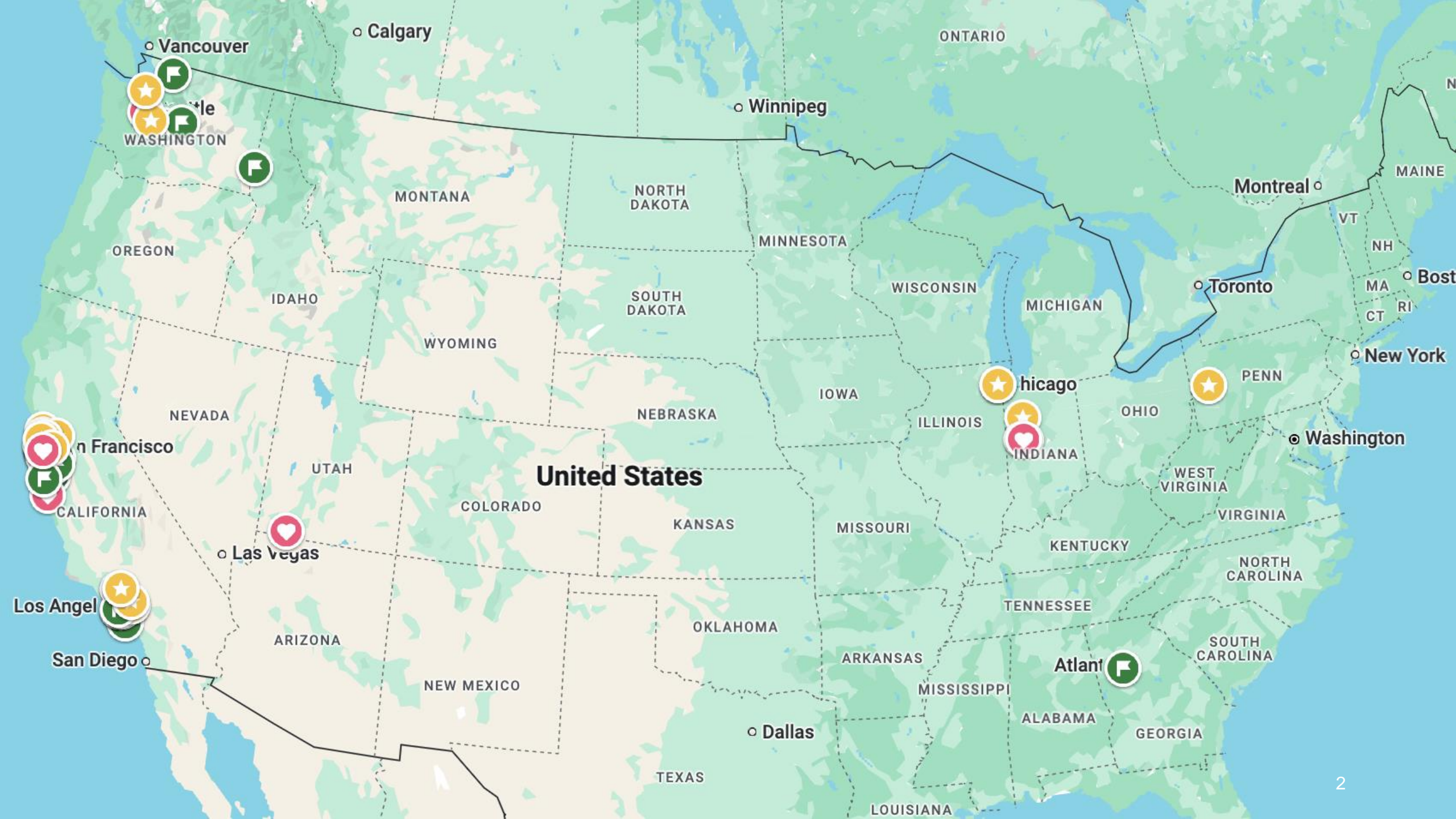


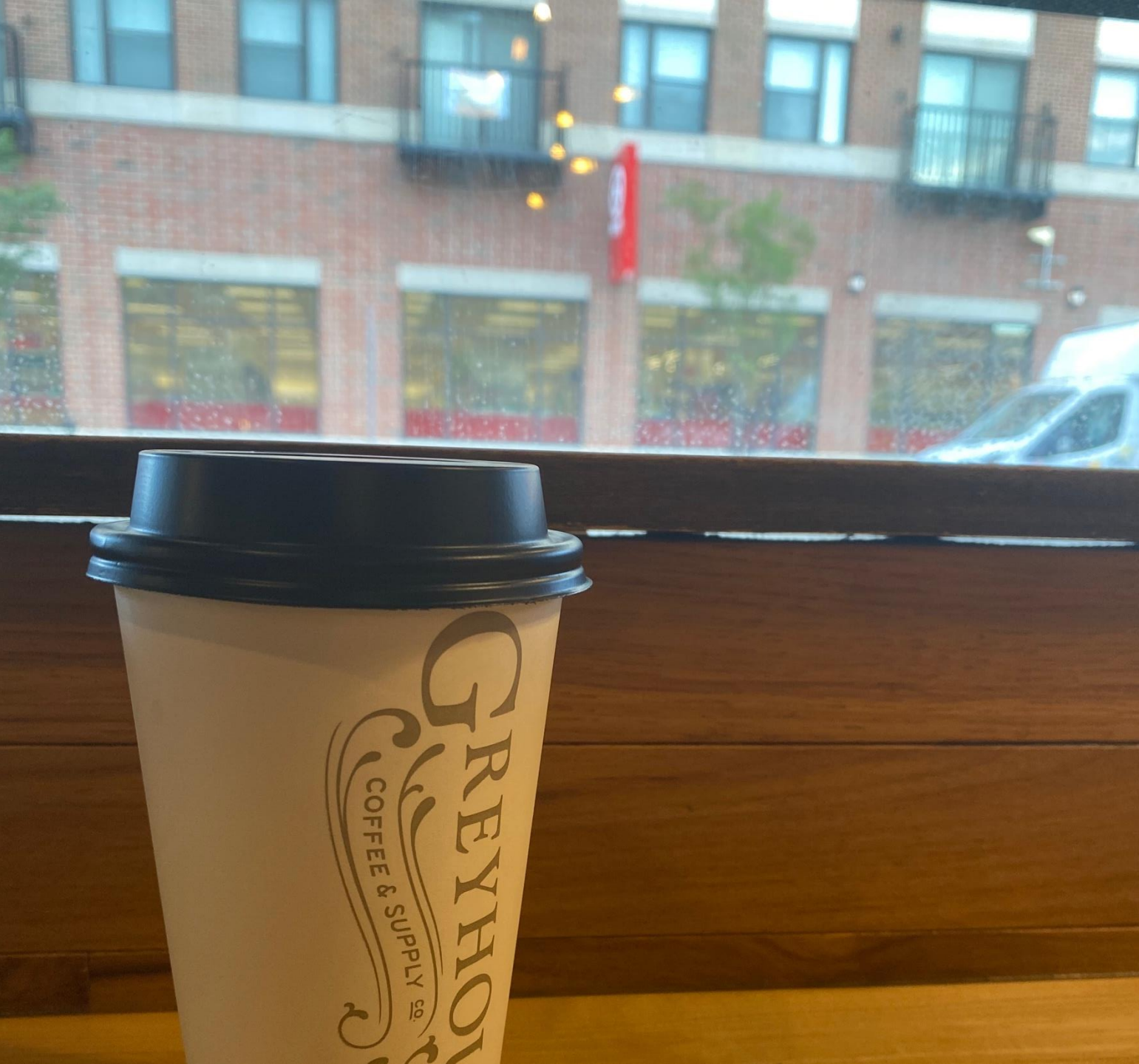
# Frequency-domain Operators

Fall 2024

Yi-Ting Chen













<https://youtu.be/bzfT16k6HEM?si=e0jhnHITQKeigGHk>



# Take It With A Grain of Salt

Apple Podcast 預覽



186 集

The American English Podcast teaches the language and culture of the United States. Through common expressions, pronunciation tips and interesting cultural snippets or stories, I hope to keep this fun, useful and interesting! All bonu更多

## American English Podcast

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2024年5月29日

### Expression: To Take It With A Grain Of Salt >

In today's episode, we'll begin by going through the commentary you guys made on Culture Shock in the United States. Afterwards, I'll tell you a joke, we'll go over the expression "to take it with a grain of salt," and we'll do a pronunciation exercise. Premium Content for this episode is available with...

▶ 播放 25 分鐘

2024年5月18日

### Chats with Shana: Culture Shock in the U.S. (Everyday Life) >

In this Chats with Shana episode, I'm going to reflect on various aspects of US culture. Although I talk about culture all the time on here, it's not often we talk about some basic things, like everyday life things that can cause culture shock. The truth is, I don't often think about the topics I'm going ...

▶ 播放 30 分鐘

# 1-D Linear Time Invariant System



## Linear System

Additivity:  $T\{x_1(t) + x_2(t)\} = T\{x_1(t)\} + T\{x_2(t)\} = y_1(t) + y_2(t)$

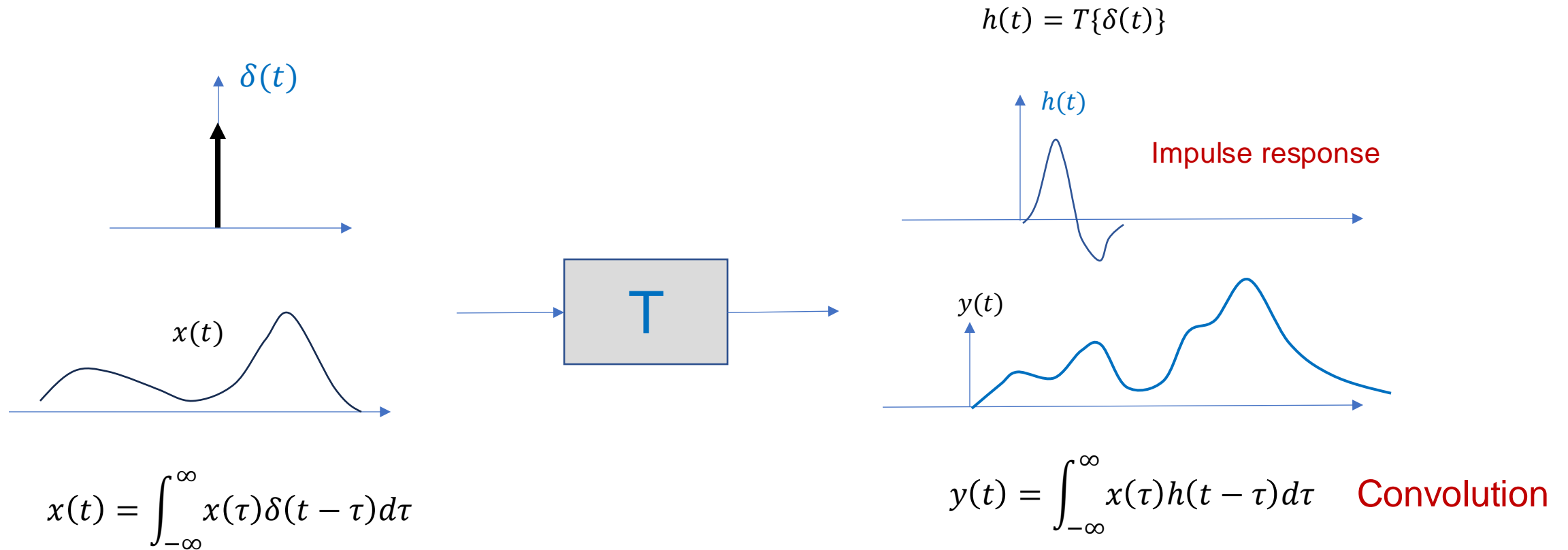
Homogeneity:  $T\{ax(t)\} = aT\{x(t)\} = ay(t)$

## Time-Invariant System

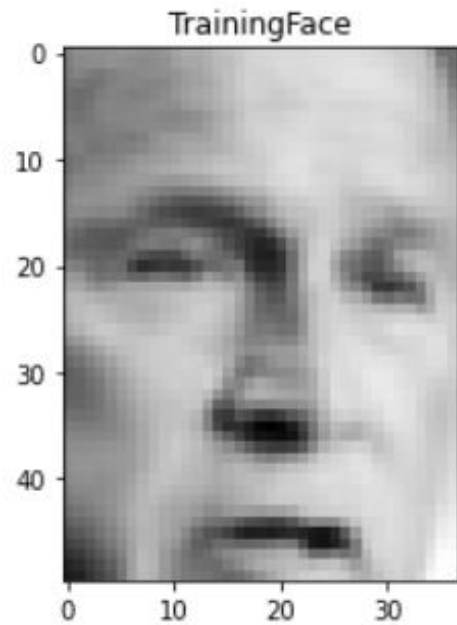
If  $y(t) = T\{x(t)\}$ , then  $y(t - t_0) = T\{x(t - t_0)\}$ .



# Summary



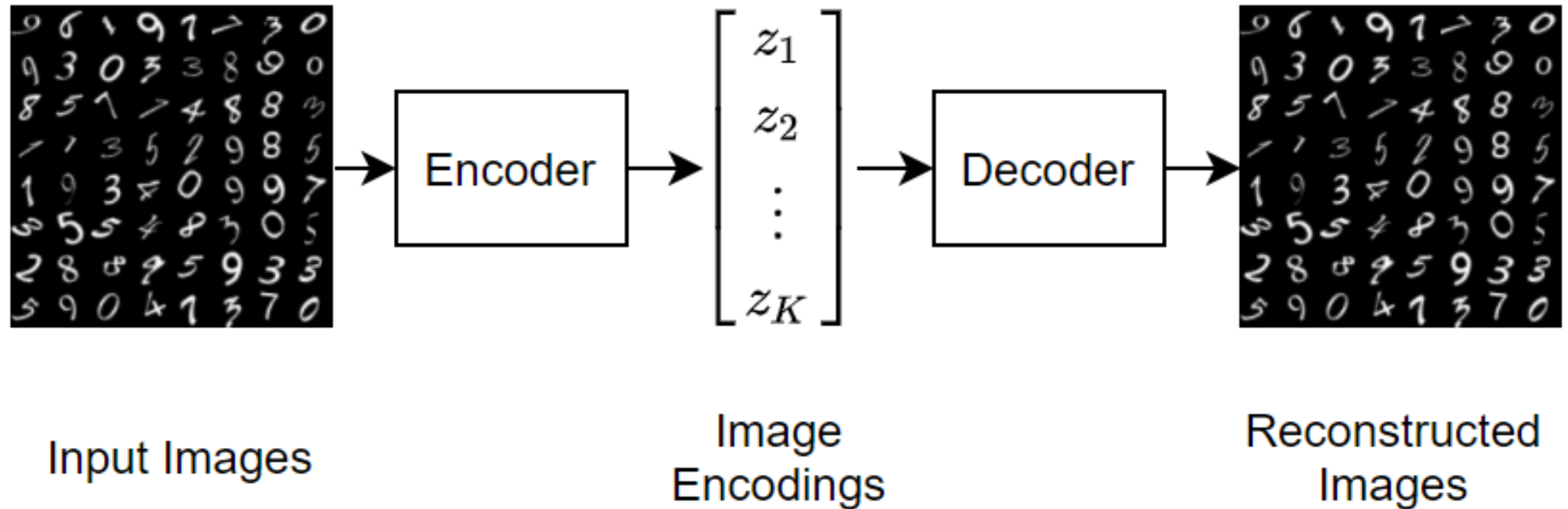
# Eigenfaces



=



# Variational Autoencoder (VAE)





# Frequency-Domain Analysis (1/3)

$$e^{j2\pi ft} = \cos(2\pi ft) + j\sin(2\pi ft)$$

$$\begin{aligned} x(t) = e^{j2\pi ft} &\longrightarrow \boxed{\text{T}} \longrightarrow y(t) = \int_{-\infty}^{\infty} x(\tau)h(t-\tau)d\tau \\ &= \int_{-\infty}^{\infty} x(t-\tau)h(\tau)d\tau \\ &= \int_{-\infty}^{\infty} e^{j2\pi f(t-\tau)}h(\tau)d\tau \\ &= e^{j2\pi ft} \int_{-\infty}^{\infty} e^{-j2\pi f\tau}h(\tau)d\tau \\ &\equiv H(f)e^{j2\pi ft} \end{aligned}$$

## **H(f): Frequency Response**

This is a complex-valued function that characterizes how the system responds to a sinusoid of frequency  $f$ . It typically includes both a gain (magnitude) and a phase shift.

$$y(t) = |H(f)|e^{j(2\pi ft + \arg(H(f)))}$$

# Frequency-Domain Analysis (2/3)

## Fourier Transform Pair

$$X(f) = \int_{-\infty}^{\infty} x(t)e^{-j2\pi ft} dt$$

where  $e^{-j2\pi ft} = \cos(2\pi ft) - j\sin(2\pi ft)$

$$x(t) = \int_{-\infty}^{\infty} X(f)e^{j2\pi ft} df$$

where  $e^{j2\pi ft} = \cos(2\pi ft) + j\sin(2\pi ft)$

$$X(f) = \text{Re}\{X(f)\} + j\text{Im}\{X(f)\} = |X(f)|e^{j\angle X(f)}$$

$|X(f)|$  Magnitude

$\angle X(f)$  Phase

# Frequency-Domain Analysis (3/3)

$$x(t) = \int_{-\infty}^{\infty} X(f) e^{j2\pi f t} df \longrightarrow \boxed{\text{T}} \longrightarrow y(t) = \int_{-\infty}^{\infty} X(f) T\{e^{j2\pi f t}\} df$$
$$= \int_{-\infty}^{\infty} X(f) H(f) e^{j2\pi f t} df$$

$\Rightarrow Y(f) = X(f) H(f)$



We will not have classes next week!

ROAD++ @ ECCV2024

HomeAccepted PapersChallengeDatasetSpeakersVenueCall for PapersWorkshop Archive



# ROAD++: The Third Workshop & Challenge: Event Detection for Situation Awareness in Autonomous Driving

Co-hosted by ECCV 2024

Sep 29 , MiCo Milano





# We will not have lecture on 10/8, but I will record an offline lecture and upload to E3.



[https://developmental-robotics.jp/en/members/yukie\\_nagai/](https://developmental-robotics.jp/en/members/yukie_nagai/)



<https://homes.luddy.indiana.edu/djcran>