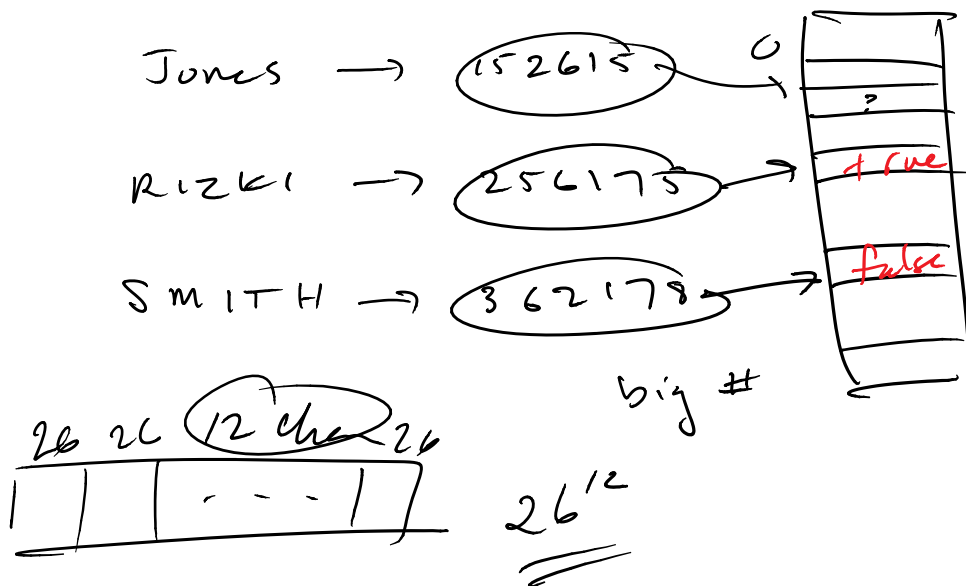


		<u>Insert/Remove</u>	<u>Search</u>
<u>Array</u>	sort	$O(N)$	$O(\log n)$
	unsort	$O(1)$	$O(N)$
<u>List</u>		$O(1)$	$O(N)$
<u>Tree</u>	balanced	$O(\log n)$	$O(\log n)$
		$O(1)$	$O(1)$

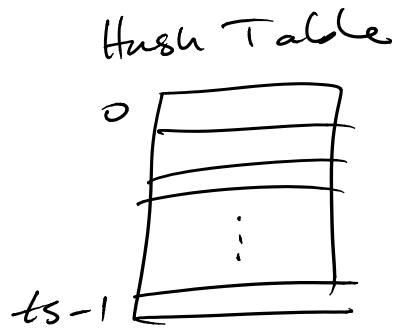


h: Key space → address space
 very large moderate

Hash Table

Hash Function

$h(\text{key}) = \text{table location}$



Keys $h(\text{keys})$ Hash Table

27 5

15 4

18 7

26 ④

14 3

collision
collision handling
technique



table size = 11

$O(ts)$

$$h(\text{key}) = \text{key} \% ts$$

$$= \text{key} \% 11$$

linear probing to resolve collision

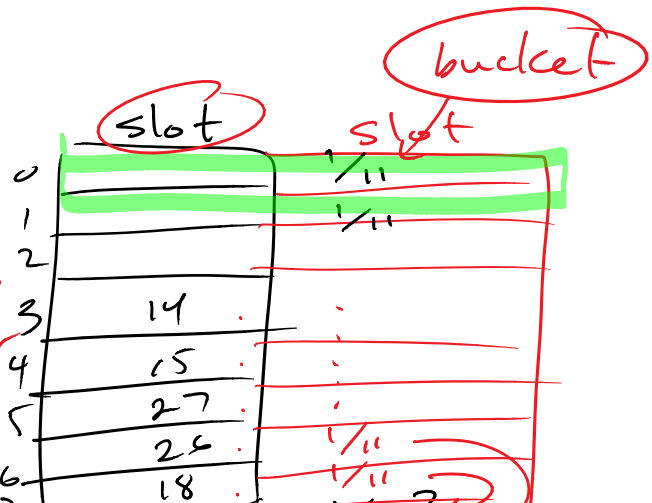
$$h(\text{key}) = (\text{key} + i) \% ts \quad i = 1, 2, 3, \dots, ts-1$$

probability
of a collision

$$\lambda = \frac{N}{ts} = \frac{5}{11}$$

$N = 5$

primary
cluster



$$\lambda = \frac{N}{ts} = \frac{5}{11}$$

↑
load factor

$$ts = 11$$

1 cu

5	25	1/11
6	18	1/11
7		1/11 ?
8		
9		
10		6/11

linear probing

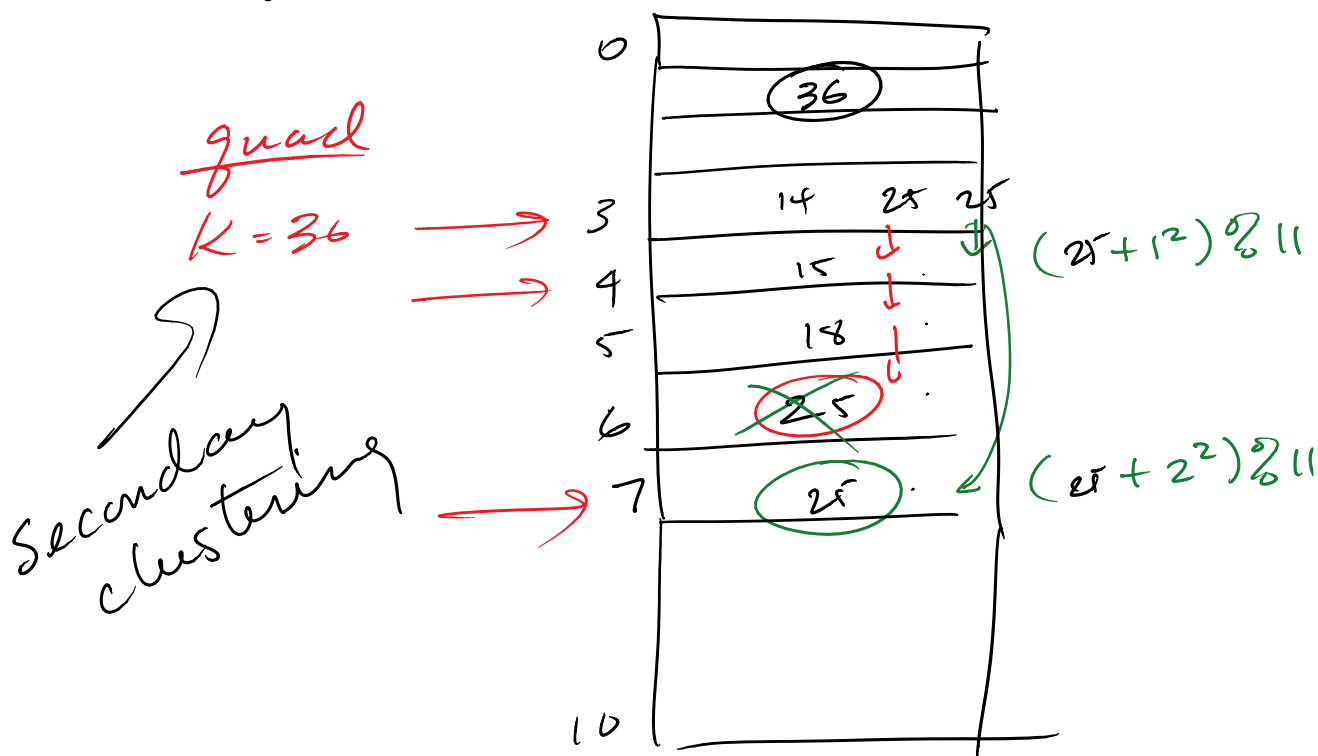
$$h(k) = (k + i) \% ts$$

$i = 1, 2, 3, \dots$

quadratic probing

$$h(k) = (k + i^2) \% ts$$

$i = 1, 2, 3, \dots$



double hash

$$h(k) = k \% ts$$

$$\begin{cases} h'(k) = k \% ts' \\ h(k) = (h(k) \% ts + h'(k) \% ts') \% ts \end{cases}$$

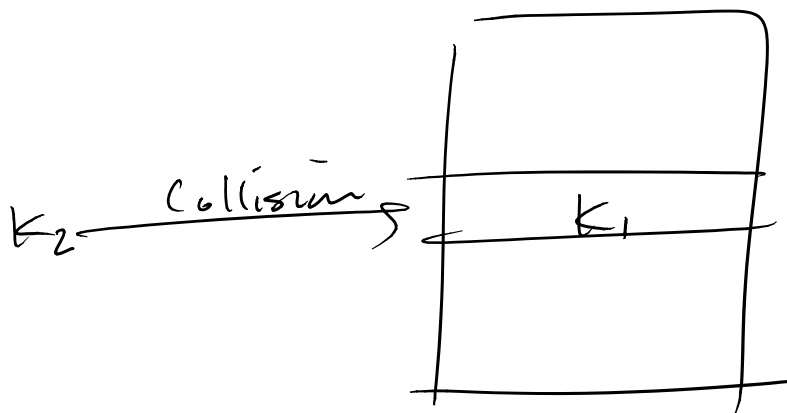
$$\left\{ \begin{aligned} h(k) &= (k + (h'(k) \% ts) \cdot i) \% ts \\ i &= 1, 2, 3, \dots \end{aligned} \right.$$

$$h(k) = k \% 11$$

$$h'(k) = (k \% 7) + 1$$

$$\left\{ \begin{aligned} h(k) &= (k + h'(k) \cdot i) \% 11 \end{aligned} \right.$$

<u>Keys</u>	<u>$h(k)$</u>
27	3
15	4
18	7
14	<div style="display: inline-block; vertical-align: middle;"> $(14 \% 7) + 1 = \boxed{1}$ $\textcircled{3} \rightarrow \textcircled{4} \rightarrow \textcircled{5}$ </div>
26	<div style="display: inline-block; vertical-align: middle;"> $(26 \% 7) + 1 = \boxed{6}$ $\textcircled{4} \rightarrow \textcircled{10}$ </div>



linear
tests
every where

Quadratic
if table
is prime#

double hash
+ prime#

double room
 ts prime[#]
 ts' prime[#]

