

Q. Calculate min-max normalization of the following data:

$$\text{newMax} = 1 \quad \text{newMin} = 0$$

$$\text{marks} = 8, 10, 15, 20$$

$$A = \quad V' = \frac{V - \text{Min}_A}{\text{Max}_A - \text{Min}_A} (\text{newMax}_A - \text{newMin}_A) + \text{newMin}_A.$$

$$\Rightarrow \text{Min}_A = 8 \quad \text{Max}_A = 20$$

$$\text{newMax}_A = 1 \quad \text{newMin}_A = 0$$

$$\Rightarrow \cancel{8} V' = \frac{8-8}{20-8} (1-0) + 0 = \underline{0}$$

$$\Rightarrow V' = \frac{10-8}{20-8} (1-0) + 0 = \underline{0.1667}$$

$$\Rightarrow V' = \frac{15-8}{20-8} (1-0) + 0 = \underline{0.5833}.$$

$$\Rightarrow V' = \frac{20-8}{20-8} (1-0) + 0 = \underline{1}$$

Using Z-score

$$V' = \frac{V_i - \bar{A}}{\sigma_A}$$

A \rightarrow mean of observation

$$\Rightarrow \frac{8+10+15+20}{4} = \underline{13.25}$$

$$SD = \sigma = \sqrt{\sigma^2}$$

$$\sigma^2 = \left(\frac{1}{N} \sum_{i=1}^N x_i^2 - \bar{x}^2 \right) = \frac{1}{4} (8^2 + 10^2 + 15^2 + 20^2) - (13.25^2)$$

$$\boxed{N=4}$$

$$= \frac{789}{4} - (13.25)^2 = \underline{\underline{21.6875}}$$

$$\sigma = \sqrt{21.6875} = \underline{\underline{4.657}}$$

$$Z_{\text{score}} = \frac{x - \mu}{\sigma}$$

$$8 \Rightarrow \frac{8 - 13.25}{4.657} = \underline{\underline{-1.127}}$$

$$10 \Rightarrow \frac{10 - 13.25}{4.657} = \underline{\underline{-0.697}}$$

$$15 \Rightarrow \frac{15 - 13.25}{4.657} = \underline{\underline{0.376}}$$

$$20 \Rightarrow \frac{20 - 13.25}{4.657} = \underline{\underline{1.45}}$$