

## STA6703 SML HW6

## Directions

Please submit **one PDF** file including all your reports (answer + code + figures + comments; must be easily readable and have file size under a few megabytes) and **one R or Python code script**. The R/Python script is supplementary material to ensure that your code runs correctly. If you are using RMarkdown, please also include your `.Rmd` file.

Place these two (or three) files in a folder, make a zip or rar archive, and submit the archive electronically via Dropbox file request at [tinyurl.com/nbliznyuk-submit-files](https://www.dropbox.com/request/4333333333333333) (on the landing page, enter your name so that we know it is you and email so that you get a confirmation).

**Deadline:** 01-Nov-2022, 10:00 PM EST.

### Practice/Optional Problems (do not submit)

1. Complete the R tutorial in the ISLR sections 6.5-6.7. You may find the Youtube videos by Trevor Hastie helpful; for links, see file `!_youtube_lab_links.txt` in the subfolder "`[2].code/islr_labs/`"
2. Implementing normal-theory linear regression model with an  $L_2$  penalty by hand: extend your implementation of the negative (Gaussian) log-likelihood from hw3 by adding the ridge penalty. Can this objective function be minimized analytically? If the  $L_2$  penalty is replaced by the  $L_1$  penalty, can the resulting objective function be minimized analytically? Briefly explain.
3. Implementing a logistic regression model with an  $L_2$  penalty by hand: extend your implementation of logistic regression (with multiple covariates) from hw4 by adding the ridge penalty. Can this objective function be minimized analytically?
4. "Honest"  $C_p$  in the multiple linear regression: the version this criterion motivated by the ISLR authors as the "training MSE corrected for overfitting" is somewhat deficient in assuming either that  $\sigma^2$  is known or is estimated by  $\hat{\sigma}^2$  (independently of the RSS for each given model fit). Suppose  $\hat{\sigma}^2 = \text{RSS}/(n - k - 1)$ , where the RSS comes from the current model fit; i.e.,  $\hat{\sigma}^2$  will be different for different models (even if  $k$  is the same). Show that, still,  $C_p$  is an increasing (linear) function of RSS (with the slope and intercept independent of the RSS). Hence, conclude that ranking the models with exactly  $k$  predictors with respect to  $C_p$  is equivalent to ranking them with respect to RSS.
5. "Honest" AIC and BIC in the multiple linear regression: for the multiple linear regression with iid  $\text{Normal}(0, \sigma^2)$  errors (the same version considered in class after ch.03), show that the deviance is an increasing function of RSS. Hence conclude that, for a fixed  $k$  (hence, fixed  $d$ ), ranking the models with exactly  $k$  predictors using RSS, AIC and BIC produces the same ordering (and hence the best model).

### Required Problems (for submission)

ISLR ch.6: 1,2,4,8