# Modern Cryptography and Its Applications

# 9 Message Authentication

Ch12 in textbook

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# **Key Points of Lecture**

- Two security services:
  - Authentication
  - Data Integrity
- Two security mechanism: Irreversible encipherment mechanisms
  - Hash function
  - Message Authentication Codes (MAC)





 Table 1.4
 Relationship Between Security Services and Mechanisms

					MECHANISM							
	SERVICE	/¢;	nciphet O	ngital s	gratur geess	antiol A	of the ni	cation control	adding outing	gontrol John tra	idon	
	Peer entity authentication	Y	Y			Y						
	Data origin authentication	Y	Y									
	Access control			Y								
	Confidentiality	Y						Y				
	Traffic flow confidentiality	Y					Y	Y				
	Data integrity	Y	Y		Y							
	Nonrepudiation		Y		Y				Y			
	Availability				Y	Y						

no single mechanism that will support all services required



### **Security Service & Attack**

#### **Security Service**

Data Confidentiality

- Message Authentication
- Data Integrity

Non-repudiation

#### **Security Attack**

Disclosure Traffic analysis

Masquerade (伪装) Content modification Sequence modification Timing modification

Source repudiation

**Destination repudiation** 

#### **Measures & Attack**

#### **Measures**

Encryption (discussed before)

Message Authentication

- DS: digital signatures
- Combination of the use of DS and a special designed protocol

#### **Security Attack**

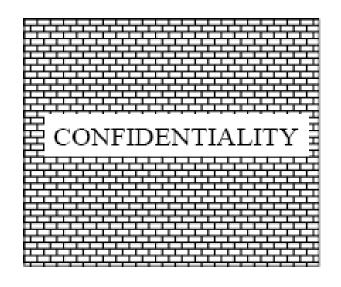
Disclosure Traffic analysis

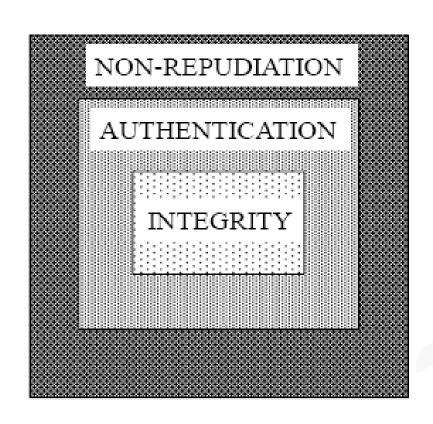
Masquerade (伪装) Content modification Sequence modification Timing modification

Source repudiation

**Destination repudiation** 

### **Relations among Security Services**

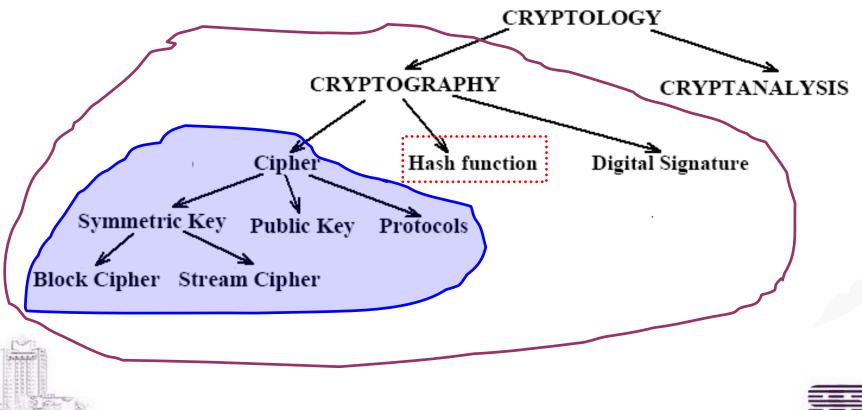






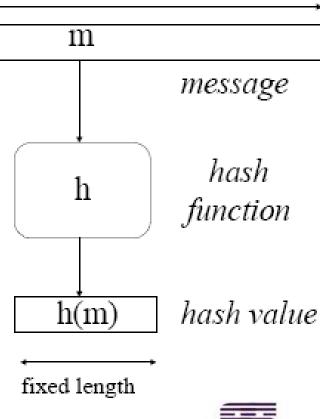


# Basic security mechanism



### **Hash Function**

- Hash function h(m)
   Basic Requirements
  - 1) Public description, no key.
  - 2) Compression
  - arbitrary length input → fixed length output
  - 4) *h(m)* is easy to compute (hw and sw).





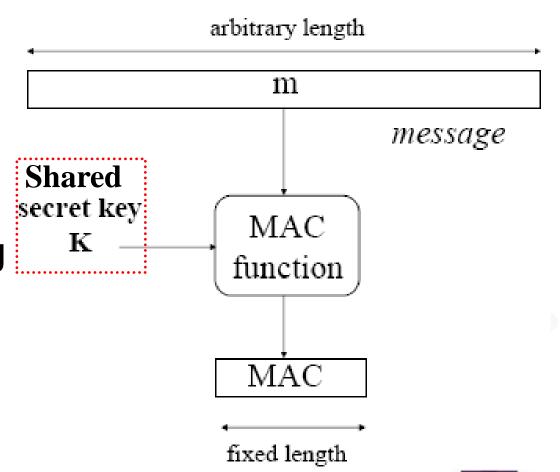
arbitrary length

### **MAC - Message Authentication Codes**

MAC=C(k,m)

– HMAC: keyed hash functions

– CMAC: CipherBlock ChainingMAC





Software Bo

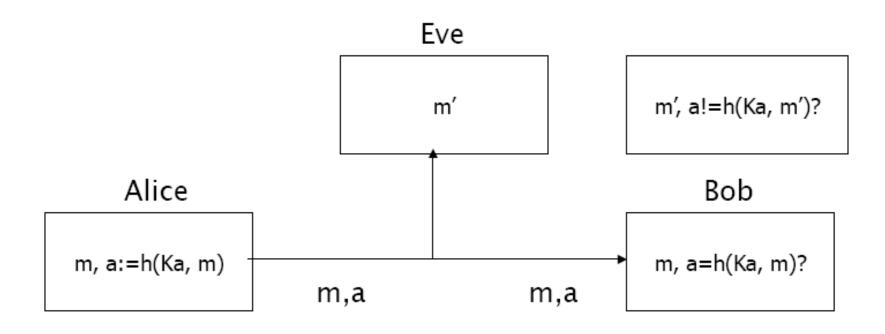
# **MAC Properties**

a MAC is a cryptographic checksum
 MAC = C<sub>K</sub> (M)

- condenses(压缩) a variable-length message M
- using a secret key K
- to a fixed-sized authenticator
- is a many-to-one function
  - potentially many messages have same MAC
  - but finding these needs to be very difficult



# **MAC & Integrity**



Ka: Authentication key, share by Alice and Bob

a: Message Authentication Code (MAC)

#### 前提:

- 《1.(抗碰撞性)若m'≠m,则h(Ka,m)必定≠h(Ka,m')
  - 2.只有知道密钥ka的人,才能计算出m的验证码h(Ka,m')



### **Outline**

- Message Authentication Functions
- Requirements For Message Authentication Code (MAC)
- Security Of MACs
- MACs Based On Hash Functions: HMAC
- MACs Based On Block Ciphers: DAA and **CMAC**





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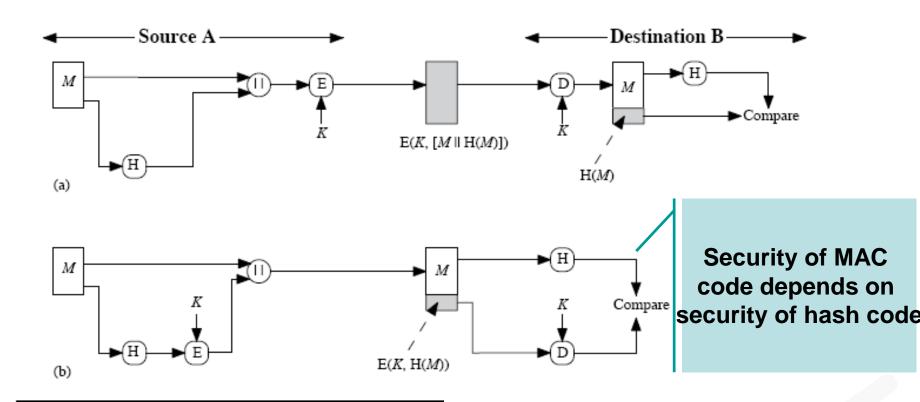


# Message Authentication

- message authentication
  - is concerned with:
    - protecting the integrity of a message
    - validating identity of originator
    - non-repudiation of origin (dispute resolution)
  - has two levels of functionality (like digital signature)
    - · authenticator: used to authenticate a message
    - primitive: used to verify the authenticity of a message by a receiver
- three types of function used to produce an authenticator:
  - hash function
  - message encryption
  - message authentication code (MAC)



# (1) Use Hash Function



 $A \rightarrow B: E(K, [M || H(M)])$ 

- Provides confidentiality
  - —Only A and B share K
- ·Provides authentication
  - —H(M) is cryptographically protected

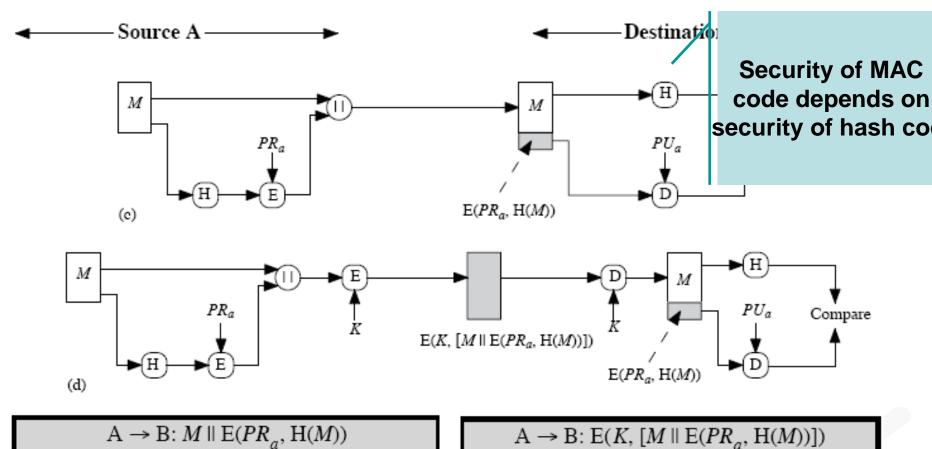
 $A \rightarrow B: M \parallel E(K, H(M))$ 

- Provides authentication
  - —H(M) is cryptographically protected

(b) Encrypt hash code - shared secret key

(a) Encrypt message plus hash code

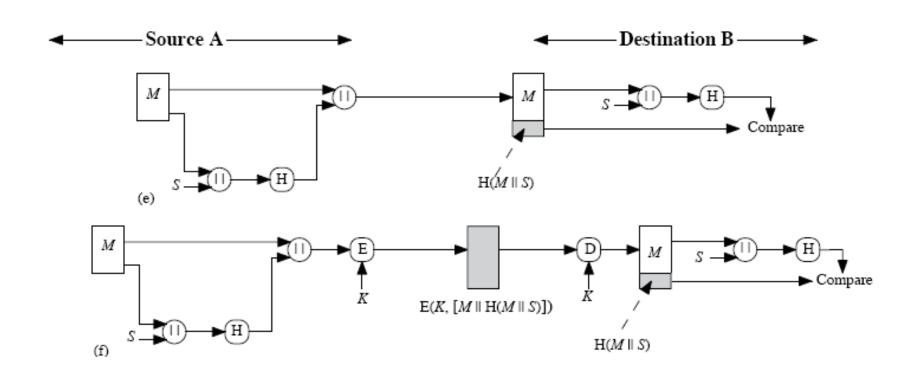




- $A \rightarrow B: M \parallel E(PR_{\alpha}, H(M))$
- Provides authentication and digital signature
  - —H(M) is cryptographically protected
  - —Only A could create  $E(PR_a, H(M))$

- Provides authentication and digital
- signature
- Provides confidentiality
  - —Only A and B share K

- (c) Encrypt hash code sender's private key
- (d) Encrypt result of (c) shared secret key



 $A \rightarrow B: M \parallel H(M \parallel S)$ 

- •Provides authentication
  - -Only A and B share S
- (e) Compute hash code of message plus secret value

#### $A \rightarrow B: E(K, [M \parallel H(M \parallel S)])$

- Provides authentication
  - —Only A and B share S
- Provides confidentiality
  - —Only A and B share K

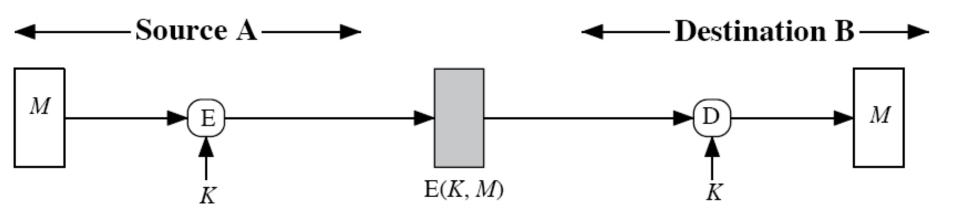
(f) Encrypt result of (e)

### **Choice for Only Authentication**

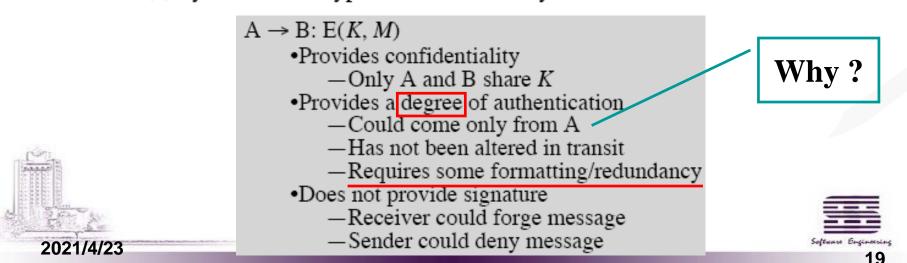
- When confidentiality is not required, encryption to the entire message should be avoid:
  - Encryption software is relatively slow
  - Encryption hardware costs are not negligible
  - Encryption hardware is optimized toward large data sizes
  - Encryption algorithms may be covered by patents

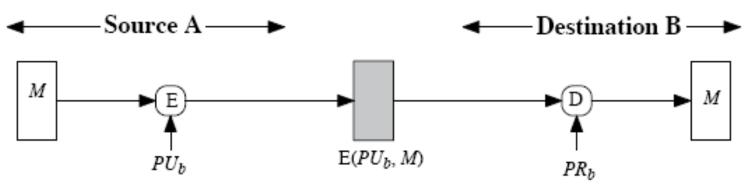
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## (2) Use Message Encryption



(a) Symmetric encryption: confidentiality and authentication





(b) Public-key encryption: confidentiality



(c) Public-key encryption: authentication and signature



(d) Public-key encryption: confidentiality, authentication, and signature



#### $A \rightarrow B: E(PU_b, M)$

- Provides confidentiality
  - —Only B has PR<sub>b</sub> to decrypt
- ·Provides no authentication
  - —Any party could use  $PU_b$  to encrypt message and claim to be A
    - (b) Public-key (asymmetric) encryption: confidentiality

#### $A \rightarrow B: E(PR_a, M)$

- Provides authentication and signature
  - —Only A has PR<sub>a</sub> to encrypt
  - -Has not been altered in transit
  - —Requires some formatting/redundancy
  - —Any party can use  $PU_a$  to verify signature
    - (c) Public-key encryption: authentication and signature

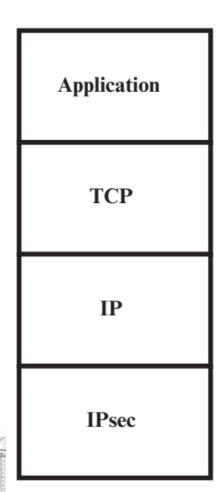
#### $A \rightarrow B: E(PU_b, E(PR_a, M))$

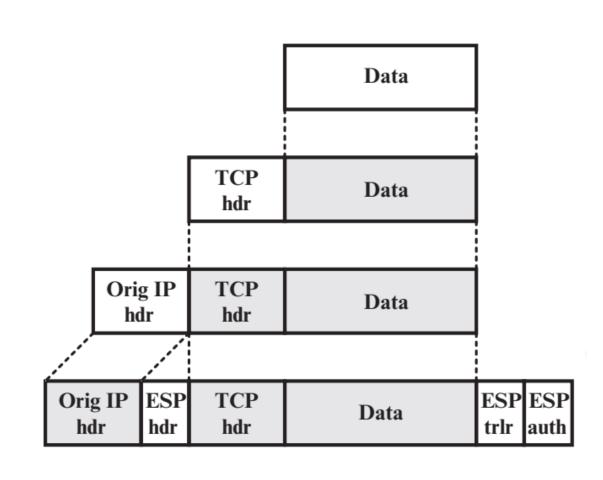
- Provides confidentiality because of PU<sub>b</sub>
- Provides authentication and signature because of PR<sub>a</sub>
- (d) Public-key encryption: confidentiality, authentication, and signature





Figure 20.9 shows the protocol architecture for the two modes.

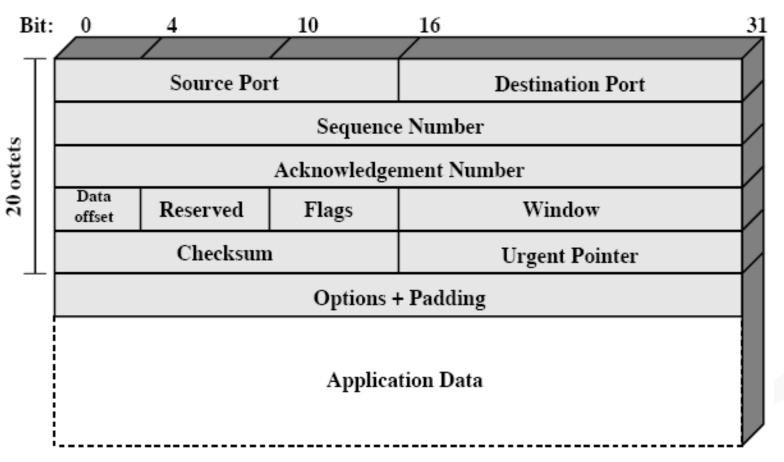




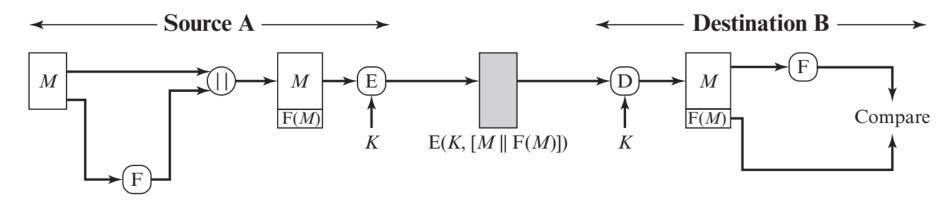
(a) Transport mode

Software Engineering

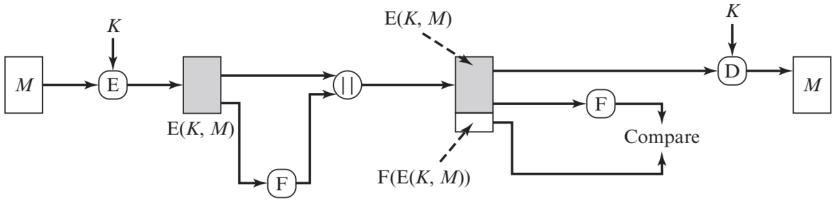
# Example







(a) Internal error control

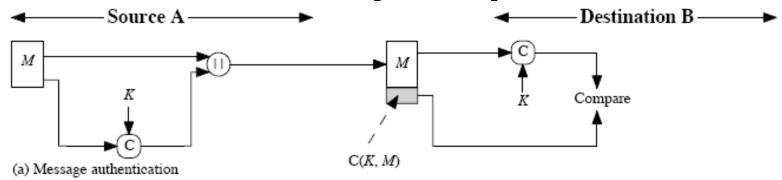


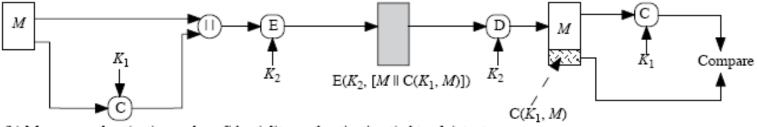
(b) External error control

Figure 12.2 Internal and External Error Control

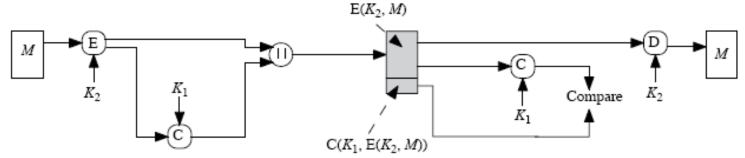


# (3) Use MAC: C(K,M)





(b) Message authentication and confidentiality; authentication tied to plaintext



(c) Message authentication and confidentiality; authentication tied to ciphertext

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 $A \rightarrow B: M \parallel C(K, M)$ •Provides authentication
—Only A and B share K

(a) Message authentication

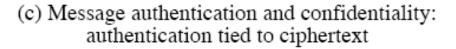
 $A \rightarrow B: E(K_2, [M || C(K, M)])$ 

- ·Provides authentication
  - —Only A and B share  $K_1$
- Provides confidentiality
  - —Only A and B share  $K_2$

(b) Message authentication and confidentiality: authentication tied to plaintext

 $\mathsf{A}\to\mathsf{B}\colon\mathsf{E}(K_2,M) \mid\mid \mathsf{C}(K_1,\mathsf{E}(K_2,M))$ 

- Provides authentication
  - —Using  $K_1$
- Provides confidentiality
  - —Using  $K_2$





### **Outline**

- **Message Authentication Functions**
- Requirements For Message Authentication Code (MAC)
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- MACs Based On Block Ciphers: DAA and **CMAC**





 Brute-force attack to discover the authentication key is difficult (more effort than a decryption key of the same length)

#### Round 1

Given:  $M_1$ ,  $T_1 = \text{MAC}(K, M_1)$ Compute  $T_i = \text{MAC}(K_i, M_1)$  for all  $2^k$  keys Number of matches  $\approx 2^{(k-n)}$ 

#### Round 2

Given:  $M_2$ ,  $T_2 = MAC(K, M_2)$ 

Compute  $T_i = \text{MAC}(K_i, M_2)$  for the  $2^{(k-n)}$  keys resulting from Round 1

Number of matches  $\approx 2^{(k-2\times n)}$ 



On average,  $\alpha$  rounds will be needed  $k = \alpha \times n$ .

 Other attacks: to find a collision, namely construct a different message with the same MAC

- **E.g. Let Message**  $M = (X_1 || X_2 || ... || X_m)$
- So, you can construct another message  $Y = Y_1 || Y_2 || Y_3 || \dots || Y_{m-1} || Y_m$ , where

$$Y_m = Y_1 \oplus Y_2 \oplus \cdots \oplus Y_{m-1} \oplus \Delta(M)$$

and you will find MAC(Y) = MAC(M)



### Requirements for MACs P392

- 1. knowing a message and MAC, is infeasible to find another message with same MAC
  - infeasible to find collision
- 2. MACs should be uniformly distributed
  - Resistance against brute-force attack based on chosen plaintext
- 3. MAC should depend equally on all bits of the message
  - "weak spots" of message don't exit



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#### Brute-Force Attacks:

#### to find the collision

**Computation resistance:** Given one or more text-MAC pairs  $[x_i, MAC(K, x_i)]$ , it is computationally infeasible to compute any text-MAC pair [x, MAC(K, x)] for any new input  $x \neq x_i$ .

- to find the authentication key
- Cryptanalysis
  - exploit some property of the algorithm other than an exhaustive search.
  - an ideal MAC algorithm will require a cryptanalytic effort greater than or equal to the brute-force effort.



# Example: Simple Hash Functions ----using XOR

#### Case 1:

b→C, where C<sub>i</sub>=b<sub>i1</sub>⊕b<sub>i2</sub>⊕ ...⊕b<sub>im</sub>
 where

 $C_i = i$ th bit of the hash code,  $1 \le i \le n$  m = number of n-bit blocks in the input  $b_{ij} = i$ th bit in jth block  $\oplus = \text{XOR operation}$ 

- produces a simple parity for each bit position as a longitudinal(经度) redundancy check which is effective for random data as a data integrity check.
- easy to affected by data format





# **Example: Simple Hash Functions** ----using XOR

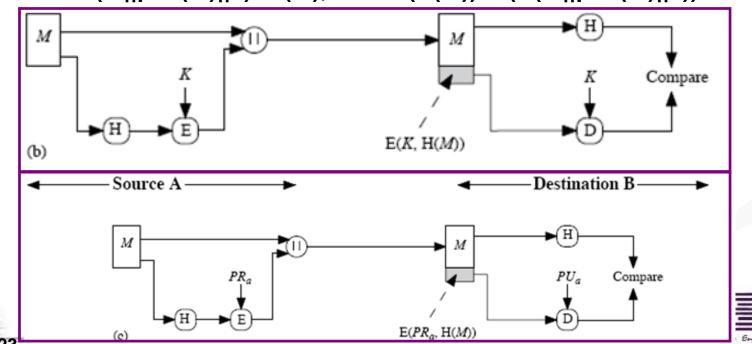
- Case 2: (improvement based on case 1)
  - Process each successive n-bit block of data as follows:
    - Rotate the current hash value to the left by one bit.
    - XOR the block into the hash value.
    - E.g. if  $m = m_1 || m_2$ , then  $H(m_1 || m_2 || pad(m_2)) = LR_1(H(m_1)) \oplus (m_2 || pad(m_2))$
  - Easy to forge by appending a block
    - Assume m and H(m) is known, easy to find x s.t. H(m||pad(m)||x)=H(m).
    - $H(m||pad(m)|| x)=LR_1(H(m))\oplus x=H(m) => x=LR_1(H(m))\oplus H(m).$





# 1<sup>st</sup> improvement based on case 2 ——Append encrypted hash code

- Case3:using encrypted Hash code (improvement based on case 2)
  - where hash code is generated according method in case 2.
  - Easy to forge by appending a block, the same as Case 2.
    - easy to find x s.t. H(m||pad(m)||x)=H(m)
    - if H(m||pad(m)||x)=H(m), then E(H(m))=E(H(m||pad(m)||x))



### 2<sup>nd</sup> improvement based on case 2 -Authenticate then Encrypt

Case 4: transit  $Y=E(K, [X || H(X)])=Y_1||Y_2||Y_3||...$ 

1) where hash code is generated according method in case 2.

For a message X of 64-bit blocks  $X_1$ ,  $X_2$ ,...,  $X_N$ , appending hash value  $X_1 \oplus X_2 \oplus ... \oplus X_N$  as H(M) (denoted as  $X_{N+1}$ )

But  $X_{N+1}$  is the hash code:

$$\begin{aligned} X_{N+1} &= X_1 \bigoplus X_2 \bigoplus ... \bigoplus X_N = \mathbf{H}(\mathbf{X}) \\ &= [IV \bigoplus D(K, Y_1)] \bigoplus [Y_1 \bigoplus D(K, Y_2)] \bigoplus ... \bigoplus [Y_{N1} \bigoplus ... \bigoplus D(K, Y_N)] \end{aligned}$$

- 2) Encrypt X=  $X_1X_2...X_{N+1}$  by CBC mode as Y,then  $\begin{cases} X_1 = IV \bigoplus D(K, Y_1) \\ X_i = Y_{i1} \bigoplus D(K, Y_i) \\ X_{N+1} = Y_N \bigoplus D(K, Y_{N+1}) \end{cases}$  Case 4 Is Not secure
- - Hash code would not change if the ciphertext blocks were permuted



#### Y'=Y2||Y1||Y3||...

Y=Y1||Y2||Y3||... Y'=Y2||Y1||Y3||...

• A

Y=E(K, [M || H(M)]) =Y1||Y2||Y3||...||Yn+1 Compute D(K,Y') = M'|| Xn+1',and Verify Xn+1'==H(M')? If Xn+1'==H(M'), B think Y is not changed during transmission.

if M=X1 ||X2 ||X3||...Xn, H(M)=Xn+1=X1⊕X2⊕ ... ⊕Xn



- if Attacker can intercept Y = E(K, [M || H(M)])=Y<sub>1</sub>||Y<sub>2</sub>||Y<sub>3</sub>||... from A to B and modify Y to Y'= Y<sub>2</sub>||Y<sub>1</sub>||Y<sub>3</sub>||..., then send Y' to B.
- B will decrypt and obtain M' and H(M')

- 
$$X_2'=Y_2 \oplus D(K,Y_1)\neq X_2$$

- 
$$X_3'=Y_1 \oplus D(K,Y_3) \neq X_3$$

$$-X_4'=Y_3 \oplus D(K,Y_4)=X_4$$

– .....

$$- \quad \mathbf{X_{n+1}} \mathbf{'=Y_n} \oplus \mathbf{D(K,Y_{n+1})} \mathbf{=X_{n+1}}$$

Obviously, Xn+1'==H(M').
But M' was modified in fact

• so, X<sub>n+1</sub>'==X<sub>1</sub>'⊕X<sub>2</sub>'⊕...⊕X<sub>n</sub>', B verify M' is not modified during transimission. But M' was modified in fact.

$$X_1 = IV \bigoplus D(K, Y_1)$$

$$X_i = Y_{i1} \oplus D(K, Y_i)$$

$$X_{N+1} = Y_N \bigoplus D(K, Y_{N+1})$$



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# **Keyed Hash Functions as MACs**

- want a MAC based on a hash function
  - because hash functions are generally faster than symmetric block cipher
  - code for crypto hash functions widely available
- hash includes a key along with message
- original proposal:
  - KeyedHash= Hash(Key|Message) forge?
  - KeyedHash= Hash (Message | Key) collision?

#### **HMAC**

- specified as Internet standard RFC2104
- uses hash function on the message:

- where K<sup>+</sup> is the key padded out to size b bits
- and opad, ipad are specified padding constants
- overhead is just 3 more hash calculations than the message needs alone
- any hash function can be used
   eg. SHA-1, RIPEMD-160, Whirlpool



#### **HMAC Overview**

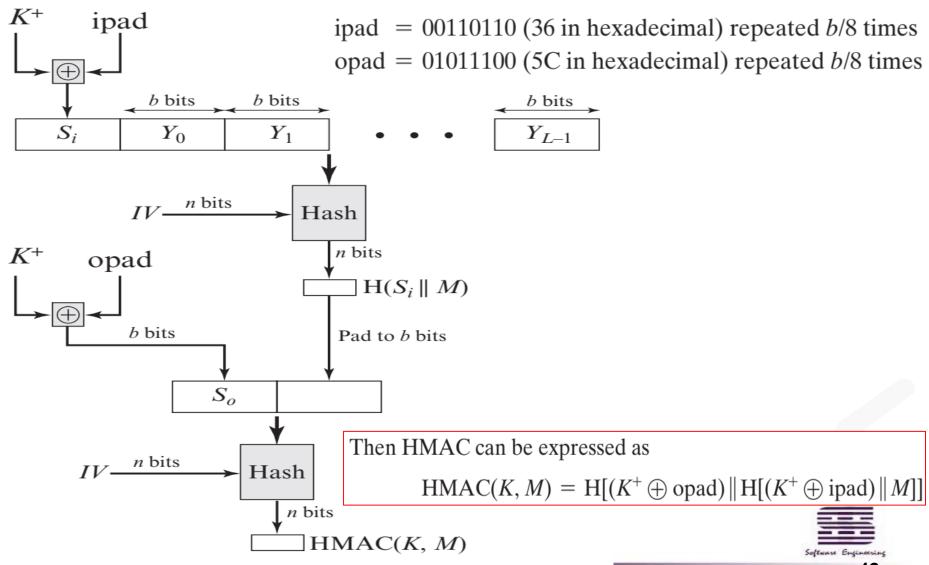
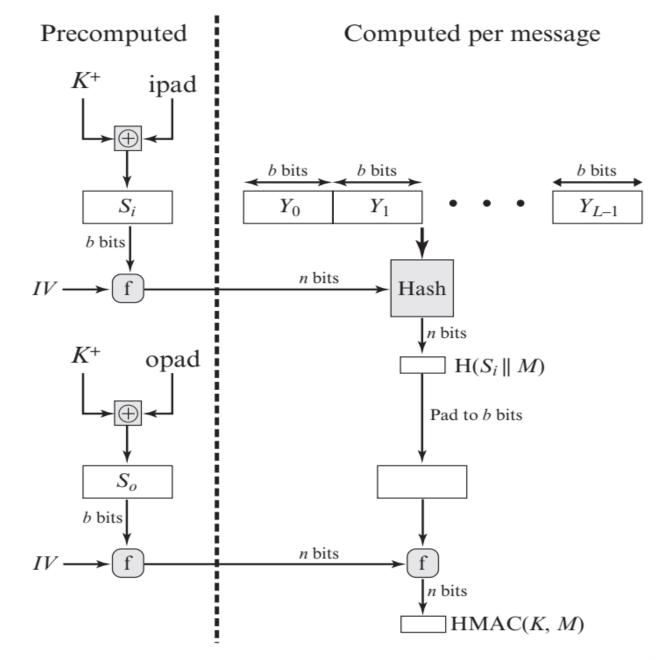


Figure 12.5 HMAC Structure





# **HMAC Security**

- proved security of HMAC relates to that of the underlying hash algorithm
- attacking HMAC requires either:
  - brute force attack on key used
  - birthday attack (but since keyed would need to observe a very large number of messages)
- choose hash function used based on speed verses security constraints



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# **Example: DAA --- CBC-MAC:Using Symmetric Ciphers for MACs**

- can use any block cipher chaining mode and use final block as a MAC
- Data Authentication Algorithm (DAA)(FIPS PUB 113) is a widely used MAC based on DES-CBC
  - is both a FIPS publication (FIPS PUB 113) and an ANSI standard (X9.17).
  - using IV=0 and zero-pad of final block
  - encrypt message using DES in CBC mode
  - and send just the final block as the MAC
    - or the leftmost M bits (16≤M≤64) of final block
- but final MAC is now too small for security: ≤64
- Easy to forge for DAA:
  - if message M has only one block X, then T = MAC(K, X)= MAC(K, X||pad(X)||X ⊕ T). So, easy to find a collusion pair(X, X||pad(X)||X ⊕ T).
  - Thus, only messages of one fixed length of mn bits are processed
  - replaced by newer and stronger algorithms adopted by NIST
     SP800-38B (see P75 in slides)

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# Data Authentication Algorithm

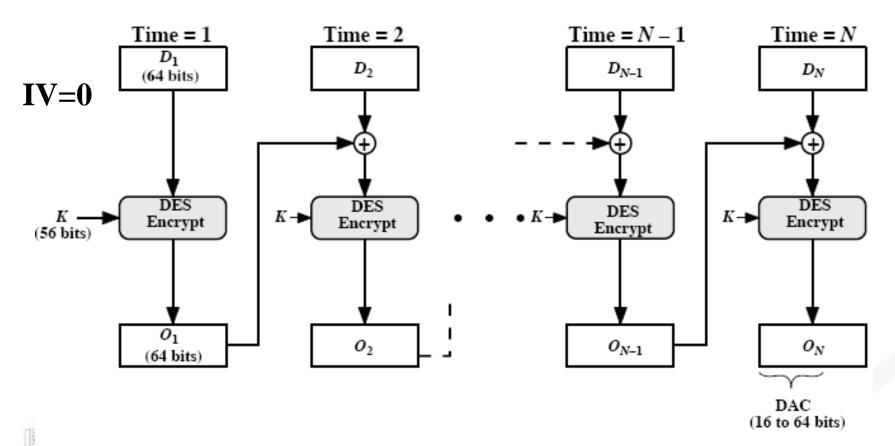


Figure 11.6 Data Authentication Algorithm (FIPS PUB 113)

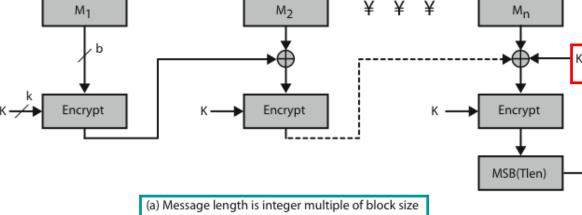


## **CMAC Overview**

$$C_1 = \mathsf{E}(K, M_1)$$

$$C_2 = E(K, [M_2 \bigoplus C_1])$$

$$C_3 = E(K, [M_3 \bigoplus C_2])$$



 $C_n = E(K, [M_n \bigoplus C_{n-1} \bigoplus K_1])$ 

 $= MSB_{Tlen}(C_n)$ 

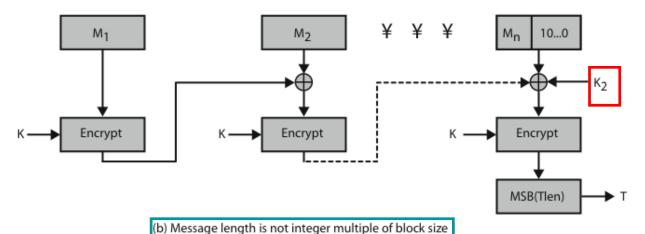


Figure 12.12 Cipher-Based Message Authentication Code (CMAC)



## **CMAC**

- previously saw the DAA (<u>CBC-MAC</u>)
  - use DES-CBC
  - widely used in govt & industry
  - but has message size limitation
  - have security weaknesses
- can overcome using 2 keys & padding
  - two n-bit keys could be derived from the k-bit encryption key
  - the final block is padded to the right (least significant bits) with a 1 and as many 0s as necessary
- thus forming the Cipher-based Message Authentication Code (CMAC)
- adopted by NIST SP800-38B for use with AES and triple DES

# Summary

- message authentication using
  - message encryption
  - MACs
  - hash functions

- HMAC authentication using hash function
- CMAC authentication using a block cipher





# **Key Terms**

authenticator Cipher-Based Message Authentication Code (CMAC) CMAC Counter with Cipher Block Chaining-Message Authentication Code (CCM)

cryptographic checksum cryptographic hash function Data Authentication Algorithm (DAA) Galois/Counter Mode (GCM) HMAC.

key encryption key Key Wrap mode key wrapping message authentication message authentication code (MAC)





# **Review Questions**

- 12.1 What types of attacks are addressed by message authentication?
- 12.2 What two levels of functionality comprise a message authentication or digital signature mechanism?
- 12.3 What are some approaches to producing message authentication?
- 12.4 When a combination of symmetric encryption and an error control code is used for message authentication, in what order must the two functions be performed?



# **Review Questions**

- 12.5 What is a message authentication code?
- 12.6 What is the difference between a message authentication code and a one-way hash function?
- 12.8 Is it necessary to recover the secret key in order to attack a MAC algorithm?
- Is it secure to generate message authentication code by using DAA, why?
- Is it secure to generate message authentication code by using Hash(Message||Pad(M)||key), why?
- Is it secure to generate message authentication code by using Hash(key||Message), why?

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# Thanks!





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