

- In class Exercise

- Prove that  $L = \{ww^R, w \in \{a,b\}^*\}$  is NOT regular.

\* All strings are of even length and 2<sup>nd</sup> half of string is a mirror (reverse) of the 1<sup>st</sup> half.

- For the language, the 1<sup>st</sup> half is  $w = xy$  and the 2<sup>nd</sup> half  $w^R = z$

- Using an example string of  $\overbrace{aaa}^w \overbrace{bbbbaaa}^{w^R}$  with  $m = 10$   
 $\begin{array}{ccccc} & & w & & w^R \\ & & \overbrace{aaa} & & \overbrace{bbbbaaa} \\ & x & y & & z \end{array}$

$$|xy| \leq 10 \Rightarrow |xy| = 3 \quad \checkmark$$

$$|y| \geq 1 \Rightarrow |y| = 2 \quad \checkmark$$

- If  $i=2$  then  $xy^iz$  would be  $a(aa)^2 bbbbaaa$ , this would result in a string with more a's in  $w$  than in  $w^R$ . This is a contradiction, Thus  $L$  is not regular.