

Step	Algorithm: $[C] := \text{FUNCTION_NAME_REC}(A, B, C)$
1a	$\{C = \widehat{C}$
4	$A \rightarrow \left(\begin{array}{c c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right), C \rightarrow \left(\begin{array}{c c} C_{TL} & C_{TR} \\ \hline C_{BL} & C_{BR} \end{array} \right)$ <p>where A_{TL} is 0×0, C_{TL} is 0×0</p>
2	$\left\{ \left(\begin{array}{c c} C_{TL} & C_{TR} \\ \hline C_{BL} & C_{BR} \end{array} \right) = \left(\begin{array}{c c} A_{TL} \otimes B & \widehat{C}_{TR} \\ \hline \widehat{C}_{BL} & \widehat{C}_{BR} \end{array} \right) \right\}$
3	while $m(A_{TL}) < m(A)$ do
2,3	$\left\{ \left(\begin{array}{c c} C_{TL} & C_{TR} \\ \hline C_{BL} & C_{BR} \end{array} \right) = \left(\begin{array}{c c} A_{TL} \otimes B & \widehat{C}_{TR} \\ \hline \widehat{C}_{BL} & \widehat{C}_{BR} \end{array} \right) \wedge m(A_{TL}) < m(A) \right\}$
5a	<p>Determine block size b</p> $\left(\begin{array}{c c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right) \rightarrow \left(\begin{array}{c cc} A_{00} & A_{01} & A_{02} \\ \hline A_{10} & A_{11} & A_{12} \\ A_{20} & A_{21} & A_{22} \end{array} \right), \left(\begin{array}{c c} C_{TL} & C_{TR} \\ \hline C_{BL} & C_{BR} \end{array} \right) \rightarrow \left(\begin{array}{c cc} C_{00} & C_{01} & C_{02} \\ \hline C_{10} & C_{11} & C_{12} \\ C_{20} & C_{21} & C_{22} \end{array} \right)$ <p>where A_{11} is $b \times b$, C_{11} is $b \times b$</p>
6	$\left\{ \left(\begin{array}{c cc} C_{00} & C_{01} & C_{02} \\ \hline C_{10} & C_{11} & C_{12} \\ C_{20} & C_{21} & C_{22} \end{array} \right) = \left(\begin{array}{c cc} A_{00} \otimes B & \widehat{C}_{01} & \widehat{C}_{02} \\ \hline \widehat{C}_{10} & \widehat{C}_{11} & \widehat{C}_{12} \\ \widehat{C}_{20} & \widehat{C}_{21} & \widehat{C}_{22} \end{array} \right) \right\}$
8	$C_{01} = A_{01} \otimes B$ $C_{10} = A_{10} \otimes B$ $C_{11} = A_{11} \otimes B$
7	$\left\{ \left(\begin{array}{c cc} C_{00} & C_{01} & C_{02} \\ \hline C_{10} & C_{11} & C_{12} \\ C_{20} & C_{21} & C_{22} \end{array} \right) = \left(\begin{array}{c cc} A_{00} \otimes B & A_{01} \otimes B & \widehat{C}_{02} \\ \hline A_{10} \otimes B & A_{11} \otimes B & \widehat{C}_{12} \\ \widehat{C}_{20} & \widehat{C}_{21} & \widehat{C}_{22} \end{array} \right) \right\}$
5b	$\left(\begin{array}{c c} A_{TL} & A_{TR} \\ \hline A_{BL} & A_{BR} \end{array} \right) \leftarrow \left(\begin{array}{c cc} A_{00} & A_{01} & A_{02} \\ \hline A_{10} & A_{11} & A_{12} \\ A_{20} & A_{21} & A_{22} \end{array} \right), \left(\begin{array}{c c} C_{TL} & C_{TR} \\ \hline C_{BL} & C_{BR} \end{array} \right) \leftarrow \left(\begin{array}{c cc} C_{00} & C_{01} & C_{02} \\ \hline C_{10} & C_{11} & C_{12} \\ C_{20} & C_{21} & C_{22} \end{array} \right)$
2	$\left\{ \left(\begin{array}{c c} C_{TL} & C_{TR} \\ \hline C_{BL} & C_{BR} \end{array} \right) = \left(\begin{array}{c c} A_{TL} \otimes B & \widehat{C}_{TR} \\ \hline \widehat{C}_{BL} & \widehat{C}_{BR} \end{array} \right) \right\}$
	endwhile
2,3	$\left\{ \left(\begin{array}{c c} C_{TL} & C_{TR} \\ \hline C_{BL} & C_{BR} \end{array} \right) = \left(\begin{array}{c c} A_{TL} \otimes B & \widehat{C}_{TR} \\ \hline \widehat{C}_{BL} & \widehat{C}_{BR} \end{array} \right) \wedge \neg(m(A_{TL}) < m(A)) \right\}$
1b	$\{C = A \otimes B$