

Hashing expected number  
of probes for a successful  
search using quadratic or  
double hash is

$$\ominus \frac{1}{\lambda} \log_e (1 - \lambda)$$

$$\boxed{\frac{1}{\lambda} \log_e \left( \frac{1}{1 - \lambda} \right)}$$

$$\boxed{\frac{1}{1 - \lambda}}$$

Floyd's Algorithm (1956)

→ All paths shortest path

Warshall's Algorithm (1952)

↳ Transitive Closure

## 9 Transitive Closure

Given a boolean adjacency matrix  $A$

```

for (int i = 0; i < |V|; i++)
  for (int j = 0; j < |V|; j++)
    for (int k = 0; k < |V|; k++)
       $A[i][j] = A[i][j] \vee$ 
       $(A[i][k] \wedge A[k][j])$ 

```



	0	1	2	3
0	0	1	0	0
1	0	0	1	0
2	0	0	0	1
3	0	1	0	0

$k=0$

[ ]

$i \rightarrow j$   
 $i \xrightarrow{1} j$   
 $i \xrightarrow{*} j$

Reachability matrix

reachability - 7  
Matrix

## Undirected Graphs $G=(V,E)$

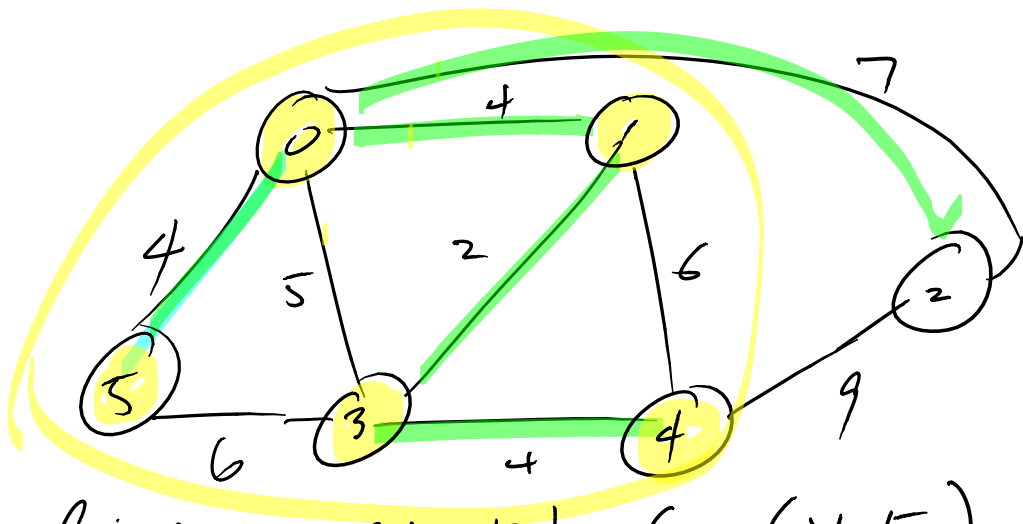


$(0,1)$

or

$(1,0)$

same  
edge



Given a graph  $G=(V,E)$  a spanning tree is set of edges  $E_s \subseteq E$  such that all vertices in  $V$  are represented in  $E_s$

A minimum cost spanning tree. (may not be unique)

