

Goal Programming

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x_1 = Number of Units Contributed from Product 1

x_2 = Number of Units Contributed from Product 2

x_3 = Number of Units Contributed from Product 3

Employment Level:

$$y_1 = 6x_1 + 4x_2 + 5x_3 - 50$$

if $y_1 \geq 0$ then y_{1p} if $y_1 < 0$ then y_{1m}

y_1 is the difference in the number of employees from the given goal of 5,000 it will take to produce the number of all 3 widgets. This number could be positive or negative.

Earning next year:

$$y_2 = 8x_1 + 7x_2 + 5x_3 - 75$$

if $y_2 \geq 0$ then y_{2p} (y_{2p} means more earnings which is a good thing so we wouldn't penalize for that) if $y_2 < 0$ then y_{2m}

y_2 is the same concept as y_1 but for earning. Given goal is 75M and y_2 will be the difference from that goal. We want more earning than 75M but not too much so we don't set high expectation for shareholders. This number could be positive or negative.

Management's Objective Function:

$$\text{Maximize: } Z = 20x_1 + 15x_2 + 25x_3 - 6(y_{1p} - y_{1m}) - 3(y_{2m})$$

Profit Obj Function:

$$\text{Maximize: } Z = 20x_1 + 15x_2 + 25x_3$$

Constraints:

$$6x_1 + 4x_2 + 5x_3 - (y_{1p} - y_{1m}) = 50$$

$$8x_1 + 7x_2 + 5x_3 - y_{2m} \geq 75$$

$$x_1, x_2, x_3 \geq 0$$

Solving the Linear programming model

```
library(lpSolveAPI)
```

```
## Warning: package 'lpSolveAPI' was built under R version 4.1.3
```

Objective Function

```

lprec = make.lp(0, 3)

set.objfn(lprec, c(20, 15, 25))

lp.control(lprec, sense = 'max')

```

```

## $anti.degen
## [1] "fixedvars" "stalling"
##
## $basis.crash
## [1] "none"
##
## $bb.depthlimit
## [1] -50
##
## $bb.floorfirst
## [1] "automatic"
##
## $bb.rule
## [1] "pseudononint" "greedy"          "dynamic"          "rcostfixing"
##
## $break.at.first
## [1] FALSE
##
## $break.at.value
## [1] 1e+30
##
## $epsilon
##      epsb      epsd      epsel      epsint  epsperturb  epspivot
##      1e-10      1e-09      1e-12      1e-07       1e-05       2e-07
##
## $improve
## [1] "dualfeas" "thetagap"
##
## $infinite
## [1] 1e+30
##
## $maxpivot
## [1] 250
##
## $mip.gap
## absolute relative
##      1e-11      1e-11
##
## $negrangle
## [1] -1e+06
##
## $obj.in.basis
## [1] TRUE
##
## $pivoting
## [1] "devex"      "adaptive"
##

```

```
## $presolve
## [1] "none"
##
## $scalelimit
## [1] 5
##
## $scaling
## [1] "geometric" "equilibrate" "integers"
##
## $sense
## [1] "maximize"
##
## $simplextype
## [1] "dual" "primal"
##
## $timeout
## [1] 0
##
## $verbose
## [1] "neutral"
```

Constraints

```
add.constraint(lprec, c(6, 4, 5), "=", 50)
add.constraint(lprec, c(8, 7, 5), ">=", 75)
```

```
solve(lprec)
```

```
## [1] 0
```

```
get.objective(lprec)
```

```
## [1] 208.3333
```

```
get.variables(lprec)
```

```
## [1] 0.000000 8.333333 3.333333
```