Total points: 10

Section 5.1 #9 b) #12 b) #22

Section 5.2 #20 (please show the grammar in example 5.5 is ambiguous.)

### Section 5.1

9b. Find context-free grammars for the following languages (with  $n \ge 0$ ,  $m \ge 0$ ).

$$L = \{a^nb^m : n = m - 1\}.$$

#### **Answer**

$$S \rightarrow aSb \mid b$$

12b. Find context-free grammars for the following languages (with  $n \ge 0$ ,  $m \ge 0$ ,  $k \ge 0$ ).

$$L = \{a^n b^m c^k : n = m \text{ or } m \neq k\}.$$

### Answer

 $S \rightarrow S1|S2$ 

 $S1 \rightarrow S1c \mid A$ 

 $A \rightarrow aAb \mid \lambda$ 

 $S2 \rightarrow aS2 \mid B$ 

 $B \rightarrow CD \mid DE$ 

 $C \rightarrow bC \mid b$ 

 $D \rightarrow bDc \mid \lambda$ 

 $E \rightarrow cE \mid c$ 

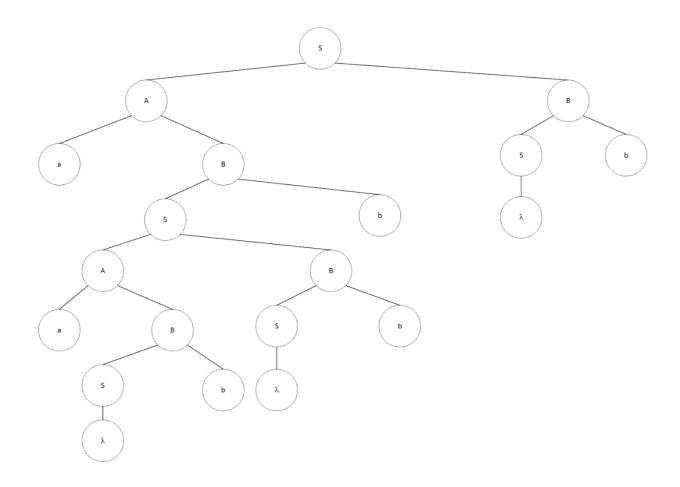
22. (4pts) Show a derivation tree for the string aabbbb with grammar

 $S \rightarrow AB | \lambda$ 

 $A \rightarrow aB$ 

 $B \rightarrow Sb$ .

#### **Answer**



# Section 5.2

20. (4pts) Show that the following grammar is ambiguous.

$$S \rightarrow aAB$$
  
 $A \rightarrow bBb$   
 $B \rightarrow A \mid \lambda$ 

### Answer

# **Derivation 1**

$$\mathsf{S} \Rightarrow \mathsf{aAB} \Rightarrow \mathsf{abBbB} \Rightarrow \mathsf{abAbB} \Rightarrow \mathsf{abbBbbB} \Rightarrow \mathsf{abbAbb} \Rightarrow \mathsf{abbbBbbbB} \Rightarrow \mathsf{abbbbbb}$$

# **Derivation 2**

$$S \Rightarrow aAB \Rightarrow abBbB \Rightarrow abbB \Rightarrow abbbAb \Rightarrow abbbbbbb \Rightarrow abbbbbb$$

There exists 2 left-most derivations for the string abbbbbb, so the grammar is ambiguous.

**Grading:** students can also draw two different parse trees to show the grammar is ambiguous.