## **Problem Set: Lesson 2**

CDS 292. Fall, 2023

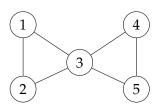
## **Instructions**

In this document you will find a set of problems intended to be answered **by hand**, scanned and submitted to Blackboard. Make sure your document is well organized and contains readable responses to the questions. **Show your work! Full credit requires this. An answer without procedure is likely to elicit zero points.** There is one addendum to this handwritten rule: any required plot can be either scanned or sent as an additional file to your submission. If you choose to submit separate files with your plots, make sure they are labeled and can be easily identified.

Note: Python code questions will occur in problem sets. The answers have to be handwritten and must respect all Python syntax rules including proper indentation of code.

**Total Points: 12** 

- 1. Calculate the maximum number of links for a network of
  - (a) [1/2 point] n = 5
  - (b)  $[\frac{1}{2} point] n = 10$
  - (c) [1/2 point] n = 15
  - (d) [1/2 point] n = 20
- 2. [2 points] Network G has a set V(G) with 15 elements and a set E(G) with 35 elements. Calculate the density of network G.
- 3. Using the network below:



- (a) [1 point] Write the node set
- (b) [1 point] Write the link set
- 4. [1 point] Using the following sets

$$V(G) = \{1, 2, 3, 4, 5, 6, 7, 8\}$$
  
 
$$E(G) = \{(1, 2), (6, 1), (2, 3), (3, 4), (4, 5), (6, 5)\}$$

Draw the network *G* 

- 5. Follow the steps below to create a network and extract some quantities of it.
  - (a) [1 point] Start by creating 20 nodes.
  - (b) [1 point] Among the nodes created, connect some of them to produce 30 links. HINT: We don't really care which nodes to connect, the only thing that should match is m.
  - (c) [1 point] Calculate the density of your created network using any Python function at your disposal (or write your own).
- 6. [2 points] A section of CDS 292 has 25 students that start the semester not knowing each other. By the end of the semester, 30 friendships were formed. What is the density of this social network? How many more friendships would be needed for the social network to be a complete network?

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2 6	Problem Set a.
(la)	n=5, max number assumes network is a complete network.  density, amount of actual/max. Completeness of network?
E E	Memplete /m = links, n = nocles / 5 nodes, what's maximum amount of links in the network. links exist between two nodes.
6	Mcomplete(5) = (3) Binomial looks for combinations, n(n-1)/2
6	(5)(4)/2 = 20/2 (10 maximum number of links)
	$N=10 \ V(6)=\{0,0,0,0,0,0,0,0,0,0,0,0,0,0,0,0,0,0,0,$
5 6	(10)(9)/2 = 90/2 (45 links possible)
(1c.	between 2 nodes, use hinomial for combination checks
6	[3]; (15)(14)/2, 210/2, (05 possible)
	20 nodes? (26)(19)/2 [190 max number)
	Every 5 node increase increases gap by +25.  V(6) = Vertices, or nodes, or n. Set containing all nodes in network
	V(6) has 15 nodes le lements.  E(6), edges, links, has 35 elements. / density, P, O to 1.
	$\binom{15}{3} = (15)(14)/2 = 105 \text{ max number of links, actual} = 35 '/100' / 100$

