

MP5 Report

A1.

Time update

$$x_k = Ax_{k-1} + Bu_{k-1}$$

$$P_k = AP_{k-1}A^T + Q$$

In order to calculate time update x_k we compute x_k previous and use u_k our data. x_k is initially $[0,0]$ but then in a loop we will compute a more precise x_k based on the data u_k . We compute x_k time update or x_k time by $x_{\text{time}} = x_k \text{ previous} + u_k$.

In order to calculate P_k we add our system noise Q to P_k in every iteration. Q is the given matrix in the pdf. $P_{k \text{ time}} = p_k + Q$

Measurement update

$$x_k = x_k + K_k(z_k - Hx_k)$$

$$K_k = p_k H^T / (H p_k H^T + R)$$

$$P_k = (I - K_k H) p_k$$

In order to calculate measurement update x_k we must first calculate K_k . k_k is calculated by taking p_k from time update and multiplying it by the inverse of calculated p_k from time update + the given measurement noise.

Now that we have K_k we can calculate x_k measurement. $x_k \text{ measurement} = x_k \text{ from time update} + K_k \text{ dot product with the difference of } z_k - x_k \text{ (time update)}$. z_k is from the given data.

Lastly we can calculate p_k for measurement update. All we have to do is dot product the matrix from time update by the difference of the identity matrix and K_k .

A4. After testing multiple lambda values for the $P = \lambda I$ equation we chose the lambda value 0.3285 which we believed yielded the best results after testing. Below is the graph of or observation and estimates. Observation being red and estimates being blue.

