

Phy cpt 3

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Matriculation Physics: Momentum and Impulse (Q4)

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Example 1

A 500 g squash ball is travelling on its right with a speed of 5 m s^{-1} . It then hits the wall and bounce back with the same speed in 0.3 s . Find the
a) momentum of the squash ball (Answer: 2.5 kg ms^{-1})
b) impulse of the ball (Answer: -5 kg ms^{-1})
c) impulsive force on the ball (Answer: -16.67 N)

$$u = 5 \quad v = -5$$
$$J = \Delta p = m(v - u) = 0.5(-5 - 5) = -5 \text{ kg ms}^{-1}$$
$$F = \frac{J}{\Delta t} = \frac{-5}{0.3} = -16.67 \text{ N}$$

Example 2

A 0.20 kg tennis ball strikes the wall horizontally with a speed of 100 m s^{-1} and it bounces off with a speed of 70 m s^{-1} in the opposite direction.

a) Calculate the magnitude of impulse delivered to the ball by the wall. (Answer: 34 N s)
b) If the ball is in contact with the wall for 10 ms , determine the magnitude of average force exerted by the wall on the ball (Answer: 3400 N)

$$J = m(v - u) = 0.2(-70 - 100) = -34 \text{ kg ms}^{-1}$$
$$F = \frac{J}{\Delta t} = \frac{-34}{0.01} = -3400 \text{ N}$$

Example 3

A baseball with a mass of 0.2 kg is moving towards a player with a speed of 50 m s^{-1} . The player then hits the ball with his bat. The bat exerts an average force of $8.0 \times 10^3 \text{ N}$ on the ball for 1.6 ms . The average force is directed in the opposite direction to the initial velocity of the ball. Calculate the final speed of the ball. (Assume that u is to the left and F is to the right)

$$J = F \Delta t = 8.0 \times 10^3 \times 1.6 \times 10^{-3} = 12.8 \text{ kg ms}^{-1}$$
$$m(v - u) = J \Rightarrow 0.2(v - (-50)) = 12.8 \Rightarrow v = 14 \text{ m s}^{-1}$$

Exercise 3.1:

1. A steel ball with mass 40.0 g is dropped from a height of 2.00 m onto a horizontal steel slab. The ball rebounds to a height of 1.60 m .
a) Calculate the impulse delivered to the ball during impact.
b. If the ball is in contact with the slab for 2.00 ms , determine the average force on the ball during impact.

$$J = m(v_2 - v_1) = 0.04(5.6079 - (-0.475)) = 0.475 \text{ kg ms}^{-1}$$
$$F = \frac{J}{\Delta t} = \frac{0.475}{2.00 \times 10^{-3}} = 237.5 \text{ N}$$

2. A golf ball ($m = 46.0 \text{ g}$) is struck with a force that makes an angle of 45° with the horizontal. The ball lands 200 m away on a flat fairway. If the golf club and ball are in contact for 1.00 ms , calculate the average force of impact. (neglect the air resistance).

$$J = F \Delta t = 0.046(4.91945) = 0.233 \text{ kg ms}^{-1}$$
$$F = \frac{J}{\Delta t} = \frac{0.233}{1.00 \times 10^{-3}} = 233 \text{ N}$$

Example 4

Figure shows an object A of mass 200 g collides head-on with object B of mass 100 g . After the collision, B moves at a speed of 3 m s^{-1} to the left. Determine the velocity of object A after collision. Is the collision elastic or inelastic? (Answer: -3.5 m s^{-1})

$$m_B u_B + m_A u_A = m_B v_B + m_A v_A$$
$$0.1(-6) + 0.2(3) = 0.1(-3) + 0.2v_A \Rightarrow v_A = -3.5 \text{ m s}^{-1}$$

Example 5

A car of mass 3000 kg travelling with a velocity of 90 km h^{-1} collides with a stationary car of mass 2000 kg . After collision, the two cars move with the same velocity v . What is the velocity v ? Calculate the impulse of the first car. (Answer: 15 ms^{-1} , $-30 \times 10^3 \text{ kg ms}^{-1}$)

$$m_1 u_1 + m_2 u_2 = (m_1 + m_2) v$$
$$3000 \left(\frac{90 \times 1000}{3600} \right) + 2000(0) = (3000 + 2000)v \Rightarrow v = 15 \text{ ms}^{-1}$$
$$J = m(v - u) = 3000(15 - \frac{90 \times 1000}{3600}) = -30000 \text{ kg ms}^{-1}$$

Example 6

A bullet fired from a pistol has a mass of 8.0 g and a muzzle speed of 352 m s^{-1} . If the mass of the gun is 0.9 kg , what is its recoil speed when fired horizontally? (Answer: -3.13 ms^{-1})

$$m_1 u_1 + m_2 u_2 = m_1 v_1 + m_2 v_2$$
$$0.008(352) + 0.9(0) = 0.008v_1 + 0.9v_2 \Rightarrow v_2 = -3.13 \text{ ms}^{-1}$$

Matriculation Physics: Conservation of Linear Momentum (Q7)

Example 7

A tennis ball of mass m_1 moving with initial velocity u_1 collides with a soccer ball of mass m_2 initially at rest. After the collision, the tennis ball is deflected 50° from its initial direction with a velocity v_1 as shown in figure. Suppose that $m_1 = 250 \text{ g}$, $m_2 = 900 \text{ g}$, $u_1 = 20 \text{ m s}^{-1}$ and $v_1 = 4 \text{ m s}^{-1}$. Calculate the magnitude and direction of soccer ball after the collision.

$$m_1 u_1 = m_1 v_1 \cos 50^\circ + m_2 v_2 \cos \theta$$
$$0.25(20) = 0.25(4 \cos 50^\circ) + 0.9(v_2 \cos \theta)$$
$$v_2 = 4.91 \text{ m s}^{-1}, \theta = 9.97^\circ$$

Example 8

A ball moving with a speed of 17 m s^{-1} strikes an identical ball that is initially at rest. After the collision, the incoming ball has been deviated by 45° from its original direction and the struck ball moves off at 30° from the original direction as shown in figure. Calculate the speed of each ball after the collision.

$$m_1 u_1 = m_1 v_1 \cos 45^\circ + m_2 v_2 \cos 30^\circ$$
$$17 = v_1 \cos 45^\circ + v_2 \cos 30^\circ$$
$$m_1 u_1 \sin 45^\circ = m_1 v_1 \sin 45^\circ + m_2 v_2 \sin 30^\circ$$
$$17 \sin 45^\circ = v_1 \sin 45^\circ + v_2 \sin 30^\circ$$
$$v_1 = 12.45 \text{ m s}^{-1}, v_2 = 8.80 \text{ m s}^{-1}$$

Example 9

A 1 kg ball moves to the right at 4 m s^{-1} and collides head-on with a stationary 2 kg ball. Calculate the final velocity of each ball after the elastic collision. (Answer: 2.67 ms^{-1} , -1.34 ms^{-1})

$$m_1 u_1 + m_2 u_2 = m_1 v_1 + m_2 v_2$$
$$1(4) + 2(0) = 1v_1 + 2v_2$$
$$4 = v_1 + 2v_2$$
$$v_1 = 4 - 2v_2$$
$$\frac{1}{2} m_1 u_1^2 + \frac{1}{2} m_2 u_2^2 = \frac{1}{2} m_1 v_1^2 + \frac{1}{2} m_2 v_2^2$$
$$\frac{1}{2}(1)(4)^2 = \frac{1}{2}(1)v_1^2 + \frac{1}{2}(2)v_2^2$$
$$8 = v_1^2 + 2v_2^2$$
$$8 = (4 - 2v_2)^2 + 2v_2^2$$
$$8 = 16 - 16v_2 + 4v_2^2 + 2v_2^2$$
$$0 = 8 - 16v_2 + 6v_2^2$$
$$0 = 2(4 - 4v_2 + 3v_2^2)$$
$$0 = 2(3v_2^2 - 4v_2 + 4)$$
$$0 = 3v_2^2 - 4v_2 + 4$$
$$v_2 = 2.67 \text{ ms}^{-1}, v_1 = -1.34 \text{ ms}^{-1}$$

FIGURE 3.1

FIGURE 3.1 shows a 12 g bullet shot vertically into a 5 kg block and lifting it upwards to a maximum height of 4 mm . The bullet travelled for 4 ms in the block before stopping completely. Calculate the
i) speed of the block and bullet just after the collision.
ii) impulse on the block.

$$m_1 u_1 + m_2 u_2 = (m_1 + m_2) v$$
$$0.012(1000) + 5(0) = (0.012 + 5)v \Rightarrow v = 2.4 \text{ m s}^{-1}$$
$$J = \Delta p = m(v - u) = 0.012(2.4 - 0) = 0.0288 \text{ kg ms}^{-1}$$

FIGURE 3.3

Object A and B, of masses 1.5 kg and 2.0 kg respectively, are on a horizontal plane as shown in FIGURE 3.3. B is at rest but A moves at constant speed 4.0 m s^{-1} towards B. After collision, A moves in the opposite direction at constant speed 2.0 m s^{-1} while B moves at constant speed towards a vertical wall. When B strikes the wall, the wall exerts an impulse of magnitude 15 N s on B. Determine the speed of B after B has collided with the wall.

$$m_1 u_1 + m_2 u_2 = m_1 v_1 + m_2 v_2$$
$$1.5(4) + 2(0) = 1.5(-2) + 2v_2 \Rightarrow v_2 = 4.5 \text{ m s}^{-1}$$
$$J = F \Delta t = 15 \text{ N s}$$
$$m(v - u) = J \Rightarrow 2(v - 4.5) = 15 \Rightarrow v = 7.5 \text{ m s}^{-1}$$

FIGURE 3.4

A car with the velocity of 2 m s^{-1} collides with another car which is at rest as shown in FIGURE 3.4. The second car is initially at rest. After the collision, car A moves at 1 m s^{-1} and B moves horizontally. Calculate the final velocity of each car after the collision. Assume the collision is elastic.

$$m_1 u_1 + m_2 u_2 = m_1 v_1 + m_2 v_2$$
$$2m_1(2) + m_2(0) = m_1(1) + m_2 v_2$$
$$4m_1 = m_1 + m_2 v_2 \Rightarrow v_2 = 3 \text{ m s}^{-1}$$

Types of Collisions

ELASTIC COLLISION

The total kinetic energy of a system is conserved.

$$\sum KE_{\text{before}} = \sum KE_{\text{after}}$$

Light - KE is NOT a vector

$$\frac{1}{2} m_1 u_1^2 + \frac{1}{2} m_2 u_2^2 = \frac{1}{2} m_1 v_1^2 + \frac{1}{2} m_2 v_2^2$$

6

A 20-kg object sitting at rest is struck elastically head-on collision with a 10-kg object initially moving at 3.0 m s^{-1} . Find the final velocity of 20-kg object after collision.

$$m_1 u_1 + m_2 u_2 = m_1 v_1 + m_2 v_2$$
$$20(0) + 10(3) = 20v_1 + 10v_2$$
$$0 = 2v_1 + v_2$$
$$v_2 = -2v_1$$
$$\frac{1}{2} m_1 u_1^2 + \frac{1}{2} m_2 u_2^2 = \frac{1}{2} m_1 v_1^2 + \frac{1}{2} m_2 v_2^2$$
$$\frac{1}{2}(20)(0)^2 + \frac{1}{2}(10)(3)^2 = \frac{1}{2}(20)v_1^2 + \frac{1}{2}(10)(-2v_1)^2$$
$$45 = 20v_1^2 + 20v_1^2$$
$$45 = 40v_1^2$$
$$v_1 = 1.07 \text{ m s}^{-1}, v_2 = -2.14 \text{ m s}^{-1}$$