

Section 4.1 #10

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10. (10pts) The symmetric difference of two sets S_1 and S_2 is defined as

$$S_1 \oplus S_2 = \{x : x \in S_1 \text{ or } x \in S_2, \text{ but not in both } S_1 \text{ and } S_2\}.$$

Show that the family of regular languages is closed under the symmetric difference.

Answer

$S_1 \oplus S_2 = (S_1 - S_2) \cup (S_2 - S_1)$, closed under difference and union of regular languages, or

$S_1 \oplus S_2 = (S_1 \cup S_2) - (S_1 \cap S_2)$, closed under union, intersection, and difference of regular languages or

$S_1 \oplus S_2 = (S_1 \cup S_2) \cap \overline{(S_1 \cap S_2)}$, closed under union, intersection, and complement.

Grading: any one of the three ways would be fine. Need to mention closure property (or closed) under different operations. Partial points can be given.