

Kurs Bio144:

Datenanalyse in der Biologie

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Lecture 8: Interpretation, causality, cautionary notes

26./27. April 2018

Overview

- P -values: Interpretation and (mis-)use
- Statistical significance vs biological relevance
- Relative importance of regression terms
- Causality vs correlation
- Bradford-Hill criteria for causal inference
- Experimental vs observational studies

Course material covered today

The lecture material of today is based on the following literature:

- Literature and articles that you will have to read in the second self-study week (second week of May).

Recap of previous lecture

- Model selection is difficult.
- Information criteria: AIC, AIC_c and BIC
→ **model fit vs model complexity**
- **Predictive** vs **explanatory** models.
- Automatic model selection is inappropriate for explanatory models!
- Caveats of p -values: biological relevance vs statistical significance

P-values

Recap:

P-values are often used for *statistical testing*, e.g. by checking if $p < 0.05$.

Examples:

- T-test for a difference between two samples.
- χ^2 -test for independence of two discrete distributions.
- Test if a regression coefficient $\beta_x \neq 0$ in a regression model.

Such tests are useful whenever a **decision** needs to be made (e.g., in clinical trials, intervention actions in ecology etc.).

P-values in regression models

In regression modeling, the p -value is often used as an indicator of covariate importance. Remember the mercury example:

| | Coefficient | 95%-confidence interval | p -value |
|----------------|-------------|-------------------------|------------|
| Intercept | -0.68 | from -0.88 to -0.47 | < 0.0001 |
| log10(Hg_soil) | 0.033 | from -0.05 to 0.11 | 0.42 |
| vegetables | 0.07 | from -0.03 to 0.17 | 0.18 |
| migration | -0.036 | from -0.19 to 0.12 | 0.65 |
| smoking | 0.27 | from 0.06 to 0.48 | 0.012 |
| sqrt(amalgam) | 0.33 | from 0.24 to 0.42 | < 0.0001 |
| age | -0.042 | from -0.06 to -0.02 | 0.0004 |
| mother | -1.03 | from -1.70 to -0.35 | 0.003 |
| sqrt(fish) | 0.079 | from 0.03 to 0.13 | 0.004 |
| last_fish | 0.30 | from 0.15 to 0.45 | < 0.0001 |
| age:mother | 0.055 | from 0.03 to 0.08 | 0.0002 |

A common practice is to look only at the p -value and use $p < 0.05$ to decide whether a variable has an influence or not ("is significant or not").

P-values criticism

P-value **criticism** is as **old** as statistical significance testing (1920s!). Issues:

- The sharp line $p < 0.05$ is **arbitrary** and significance testing according to it may lead to *mindless statistics* (Gigerenzer, 2004).
- *P*-hacking / data dredging: Search until you find a result with $p < 0.05$.
- Publication bias: Studies with $p < 0.05$ are more likely to be published than “non-significant” results.
- Recent articles in *Science*, *Nature* or a statement by the *American Statistical Association* (ASA) in March 2016 show that the debate still continues (Goodman, 2016; Wasserstein and Lazar, 2016).
- Model selection using *p*-values may lead to a **model selection bias** (see last week).

P-values even made it into NZZ (April 2016)



NZZ Donnerstag 3. April 2016

Wissen

Übereschätzte Statistiken

Daten-Analysen entscheiden heute darüber, ob ein Medikament als wirksam gilt. Bloss verstehen viele Forscher die Bedeutung dieser Berechnungen gar nicht. **Von Patrick Imhasly**

Kritiker machen keinen recht nur Menschen, sondern auch statistische Kriterien. Das gilt besonders für den sogenannten p-Wert, ein den jeder Mähdichsel und jeder Statistiker in Konstanz kennt, vor allem aber jeder, der im weitesten Sinne mit Statistik zu tun hat. Insbesondere ist der p-Wert indes auf die Gefahr hin geraten. Denn was der Vater der modernen Statistik, der britische Genetiker Ronald Fisher, 1925 als eine Art informelles Screening für die Aussagekraft von Daten entwickelt, ist in der Praxis oftmals zu einem simplen Lackmustest verkommen.

Dreht die statistische Analyse von Daten einen p-Wert (0,05 Prozent) oder auch besser «0,01 Prozent», gehen diese als signifikant – den Daten wird dann automatische Neuvalidität zugewiesen. Das erneuert etwas darüber, ob ein neues Medikament als wirksam eingestuft wird oder als Fehlforschung. In einem angeborenen Fachhahn publiziert man. «Der p-Wert war aber wie das Gold, wissenschaftliches Denken ausser Kraft zu setzen, ist auch nach dem statistischen Versteigerer (ASA), jüngst öffentlich beklagt.

Wissenschaftler verwenden den p-Wert immer häufiger, ohne zu verstehen, was er bedeutet – das fordert wichtige Forschung und untergebt die Glaubwürdigkeit der Wissenschaft. Der Mediziner und Epidemiologe John Ioannidis von der Universität Stanford gewährt in einem Kommentar von «drogenabhängigen» über falsche Gebrauch des p-Wertes ist demnach einfach und erfordert so entzerrt, dass manche sich

wenden danach – vor allem wenn sie mit Forschungsgeldern und Publikationen beehrt werden – Angesichts der Missstände ist auch die ASA jetzt versichert, zum ersten Mal in ihrer fast 100-jährigen Geschichte Empfehlung zu widerrufen, wie man mit einer statistischen Grösse verfahren umgeht.

Wider die Null-Hypothese

«Der p-Wert sagt nicht das aus, was man gemeint hat von ihm erwartet», erklärt der Berner Epidemiologe Peter Kün, der mit seinem am Apple Health Research Center der Universität Toronto tätig ist. Das bedeutet: Der p-Wert misst nicht die Wahrscheinlichkeit, dass eine bestimmte Hypothese zutrifft, und auch nicht, ob ein bestimmtes Resultat zufällig zustande gekommen ist, wie die ASA fordert. Vielmehr misst er, wie wahrscheinlich es ist, dass ein bestimmtes Resultat zu finden ist, wenn die Null-Hypothese zutrifft, dass es keine Beziehung zwischen den Variablen gibt.

Die Hypothese in einer Patiententherapie könnte zum Beispiel lauten, dass ein Medikament A gegen Herz-Kreisläufers besser wirkt als ein Medikament B. Die Null-Hypothese besagt dann genau das Gegenteil davon, nämlich dass das Medikament B nicht besser wirkt als das Medikament A. Beim Test beschränkt der Forscher im Prinzip, wie gross die Wahrscheinlichkeit für die Aufnahme

«Studien führen heute zu demassen vielen Daten, dass man allen Unfug testen kann und so zu Hunderten von p-Werten kommt.»



Daten werden meist von Leuten analysiert, die nicht dafür ausgebildet sind.

5%
kleiner als dieser Wert muss die signifikante p-Wert in einem statistischen Test sein, dann gelten die Daten aus einer Studie als aussagekräftig. Doch die Grenze ist willkürlich gewählt. (jein.)

von einer tatsächlich festgestellten oder noch grossen Unterschied zwischen den beiden untersuchten Medikamenten ist – unter der Annahme, dass die Null-Hypothese stimmt. Diese Wahrscheinlichkeit ist der p-Wert, und je geringer er ist, desto weniger spricht für die Null-Hypothese. Ein p-Wert von 0,05 bedeutet, dass das festgestellte Resultat aus noch etwas mehr als 20 Versuchen mit einer Wahrscheinlichkeit von lediglich 5 Prozent zustande kommen kann – und nicht, dass eine bestimmte Hypothese mit einer Sicherheit von 95 Prozent wahr ist. Über die eigentlich zutreffende Hypothese kann der p-Wert nur indirekt etwas aussagen, weil er über zwei Seiten gelächelt ist. Der zentrale Wert liefert also keine alternativen Beweise für einen positiven Unterschied oder Zusammenhang. «Der p-Wert ist eine bedingte und nicht eine absolute Wahrscheinlichkeit», erklärt Peter Kün. «Deshalb kann das Verhalten viele Forscher nicht, und es interessiert sie auch nicht.» Kün kommt, dass die Signifikanzgrenzen von 5 Prozent bzw. 1 Prozent faktisch entstanden sind, aber wenig klar definierte Werte sind. Ronald Fisher, der Erfinder des p-Werts, obwohl es sehr früh ausdrücklich, die Interpretation des erprobten Fenchens, ab welcher Grösse ein p-Wert in einer Untersuchung Aussagekraft haben soll. «Trotzdem haben sich die willkürlich gewählten Signifikanzgrenzen im Gehirn von Generationen von Forschern gebildet», sagt Leonhard Held vom Institut für Epidemiologie, Biostatistik und Prävention der Universität Zürich. Die britischen Biostatistiker Jonathan Sterne und George Davey Smith haben schon vor 15 Jahren im «British Medical Journal» dazu

aufgerufen, die Resultate von medizinischen Studien in Formeln als signifikant oder nichtsignifikant zu markieren, sondern im Kontext der gesamten Untersuchung und anhand anderer Ergebnisse zu interpretieren. Gezeigt hat das herzlich wenig, wie das Team von John Ioannidis in einer neuen entscheidenden Studie festgelegt hat. Demnach sind in den vergangenen 15 Jahren in der biomedizinischen Forschung immer mehr Studien erschienen, die p-Werte angaben, die nicht immer klar signifikant ausfielen. Gleichzeitig wuchs die Zahl von Publikationen zu den festgelegten Effekten immer stärker (JAMA, Bd. 315, S. 334).

Es gibt Alternativen

Das Problem ist dabei nicht nur, dass der p-Wert ein eigentlich einfaches statistisches Instrument ist. «Studien führen heute zu demassen vielen Daten, dass man allen Unfug testen kann und so zu Hunderten von p-Werten kommt», erklärt Leonhard Held. «Der p-Wert ist eine bedingte und nicht eine absolute Wahrscheinlichkeit, dass ein bestimmtes Resultat zu finden ist, wenn die Null-Hypothese zutrifft, dass es keine Beziehung zwischen den Variablen gibt.»

Kün empfiehlt, die Resultate von Studien mindestens mit Vertrauensintervallen zu versehen, die spezifische Aussagen über die Unsicherheit einer Schätzung machen. Und Held empfiehlt alternative Mass für statistische Evidenz – zum Beispiel Bayes'sche Faktoren. Mit diesen Hilfe lässt sich die Wahrscheinlichkeit einer Hypothese im hand der Daten argumen, statt dass diese wie beim p-Wert nach einem Schema-Wissens-Schema angenommen oder abgelehnt wird.

Note: R.A. Fisher, the “inventor” of the p -value (1920s) didn't mean the p -value to be used in the way it is used today (which is: doing a single experiment and use $p < 0.05$ for a conclusion)!

From Goodman (2016):

Fisher used “significance” merely to indicate that an observation was worth following up, with refutation of the null hypothesis justified only if further experiments “rarely failed” to achieve significance. This is in stark contrast to the modern practice of making claims based on a single demonstration of statistical significance.

The misuse of p -values has led to a **reproducibility crisis** in science!

Why Most Published Research Findings Are False

John P. A. Ioannidis

Summary

There is increasing concern that most current published research findings are false. The probability that a research claim is true may depend on study power and bias, the number of other studies on the same question, and, importantly, the ratio of true to no relationships among the relationships probed in each scientific field. In this framework, a research finding is less likely to be true when the studies conducted in a field are smaller; when effect sizes are smaller; when there is a greater number and lesser preselection of tested relationships; where there is greater flexibility in designs, definitions, outcomes, and analytical modes; when there is greater financial and other interest and prejudice; and when more teams are involved in a scientific field in chase of statistical significance. Simulations show that for most study designs and settings, it is more likely for a research claim to be false than true. Moreover, for many current scientific fields, claimed research findings may often be simply accurate measures of the prevailing bias. In this essay, I discuss the implications of these problems for the conduct and interpretation of research.

factors that influence this problem and some corollaries thereof.

Modeling the Framework for False Positive Findings

Several methodologists have pointed out [9–11] that the high rate of nonreplication (lack of confirmation) of research discoveries is a consequence of the convenient, yet ill-founded strategy of claiming conclusive research findings solely on the basis of a single study assessed by formal statistical significance, typically for a p -value less than 0.05. Research is not most appropriately represented and summarized by p -values, but, unfortunately, there is a widespread notion that medical research articles

It can be proven that most claimed research findings are false.

should be interpreted based only on p -values. Research findings are defined here as any relationship reaching formal statistical significance, e.g., effective interventions, informative predictors, risk factors, or associations.

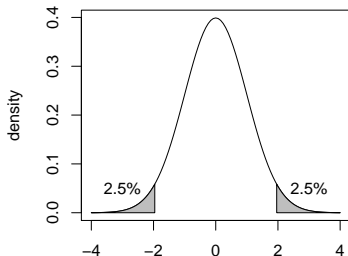
is characteristic of the field and can vary a lot depending on whether the field targets highly likely relationships or searches for only one or a few true relationships among thousands and millions of hypotheses that may be postulated. Let us also consider, for computational simplicity, circumscribed fields where either there is only one true relationship (among many that can be hypothesized) or the power is similar to find any of the several existing true relationships. The pre-study probability of a relationship being true is $R/(R+1)$. The probability of a study finding a true relationship reflects the power $1 - \beta$ (one minus the Type II error rate). The probability of claiming a relationship when none truly exists reflects the Type I error rate, α . Assuming that c relationships are being probed in the field, the expected values of the 2×2 table are given in Table 1. After a research finding has been claimed based on achieving formal statistical significance, the post-study probability that it is true is the positive predictive value, PPV. The PPV is also the complementary probability of what Wacholder et al. have called the false positive report probability [10]. According to the 9

What is the problem with the p -value?

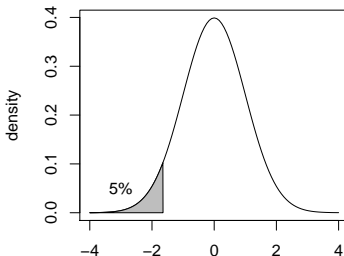
Many applied researchers do not **really** understand what the p -value actually is.

The **formal definition of p -value** is the probability to observe a data summary (e.g., an average) that is at least as extreme as the one observed, given that the Null Hypothesis is correct.

Two-sided p -value



One-sided p -value



Test yourself: Klicker-Exercise

► Klicker-Exercise

<http://www.klicker.uzh.ch/bkx>

+ Discussion of the results!

What is the problem with the p -value? II

- The p -value is often used to classify results into “significant” and “non-significant”. Typically: $p < 0.05$ vs $p \geq 0.05$.
- However, this is often too crude!
- It is much better to have a more **gradual interpretation of the p -value** (see slide 18).

Probably the most important point to remember:

The p -value is **not** the probability that the Null Hypothesis is true!!!

Quote from ASA statement:

In February, 2014, George Cobb, Professor Emeritus of Mathematics and Statistics at Mount Holyoke College, posed these questions to an ASA discussion forum:

Q: Why do so many colleges and grad schools teach $p = .05$?

A: Because that's still what the scientific community and journal editors use.

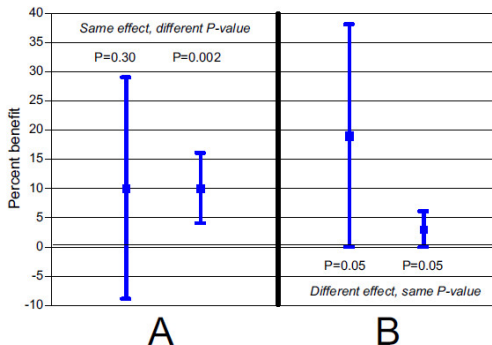
Q: Why do so many people still use $p = 0.05$?

A: Because that's what they were taught in college or grad school.

Significance vs relevance

In regression models:

- A low p -value does not automatically imply that a variable is “important”.
- “Is there an effect?” v.s. “How much of an effect is there?”.



In addition:

A large p -value (e.g., $p > 0.05$) does not automatically imply that a variable is “unimportant”.

Absence of evidence is not evidence of absence (Altman and Bland, 1995).

In other words:

One cannot prove the Null Hypothesis!!

Several reasons may lead to large p -values:

- Low sample size (\rightarrow low power).
- The truth is not “far” from the null hypothesis.
Example: Small effect sizes in regression models.
- Collinear covariates.

Shall we abolish p -values?

No: p -values are not “good” or “bad”. They contain important information, and they have **strengths** and **weaknesses**.

Suggestions:

- 1 Use p -values, but don't over-interpret them, **use them properly**.
- 2 Look at **effect sizes** and **confidence intervals**.
- 3 Look at **relative importances** of covariates.
- 4 **Don't use p -values for model selection.**

Suggestion 1: Proper interpretation of p -values

Rather than a black-and-white decision ($p < 0.05$), Martin Bland suggests to regard p -values as continuous measures for statistical evidence (Introduction to Medical Statistics, 4th edition, Oxford University Press):

| | |
|--------------------|---|
| $p > 0.1$ | little or no evidence against the null hypothesis |
| $0.1 > p > 0.05$ | weak evidence |
| $0.05 > p > 0.01$ | moderate evidence |
| $0.01 > p > 0.001$ | strong evidence |
| $p < 0.001$ | very strong evidence |

But: The level of significance must also depend on the context!

The most recent suggestion by 72 authors in the field:

Redefine statistical significance

We propose to change the default P -value threshold for statistical significance from 0.05 to 0.005 for claims of new discoveries.

(Benjamin et al., 2017, Nature Human Behaviour)

Their suggestion: replace $p < 0.05$ by $p < 0.005$. More precisely:

- Use $p < 0.005$ for **statistical significance**.
- Use $0.005 < p < 0.05$ as **suggestive evidence**.

In the Hg example:

| | Coefficient | 95%-confidence interval | p-value |
|----------------|-------------|-------------------------|----------|
| Intercept | -0.68 | from -0.88 to -0.47 | < 0.0001 |
| log10(Hg_soil) | 0.033 | from -0.05 to 0.11 | 0.42 |
| vegetables | 0.07 | from -0.03 to 0.17 | 0.18 |
| migration | -0.036 | from -0.19 to 0.12 | 0.65 |
| smoking | 0.27 | from 0.06 to 0.48 | 0.012 |
| sqrt(amalgam) | 0.33 | from 0.24 to 0.42 | < 0.0001 |
| age | -0.042 | from -0.06 to -0.02 | 0.0004 |
| mother | -1.03 | from -1.70 to -0.35 | 0.003 |
| sqrt(fish) | 0.079 | from 0.03 to 0.13 | 0.004 |
| last_fish | 0.30 | from 0.15 to 0.45 | < 0.0001 |
| age:mother | 0.055 | from 0.03 to 0.08 | 0.0002 |

- **Little or no evidence:** Hg soil, vegetables from garden, migration background
- **Moderate evidence:** Smoking
- **Strong evidence:** Mother, monthly fish consumption
- **Very strong evidence:** Amalgam, age, last fish ($>$ or $<$ 3 days), interaction of age and mother

Suggestion 2: Report effect sizes....

Ask: **Is the effect size relevant?**

Example

WHO recommendation concerning smoking and the consumption of processed meat. Both, smoking and meat consumption, appear to be carcinogenic.

- 50g processed meat per day increases the risk for colon cancer by a factor of 1.18 (+18%).
- Smoking increases the risk for cancer by a factor of 3.6 (+260%).

Thus: Although both, meat consumption and smoking, are carcinogenic (“significant”), their **effect sizes are vastly different!**

Paul D. Ellis writes in his book *The Essential Guide to Effect Sizes* (2010, chapter 2):

*Indeed, statistical significance, which partly reflects sample size, may say nothing at all about the practical significance of a result. [...] To extract meaning from their results [...] scientists need to look beyond p values and effect sizes and **make informed judgments about what they see.***

...and 95% CIs

Ask: Which range of true effects is statistically consistent with the observed data?

Example

Body fat example, slide 39 of lecture 2.

The effect estimate for the effect of BMI on body fat is given as

$\hat{\beta}_{BMI} = 1.82$, 95% CI from 1.61 to 2.03.

Interpretation: for an increase in the bmi by one index point, roughly 1.82% percentage points more bodyfat are expected, and all true values for β_{BMI} between 1.61 and 2.03 are **compatible with the observed data**.

However...

- The choice of the 95% is again somewhat arbitrary. We could also go for 90% or 99% or any other interval, but 95% has established as a commonly accepted range.
- The 95% CI should **not be misused for simple hypothesis testing** in the sense of

“Is 0 in the confidence interval or not?”

Because this boils down to checking whether $p < 0.05$...

Suggestion 3: Look at relative importances of covariates

- Ultimately, the popularity of p -values in regression models is based on the wish to judge which covariates are **relevant** in a model, particularly in observational studies.
- The problem with this: Low p -values do not automatically imply high relevance (Cox, 1982).
- Alternative: **relative importances** of explanatory variables that measure the proportion (%) of the responses' variability explained by each variable.

Relative importance: Decomposing R^2

Remember: R^2 indicates the proportion of variance explained by **all** covariates in a model

$$y_i = \beta_0 + \beta_1 x_i^{(1)} + \beta_2 x_i^{(2)} + \dots + \beta_m x_i^{(m)} + e_i .$$

The aim of **relative importance** is to **decompose** R^2 such that

- each variable $x^{(j)}$ is attributed a fair share r_j .
- the sum of all importances sums up to R , that is, $\sum_{j=1}^m r_j = R^2$.

Further, it is required that

- all shares are ≥ 0 .

Question: How would you define/calculate relative importance?

- **Idea 1:** Fit simple models including only one covariate at the time, *i.e.*:

$$y_i = \beta_0 + \beta_j x_i^{(j)} + e_i$$

for each variable $x^{(j)}$ and use the respective R^2 as r_j .

- **Idea 2:** Fit the linear model twice, once with and once without the covariate of interest, and then take the **increase** of R^2 as r_j .

Problem: In practice, regressors $x^{(j)}$ are *always correlated*, thus both ideas lead to $\sum_j r_j \neq R^2$!

To understand the problem of ideas 1 and 2, let us fit three models for $\log(Hg_{\text{urine}})$ with

- $x^{(1)} = \sqrt{\text{Number of monthly fish meals}}$
- $x^{(2)} = \text{binary indicator if last fish meal was less than 3 days ago.}$

These two variables are correlated (people who consume a lot of fish are more likely to have it consumed within the last 3 days).

$$y_i = \beta_0 + \beta_1 x_i^{(1)} + e_i \quad R^2 = 0.12 \quad (1)$$

$$y_i = \beta_0 + \beta_2 x_i^{(2)} + e_i \quad R^2 = 0.08 \quad (2)$$

$$y_i = \beta_0 + \beta_1 x_i^{(1)} + \beta_2 x_i^{(2)} + e_i \quad R^2 = 0.14 \quad (3)$$

Note: The R^2 of model (3) with both covariates is much less than the sum of the R^2 from models (1) and (2)!

⇒ The increase of R^2 upon inclusion of a covariate depends on the covariates that are already in the model!

A better way to calculate relative importance?

Various proposals to calculate relative importance (R^2 decomposition) have been proposed. The (currently) most useful is given by the following idea, called **LMG** (Lindemann, Merenda and Gold 1980):

- Fit the model for **all possible orderings of the covariates**.
- Record the increase in R^2 each time a variable is included.
- **Average** over all orderings of the covariates.

Luckily, the R-package `relaimpo` (Groemping 2006) contains the function `calc.relimp()` that does this for us!

Hg results

Which proportion (%) of variance in $\log(Hg_{urine})$ is explained by each covariate? Interpret the table below:

```
> library(relaimpo)
> lmg.hg <- calc.relimp(r.lm.hg)$lmg
```

| Variable | Rel. imp. (%) | p-value |
|-------------------|---------------|---------|
| $\log(Hg_{soil})$ | 0.10 | 0.42 |
| Vegetable | 0.46 | 0.18 |
| Migration | 0.43 | 0.65 |
| Smoking | 1.21 | 0.012 |
| Amalgam | 19.69 | <0.0001 |
| Age | 1.25 | 0.0004 |
| Mother | 1.08 | 0.0031 |
| Fish | 7.26 | 0.0042 |
| Last fish | 7.34 | <0.0001 |
| Age:mother | 6.56 | 0.0002 |

Several variables have very low p -values, but their relative importance differs clearly.

⇒ Relative importance gives intuitive **complementary information** to p -values, effect sizes and confidence intervals!

Does relative importance solve all the problems?

Unfortunately not...

Relative importance should be understood as **a complement to standard statistical output.**

There are several limitations to it:

- Rel.imp. of a variable may heavily depend on the other variables included in the model, especially when there are strongly correlated variables (see slide 33).
- Hard to generalize to other, non-linear regression models.

Example

Compare the estimated relative importance for the variable `fish` (monthly fish meals) for two cases:

Model 1

Original Hg model.

Model 2

Model **without the indicator variable `last_fish`**.

- **Case 1:** Relative importance of `fish`: 7.26% (see slide 30).
- **Case 2:** Relative importance of `fish`: 10.75% .

Interpretation: If one of two correlated variables is removed, the other absorbs some of the importance from it.

Causality vs correlation

In **explanatory models** the ultimate goal usually is to reveal **causal relationships** between the covariates and the response.

Examples:

- Does Hg in the soil influence Hg-levels in humans?
- Does inbreeding negatively affect population growth of Swiss Alpine ibex (Steinbock)?
- Does exposure to Asbest lead to illness or death?
- ...

However: Regression models actually only reveal associations, that is, **correlations** between x and y !

Example: Breakfast eating and teen obesity

Please read the following article and answer the questions below:

[http://www.webmd.com/diet/news/20080303/
eating-breakfast-may-beat-teen-obesity](http://www.webmd.com/diet/news/20080303/eating-breakfast-may-beat-teen-obesity)

Questions:

- Does the cited study show that teens that eat breakfast are generally less obese?
- Does this automatically imply that eating breakfast **leads to** less obesity among teens?

Look at a regression model including covariate x and response y . If the coefficient β_x is “significant”, there are several possible reasons for this:

- 1 x is a **cause** for y . Write: $x \rightarrow y$

Example: x is fish consumption and y is mercury concentration in the urine.

This is the desired situation!

- 2 y (partially) causes x , that is $y \rightarrow x$.

Example: x is *IQ* and y is *school education*.

In that case, the model is not correctly specified!

- 3 There is another covariate z that both influences x and y

$$z \rightarrow x \quad \text{and} \quad z \rightarrow y .$$

$\rightarrow x$ and y **covary**, but do not cause each other.

In the teen obesity example, all three reasons are possible – perhaps even at the same time!

Ideas:

- No breakfast (**x**) \rightarrow Obesity (**y**)
- Obesity (**y**) \rightarrow No breakfast (**x**)
- Large dinner (**z**) \rightarrow Obesity (**y**)

and

Large dinner (**z**) \rightarrow No breakfast (**x**)

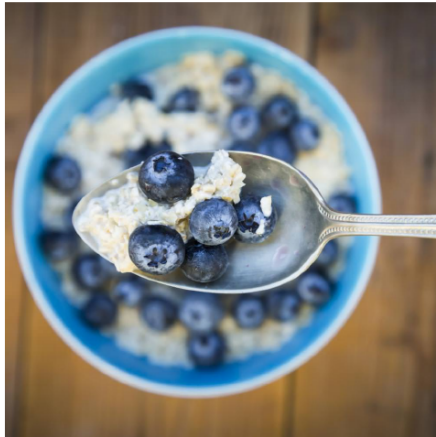
Many other ideas are possible...

In fact, see a recent article in NZZ am Sonntag (temporarily available from OpenEdX):

Der Mythos vom Kaiser-Frühstück

Morgens frühstücken hilft nicht beim Abnehmen, könnte aber den Stoffwechsel günstig beeinflussen.

von Felicitas Witte / 16.3.2017



Ein gesundes Frühstück kann die Lust auf Snacks reduzieren. (Bild: Getty Images/Westend61)

On the following website you find many “spurious correlations”, where the **causality is very obviously missing**:

<http://www.tylervigen.com/spurious-correlations>

(More about it in the BC material of this unit!)

Bradford-Hill-Criteria for causal inference I

In 1965 the Epidemiologist Bradford Hill presented a list of criteria to assess whether there is some causality or not. However, he wrote “None of my nine viewpoints can bring indisputable evidence for or against the cause-and-effect hypothesis and none can be required *sine qua non*.”

Bradford-Hill Criteria:

- 1 **Strength:** A causal relationship is likely when the observed association is strong.
- 2 **Consistency:** A causal relationship is likely if multiple independent studies show similar associations.
- 3 **Specificity:** A causal relationship is likely when a covariate x is associated only with one potential outcome y and not with other outcomes.
- 4 **Temporality:** The effect has to occur after the cause.

Bradford-Hill-Criteria for causal inference II

- 5 **Biological gradient:** Greater exposure should generally lead to greater incidence of the effect.
- 6 **Plausibility:** A plausible mechanism is helpful.
- 7 **Coherence:** Coherence between findings in the lab and in the field / population increases the likelihood of an effect.
- 8 **Analogy:** Similar factors have a similar effect.
- 9 **Experiment:** Evidence from an experiment is valuable.

Experimental vs observational studies

Experimental studies are relevant in biology and even more so in medicine, e.g., in the context of clinical trials where novel drugs are tested.

The teen obesity study was an **observational study**:

- All study participants only had to report their behaviour.
- None of them was assigned to a treatment group.
- There was **no intervention**.

An observed effect is more likely to be *causal* if participants were *randomly assigned* to a group, here: breakfast eating yes/no.

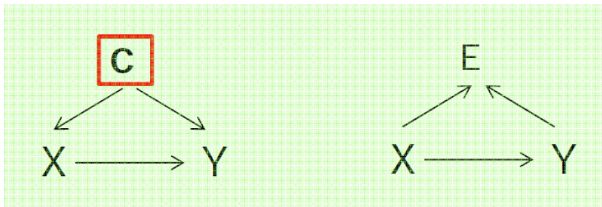
Observational study (“Erhebung”): Experimental study:

- Observation of subjects / objects in a real-world (existing) situation.
 - Variables are usually correlated.
 - Often more variables than can be included in the model.
 - **Examples:** Influence of pollutants (mercury) on humans, studies of wild animal populations, epidemiological studies,...
- Observation of subjects / objects in a constructed (experimental) situation.
 - Variables are controlled and uncorrelated (given a good study design!).
 - Usually all variables enter the model, **no model selection**.
 - **Examples:** Field experiments; clinical studies; psychological or pedagogical experiments,...

| | Observational study | Experiment |
|-----------------------|---|--|
| Situation | Existing, cannot be influenced | Artificial, designed |
| Analysis | Difficult (see model selection issues) | Simple no model selection |
| Interpretation | Difficult, especially w.r.t. causality | Clear, “proofs” causal relationship |

Causality considerations for model selection

It is **widely unknown** that a model can be broken by the inclusion of a “wrong” covariate, which is causally associated in the wrong direction:



Remember: Avoid to include covariates in your model that are **caused** by the outcome!

Example: ...

Summary

- Try to understand the definition and the meaning of p -values.
- Correct understanding, use and interpretation of p -values: Do not use the “mindless” $p < 0.05$ criterion!!
- Statistical significance vs biological relevance: Ask for the effect size and confidence interval, and reflect what it means, instead of only reporting p -values alone.
- The p -value is not “bad”, it contains useful information, but it has to be used properly.
→ 3 suggestions or alternatives (gradual interpretation of p -values, effect sizes and CIs, relative importances).
- Correlation should not be mistaken for causality.
- Experimental studies are better suited to reveal causality than observational studies!

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