

# Class Exercise 1

## Solutions

# Solutions (Problem 1 and 2)

- $p(x) = -5 + 3x + 8x^2 - 2x^4$

- Problem 8c (Section 1.1, page 15)

$$p(x) = 6(x + 2)^3 + 9(x + 2)^7 + 3(x + 2)^{15} - (x + 2)^{31}$$

Solution:

$$p(x) = -5 + 3x + 8x^2 - 2x^4$$

$$p(x) = -5 + x(3 + x(8 + x^2(-2)))$$

$$\text{Let } y = x + 2$$

$$p(x) = 6y^3 + 9y^7 + 3y^{15} - y^{31}$$

$$p(x) = y^3(6 + y^4(9 + y^8(3 + y^{16}(-1))))$$

# Solutions Problem 3 and 4

- Problem 3:

$$\begin{array}{r} 1 \quad -4 \quad 7 \quad -5 \quad -2 \\ 2) \quad \quad 2 \quad -4 \quad 6 \quad 2 \\ \hline 1 \quad -2 \quad 3 \quad 1 \quad 0 \end{array}$$

- Thus, we have  $p(2) = 0$ , and

$$x^4 - 4x^3 + 7x^2 - 5x - 2 = (x - 2)(x^3 - 2x^2 + 3x + 1)$$

- Problem 4:

$$\begin{array}{r} 2 \quad 0 \quad 9 \quad -16 \quad 12 \\ -6) \quad \quad -12 \quad 72 \quad -486 \quad 3012 \\ \hline 2 \quad -12 \quad 81 \quad -502 \quad 3024 \end{array}$$

Hence,  $p(-6) = 3024$

# Solutions

- Page 16, Exercise 18b (Section 1.1) Calculate  $p'(2)$

$$p(x) = 2x^4 - 3x^3 - 5x^2 + 3x + 8 \text{ at } x = 2$$

- Solution

$$\begin{array}{r} 2) \quad \begin{array}{rrrrr} 2 & -3 & -5 & 3 & 8 \\ & 4 & 2 & -6 & -6 \\ \hline & 2 & 1 & -3 & -3 & 2 \end{array} \\ 2) \quad \begin{array}{rrrr} & 4 & 10 & 14 \\ \hline & 2 & 5 & 7 & 11 \end{array} \end{array}$$

$$p(2) = 2 \text{ and } p'(2) = 11$$