Input PD code or string to snappy (use to reproduce the drawing):

 $8_3$ 

Output PD code drawn by snappy:

[(5, 1, 6, 16), (11, 2, 12, 3), (9, 4, 10, 5), (15, 7, 16, 6),(13, 9, 14, 8), (3, 10, 4, 11), (1, 12, 2, 13), (7, 15, 8, 14)]

Arcs composing region <---> Region key

 $\{1, 6, 8, 13, 15\} < \longrightarrow 41282$  $\{1, 3, 5, 10, 12\} < ---> 5162$  $\{2,\,4,\,9,\,11,\,13\}<\!\!-\!\!-\!\!>10772$  $\{2, 12\} < \longrightarrow 4100$  $\{11, 3\} < ---> 2056$ {10, 4} <---> 1040

 $\{5, 7, 9, 14, 16\} < ---> 82592$ 

{16, 6} <---> 65600

{15, 7} <---> 32896 {8, 14} <---> 16640

0

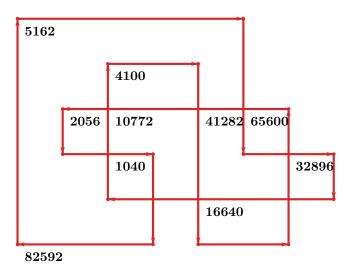
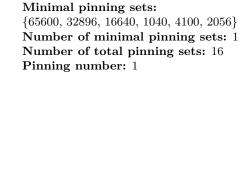
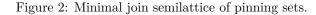


Figure 1: Snappy loop plot.





Input PD code or string to snappy (use to reproduce the drawing): Output PD code drawn by snappy: [(4, 1, 5, 2), (6, 3, 1, 4), (2, 5, 3, 6)] $\{1, 4\} < ---> 18$  $\{1, 3, 5\} < \longrightarrow 42$  $\{2, 4, 6\} < \longrightarrow 84$ {2, 5} <---> 36  $\{3,\,6\}<\!\!-\!\!-\!\!>72$ 

0

Minimal pinning sets: {72, 18, 36} Number of minimal pinning sets: 1 Number of total pinning sets: 4 Pinning number: 1

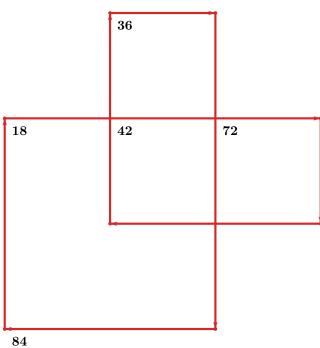


Figure 3: Snappy loop plot.

Figure 4: Minimal join semilattice of pinning sets.

Input PD code or string to snappy (use to reproduce the drawing):

41

Output PD code drawn by snappy:

[(3, 1, 4, 8), (5, 2, 6, 3), (7, 5, 8, 4), (1, 6, 2, 7)]

Arcs composing region <---> Region key

 $\{1, 4, 7\} < ---> 146$ 

 $\{1, 3, 6\} < ---> 74$ 

 $\{2, 5, 7\} < \longrightarrow 164$ 

 $\{2, 6\} < ---> 68$ 

 $\{8,\,3,\,5\}<\!\!-\!\!-\!\!>296$ 

 $\{8, 4\} < ---> 272$ 

Minimal pinning sets: {272, 74, 164, 68}

{272, 146, 296, 68}

Number of minimal pinning sets: 2 Number of total pinning sets: 7

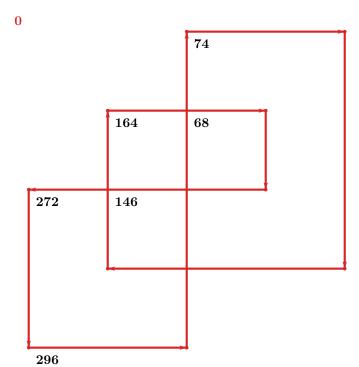


Figure 5: Snappy loop plot.

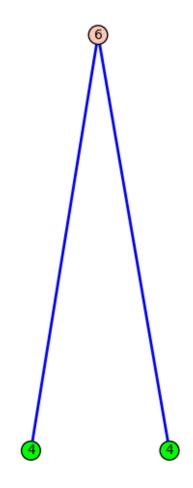


Figure 6: Minimal join semilattice of pinning sets.

{10, 5} <---> 1056

Minimal pinning sets: {1056, 528, 66, 132, 264} Number of minimal pinning sets: 1 Number of total pinning sets: 4 Pinning number: 1

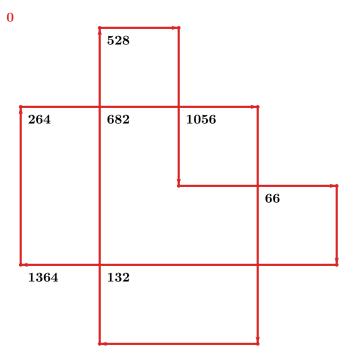


Figure 7: Snappy loop plot.

Figure 8: Minimal join semilattice of pinning sets.

```
Input PD code or string to snappy (use to reproduce the drawing):

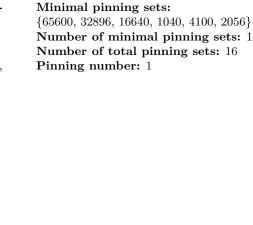
83
```

```
Output PD code drawn by snappy: [(5, 1, 6, 16), (11, 2, 12, 3), (9, 4, 10, 5), (15
```

 $[(5,\,1,\,6,\,16),\,(11,\,2,\,12,\,3),\,(9,\,4,\,10,\,5),\,(15,\,7,\,16,\,6),\\(13,\,9,\,14,\,8),\,(3,\,10,\,4,\,11),\,(1,\,12,\,2,\,13),\,(7,\,15,\,8,\,14)]$ 

```
 \begin{cases} 1, 6, 8, 13, 15 \} < \longrightarrow 41282 \\ \{1, 3, 5, 10, 12 \} < \longrightarrow 5162 \\ \{2, 4, 9, 11, 13 \} < \longrightarrow 10772 \\ \{2, 12 \} < \longrightarrow 4100 \\ \{11, 3 \} < \longrightarrow 2056 \\ \{10, 4 \} < \longrightarrow 1040 \\ \{5, 7, 9, 14, 16 \} < \longrightarrow 82592 \\ \{16, 6 \} < \longrightarrow 65600 \\ \{15, 7 \} < \longrightarrow 32896 \\ \{8, 14 \} < \longrightarrow 16640
```

0



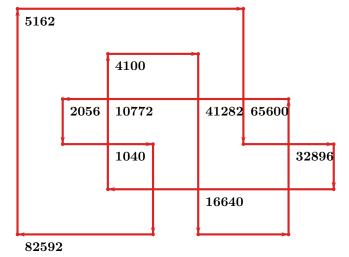


Figure 9: Snappy loop plot.

Figure 10: Minimal join semilattice of pinning sets.

Input PD code or string to snappy (use to reproduce the drawing):

 $9_{2}4$ 

Output PD code drawn by snappy:

 $[(10,\,1,\,11,\,2),\,(16,\,4,\,17,\,3),\,(18,\,6,\,1,\,5),\,(14,\,7,\,15,\,8),\\(2,\,9,\,3,\,10),\,(8,\,12,\,9,\,11),\,(6,\,13,\,7,\,14),\,(12,\,15,\,13,\,16),\,(4,\,18,\,5,\,17)]$ 

Arcs composing region <---> Region key

```
 \begin{array}{l} \{1,\,3,\,5,\,10,\,17\} < \longrightarrow > 132138 \\ \{1,\,6,\,8,\,11,\,14\} < \longrightarrow > 18754 \\ \{2,\,10\} < \longrightarrow > 1028 \\ \{9,\,2,\,11\} < \longrightarrow > 2564 \\ \{16,\,9,\,3,\,12\} < \longrightarrow > 70152 \\ \{17,\,4\} < \longrightarrow > 131088 \\ \{4,\,6,\,13,\,16,\,18\} < \longrightarrow > 335952 \\ \{18,\,5\} < \longrightarrow > 262176 \\ \{14,\,7\} < \longrightarrow > 16512 \\ \{15,\,13,\,7\} < \longrightarrow > 41088 \\ \{8,\,12,\,15\} < \longrightarrow > 37120 \\ \end{array}
```

Minimal pinning sets:

{262176, 16512, 37120, 131088, 1028} {262176, 16512, 41088, 131088, 1028}

Number of minimal pinning sets: 2 Number of total pinning sets: 96

Pinning number: 2

0

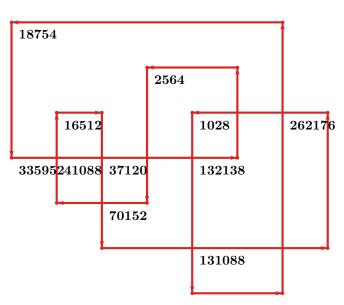


Figure 11: Snappy loop plot.

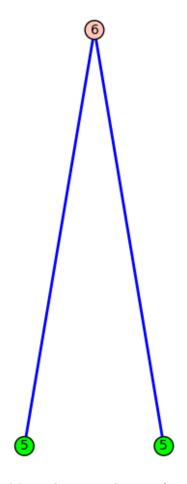


Figure 12: Minimal join semilattice of pinning sets.

### Input PD code or string to snappy (use to reproduce the drawing):

[(1, 7, 2, 6), (3, 8, 4, 9), (5, 11, 6, 10), (16, 12, 1, 11), (213, 3, 14), (4, 16, 5, 15), (7, 12, 8, 13), (9, 15, 10, 14)

#### Output PD code drawn by snappy:

10, 6, 11), (16, 11, 1, 12), (7, 13, 8, 12), (2, 14, 3, 13)

# 

 $\{1, 12, 7\} < \longrightarrow 4226$ 

 $\{1, 11, 6\} < ---> 2114$ 

 $\{2, 13, 7\} < ---> 8324$ 

 $\{2, 10, 6, 14\} < \longrightarrow 17476$ 

{8, 3, 13} <---> 8456

 $\{9, 3, 14\} < \longrightarrow 16904$ 

 $\{8, 16, 4, 12\} < ---> 69904$ 

 $\{9, 4, 15\} < ---> 33296$ 

 $\{16, 11, 5\} < \longrightarrow 67616$ 

 $\{10, 5, 15\} < ---> 33824$ 

#### Minimal pinning sets:

{67616, 33296, 2114, 8324, 16904}  $\{33824,\,69904,\,2114,\,8324,\,16904\}$ 

{33824, 33296, 2114, 8324, 8456}

 $\{67616, 33296, 2114, 8324, 8456\}$ 

{67616, 33824, 4226, 8456, 16904}

{67616, 33296, 4226, 17476, 8456}

{67616, 33824, 4226, 8324, 16904}

{67616, 33296, 4226, 8324, 16904}

 $\{33824,\ 33296,\ 4226,\ 2114,\ 8456\}$ 

{33824, 4226, 2114, 8456, 16904}

Number of minimal pinning sets: 10 Number of total pinning sets: 160

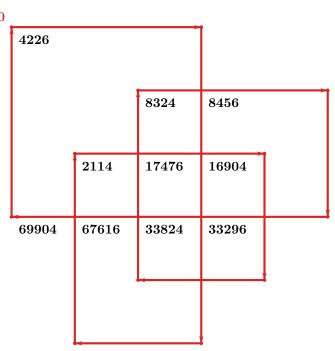


Figure 13: Snappy loop plot.

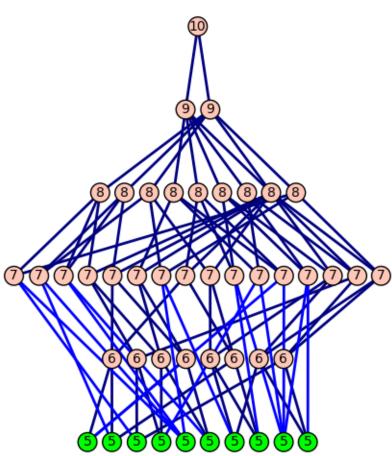


Figure 14: Minimal join semilattice of pinning sets.

### Input PD code or string to snappy (use to reproduce the drawing):

[(1, 7, 2, 6), (4, 9, 5, 10), (2, 12, 3, 11), (7, 13, 8, 12),(18, 13, 1, 14), (3, 17, 4, 16), (5, 14, 6, 15), (8, 18, 9, 17),(10, 15, 11, 16)

# Output PD code drawn by snappy:

[(17, 5, 18, 4), (2, 7, 3, 8), (18, 10, 1, 9), (5, 11, 6, 10),(16, 11, 17, 12), (3, 12, 4, 13), (8, 13, 9, 14), (1, 15, 2, 14),(6, 16, 7, 15)

### Arcs composing region <---> Region key

 $\{1, 9, 14\} < ---> 16898$  $\{1, 10, 6, 15\} < \longrightarrow 33858$ {8, 2, 14} <---> 16644  $\{2, 15, 7\} < \longrightarrow 32900$ {8, 3, 13} <---> 8456  $\{16, 3, 12, 7\} < ---> 69768$  $\{9, 18, 4, 13\} < ---> 270864$ 

 $\{17, 4, 12\} < ---> 135184$ 

 $\{10, 18, 5\} < ---> 263200$  $\{17, 11, 5\} < \longrightarrow 133152$ 

{16, 11, 6} <---> 67648

 $\{263200, 135184, 67648, 16644\}$ 

Minimal pinning sets:

{263200, 133152, 67648, 270864, 16644, 69768}

{133152, 67648, 270864, 32900, 16644}

{133152, 67648, 33858, 270864, 16644, 135184}

 $\{263200, 133152, 33858, 135184, 16644, 69768\}$ 

{133152, 270864, 33858, 16644, 69768}

{133152, 135184, 33858, 16644, 8456}

{133152, 270864, 33858, 32900, 16644, 8456}

{133152, 8456, 16898, 32900}

{263200, 67648, 16898, 135184, 32900, 8456}

{263200, 133152, 16898, 16644, 69768}

{133152, 270864, 16898, 32900, 16644, 69768}

{133152, 16898, 33858, 16644, 8456, 69768}

Number of minimal pinning sets: 13

Number of total pinning sets: 395

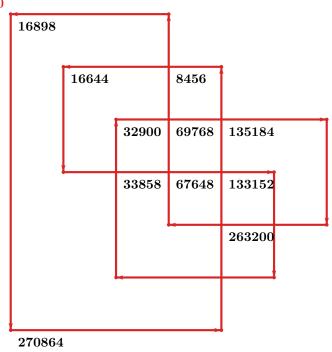


Figure 15: Snappy loop plot.

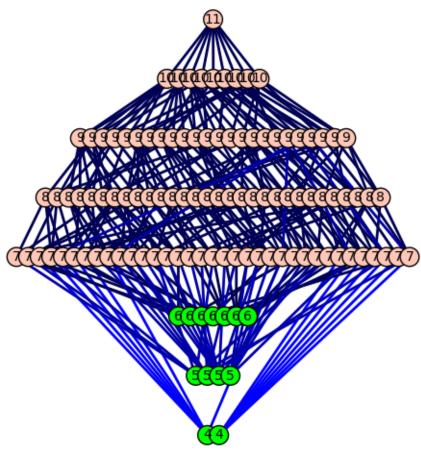


Figure 16: Minimal join semilattice of pinning sets.

# Input PD code or string to snappy (use to reproduce the drawing):

[(24, 6, 1, 5), (3, 10, 4, 11), (1, 13, 2, 12), (6, 14, 7, 13), (2, 17, 3, 18), (8, 15, 9, 16), (11, 19, 12, 18), (4, 20, 5, 19), (7, 23, 8, 22), (9, 20, 10, 21), (14, 24, 15, 23), (16, 21, 17, 22)]

#### Output PD code drawn by snappy:

[(22, 4, 23, 3), (1, 8, 2, 9), (23, 11, 24, 10), (4, 12, 5, 11), (6, 13, 7, 14), (24, 15, 1, 16), (9, 17, 10, 16), (2, 18, 3, 17), (7, 18, 8, 19), (14, 19, 15, 20), (5, 21, 6, 20), (12, 22, 13, 21)]

#### Arcs composing region <---> Region key

 $\begin{array}{l} \{16,\,1,\,9\} < \longrightarrow >66050 \\ \{8,\,1,\,19,\,15\} < \longrightarrow >557314 \\ \{9,\,2,\,17\} < \longrightarrow >131588 \\ \{8,\,2,\,18\} < \longrightarrow >262404 \\ \{17,\,10,\,3,\,23\} < \longrightarrow >8520712 \\ \{3,\,7,\,13,\,18,\,22\} < \longrightarrow >4464776 \\ \end{array}$ 

 $\{11, 4, 23\} < \longrightarrow 8390672$  $\{4, 12, 22\} < \longrightarrow 4198416$ 

{5, 11, 15, 20, 24} <---> 17860640

{21, 12, 5} <---> 2101280

 $\{20, 6, 14\} < ---> 1065024$ 

 $\{21,\,13,\,6\}<\!\!-\!\!-\!\!>2105408$ 

 $\{19,\,14,\,7\}<\!\!-\!\!-\!\!>540800$ 

 $\{16,\,24,\,10\}<\!\!-\!\!-\!\!>16843776$ 

#### Minimal pinning sets:

{2105408, 540800, 16843776, 4198416, 131588} {2101280, 1065024, 540800, 16843776, 131588, 4198416} {2101280, 2105408, 540800, 16843776, 131588, 8390672} {2101280, 1065024, 540800, 16843776, 131588, 8390672} {1065024, 2105408, 557314, 16843776, 131588, 4198416} {2101280, 1065024, 557314, 16843776, 131588, 4198416} {2101280, 1065024, 557314, 16843776, 131588, 8390672} {2101280, 2105408, 66050, 540800, 262404, 8390672} {2101280, 1065024, 66050, 8390672, 262404} {2105408, 540800, 66050, 8390672, 262404, 4198416} {1065024, 2105408, 66050, 8390672, 262404, 4198416} {2105408, 540800, 66050, 4198416, 262404, 8520712} {1065024, 2105408, 66050, 4198416, 262404, 8520712} {2101280, 1065024, 66050, 4198416, 262404, 8520712} {1065024, 2105408, 66050, 4198416, 131588} {2101280, 1065024, 66050, 4198416, 131588} {17860640, 2105408, 66050, 540800, 131588, 4198416} {2101280, 2105408, 66050, 540800, 131588, 8390672} {2101280, 1065024, 66050, 540800, 131588, 8390672} {2105408, 540800, 66050, 8390672, 131588, 4198416} {2101280, 1065024, 66050, 8390672, 131588, 4464776} {2105408, 540800, 66050, 4198416, 131588, 8520712} {2101280, 1065024, 66050, 557314, 131588, 8390672}

Number of minimal pinning sets: 23 Number of total pinning sets: 2400

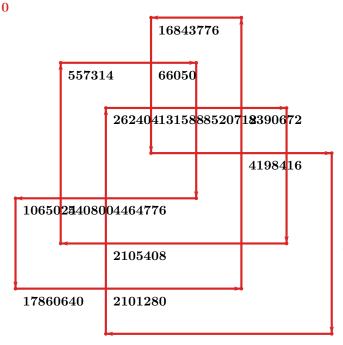


Figure 17: Snappy loop plot.

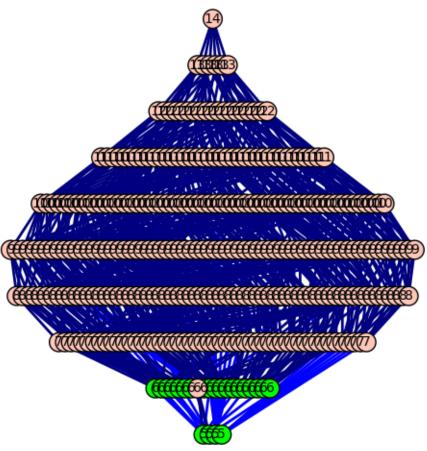


Figure 18: Minimal join semilattice of pinning sets.