

max node

$(1)$   
 $2^{1-1} + 1$

$(3)$   
 $2^{2-1} + 1$

$(7)$   
 $2^{3-1} + 1$

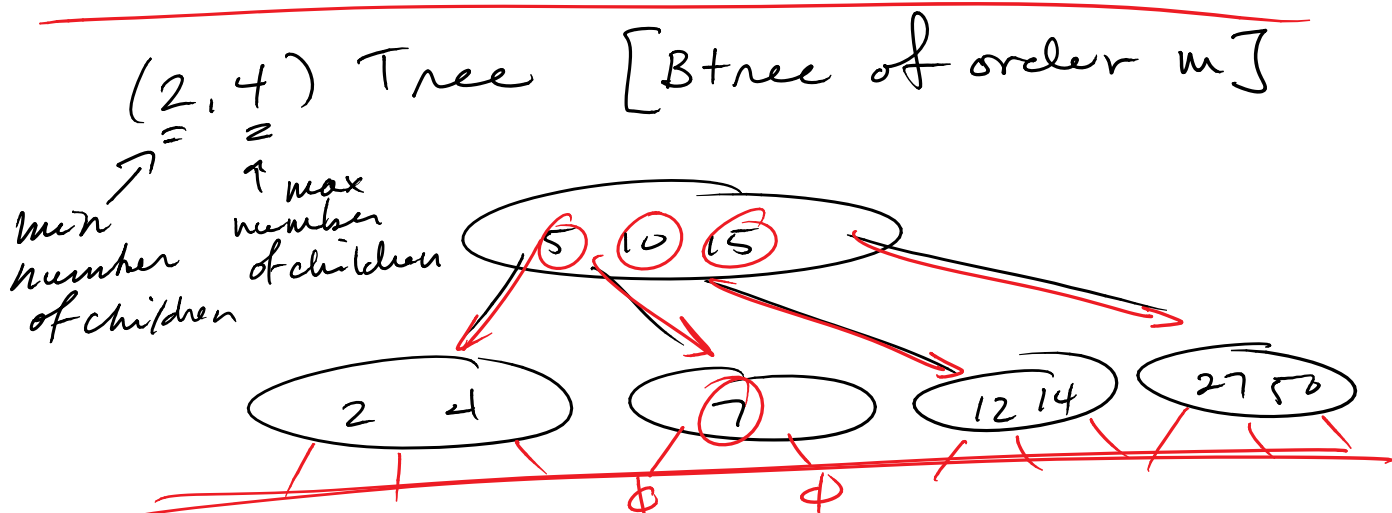
$(15)$   
 $2^{4-1} + 1$

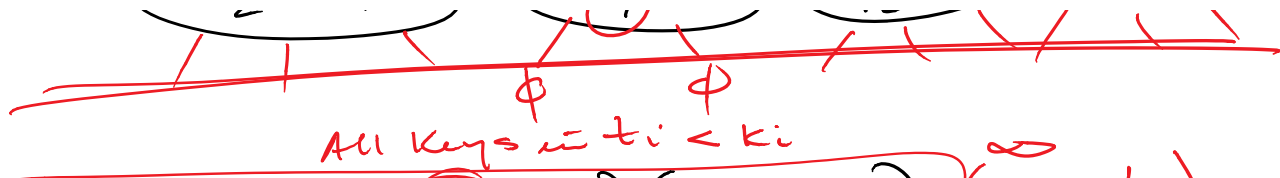
$(31)$   
 $2^{5-1} + 1$

Search, insert, delete  $O(\log n)$

insert - at most requires 1 rotate

delete - at most  $\log n$  rotation





All keys in  $t_i < k_i$

$t_0 (k_1, t_1) (\textcircled{k_2}, t_2) (k_3, t_3) (\infty, t_4)$

All values in  $t_{i-1} < k_i$

All values in  $t_i \geq k_i$

And  $k_i \leq k_{i+1}$  for  $i = 1 \dots 3$

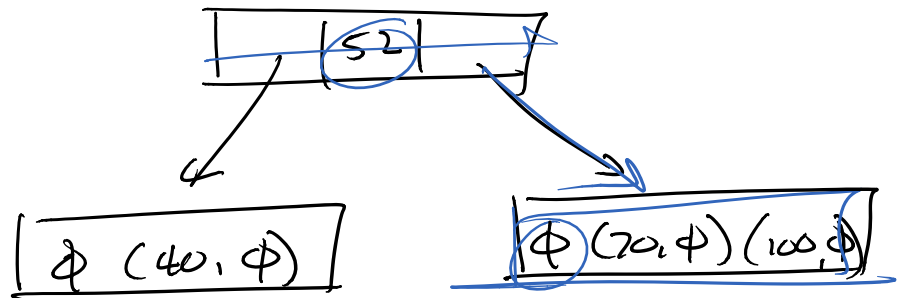
~~$\phi$~~  | 100 |  $\phi$

(52,  $\phi$ )  $\phi$  | (52,  $\phi$ ) | (100,  $\phi$ )

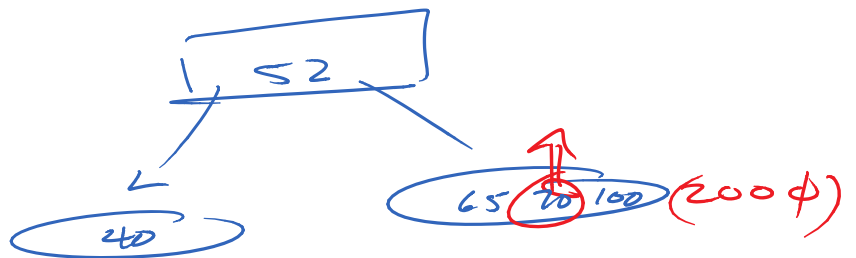
(40,  $\phi$ )  $\phi$  | (40,  $\phi$ ) | (52,  $\phi$ ) | (100,  $\phi$ )  $4/2 = 2$

(70,  $\phi$ )  $\phi$  | (40,  $\phi$ ) |  $\phi$  | (52,  $\phi$ ) | (70,  $\phi$ ) | (100,  $\phi$ )

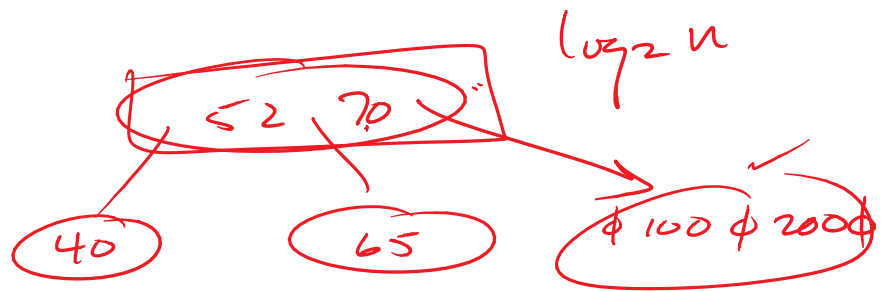
65



200



2, 4  
Btree of  
order 4



Btree of  
order 400

$$\begin{array}{l}
 1 \\
 400 \\
 400^2 \\
 400^3 \sim 64,000,000
 \end{array}$$