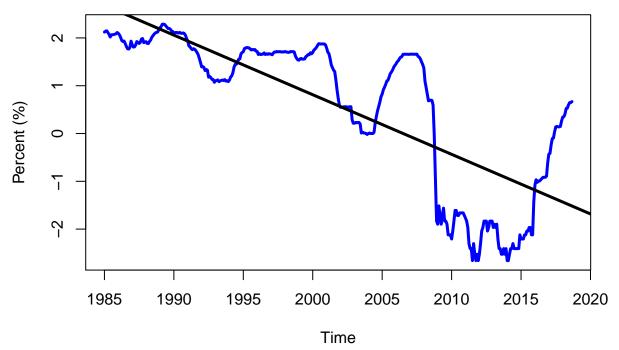
```
ylab = 'Percent')
abline(reg = lm(fedFund ~ time(fedFund)), lwd = 3)
title(main = 'Federal Funds Rate')
```

#### **Federal Funds Rate**

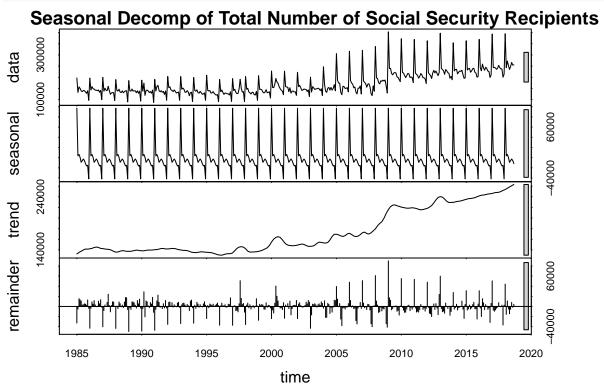


```
plot(log(fedFund),
        col = 'blue',
        lwd = 3,
        ylab = 'Percent (%)')
abline(reg = lm(log(fedFund) ~ time(log(fedFund))), lwd = 3)
title(main = 'Log of Federal Funds Rate')
```

### Log of Federal Funds Rate



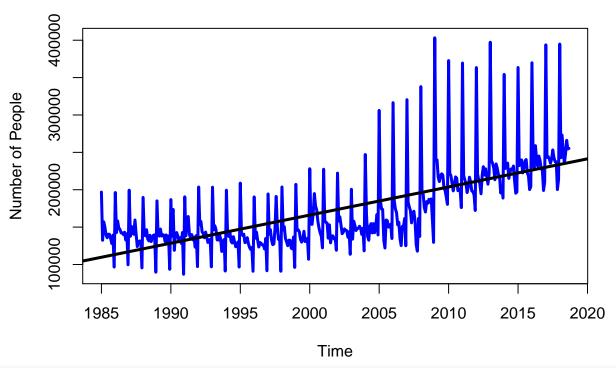
```
plot(stl(totalRetired, s.window = "period"), lwd = 1)
title(main = 'Seasonal Decomp of Total Number of Social Security Recipients')
```



```
plot(totalRetired,
    col = 'blue',
    lwd = 3,
```

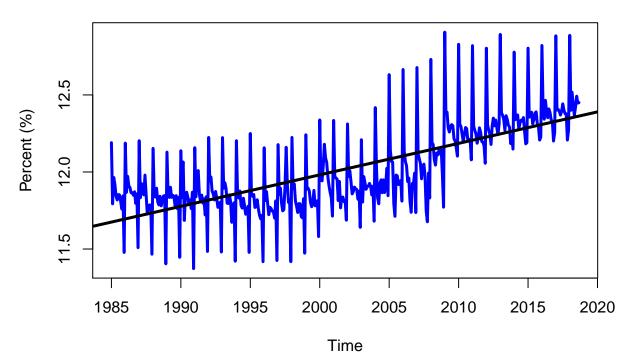
```
ylab = 'Number of People')
abline(reg = lm(totalRetired ~ time(totalRetired)), lwd = 3)
title(main = 'Total Number of Social Security Recipients')
```

#### **Total Number of Social Security Recipients**



```
plot(log(totalRetired),
        col = 'blue',
        lwd = 3,
        ylab = 'Percent (%)')
abline(reg = lm(log(totalRetired) ~ time(log(totalRetired))), lwd = 3)
title(main = 'Log of Total Number of Social Security Recipients')
```

#### **Log of Total Number of Social Security Recipients**



```
# Remove nominal values aside indicators of positive change
df2 <- df1[, c(1, 8:10, 11:18, 32:44, 58:96, 110:122)]
# remove components of the total SS Retirees (male + female = total) and percent increases and decrease
df3 <- df2[, c(1:2, 8:9, 13:77)]
# Hypothesis Tests ####
# Stationarity Loop Testing
statVars <- matrix(data = NA, nrow = 68, ncol = 2)
df3TS <- ts(
  df3,
  start = c(1985, 12),
  end = c(2018, 9),
  frequency = 12
)
for (i in c(1:68)) {
  statVars[i,1] <- i+1
  statVars[i,2] <- adf.test(df3TS[,i+1], alternative = 'stationary')[[4]]</pre>
}
```

```
## Warning in adf.test(df3TS[, i + 1], alternative = "stationary"): p-value
## smaller than printed p-value

## Warning in adf.test(df3TS[, i + 1], alternative = "stationary"): p-value
## warning in adf.test(df3TS[, i + 1], alternative = "stationary"): p-value
## smaller than printed p-value

## Warning in adf.test(df3TS[, i + 1], alternative = "stationary"): p-value
## warning in adf.test(df3TS[, i + 1], alternative = "stationary"): p-value
## warning in adf.test(df3TS[, i + 1], alternative = "stationary"): p-value
```

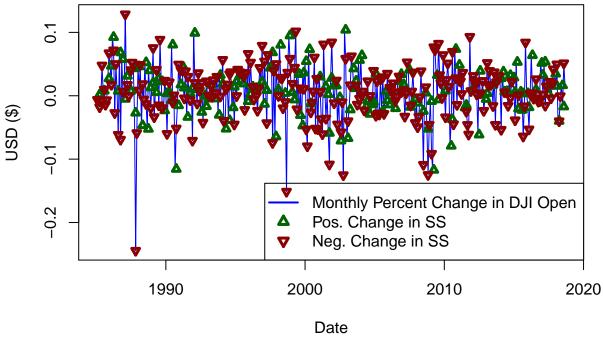
```
## Warning in adf.test(df3TS[, i + 1], alternative = "stationary"): p-value
## smaller than printed p-value
## Warning in adf.test(df3TS[, i + 1], alternative = "stationary"): p-value
## smaller than printed p-value
## Warning in adf.test(df3TS[, i + 1], alternative = "stationary"): p-value
## smaller than printed p-value
## Warning in adf.test(df3TS[, i + 1], alternative = "stationary"): p-value
## smaller than printed p-value
## Warning in adf.test(df3TS[, i + 1], alternative = "stationary"): p-value
## smaller than printed p-value
## Warning in adf.test(df3TS[, i + 1], alternative = "stationary"): p-value
## smaller than printed p-value
## Warning in adf.test(df3TS[, i + 1], alternative = "stationary"): p-value
## smaller than printed p-value
## Warning in adf.test(df3TS[, i + 1], alternative = "stationary"): p-value
## smaller than printed p-value
## Warning in adf.test(df3TS[, i + 1], alternative = "stationary"): p-value
## smaller than printed p-value
## Warning in adf.test(df3TS[, i + 1], alternative = "stationary"): p-value
## smaller than printed p-value
## Warning in adf.test(df3TS[, i + 1], alternative = "stationary"): p-value
## smaller than printed p-value
## Warning in adf.test(df3TS[, i + 1], alternative = "stationary"): p-value
## smaller than printed p-value
## Warning in adf.test(df3TS[, i + 1], alternative = "stationary"): p-value
## smaller than printed p-value
## Warning in adf.test(df3TS[, i + 1], alternative = "stationary"): p-value
## smaller than printed p-value
## Warning in adf.test(df3TS[, i + 1], alternative = "stationary"): p-value
## smaller than printed p-value
## Warning in adf.test(df3TS[, i + 1], alternative = "stationary"): p-value
## smaller than printed p-value
## Warning in adf.test(df3TS[, i + 1], alternative = "stationary"): p-value
## smaller than printed p-value
## Warning in adf.test(df3TS[, i + 1], alternative = "stationary"): p-value
## smaller than printed p-value
```

```
## Warning in adf.test(df3TS[, i + 1], alternative = "stationary"): p-value
## smaller than printed p-value
## Warning in adf.test(df3TS[, i + 1], alternative = "stationary"): p-value
## smaller than printed p-value
## Warning in adf.test(df3TS[, i + 1], alternative = "stationary"): p-value
## smaller than printed p-value
## Warning in adf.test(df3TS[, i + 1], alternative = "stationary"): p-value
## smaller than printed p-value
## Warning in adf.test(df3TS[, i + 1], alternative = "stationary"): p-value
## smaller than printed p-value
## Warning in adf.test(df3TS[, i + 1], alternative = "stationary"): p-value
## smaller than printed p-value
## Warning in adf.test(df3TS[, i + 1], alternative = "stationary"): p-value
## smaller than printed p-value
## Warning in adf.test(df3TS[, i + 1], alternative = "stationary"): p-value
## smaller than printed p-value
## Warning in adf.test(df3TS[, i + 1], alternative = "stationary"): p-value
## smaller than printed p-value
## Warning in adf.test(df3TS[, i + 1], alternative = "stationary"): p-value
## smaller than printed p-value
## Warning in adf.test(df3TS[, i + 1], alternative = "stationary"): p-value
## smaller than printed p-value
## Warning in adf.test(df3TS[, i + 1], alternative = "stationary"): p-value
## smaller than printed p-value
## Warning in adf.test(df3TS[, i + 1], alternative = "stationary"): p-value
## smaller than printed p-value
## Warning in adf.test(df3TS[, i + 1], alternative = "stationary"): p-value
## smaller than printed p-value
## Warning in adf.test(df3TS[, i + 1], alternative = "stationary"): p-value
## smaller than printed p-value
## Warning in adf.test(df3TS[, i + 1], alternative = "stationary"): p-value
## smaller than printed p-value
## Warning in adf.test(df3TS[, i + 1], alternative = "stationary"): p-value
## smaller than printed p-value
## Warning in adf.test(df3TS[, i + 1], alternative = "stationary"): p-value
## smaller than printed p-value
```

```
## Warning in adf.test(df3TS[, i + 1], alternative = "stationary"): p-value
## smaller than printed p-value
## Warning in adf.test(df3TS[, i + 1], alternative = "stationary"): p-value
## smaller than printed p-value
## Warning in adf.test(df3TS[, i + 1], alternative = "stationary"): p-value
## smaller than printed p-value
## Warning in adf.test(df3TS[, i + 1], alternative = "stationary"): p-value
## smaller than printed p-value
## Warning in adf.test(df3TS[, i + 1], alternative = "stationary"): p-value
## smaller than printed p-value
## Warning in adf.test(df3TS[, i + 1], alternative = "stationary"): p-value
## smaller than printed p-value
## Warning in adf.test(df3TS[, i + 1], alternative = "stationary"): p-value
## smaller than printed p-value
## Warning in adf.test(df3TS[, i + 1], alternative = "stationary"): p-value
## smaller than printed p-value
## Warning in adf.test(df3TS[, i + 1], alternative = "stationary"): p-value
## smaller than printed p-value
## Warning in adf.test(df3TS[, i + 1], alternative = "stationary"): p-value
## smaller than printed p-value
## Warning in adf.test(df3TS[, i + 1], alternative = "stationary"): p-value
## smaller than printed p-value
## Warning in adf.test(df3TS[, i + 1], alternative = "stationary"): p-value
## smaller than printed p-value
## Warning in adf.test(df3TS[, i + 1], alternative = "stationary"): p-value
## smaller than printed p-value
## Warning in adf.test(df3TS[, i + 1], alternative = "stationary"): p-value
## smaller than printed p-value
## Warning in adf.test(df3TS[, i + 1], alternative = "stationary"): p-value
## smaller than printed p-value
## Warning in adf.test(df3TS[, i + 1], alternative = "stationary"): p-value
## smaller than printed p-value
# Reject the null when p < 0.05. So, the variables associated with this are
# likely stationary and useful for prediction of time series
dfStatSelect<- statVars[,1][statVars[,2] < 0.05]</pre>
dfStationary<- df3[,c(1,dfStatSelect)]</pre>
```

```
# Visualizations ####
plot(
  x = dfStationary$date,
  y = dfStationary$percChangeRealDJIopen,
  col = 'blue',
  lwd = 1,
 type = '1',
 ylab = 'USD ($)',
 xlab = 'Date'
points(
  x = dfStationary$date[df$postotalSSRetired == 1],
  y = dfStationary$percChangeRealDJIopen[dfStationary$postotalSSRetired == 1],
  pch = 24,
 col = 'darkgreen',
 cex = 0.8,
  lwd = 3
points(
 x = dfStationary$date[dfStationary$postotalSSRetired == 0],
  y = dfStationary$percChangeRealDJIopen[dfStationary$postotalSSRetired == 0],
 pch = 25,
  col = 'darkred',
  cex = 0.8,
  lwd = 3
legend(
  'bottomright',
  legend = c(
    'Monthly Percent Change in DJI Open',
    c('Pos. Change in SS', 'Neg. Change in SS')
  ),
  lty = c(1, c(NA, NA)),
  pch = c(NA, c(24, 25)),
  col = c('blue', c('darkgreen', 'darkred')),
  bg = c(NA, c('darkgreen', 'darkred')),
 1wd = c(2, c(3, 3))
title(main = 'Monthly % Change in Real DJI Open (Sep 2018 USD)')
```

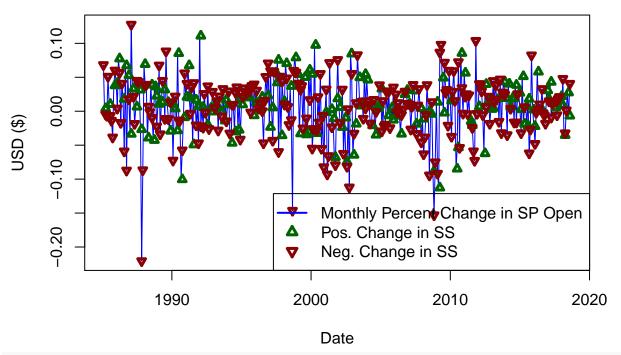
### Monthly % Change in Real DJI Open (Sep 2018 USD)



```
plot(
  x = dfStationary$date,
  y = dfStationary$percChangeRealSPopen,
  col = 'blue',
  lwd = 1,
  type = '1',
  ylab = 'USD (\$)',
  xlab = 'Date'
points(
  x = dfStationary$date[df$postotalSSRetired == 1],
  y = dfStationary percChangeRealSPopen[dfStationary postotalSSRetired == 1],
  pch = 24,
  col = 'darkgreen',
  cex = 0.8,
  lwd = 3
)
points(
  x = dfStationary$date[dfStationary$postotalSSRetired == 0],
  y = dfStationary$percChangeRealSPopen[dfStationary$postotalSSRetired == 0],
  pch = 25,
  col = 'darkred',
  cex = 0.8,
  lwd = 3
)
legend(
  'bottomright',
  legend = c(
    'Monthly Percent Change in SP Open',
    c('Pos. Change in SS', 'Neg. Change in SS')
```

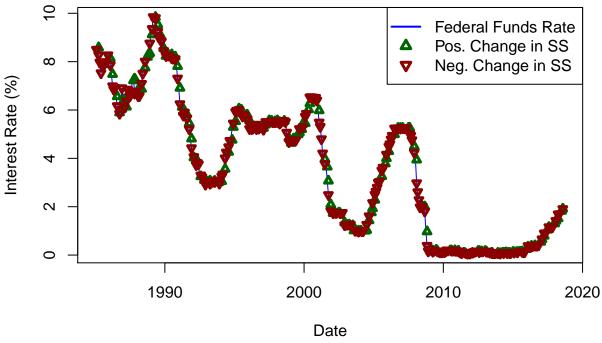
```
),
  lty = c(1, c(NA, NA)),
  pch = c(NA, c(24, 25)),
  col = c('blue', c('darkgreen', 'darkred')),
  bg = c(NA, c('darkgreen', 'darkred')),
  lwd = c(2, c(3, 3))
)
title(main = 'Monthly % Change in Real S&P500 Open (Sep 2018 USD)')
```

#### Monthly % Change in Real S&P500 Open (Sep 2018 USD)



```
plot(
  x = dfStationary$date,
  y = dfStationary$fedFundRate,
  col = 'blue',
 lwd = 1,
  type = '1',
  ylab = 'Interest Rate (%)',
  xlab = 'Date'
)
points(
  x = dfStationary$date[df$postotalSSRetired == 1],
  y = dfStationary$fedFundRate[dfStationary$postotalSSRetired == 1],
 pch = 24,
  col = 'darkgreen',
  cex = 0.8,
  lwd = 3
)
points(
  x = dfStationary$date[dfStationary$postotalSSRetired == 0],
 y = dfStationary$fedFundRate[dfStationary$postotalSSRetired == 0],
```

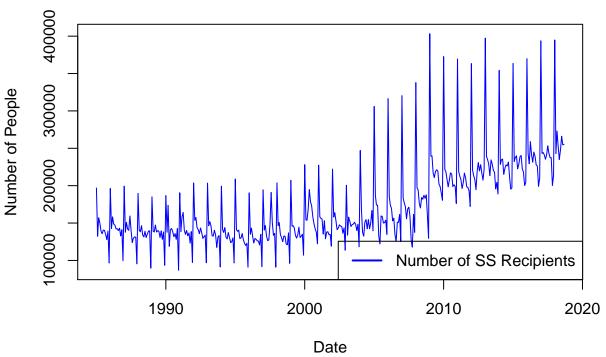
#### **Federal Funds Rate**



```
plot(
    x = df$date,
    y = df$totalSSRetired,
    col = 'blue',
    lwd = 1,
    type = 'l',
    ylab = 'Number of People',
    xlab = 'Date'
)
legend(
    'bottomright',
    legend = c('Number of SS Recipients'),
    lty = c(1),
```

```
col = c('blue'),
lwd = c(2)
)
title(main = 'Total Retired on Social Security')
```

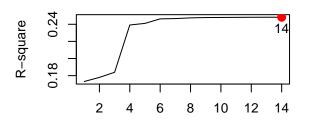
#### **Total Retired on Social Security**

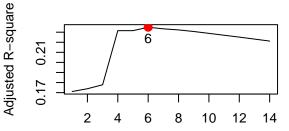


```
# Selection ####
# Set a few dataframes for different variables
dfDiff <- dfStationary[,c(2:5,7:19)]</pre>
dfPosChange <- dfStationary[,c(2:5, 20:45)]</pre>
dfPerc <- dfStationary[,c(2:5, 46:58)]</pre>
# Run the selections
# Differences ####
# SeqRep
regFitSelect <- regsubsets(</pre>
  postotalSSRetired~.,
  data=dfDiff,
  method= 'seqrep',
  nvmax=17)
## Warning in leaps.setup(x, y, wt = wt, nbest = nbest, nvmax = nvmax,
## force.in = force.in, : 2 linear dependencies found
## Reordering variables and trying again:
regSummary <- summary(regFitSelect)</pre>
names(regSummary)
                                              "cp"
## [1] "which"
                                     "adjr2"
                                                        "bic"
                                                                  "outmat" "obj"
                 "rsq"
                           "rss"
regSummary$rsq
```

```
## [8] 0.2474956 0.2478743 0.2479814 0.2480829 0.2481942 0.2482266 0.2482272
regSummary$adjr2
## [1] 0.1711130 0.1738456 0.1777974 0.2315317 0.2315172 0.2349210 0.2333461
## [8] 0.2322550 0.2306938 0.2288461 0.2269832 0.2251209 0.2231675 0.2211711
par(mfrow=c(2,2))
aRSQ <- which.max(regSummary$rsq)
aARSQ <- which.max(regSummary$adjr2)</pre>
aCP <- which.min(regSummary$cp)</pre>
aBIC <- which.min(regSummary$bic)
aRSS <- which.min(regSummary$rss)
par(mfrow = c(2, 2))
plot(
  regSummary$rsq,
  xlab = "Number of regressors - SeqRep - Differences",
  ylab = "R-square",
  type = "1"
points(
  aRSQ,
  regSummary$rsq[aRSQ],
 col = "red",
 cex = 2,
  pch = 20
text (aRSQ,
     regSummary$rsq[aRSQ],
     labels = aRSQ,
     pos = 1)
plot(
  regSummary$adjr2,
  xlab = "Number of regressors - SeqRep - Differences",
 ylab = "Adjusted R-square",
  type = "1"
points(
  aARSQ,
  regSummary$adjr2[aARSQ],
 col = "red",
  cex = 2,
  pch = 20
text(aARSQ,
     regSummary$adjr2[aARSQ],
     labels = aARSQ,
     pos = 1)
plot(regSummary$cp,
     xlab = "Number of regressors - SeqRep - Differences",
     ylab = "Cp",
```

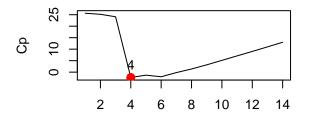
```
type = "1")
points(
 aCP,
 regSummary$cp[aCP],
 col = "red",
 cex = 2,
 pch = 20
text(aCP,
    regSummary$cp[aCP],
    labels = aCP,
    pos = 3)
plot(
 regSummary$bic,
 xlab = "Number of regressors - SeqRep - Differences",
 ylab = "BIC",
 type = "1"
points(
 aBIC,
 regSummary$bic[aBIC],
 col = "red",
 cex = 2,
 pch = 20
text(aBIC,
    regSummary$bic[aBIC],
    labels = aBIC,
   pos = 3)
```

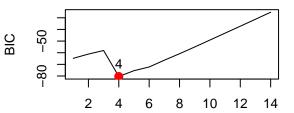




Number of regressors - SeqRep - Differences

Number of regressors – SeqRep – Differences

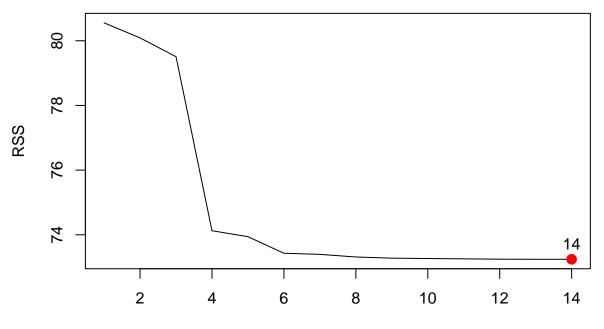




Number of regressors – SeqRep – Differences

Number of regressors – SeqRep – Differences

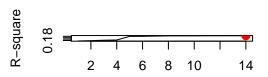
```
par(mfrow = c(1, 1))
plot(
  regSummary$rss,
  xlab = "Number of regressors - SeqRep - Differences",
  ylab = "RSS",
  type = "1"
)
points(
  aRSS,
  regSummary$rss[aRSS],
  col = "red",
  cex = 2,
  pch = 20
text(aRSS,
     regSummary$rss[aRSS],
     labels = aRSS,
     pos = 3)
```

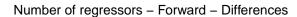


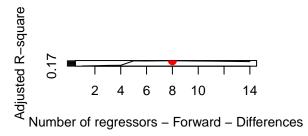
Number of regressors - SeqRep - Differences

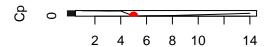
```
data=dfDiff,
  method= 'forward',
  nvmax=17)
## Warning in leaps.setup(x, y, wt = wt, nbest = nbest, nvmax = nvmax,
## force.in = force.in, : 2 linear dependencies found
## Reordering variables and trying again:
## Warning in rval$lopt[] <- rval$vorder[rval$lopt]: number of items to</pre>
## replace is not a multiple of replacement length
regSummary <- summary(regFitSelect)</pre>
names(regSummary)
                                                                "outmat" "obj"
## [1] "which" "rsq"
                          "rss"
                                   "adjr2" "cp"
                                                      "bic"
regSummary$rsq
## [1] 0.1731698 0.1779456 0.1839180 0.1871817 0.2391704 0.2399022 0.2433283
## [8] 0.2463473 0.2466978 0.2469470 0.2479080 0.2480453 0.2481380 0.2482272
regSummary$adjr2
## [1] 0.1711130 0.1738456 0.1777974 0.1790331 0.2296123 0.2284146 0.2299528
## [8] 0.2310835 0.2294904 0.2277853 0.2268034 0.2249674 0.2230759 0.2211711
par(mfrow=c(2,2))
aRSQ <- which.max(regSummary$rsq)</pre>
aARSQ <- which.max(regSummary$adjr2)</pre>
aCP <- which.min(regSummary$cp)</pre>
aBIC <- which.min(regSummary$bic)</pre>
aRSS <- which.min(regSummary$rss)</pre>
par(mfrow = c(2, 2))
plot(
  regSummary$rsq,
 xlab = "Number of regressors - Forward - Differences",
  ylab = "R-square",
  type = "1"
points(
  aRSQ,
  regSummary$rsq[aRSQ],
  col = "red",
  cex = 2,
  pch = 20
text(aRSQ,
     regSummary$rsq[aRSQ],
     labels = aRSQ,
     pos = 1)
plot(
  regSummary$adjr2,
  xlab = "Number of regressors - Forward - Differences",
```

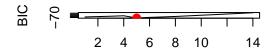
```
ylab = "Adjusted R-square",
 type = "1"
points(
 aARSQ,
  regSummary$adjr2[aARSQ],
 col = "red",
 cex = 2,
  pch = 20
text(aARSQ,
     regSummary$adjr2[aARSQ],
     labels = aARSQ,
     pos = 1)
plot(regSummary$cp,
     xlab = "Number of regressors - Forward - Differences",
     ylab = "Cp",
     type = "1")
points(
  aCP,
 regSummary$cp[aCP],
 col = "red",
  cex = 2,
  pch = 20
text(aCP,
     regSummary$cp[aCP],
     labels = aCP,
     pos = 3)
plot(
  regSummary$bic,
  xlab = "Number of regressors - Forward - Differences",
 ylab = "BIC",
 type = "1"
points(
 aBIC,
 regSummary$bic[aBIC],
 col = "red",
 cex = 2,
  pch = 20
text(aBIC,
     regSummary$bic[aBIC],
     labels = aBIC,
    pos = 3)
```







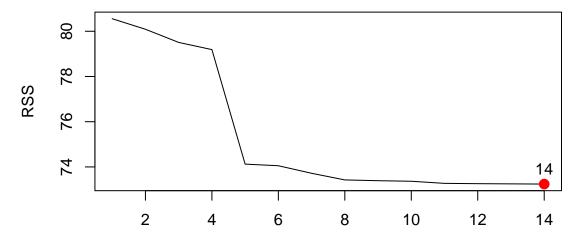




Number of regressors – Forward – Differences

Number of regressors – Forward – Differences

```
par(mfrow = c(1, 1))
plot(
  regSummary$rss,
  xlab = "Number of regressors - Forward - Differences",
  ylab = "RSS",
  type = "1"
points(
  aRSS,
  regSummary$rss[aRSS],
  col = "red",
  cex = 2,
  pch = 20
text(aRSS,
     regSummary$rss[aRSS],
     labels = aRSS,
     pos = 3)
```



Number of regressors – Forward – Differences

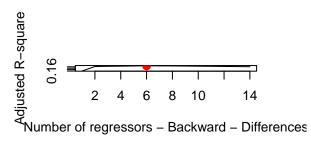
```
par(mfrow = c(2, 2))
plot(regFitSelect, scale = "r2")
plot(regFitSelect, scale = "adjr2")
plot(regFitSelect, scale = "Cp")
plot(regFitSelect, scale = "bic")
인 0,25 1
valuesForward <- c(names(coef(regFitSelect, id = 5))[-1])</pre>
# Backward
regFitSelect <- regsubsets(</pre>
  postotalSSRetired~.,
  data=dfDiff,
  method= 'backward',
  nvmax=17)
```

## Warning in leaps.setup(x, y, wt = wt, nbest = nbest, nvmax = nvmax,

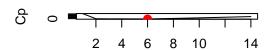
```
## force.in = force.in, : 2 linear dependencies found
## Reordering variables and trying again:
## Warning in rval$lopt[] <- rval$vorder[rval$lopt]: number of items to</pre>
## replace is not a multiple of replacement length
regSummary <- summary(regFitSelect)</pre>
names(regSummary)
                                                                "outmat" "obj"
## [1] "which" "rsq"
                          "rss"
                                   "adjr2" "cp"
                                                       "bic"
regSummary$rsq
## [1] 0.1630296 0.2273926 0.2330672 0.2364933 0.2410517 0.2463118 0.2464133
## [8] 0.2474956 0.2478743 0.2479814 0.2480829 0.2481942 0.2482266 0.2482272
regSummary$adjr2
   [1] 0.1609476 0.2235392 0.2273153 0.2288391 0.2315172 0.2349210 0.2330923
## [8] 0.2322550 0.2306938 0.2288461 0.2269832 0.2251209 0.2231675 0.2211711
par(mfrow=c(2,2))
aRSQ <- which.max(regSummary$rsq)</pre>
aARSQ <- which.max(regSummary$adjr2)</pre>
aCP <- which.min(regSummary$cp)</pre>
aBIC <- which.min(regSummary$bic)</pre>
aRSS <- which.min(regSummary$rss)</pre>
par(mfrow = c(2, 2))
plot(
  regSummary$rsq,
  xlab = "Number of regressors - Backward - Differences",
  ylab = "R-square",
  type = "1"
points(
  aRSQ,
  regSummary$rsq[aRSQ],
  col = "red",
  cex = 2,
  pch = 20
text(aRSQ,
     regSummary$rsq[aRSQ],
     labels = aRSQ,
     pos = 1)
plot(
  regSummary$adjr2,
  xlab = "Number of regressors - Backward - Differences",
  ylab = "Adjusted R-square",
  type = "1"
points(
  aARSQ,
regSummary$adjr2[aARSQ],
```

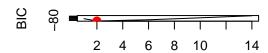
```
col = "red",
  cex = 2,
  pch = 20
)
text(aARSQ,
     regSummary$adjr2[aARSQ],
    labels = aARSQ,
    pos = 1)
plot(regSummary$cp,
     xlab = "Number of regressors - Backward - Differences",
     ylab = "Cp",
     type = "1")
points(
  aCP,
  regSummary$cp[aCP],
  col = "red",
 cex = 2,
  pch = 20
)
text(aCP,
    regSummary$cp[aCP],
    labels = aCP,
    pos = 3)
plot(
  regSummary$bic,
 xlab = "Number of regressors - Backward - Differences",
 ylab = "BIC",
 type = "1"
points(
  aBIC,
 regSummary$bic[aBIC],
 col = "red",
 cex = 2,
 pch = 20
text(aBIC,
    regSummary$bic[aBIC],
    labels = aBIC,
   pos = 3)
```





Number of regressors – Backward – Differences

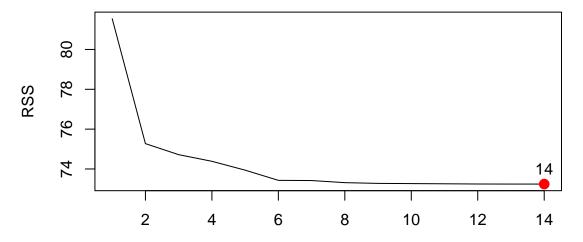




Number of regressors – Backward – Differences

Number of regressors - Backward - Differences

```
par(mfrow = c(1, 1))
plot(
  regSummary$rss,
  xlab = "Number of regressors - Backward - Differences",
  ylab = "RSS",
  type = "1"
points(
  aRSS,
  regSummary$rss[aRSS],
  col = "red",
  cex = 2,
  pch = 20
text(aRSS,
     regSummary$rss[aRSS],
     labels = aRSS,
     pos = 3)
```



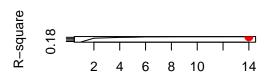
Number of regressors - Backward - Differences

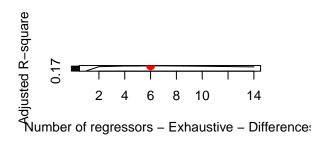
```
par(mfrow = c(2, 2))
plot(regFitSelect, scale = "r2")
plot(regFitSelect, scale = "adjr2")
plot(regFitSelect, scale = "Cp")
plot(regFitSelect, scale = "bic")
2 0,16
<del>30000</del>
valuesBackward <- c(names(coef(regFitSelect, id = 6))[-1])</pre>
# Exhaustive
regFitSelect <- regsubsets(</pre>
  postotalSSRetired~.,
  data=dfDiff,
  method= 'exhaustive',
  nvmax=17)
```

## Warning in leaps.setup(x, y, wt = wt, nbest = nbest, nvmax = nvmax,

```
## force.in = force.in, : 2 linear dependencies found
## Reordering variables and trying again:
regSummary <- summary(regFitSelect)</pre>
names(regSummary)
## [1] "which" "rsq"
                                   "adjr2" "cp"
                                                                "outmat" "obj"
                          "rss"
                                                       "bic"
regSummary$rsq
## [1] 0.1731698 0.2273926 0.2330672 0.2391592 0.2410517 0.2463118 0.2466627
## [8] 0.2474956 0.2478743 0.2479814 0.2480829 0.2481942 0.2482266 0.2482272
regSummary$adjr2
## [1] 0.1711130 0.2235392 0.2273153 0.2315317 0.2315172 0.2349210 0.2333461
## [8] 0.2322550 0.2306938 0.2288461 0.2269832 0.2251209 0.2231675 0.2211711
par(mfrow=c(2,2))
aRSQ <- which.max(regSummary$rsq)</pre>
aARSQ <- which.max(regSummary$adjr2)</pre>
aCP <- which.min(regSummary$cp)</pre>
aBIC <- which.min(regSummary$bic)</pre>
aRSS <- which.min(regSummary$rss)</pre>
par(mfrow = c(2, 2))
plot(
  regSummary$rsq,
  xlab = "Number of regressors - Exhaustive - Differences",
 ylab = "R-square",
  type = "1"
)
points(
  aRSQ,
  regSummary$rsq[aRSQ],
  col = "red",
  cex = 2,
  pch = 20
text(aRSQ,
     regSummary$rsq[aRSQ],
     labels = aRSQ,
     pos = 1)
plot(
  regSummary$adjr2,
  xlab = "Number of regressors - Exhaustive - Differences",
  ylab = "Adjusted R-square",
  type = "1"
points(
  aARSQ,
 regSummary$adjr2[aARSQ],
  col = "red",
cex = 2,
```

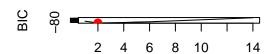
```
pch = 20
text(aARSQ,
     regSummary$adjr2[aARSQ],
     labels = aARSQ,
     pos = 1)
plot(regSummary$cp,
     xlab = "Number of regressors - Exhaustive - Differences",
     ylab = "Cp",
     type = "1")
points(
  aCP,
  regSummary$cp[aCP],
  col = "red",
  cex = 2,
  pch = 20
text(aCP,
     regSummary$cp[aCP],
     labels = aCP,
     pos = 3)
plot(
  regSummary$bic,
  xlab = "Number of regressors - Exhaustive - Differences",
 ylab = "BIC",
  type = "1"
points(
  regSummary$bic[aBIC],
  col = "red",
  cex = 2,
  pch = 20
text(aBIC,
    regSummary$bic[aBIC],
    labels = aBIC,
   pos = 3)
```





Number of regressors – Exhaustive – Difference:

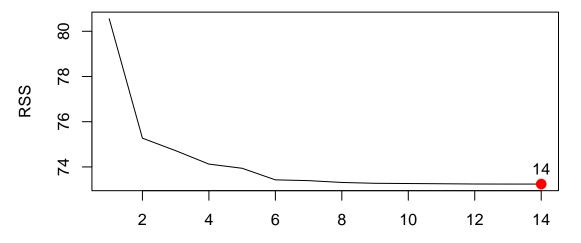




Number of regressors – Exhaustive – Difference:

Number of regressors - Exhaustive - Difference:

```
par(mfrow = c(1, 1))
plot(
  regSummary$rss,
  xlab = "Number of regressors - Exhaustive - Differences",
  ylab = "RSS",
  type = "1"
points(
  aRSS,
  regSummary$rss[aRSS],
  col = "red",
  cex = 2,
  pch = 20
text(aRSS,
     regSummary$rss[aRSS],
     labels = aRSS,
     pos = 3)
```



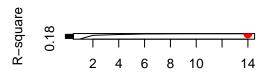
Number of regressors – Exhaustive – Differences

```
par(mfrow = c(2, 2))
plot(regFitSelect, scale = "r2")
plot(regFitSelect, scale = "adjr2")
plot(regFitSelect, scale = "Cp")
plot(regFitSelect, scale = "bic")
₩ 0,116
<u>ც</u>—მ
valuesExhaustive <- c(names(coef(regFitSelect, id = 4))[-1])</pre>
# Percentages - Fairly low value, not going to use ####
regFitSelect <- regsubsets(</pre>
  postotalSSRetired~.,
  data=dfPerc,
  nvmax=17)
```

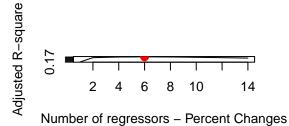
## Warning in leaps.setup(x, y, wt = wt, nbest = nbest, nvmax = nvmax,

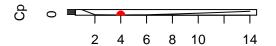
```
## force.in = force.in, : 2 linear dependencies found
## Reordering variables and trying again:
regSummary <- summary(regFitSelect)</pre>
names(regSummary)
## [1] "which" "rsq"
                                   "adjr2" "cp"
                                                                "outmat" "obj"
                          "rss"
                                                       "bic"
regSummary$rsq
## [1] 0.1734833 0.2178484 0.2228415 0.2279842 0.2305041 0.2344034 0.2348847
## [8] 0.2361503 0.2366112 0.2368900 0.2370863 0.2371085 0.2371529 0.2371530
regSummary$adjr2
## [1] 0.1714273 0.2139474 0.2170129 0.2202447 0.2208371 0.2228327 0.2213599
## [8] 0.2206799 0.2191734 0.2174725 0.2156780 0.2136949 0.2117246 0.2096984
par(mfrow=c(2,2))
aRSQ <- which.max(regSummary$rsq)</pre>
aARSQ <- which.max(regSummary$adjr2)</pre>
aCP <- which.min(regSummary$cp)</pre>
aBIC <- which.min(regSummary$bic)</pre>
aRSS <- which.min(regSummary$rss)</pre>
par(mfrow = c(2, 2))
plot(
  regSummary$rsq,
  xlab = "Number of regressors - Percent Changes",
 ylab = "R-square",
  type = "1"
)
points(
  aRSQ,
  regSummary$rsq[aRSQ],
  col = "red",
  cex = 2,
  pch = 20
text(aRSQ,
     regSummary$rsq[aRSQ],
     labels = aRSQ,
     pos = 1)
plot(
  regSummary$adjr2,
  xlab = "Number of regressors - Percent Changes",
  ylab = "Adjusted R-square",
  type = "1"
points(
  aARSQ,
 regSummary$adjr2[aARSQ],
  col = "red",
cex = 2,
```

```
pch = 20
text(aARSQ,
     regSummary$adjr2[aARSQ],
     labels = aARSQ,
     pos = 1)
plot(regSummary$cp,
     xlab = "Number of regressors - Percent Changes",
     ylab = "Cp",
     type = "1")
points(
  aCP,
  regSummary$cp[aCP],
  col = "red",
  cex = 2,
  pch = 20
text(aCP,
     regSummary$cp[aCP],
     labels = aCP,
     pos = 3)
plot(
  regSummary$bic,
  xlab = "Number of regressors - Percent Changes",
 ylab = "BIC",
  type = "1"
points(
  regSummary$bic[aBIC],
  col = "red",
  cex = 2,
  pch = 20
text(aBIC,
    regSummary$bic[aBIC],
    labels = aBIC,
   pos = 3)
```



Number of regressors – Percent Changes



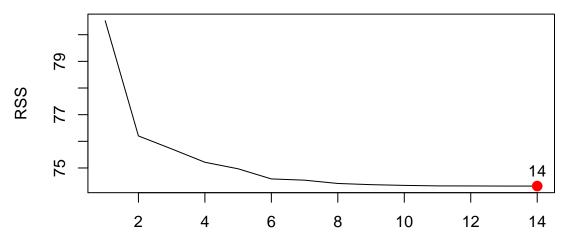


Number of regressors – Percent Changes



Number of regressors – Percent Changes

```
par(mfrow = c(1, 1))
plot(
  regSummary$rss,
  xlab = "Number of regressors - Percent Changes",
  ylab = "RSS",
  type = "1"
points(
  aRSS,
  regSummary$rss[aRSS],
  col = "red",
  cex = 2,
  pch = 20
text(aRSS,
     regSummary$rss[aRSS],
     labels = aRSS,
     pos = 3)
```

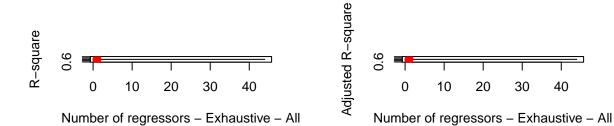


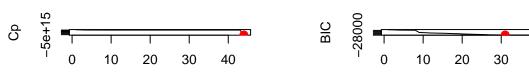
Number of regressors - Percent Changes

```
par(mfrow = c(2, 2))
plot(regFitSelect, scale = "r2")
plot(regFitSelect, scale = "adjr2")
plot(regFitSelect, scale = "Cp")
plot(regFitSelect, scale = "bic")
인 이14
S 034
                                                                       gg
# All Data Selection ####
# Exhaustive - All Data
regFitSelect <- regsubsets(</pre>
  postotalSSRetired~.,
  data=dfStationary[-1],
  method= 'exhaustive',
  really.big = TRUE,
  nvmax=56)
```

```
## Warning in leaps.setup(x, y, wt = wt, nbest = nbest, nvmax = nvmax,
## force.in = force.in, : 12 linear dependencies found
## Reordering variables and trying again:
regSummary <- summary(regFitSelect)</pre>
## Warning in log(vr): NaNs produced
names(regSummary)
## [1] "which" "rsq"
                              "adjr2" "cp"
                                               "bic"
                                                       "outmat" "obj"
                      "rss"
regSummary$rsq
## [36] 1 1 1 1 1 1 1 1 1
regSummary$adjr2
## [36] 1 1 1 1 1 1 1 1 1
par(mfrow=c(2,2))
aRSQ <- which.max(regSummary$rsq)</pre>
aARSQ <- which.max(regSummary$adjr2)</pre>
aCP <- which.min(regSummary$cp)
aBIC <- which.min(regSummary$bic)</pre>
aRSS <- which.min(regSummary$rss)
par(mfrow = c(2, 2))
plot(
 regSummary$rsq,
 xlab = "Number of regressors - Exhaustive - All",
 ylab = "R-square",
 type = "1"
points(
 aRSQ,
 regSummary$rsq[aRSQ],
 col = "red",
 cex = 2,
 pch = 20
text(aRSQ,
    regSummary$rsq[aRSQ],
    labels = aRSQ,
    pos = 1)
plot(
 regSummary$adjr2,
 xlab = "Number of regressors - Exhaustive - All",
 ylab = "Adjusted R-square",
 type = "1"
points(
 aARSQ,
```

```
regSummary$adjr2[aARSQ],
  col = "red",
  cex = 2,
  pch = 20
text(aARSQ,
     regSummary$adjr2[aARSQ],
     labels = aARSQ,
     pos = 1)
plot(regSummary$cp,
     xlab = "Number of regressors - Exhaustive - All",
     ylab = "Cp",
     type = "1")
points(
 aCP,
  regSummary$cp[aCP],
  col = "red",
 cex = 2,
  pch = 20
text(aCP,
     regSummary$cp[aCP],
     labels = aCP,
     pos = 3)
plot(
  regSummary$bic,
 xlab = "Number of regressors - Exhaustive - All",
 ylab = "BIC",
 type = "1"
points(
 aBIC,
  regSummary$bic[aBIC],
 col = "red",
 cex = 2,
  pch = 20
text(aBIC,
    regSummary$bic[aBIC],
    labels = aBIC,
    pos = 3)
```



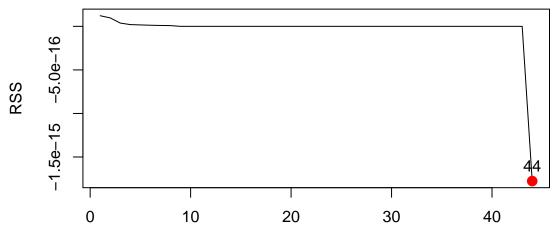


Number of regressors – Exhaustive – All

Number of regressors - Exhaustive - All

40

```
par(mfrow = c(1, 1))
plot(
  regSummary$rss,
  xlab = "Number of regressors - Exhaustive - All",
  ylab = "RSS",
  type = "1"
points(
  aRSS,
  regSummary$rss[aRSS],
  col = "red",
  cex = 2,
  pch = 20
text(aRSS,
     regSummary$rss[aRSS],
     labels = aRSS,
     pos = 3)
```



Number of regressors - Exhaustive - All

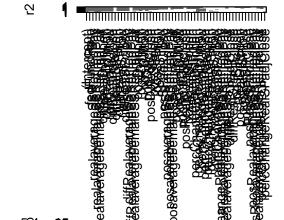
```
par(mfrow = c(2, 2))
plot(regFitSelect, scale = "r2")

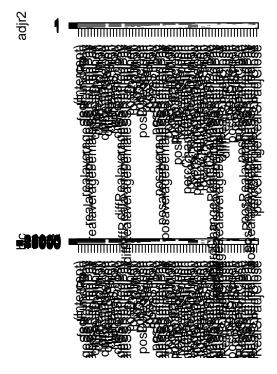
## Warning in log(vr): NaNs produced
plot(regFitSelect, scale = "adjr2")

## Warning in log(vr): NaNs produced
plot(regFitSelect, scale = "Cp")

## Warning in log(vr): NaNs produced
plot(regFitSelect, scale = "bic")

## Warning in log(vr): NaNs produced
```



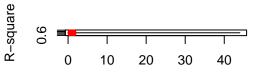


```
valuesStatExhaustive <- c(names(coef(regFitSelect, id = 31))[-1])</pre>
## Warning in log(vr): NaNs produced
# Backward
regFitSelect <- regsubsets(</pre>
 postotalSSRetired~.,
 data=dfStationary[-1],
 method= 'backward',
 really.big = TRUE,
 nvmax=55)
## Warning in leaps.setup(x, y, wt = wt, nbest = nbest, nvmax = nvmax,
## force.in = force.in, : 12 linear dependencies found
## Reordering variables and trying again:
## Warning in rval$lopt[] <- rval$vorder[rval$lopt]: number of items to</pre>
## replace is not a multiple of replacement length
regSummary <- summary(regFitSelect)</pre>
names(regSummary)
## [1] "which" "rsq"
                       "rss"
                                "adjr2" "cp"
                                                 "bic"
                                                         "outmat" "obj"
regSummary$rsq
## [36] 1 1 1 1 1 1 1 1 1
regSummary$adjr2
## [36] 1 1 1 1 1 1 1 1 1
par(mfrow=c(2,2))
aRSQ <- which.max(regSummary$rsq)</pre>
aARSQ <- which.max(regSummary$adjr2)</pre>
aCP <- which.min(regSummary$cp)</pre>
aBIC <- which.min(regSummary$bic)</pre>
aRSS <- which.min(regSummary$rss)</pre>
par(mfrow = c(2, 2))
plot(
 regSummary$rsq,
 xlab = "Number of regressors - Backward - All",
 ylab = "R-square",
 type = "1"
points(
 aRSQ,
 regSummary$rsq[aRSQ],
 col = "red",
  cex = 2,
 pch = 20
text(aRSQ,
```

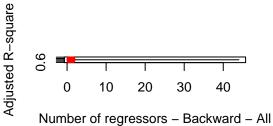
```
regSummary$rsq[aRSQ],
     labels = aRSQ,
     pos = 1)
plot(
 regSummary$adjr2,
 xlab = "Number of regressors - Backward - All",
 ylab = "Adjusted R-square",
 type = "1"
points(
 aARSQ,
  regSummary$adjr2[aARSQ],
 col = "red",
 cex = 2,
 pch = 20
text(aARSQ,
     regSummary$adjr2[aARSQ],
     labels = aARSQ,
     pos = 1)
plot(regSummary$cp,
     xlab = "Number of regressors - Backward - All",
     ylab = "Cp",
     type = "1")
points(
  aCP,
 regSummary$cp[aCP],
 col = "red",
 cex = 2,
  pch = 20
text(aCP,
     regSummary$cp[aCP],
     labels = aCP,
     pos = 3)
plot(
  regSummary$bic,
 xlab = "Number of regressors - Backward - All",
 ylab = "BIC",
 type = "1"
points(
 aBIC,
 regSummary$bic[aBIC],
 col = "red",
 cex = 2,
  pch = 20
)
text(aBIC,
    regSummary$bic[aBIC],
```

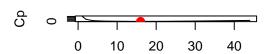
```
labels = aBIC,
pos = 3)

eg
```

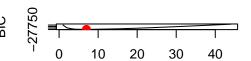


Number of regressors - Backward - All



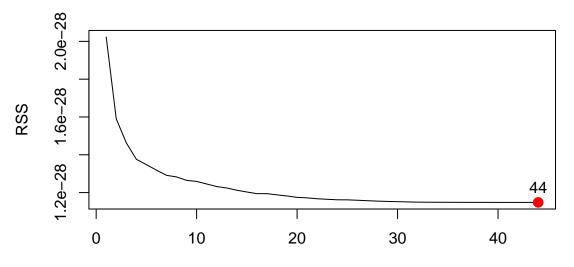


Number of regressors – Backward – All



Number of regressors - Backward - All

```
par(mfrow = c(1, 1))
plot(
  regSummary$rss,
  xlab = "Number of regressors - Backward - All",
  ylab = "RSS",
  type = "1"
points(
  aRSS,
  regSummary$rss[aRSS],
  col = "red",
  cex = 2,
  pch = 20
text(aRSS,
     regSummary$rss[aRSS],
     labels = aRSS,
     pos = 3)
```

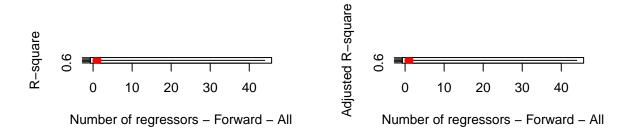


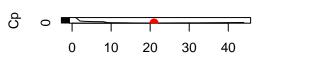
Number of regressors - Backward - All

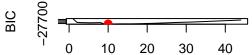
```
par(mfrow = c(2, 2))
plot(regFitSelect, scale = "r2")
plot(regFitSelect, scale = "adjr2")
plot(regFitSelect, scale = "Cp")
plot(regFitSelect, scale = "bic")
                                            adjr2
ū
        valuesStatBackward <- c(names(coef(regFitSelect, id = 7))[-1])</pre>
# Forward
regFitSelect <- regsubsets(</pre>
 postotalSSRetired~.,
 data=dfStationary[-1],
 method= 'forward',
 really.big = TRUE,
```

```
nvmax=55)
## Warning in leaps.setup(x, y, wt = wt, nbest = nbest, nvmax = nvmax,
## force.in = force.in, : 12 linear dependencies found
## Reordering variables and trying again:
## Warning in rval$lopt[] <- rval$vorder[rval$lopt]: number of items to
## replace is not a multiple of replacement length
regSummary <- summary(regFitSelect)</pre>
names(regSummary)
## [1] "which" "rsq"
                                                        "outmat" "obj"
                       "rss"
                               "adjr2" "cp"
                                               "bic"
regSummary$rsq
## [36] 1 1 1 1 1 1 1 1 1
regSummary$adjr2
## [36] 1 1 1 1 1 1 1 1 1
par(mfrow=c(2,2))
aRSQ <- which.max(regSummary$rsq)</pre>
aARSQ <- which.max(regSummary$adjr2)</pre>
aCP <- which.min(regSummary$cp)</pre>
aBIC <- which.min(regSummary$bic)
aRSS <- which.min(regSummary$rss)</pre>
par(mfrow = c(2, 2))
plot(
 regSummary$rsq,
 xlab = "Number of regressors - Forward - All",
 ylab = "R-square",
 type = "1"
)
points(
 aRSQ,
 regSummary$rsq[aRSQ],
 col = "red",
 cex = 2,
 pch = 20
text(aRSQ,
    regSummary$rsq[aRSQ],
    labels = aRSQ,
    pos = 1)
plot(
 regSummary$adjr2,
 xlab = "Number of regressors - Forward - All",
 ylab = "Adjusted R-square",
 type = "1"
```

```
points(
  aARSQ,
  regSummary$adjr2[aARSQ],
  col = "red",
  cex = 2,
  pch = 20
text(aARSQ,
     regSummary$adjr2[aARSQ],
     labels = aARSQ,
     pos = 1)
plot(regSummary$cp,
     xlab = "Number of regressors - Forward - All",
     ylab = "Cp",
     type = "1")
points(
  aCP,
  regSummary$cp[aCP],
  col = "red",
  cex = 2,
 pch = 20
text(aCP,
     regSummary$cp[aCP],
     labels = aCP,
     pos = 3)
plot(
 regSummary$bic,
  xlab = "Number of regressors - Forward - All",
 ylab = "BIC",
  type = "1"
points(
 aBIC,
 regSummary$bic[aBIC],
 col = "red",
  cex = 2,
  pch = 20
text(aBIC,
     regSummary$bic[aBIC],
     labels = aBIC,
    pos = 3)
```



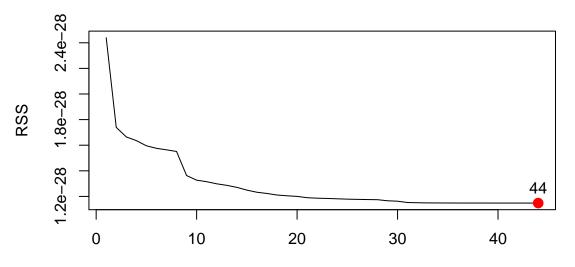




Number of regressors - Forward - All

Number of regressors - Forward - All

```
par(mfrow = c(1, 1))
plot(
  regSummary$rss,
  xlab = "Number of regressors - Forward - All",
  ylab = "RSS",
  type = "1"
points(
  aRSS,
  regSummary$rss[aRSS],
  col = "red",
  cex = 2,
  pch = 20
text(aRSS,
     regSummary$rss[aRSS],
     labels = aRSS,
     pos = 3)
```



Number of regressors – Forward – All

```
par(mfrow = c(2, 2))
plot(regFitSelect, scale = "r2")
plot(regFitSelect, scale = "adjr2")
plot(regFitSelect, scale = "Cp")
plot(regFitSelect, scale = "bic")
                                             adjr2
ū
       valuesStatForward <- c(names(coef(regFitSelect, id = 10))[-1])</pre>
fmlaForward <- as.formula(paste("postotalSSRetired ~ ", paste(valuesStatForward, collapse= "+")))</pre>
fmlaBackward <- as.formula(paste("postotalSSRetired ~ ", paste(valuesStatBackward, collapse= "+")))</pre>
fmlaExhaust <- as.formula(paste("postotalSSRetired ~ ", paste(valuesStatExhaustive, collapse= "+")))</pre>
```

# Model ####

# Setting train/test split

```
set.seed(1)
trainSample <- sample(1:nrow(dfStationary), round(nrow(dfStationary)/2), replace = F)
trainData <- dfStationary[trainSample,]</pre>
testData <- dfStationary[-trainSample,]</pre>
trainX <- trainData[,c(1, 3:58)]</pre>
trainY <- trainData[,c(1:2)]</pre>
testX <- testData[,c(1, 3:58)]
trainY <- testData[,c(1:2)]</pre>
# Logistic ####
# Exhaustive Selected model
logFit <- glm(fmlaExhaust,</pre>
              family = binomial,
              data = dfStationary)
## Warning: glm.fit: algorithm did not converge
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
summary(logFit, diagnostics=TRUE)
##
## Call:
## glm(formula = fmlaExhaust, family = binomial, data = dfStationary)
## Deviance Residuals:
         Min
                            Median
                     1Q
                                            3Q
                                                      Max
## -6.65e-05 -2.10e-08 -2.10e-08
                                      2.10e-08
                                                 7.67e-05
##
## Coefficients:
##
                                        Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                                      -3.740e+02 2.429e+06
                                                              0.000
## fedFundRate
                                      -1.826e+00 5.610e+04
                                                              0.000
                                                                        1.000
## realaverageSSRetiredPay
                                       4.457e-01 3.568e+03
                                                              0.000
                                                                        1.000
## realaverageMaleSSRetiredPay
                                       3.177e-01 1.549e+03
                                                              0.000
                                                                        1.000
## realaverageFemaleSSRetiredPay
                                      -7.487e-01 1.798e+03
                                                              0.000
                                                                        1.000
                                      8.708e-02 2.692e+02
                                                              0.000
                                                                        1.000
## diffRealDJIopen
## diffRealDJIhigh
                                      -9.536e-02 3.648e+02
                                                              0.000
                                                                        1.000
## diffRealDJIlow
                                      -9.996e-02 2.308e+02
                                                              0.000
                                                                        1.000
## diffRealDJIclose
                                      1.026e-01 2.825e+02
                                                              0.000
                                                                        1.000
## diffRealSPhigh
                                      -5.578e-02 9.441e+02
                                                              0.000
                                                                        1.000
## diffRealSPlow
                                       9.387e-01 2.054e+03
                                                              0.000
                                                                        1.000
## diffRealSPclose
                                      -8.024e-01 1.307e+03 -0.001
                                                                        1.000
## diffRealaverageSSRetiredPay
                                      -2.077e+00 1.769e+03 -0.001
                                                                        0.999
## diffRealaverageFemaleSSRetiredPay 2.315e+00 2.784e+03
                                                              0.001
                                                                        0.999
## posDJIopen
                                      -8.073e+00 3.913e+05
                                                              0.000
                                                                        1.000
## posDJIhigh
                                       8.907e+01 1.074e+05
                                                              0.001
                                                                        0.999
## posDJIlow
                                      -7.844e+00 1.396e+05
                                                              0.000
                                                                        1.000
## posDJIclose
                                      -8.014e+01 1.063e+05 -0.001
                                                                        0.999
## posDJIadjClose
                                      4.842e+01 8.540e+04
                                                              0.001
                                                                        1.000
## posSPopen
                                      -9.421e+00 1.519e+05
                                                              0.000
                                                                        1.000
                                      -5.175e+00 7.073e+04
                                                              0.000
## posSPhigh
                                                                        1.000
## posSPlow
                                      1.310e+01 3.304e+05
                                                              0.000
                                                                        1.000
```

```
## posSPadiClose
                                     -5.501e+01 8.350e+04 -0.001
                                                                     0.999
## posaverageSSRetiredPay
                                     1.374e+01 1.007e+05
                                                                     1.000
                                                            0.000
                                                            0.000
## posaverageFemaleSSRetiredPay
                                    -6.536e+01 2.678e+05
                                                                     1.000
## posRealDJIhigh
                                     -1.473e+00 8.302e+04
                                                            0.000
                                                                     1.000
## posRealDJIlow
                                    -1.582e+01 1.677e+05
                                                            0.000
                                                                     1.000
                                                                     0.999
## posRealDJIclose
                                     4.006e+01 6.266e+04
                                                            0.001
                                                                     0.998
## posRealSPopen
                                    1.578e+02 5.881e+04
                                                            0.003
                                     9.575e+01 3.884e+04
                                                                     0.998
## posRealSPhigh
                                                            0.002
## percChangeRealDJIopen
                                    -1.179e+03 4.426e+06
                                                            0.000
                                                                     1.000
                                                                     1.000
## percChangeRealDJIhigh
                                    1.768e+03 5.401e+06
                                                            0.000
## (Dispersion parameter for binomial family taken to be 1)
       Null deviance: 5.4568e+02 on 403 degrees of freedom
##
## Residual deviance: 4.0544e-08 on 372 degrees of freedom
## AIC: 64
##
## Number of Fisher Scoring iterations: 25
confint(logFit)
## Waiting for profiling to be done...
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
```

```
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
```

```
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: algorithm did not converge
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
```

```
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
##
                                             2.5 %
                                                          97.5 %
## (Intercept)
                                                NA 252002.49723
## fedFundRate
                                     -3.983147e+03
                                                     4703.37124
## realaverageSSRetiredPay
                                     -2.546648e+02
                                                      268.77575
## realaverageMaleSSRetiredPay
                                     -8.577694e+01
                                                       77.87345
## realaverageFemaleSSRetiredPay
                                     -9.572672e+01
                                                        76.17133
## diffRealDJIopen
                                                        8.84281
                                     -9.242949e+00
## diffRealDJIhigh
                                     -1.829923e+01
                                                        16.61109
## diffRealDJIlow
                                                        16.18882
                                     -1.504885e+01
## diffRealDJIclose
                                     -1.549278e+01
                                                        15.26941
## diffRealSPhigh
                                     -8.653673e+01
                                                        94.17654
## diffRealSPlow
                                     -9.404891e+01
                                                        84.85045
## diffRealSPclose
                                     -5.913237e+01
                                                        52.72950
## diffRealaverageSSRetiredPay
                                     -6.627266e+01
                                                       70.74603
## diffRealaverageFemaleSSRetiredPay -1.311546e+02
                                                      162.12368
## posDJIopen
                                     -2.341307e+04 26188.87448
## posDJIhigh
                                     -3.817369e+03
                                                    4672.39169
## posDJIlow
                                     -6.241243e+03
                                                     5712.80741
## posDJIclose
                                     -8.751598e+03
                                                     8591.31205
## posDJIadjClose
                                                     4000.15889
                                     -4.072687e+03
## posSPopen
                                     -6.995852e+03 8452.16400
## posSPhigh
                                     -3.335126e+03
                                                    3324.77570
                                     -1.239607e+04 15042.40911
## posSPlow
## posSPadjClose
                                     -3.586792e+03
                                                    3898.06575
## posaverageSSRetiredPay
                                     -3.065634e+03
                                                     3148.67282
                                     -1.515226e+04 16011.10232
## posaverageFemaleSSRetiredPay
## posRealDJIhigh
                                     -6.244430e+03
                                                    5933.91934
## posRealDJIlow
                                     -8.292697e+03
                                                    6536.94787
## posRealDJIclose
                                     -5.699962e+03
                                                     6294.56015
## posRealSPopen
                                     -1.457712e+03
                                                     1784.94750
                                     -1.023044e+03
                                                     1260.88953
## posRealSPhigh
## percChangeRealDJIopen
                                     -1.509047e+05 150183.97188
## percChangeRealDJIhigh
                                     -2.276793e+05 227418.56595
logProbs <- predict(logFit, type = 'response')</pre>
logProbs[1:10]
##
                           3
                                                     5
                                                                   6
                                        4
## 2.220446e-16 1.000000e+00 2.220446e-16 2.220446e-16 2.220446e-16
                                        9
                           8
## 1.000000e+00 4.891675e-10 2.220446e-16 2.220446e-16 1.000000e+00
logPred <- rep(NA, dim(dfStationary)[2])</pre>
logPred[logProbs > 0.5] <- 1</pre>
logPred[logProbs < 0.5] = 0
table(logPred)
## logPred
## 0
         1
```

## 240 164

```
table(logPred, dfStationary[,2])
##
## logPred
             0
##
         0 240 0
##
         1 0 164
mean(logPred == dfStationary[,2])
## [1] 1
# Testing Prediction
train <- subset(dfStationary, dfStationary$date < as.Date('2010-04-08'))</pre>
test3rdQuart <- subset(dfStationary, dfStationary, date >= as.Date('2010-04-08'))
logFit1 <- glm(fmlaExhaust,</pre>
               family = binomial,
               data = train)
## Warning: glm.fit: algorithm did not converge
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
logProbs1 <- predict(logFit1, test3rdQuart, type = 'response') # setting prediction for the testing set
logPred1 <- rep(NA, dim(train)[2])</pre>
logPred1[logProbs1 >= 0.5] = 1
logPred1[logProbs1 < 0.5] = 0
table(logPred1, test3rdQuart$postotalSSRetired)
##
## logPred1 0 1
          0 58 5
##
          1 1 37
mean(logPred1 == test3rdQuart$postotalSSRetired)
## [1] 0.9405941
Prediction accuracy is approximately 94% with a train/test split at the 3rd quartile mark of the dates.
Positive class prediction: 37/5; 88\% Negative Class prediction: 58/1; 98.3\%
# Backard Selected model
logFit <- glm(fmlaBackward,</pre>
              family = binomial,
              data = dfStationary)
summary(logFit, diagnostics=TRUE)
##
## Call:
## glm(formula = fmlaBackward, family = binomial, data = dfStationary)
##
## Deviance Residuals:
##
        Min
                   1Q
                          Median
                                        3Q
                                                  Max
## -2.87722 -0.16582 -0.06502 0.14678
                                              2.93502
##
## Coefficients:
```

```
Estimate Std. Error z value Pr(>|z|)
##
## (Intercept)
                                     -3.9626
                                                 0.8825 -4.490 7.12e-06 ***
## posDJIopen
                                                          0.854 0.392953
                                      1.0262
                                                 1.2013
## posaverageFemaleSSRetiredPay
                                                 1.2734 -1.856 0.063449 .
                                     -2.3635
## posRealDJIlow
                                      2.6609
                                                 0.7858
                                                          3.386 0.000708 ***
## posRealSPopen
                                      7.6607
                                                 0.8839
                                                          8.667 < 2e-16 ***
## percChangeRealDJIhigh
                                     31.9746 16.1912
                                                         1.975 0.048290 *
## posRealaverageFemaleSSRetiredPay -1.3853
                                                0.8903 -1.556 0.119728
                                                11.0572 -0.152 0.879418
## percChangeRealDJIadjClose
                                     -1.6774
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 545.68 on 403 degrees of freedom
## Residual deviance: 109.01 on 396 degrees of freedom
## AIC: 125.01
##
## Number of Fisher Scoring iterations: 7
confint(logFit)
##
                                         2.5 %
                                                   97.5 %
## (Intercept)
                                     -6.017531 -2.4528686
## posDJIopen
                                     -1.605622 3.2647653
## posaverageFemaleSSRetiredPay
                                     -4.803546 0.3041155
## posRealDJIlow
                                      1.316928 4.5526627
## posRealSPopen
                                      6.175544 9.7417619
## percChangeRealDJIhigh
                                      1.004724 64.9354675
## posRealaverageFemaleSSRetiredPay -3.220072 0.3118396
## percChangeRealDJIadjClose
                                    -23.719774 19.5259955
logProbs <- predict(logFit, type = 'response')</pre>
logProbs[1:10]
##
             2
                         3
                                                 5
## 0.004460318 0.974363975 0.011132525 0.002320106 0.001827138 0.996462622
                         9
                                    10
## 0.014180239 0.012967488 0.002486971 0.955606920
logPred <- rep(0, dim(dfStationary)[2])</pre>
logPred[logProbs >= 0.5] <- 1</pre>
logPred[logProbs < 0.5] <- 0</pre>
table(logPred)
## logPred
## 0
        1
## 235 169
table(logPred, dfStationary[,2])
##
## logPred
            0
##
         0 229
##
         1 11 158
```

```
mean(logPred == dfStationary[,2])
## [1] 0.9579208
# Testing Prediction
train <- subset(dfStationary, dfStationary$date < as.Date('2010-04-08'))</pre>
test3rdQuart <- subset(dfStationary, dfStationary$date >= as.Date('2010-04-08'))
logFit1 <- glm(fmlaBackward,</pre>
               family = binomial,
               data = train)
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
logProbs1 <- predict(logFit1, test3rdQuart, type = 'response') # setting prediction for the testing set
logPred1 <- rep(NA, dim(train)[2])</pre>
logPred1[logProbs1 >= 0.5] = 1
logPred1[logProbs1 < 0.5] = 0
table(logPred1, test3rdQuart$postotalSSRetired)
##
## logPred1 0 1
          0 53 3
##
          1 6 39
mean(logPred1 == test3rdQuart$postotalSSRetired)
## [1] 0.9108911
Prediction accuracy is approximately 91% with a train/test split at the 3rd quartile mark of the dates.
Positive class prediction: 39/3; 92.8% Negative Class prediction: 53/6; 89.8%
# Forward Selected model - Best Model
logFit <- glm(fmlaForward,</pre>
              family = binomial,
              data = dfStationary)
summary(logFit, diagnostics=TRUE)
##
## glm(formula = fmlaForward, family = binomial, data = dfStationary)
##
## Deviance Residuals:
        Min
                   1Q
                         Median
                                        3Q
                                                 Max
## -2.99923 -0.14379 -0.04962
                                 0.11169
                                             2.37220
## Coefficients:
                                     Estimate Std. Error z value Pr(>|z|)
                                                  1.1726 -4.828 1.38e-06 ***
## (Intercept)
                                      -5.6618
## posDJIopen
                                       0.9537
                                                  1.1957
                                                           0.798 0.4251
                                                                  0.0794 .
## posDJIclose
                                       1.6413
                                                  0.9356
                                                           1.754
## posDJIadjClose
                                                  0.7340
                                                           2.145 0.0320 *
                                       1.5744
## posaverageFemaleSSRetiredPay
                                      -2.0477
                                                  1.2833 -1.596 0.1106
## posRealSPopen
                                      8.2310
                                                  1.0236
                                                          8.041 8.90e-16 ***
## percChangeRealDJIhigh
                                      16.2008
                                                 16.7530
                                                           0.967 0.3335
```

```
## posRealSPadjClose
                                      1.7653
                                                 0.9697
                                                          1.821
                                                                  0.0687 .
## posRealaverageFemaleSSRetiredPay -1.7625
                                                 0.9146 -1.927
                                                                  0.0540 .
## percChangeRealDJIadjClose
                                     14.8932
                                                                  0.5533
                                                25.1203
                                                          0.593
## percChangeRealSPadjClose
                                     -8.7965
                                                24.4464 -0.360
                                                                  0.7190
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 545.68 on 403 degrees of freedom
## Residual deviance: 100.23 on 393 degrees of freedom
## AIC: 122.23
## Number of Fisher Scoring iterations: 8
confint(logFit)
##
                                           2.5 %
                                                      97.5 %
## (Intercept)
                                     -8.27635780 -3.59826504
## posDJIopen
                                     -1.69547870 3.16467729
                                     -0.01687701 3.75337299
## posDJIclose
                                     0.17531940 3.08661477
## posDJIadjClose
## posaverageFemaleSSRetiredPay
                                     -4.52081970 0.63960043
## posRealSPopen
                                     6.52290072 10.62645641
## percChangeRealDJIhigh
                                    -15.07388172 50.55178323
## posRealSPadjClose
                                      0.02995487 3.92774639
## posRealaverageFemaleSSRetiredPay -3.65209872 -0.02327801
## percChangeRealDJIadjClose
                                    -34.39831275 64.32052832
## percChangeRealSPadjClose
                                    -56.69350534 38.92640439
logProbs <- predict(logFit, type = 'response')</pre>
logProbs[1:10]
                                                                  6
##
                           3
                                        4
                                                     5
## 0.0009492249 0.9960759029 0.0024526558 0.0003439175 0.0380386988
                           8
                                        9
                                                    10
## 0.9981604947 0.0134793360 0.0036100750 0.0019040660 0.9981081640
logPred <- rep(NA, dim(dfStationary)[2])</pre>
logPred[logProbs > 0.5] <- 1</pre>
logPred[logProbs < 0.5] = 0
table(logPred)
## logPred
   0
## 236 168
table(logPred, dfStationary[,2])
##
## logPred
##
        0 230
                 6
##
        1 10 158
```

```
mean(logPred == dfStationary[,2])
## [1] 0.960396
# Testing Prediction
train <- subset(dfStationary, dfStationary$date < as.Date('2010-04-08'))</pre>
test3rdQuart <- subset(dfStationary, dfStationary$date >= as.Date('2010-04-08'))
logFit1 <- glm(fmlaForward,</pre>
               family = binomial,
               data = train)
logProbs1 <- predict(logFit1, test3rdQuart, type = 'response') # setting prediction for the testing set
logPred1 <- rep(NA, dim(train)[2])</pre>
logPred1[logProbs1 >= 0.5] = 1
logPred1[logProbs1 < 0.5] = 0
table(logPred1, test3rdQuart$postotalSSRetired)
##
## logPred1 0 1
##
          0 54 2
          1 5 40
mean(logPred1 == test3rdQuart$postotalSSRetired)
## [1] 0.9306931
Prediction accuracy is approximately 93% with a train/test split at the 3rd quartile mark of the dates.
Positive class prediction: 40/2; 95% Negative Class prediction: 54/5; 91.5% This is the best model.
# Check only those with good statistical significance
logFit <- glm(postotalSSRetired ~ posDJIclose + posDJIadjClose + posRealSPopen + posRealSPadjClose + p
              family = binomial,
              data = dfStationary)
summary(logFit, diagnostics=TRUE)
##
## Call:
## glm(formula = postotalSSRetired ~ posDJIclose + posDJIadjClose +
##
       posRealSPopen + posRealSPadjClose + posRealaverageFemaleSSRetiredPay,
##
       family = binomial, data = dfStationary)
##
## Deviance Residuals:
                         Median
##
        Min
                   1Q
                                        3Q
                                                 Max
## -3.06535 -0.13360 -0.05683 0.13530
                                             2.48559
##
## Coefficients:
##
                                     Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                                                  1.0182 -6.313 2.74e-10 ***
                                      -6.4278
## posDJIclose
                                       1.5484
                                                  0.9552
                                                          1.621 0.10501
## posDJIadjClose
                                                           2.623 0.00871 **
                                       1.7133
                                                  0.6531
## posRealSPopen
                                       7.7315
                                                  0.9048
                                                           8.545 < 2e-16 ***
## posRealSPadjClose
                                       1.8369
                                                  0.9750
                                                           1.884 0.05956 .
## posRealaverageFemaleSSRetiredPay -1.0678
                                                  0.6117 -1.746 0.08090 .
```

```
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
       Null deviance: 545.68 on 403 degrees of freedom
## Residual deviance: 104.59 on 398 degrees of freedom
## AIC: 116.59
##
## Number of Fisher Scoring iterations: 7
confint(logFit)
                                         2.5 %
                                                    97.5 %
## (Intercept)
                                    -8.7614151 -4.6808299
## posDJIclose
                                    -0.1244147 3.6921985
## posDJIadjClose
                                     0.4920897 3.0838235
## posRealSPopen
                                     6.2167780 9.8785185
## posRealSPadjClose
                                     0.1224186 4.0102672
## posRealaverageFemaleSSRetiredPay -2.3042923 0.1182437
logProbs <- predict(logFit, type = 'response')</pre>
logProbs[1:10]
                           3
## 0.0016134028 0.9897014801 0.0016134028 0.0005552172 0.0834023010
##
              7
                                        9
                           8
                                                     10
## 0.9952008178 0.0088844333 0.0016134028 0.0034749324 0.9952008178
logPred <- rep(0, dim(dfStationary)[2])</pre>
logPred[logProbs > 0.5] <- 1</pre>
table(logPred)
## logPred
##
   0 1
## 34 169
table(logPred, dfStationary[,2])
##
## logPred
            0
         0 33
##
               1
         1 11 158
mean(logPred == dfStationary[,2])
## [1] NA
# Testing Prediction
train <- subset(dfStationary, dfStationary$date < as.Date('2010-04-08'))</pre>
test3rdQuart <- subset(dfStationary, dfStationary$date >= as.Date('2010-04-08'))
logFit1 <- glm(postotalSSRetired ~ posDJIclose + posDJIadjClose + posRealSPopen + posRealSPadjClose + ;
               family = binomial,
               data = train)
logProbs1 <- predict(logFit1, test3rdQuart, type = 'response') # setting prediction for the testing set
logPred1 <- rep(NA, dim(train)[2])</pre>
logPred1[logProbs1 >= 0.5] = 1
```

```
logPred1[logProbs1 < 0.5] = 0
table(logPred1, test3rdQuart$postotalSSRetired)
##
## logPred1 0 1
##
          0 54 2
##
          1 5 40
mean(logPred1 == test3rdQuart$postotalSSRetired)
## [1] 0.9306931
Prediction accuracy is approximately 93% with a train/test split at the 3rd quartile mark of the dates.
Positive class prediction: 40/2; 95% Negative Class prediction: 54/5; 91.5% There is no change, but we have
reduced the number of regressors by half, from 10 to 5.
# Subset this further by selecting only those with statistical significance from this model
logFit <- glm(postotalSSRetired ~ posDJIadjClose + posRealSPopen + posRealSPadjClose + posRealaverage
              family = binomial,
              data = dfStationary)
summary(logFit, diagnostics=TRUE)
##
## Call:
  glm(formula = postotalSSRetired ~ posDJIadjClose + posRealSPopen +
       posRealSPadjClose + posRealaverageFemaleSSRetiredPay, family = binomial,
##
       data = dfStationary)
##
##
## Deviance Residuals:
##
        Min
                   1Q
                         Median
                                        3Q
                                                 Max
## -2.95006 -0.14982 -0.06188
                                 0.16107
                                             2.60136
##
## Coefficients:
##
                                     Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                                      -6.2573
                                                  0.9852 -6.351 2.14e-10 ***
## posDJIadjClose
                                       1.9282
                                                  0.6514
                                                           2.960 0.003077 **
## posRealSPopen
                                                  0.8767
                                                           8.768 < 2e-16 ***
                                       7.6875
## posRealSPadjClose
                                       2.9082
                                                  0.7852
                                                           3.704 0.000212 ***
## posRealaverageFemaleSSRetiredPay -1.1351
                                                  0.6097 -1.862 0.062626 .
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 545.68 on 403 degrees of freedom
## Residual deviance: 107.82 on 399 degrees of freedom
## AIC: 117.82
## Number of Fisher Scoring iterations: 7
confint(logFit)
##
                                          2.5 %
                                                     97.5 %
## (Intercept)
                                     -8.4911635 -4.55434311
```

## posDJIadjClose

0.7088555 3.29449737

```
## posRealSPopen
                                      6.2092825 9.74742204
                                      1.5701719 4.80067290
## posRealSPadjClose
## posRealaverageFemaleSSRetiredPay -2.3670651 0.04756246
logProbs <- predict(logFit, type = 'response')</pre>
logProbs[1:10]
##
                           3
                                                      5
                                                                    6
              2
## 0.0019128306 0.9663798429 0.0019128306 0.0006155424 0.0720274306
              7
                           8
                                         9
                                                     10
## 0.9941271498 0.0130086210 0.0019128306 0.0111603749 0.9941271498
logPred <- rep(0, dim(dfStationary)[2])</pre>
logPred[logProbs > 0.5] <- 1</pre>
table(logPred)
## logPred
##
    0
## 34 169
table(logPred, dfStationary[,2])
##
## logPred
             0
##
         0
            33
                 1
         1 11 158
mean(logPred == dfStationary[,2])
## [1] NA
# Testing Prediction
train <- subset(dfStationary, dfStationary$date < as.Date('2010-04-08'))
test3rdQuart <- subset(dfStationary, dfStationary$date >= as.Date('2010-04-08'))
logFit1 <- glm(postotalSSRetired ~ posDJIadjClose + posRealSPopen + posRealSPadjClose + posRealaverage
               family = binomial,
               data = train)
logProbs1 <- predict(logFit1, test3rdQuart, type = 'response') # setting prediction for the testing set
logPred1 <- rep(NA, dim(train)[2])</pre>
logPred1[logProbs1 >= 0.5] = 1
logPred1[logProbs1 < 0.5] = 0
table(logPred1, test3rdQuart$postotalSSRetired)
##
## logPred1 0 1
##
          0 54 2
##
          1 5 40
mean(logPred1 == test3rdQuart$postotalSSRetired)
```

## [1] 0.9306931

Prediction accuracy is approximately 93% with a train/test split at the 3rd quartile mark of the dates. Positive class prediction: 40/2; 95% Negative Class prediction: 54/5; 91.5% There is no change, but we have reduced the number of regressors from 5 to 4.

```
# Subset once more based on those with statistical significance better than 0.05
logFit <- glm(postotalSSRetired ~ posDJIadjClose + posRealSPopen + posRealSPadjClose,</pre>
              family = binomial,
              data = dfStationary)
summary(logFit, diagnostics=TRUE)
##
## Call:
## glm(formula = postotalSSRetired ~ posDJIadjClose + posRealSPopen +
       posRealSPadjClose, family = binomial, data = dfStationary)
##
##
## Deviance Residuals:
       Min
                 1Q
                      Median
                                   3Q
                                           Max
## -2.7339 -0.1139 -0.0556
                               0.2196
                                         2.7439
##
## Coefficients:
##
                     Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                      -6.4717
                                  0.9659 -6.700 2.08e-11 ***
## posDJIadjClose
                       1.4368
                                  0.5820
                                           2.469 0.013560 *
## posRealSPopen
                                  0.8341
                                           8.936 < 2e-16 ***
                       7.4540
                                           3.548 0.000388 ***
## posRealSPadjClose
                       2.7306
                                  0.7696
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
       Null deviance: 545.68 on 403 degrees of freedom
##
## Residual deviance: 111.36 on 400 degrees of freedom
## AIC: 119.36
##
## Number of Fisher Scoring iterations: 7
confint(logFit)
##
                          2.5 %
                                   97.5 %
                     -8.6700560 -4.804306
## (Intercept)
## posDJIadjClose
                      0.3477433 2.669307
## posRealSPopen
                      6.0508612 9.436552
## posRealSPadjClose 1.4244555 4.600410
logProbs <- predict(logFit, type = 'response')</pre>
logProbs[1:10]
##
                         3
                                                  5
## 0.001544224 0.918271072 0.001544224 0.001544224 0.090771223 0.994232497
                         9
                                     10
## 0.006464772 0.001544224 0.023179357 0.994232497
logPred <- rep(0, dim(dfStationary)[2])</pre>
logPred[logProbs > 0.5] <- 1</pre>
table(logPred)
## logPred
##
   0
## 34 169
```

```
table(logPred, dfStationary[,2])
##
## logPred
##
         0
            33
                  1
##
         1 11 158
mean(logPred == dfStationary[,2])
## [1] NA
# Testing Prediction
train <- subset(dfStationary, dfStationary$date < as.Date('2010-04-08'))
test3rdQuart <- subset(dfStationary, dfStationary, date >= as.Date('2010-04-08'))
logFit1 <- glm(postotalSSRetired ~ posDJIadjClose + posRealSPopen + posRealSPadjClose,</pre>
                family = binomial,
                data = train)
logProbs1 <- predict(logFit1, test3rdQuart, type = 'response') # setting prediction for the testing set
logPred1 <- rep(NA, dim(train)[2])</pre>
logPred1[logProbs1 >= 0.5] = 1
logPred1[logProbs1 < 0.5] = 0
table(logPred1, test3rdQuart$postotalSSRetired)
##
## logPred1 0 1
##
          0 54 2
          1 5 40
##
mean(logPred1 == test3rdQuart$postotalSSRetired)
## [1] 0.9306931
Prediction accuracy is approximately 93% with a train/test split at the 3rd quartile mark of the dates.
Positive class prediction: 40/2; 95% Negative Class prediction: 54/5; 91.5% There is no change, but we have
reduced the number of regressors from 4 to 3. All factors are statisticall significant.
predForm <- as.formula(postotalSSRetired ~ posDJIadjClose + posRealSPopen + posRealSPadjClose)</pre>
Switch up the train/test split to account for about 80% of the data
train80 <- subset(dfStationary, dfStationary, dfStationary, date < as.Date(dfStationary, date[round(nrow(dfStationary)])
test20 <- subset(dfStationary, dfStationary$date >= as.Date(dfStationary$date[round(nrow(dfStationary)
logFit <- glm(predForm,</pre>
              family = binomial,
               data = dfStationary)
summary(logFit, diagnostics=TRUE)
##
## glm(formula = predForm, family = binomial, data = dfStationary)
##
## Deviance Residuals:
##
       Min
                 10
                      Median
                                     30
                                              Max
## -2.7339 -0.1139 -0.0556 0.2196
                                          2.7439
```

```
##
## Coefficients:
##
                     Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                      -6.4717
                                  0.9659 -6.700 2.08e-11 ***
## posDJIadjClose
                       1.4368
                                   0.5820
                                            2.469 0.013560 *
## posRealSPopen
                       7.4540
                                   0.8341
                                            8.936 < 2e-16 ***
## posRealSPadjClose
                       2.7306
                                   0.7696
                                            3.548 0.000388 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
       Null deviance: 545.68 on 403 degrees of freedom
##
## Residual deviance: 111.36 on 400 degrees of freedom
## AIC: 119.36
##
## Number of Fisher Scoring iterations: 7
confint(logFit)
##
                           2.5 %
                                    97.5 %
                     -8.6700560 -4.804306
## (Intercept)
## posDJIadjClose
                      0.3477433 2.669307
## posRealSPopen
                      6.0508612 9.436552
## posRealSPadjClose 1.4244555 4.600410
logProbs <- predict(logFit, type = 'response')</pre>
logProbs[1:10]
##
             2
                         3
                                                  5
## 0.001544224 0.918271072 0.001544224 0.001544224 0.090771223 0.994232497
                         9
                                     10
## 0.006464772 0.001544224 0.023179357 0.994232497
logPred <- rep(0, dim(dfStationary)[2])</pre>
logPred[logProbs > 0.5] <- 1</pre>
table(logPred)
## logPred
##
    0
## 34 169
table(logPred, dfStationary[,2])
##
## logPred
             0
                 1
            33
##
         0
                 1
##
         1 11 158
mean(logPred == dfStationary[,2])
## [1] NA
# Testing Prediction
logFit1 <- glm(predForm,</pre>
               family = binomial,
               data = train80)
logProbs1 <- predict(logFit1, test20, type = 'response') # setting prediction for the testing set FROM</pre>
```

```
logPred1 <- rep(NA, dim(train80)[2])</pre>
logPred1[logProbs1 >= 0.5] = 1
logPred1[logProbs1 < 0.5] = 0
table(logPred1, test20$postotalSSRetired)
##
## logPred1 0 1
##
          0 43 1
##
          1 3 35
mean(logPred1 == test20$postotalSSRetired)
## [1] 0.9512195
Prediction accuracy is approximately 95% with a train/test split of 80/20. Positive class prediction: 43/3;
93.4% Negative Class prediction: 35/36; 97.2%. Let's check how probit fits the data
# Probit ####
As the variable of interest is generated from the differences in Total SS Recipients, which appears about
normally distributed, a probit model may be more appropriate.
probFit <- glm(predForm,</pre>
               family = binomial(link = "probit"),
               data = dfStationary)
summary(probFit, diagnostics=TRUE)
##
## Call:
## glm(formula = predForm, family = binomial(link = "probit"), data = dfStationary)
## Deviance Residuals:
                          Median
        Min
                  1Q
                                        3Q
                                                  Max
## -2.67493 -0.09598 -0.02853
                                              2.79822
                                   0.23807
##
## Coefficients:
                     Estimate Std. Error z value Pr(>|z|)
##
## (Intercept)
                      -3.3480
                                   0.4453 -7.519 5.50e-14 ***
## posDJIadjClose
                        0.7431
                                   0.2886
                                            2.575
                                                       0.01 *
## posRealSPopen
                        3.9669
                                   0.3551 11.170 < 2e-16 ***
## posRealSPadjClose
                        1.2930
                                   0.3300
                                            3.918 8.91e-05 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
       Null deviance: 545.68 on 403 degrees of freedom
## Residual deviance: 110.30 on 400 degrees of freedom
## AIC: 118.3
## Number of Fisher Scoring iterations: 8
confint(probFit)
```

```
## 2.5 % 97.5 %
## (Intercept) -4.3500091 -2.558896
```

```
## posDJIadjClose
                       0.1993879 1.337637
## posRealSPopen
                       3.3429631 4.773703
## posRealSPadjClose 0.7017883 2.036072
probProbs <- predict(probFit, type = 'response')</pre>
probProbs[1:10]
##
                             3
                                                        5
                                                                       6
               2
## 0.0004069635 0.9134087643 0.0004069635 0.0004069635 0.0947859691
              7
                            8
                                          9
                                                       10
## 0.9960355244 0.0045953487 0.0004069635 0.0199403179 0.9960355244
probPred <- rep(NA, dim(dfStationary)[2])</pre>
probPred[probProbs >= 0.5] <- 1</pre>
probPred[probProbs < 0.5] <- 0</pre>
table(probPred)
## probPred
##
    0 1
## 235 169
table(probPred, dfStationary$postotalSSRetired)
##
## probPred
                   1
##
          0 229
                   6
          1 11 158
mean(probPred == dfStationary$postotalSSRetired)
## [1] 0.9579208
# Testing Prediction
probFit1 <- glm(predForm,</pre>
                 family = binomial(link = "probit"),
                 data = train)
probProbs1 <- predict(probFit1, test3rdQuart, type = 'response') # setting prediction for the testing s</pre>
probPred1 <- rep(0, dim(train)[2])</pre>
probPred1[probProbs1 >= 0.5] <- 1</pre>
probPred1[probProbs1 < 0.5] <- 0</pre>
table(probPred1, test3rdQuart$postotalSSRetired)
##
## probPred1 0 1
           0 54 2
##
           1 5 40
mean(probPred1 == test3rdQuart$postotalSSRetired)
## [1] 0.9306931
Prediction accuracy is approximately 93% with a train/test split at the 3rd quartile mark of the dates.
Positive class prediction: 40/2; 95.2% Negative Class prediction: 54/5; 91.5%.
# Test it at the 80/20 split
train80 <- subset(dfStationary, dfStationary$date < as.Date(dfStationary$date[round(nrow(dfStationary)]</pre>
```

```
test20 <- subset(dfStationary, dfStationary$date >= as.Date(dfStationary$date[round(nrow(dfStationary)])
probFit1 <- glm(predForm,</pre>
                 family = binomial(link = "probit"),
                 data = train)
probProbs1 <- predict(probFit1, test20, type = 'response') # setting prediction for the testing set FRO</pre>
probPred1 <- rep(0, dim(train80)[2])</pre>
probPred1[probProbs1 >= 0.5] <- 1</pre>
probPred1[probProbs1 < 0.5] <- 0</pre>
table(probPred1, test20$postotalSSRetired)
##
## probPred1 0 1
##
           0 43 1
           1 3 35
mean(probPred1 == test20$postotalSSRetired)
## [1] 0.9512195
```

Prediction accuracy is approximately 95% with a train/test split of 80/20. Positive class prediction: 43/3; 93.4% Negative Class prediction: 35/1; 97.2% This prediction accuracy is the same as the logit model