

The Magic behind Remote-control Service of Firefox OS TV

J-PAKE over TLS

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Remote-control

What we are trying to do?

Turn Firefox Android into a TV remote-controller

Demo

<https://ody.sh/vtsKB00GVv>

J-PAKE over TLS

When you see this topic, you must think...

- what is J-PAKE ?
- is it a kind of PAKE ?
- and what is PAKE ?
- what's the difference between J-PAKE and the others ?
- hmm....TLS is stranger again for me...

So, here is the outline

- TLS
- PAKE
 - Security Requirements
 - General Two-stage Framework
 - Diffie-Hellman Key Exchange
 - DH-EKE
 - SPEKE
- J-PAKE
 - Intro
 - Protocol
 - Zero-Knowledge Proof
- J-PAKE over TLS
- Discussion



TLS

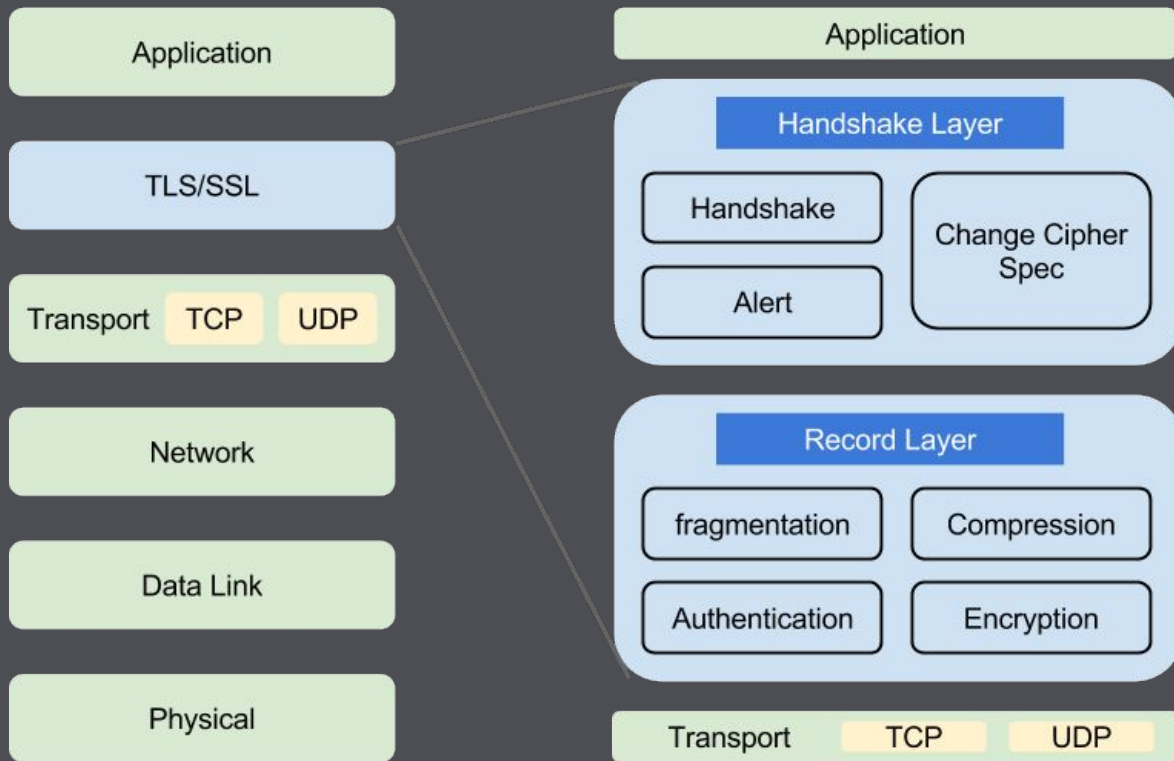
Intro of TLS

- Its predecessor is SSL, invented by NetScape
- https = http over TLS
- Make sure the channel is
 - Confidential
 - Authenticated
- Needs a trusted third party
 - Public key infrastructure(PKI)
- Symmetric encryption

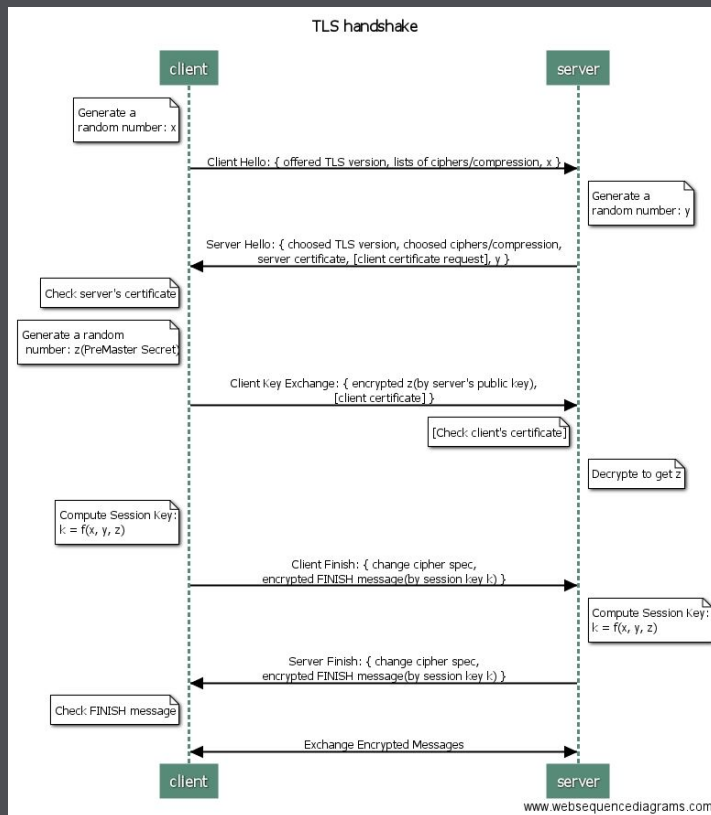


tion (US) | https://www.mozilla.o

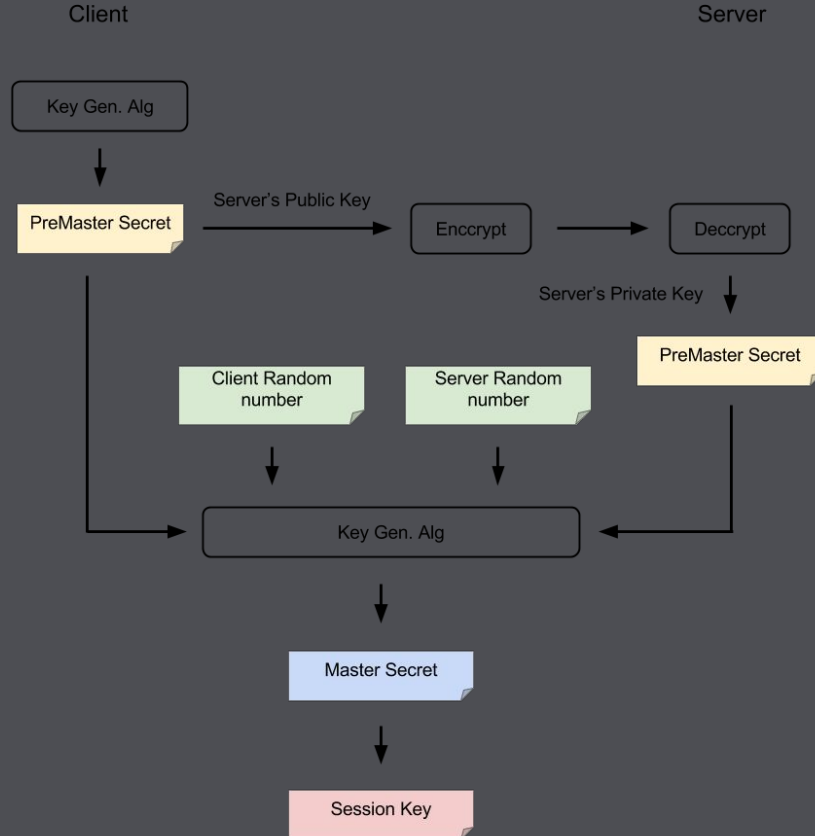
TLS layer in OSI model



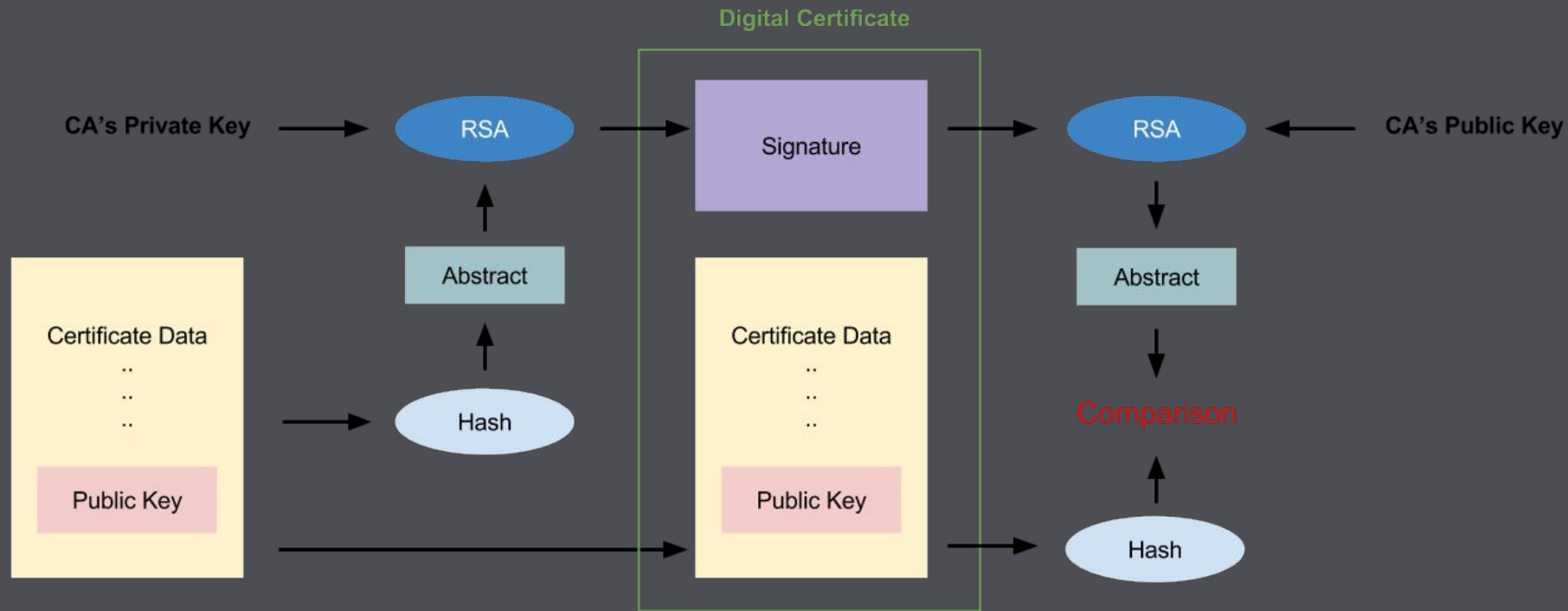
TLS handshake



TLS session key



TLS certificate authentication



why don't we just use TLS?

- There is no PKI in local network
- TLS can still establish a confidential channel without authentication
- So, we need to use other alternative to authenticate
 - PAKE can be used as an authentication method
- PAKE over TLS
 - [Secure Modular Password Authentication for the Web Using Channel Bindings](#)



PAKE

Intro of PAKE

- Multiple parties can establish a **shared** cryptographic keys based on their same knowledge of a password by messages exchange via an insecure channel
- The unauthorized party who doesn't possess the password has no way to get the password
- It can use weak **human-memorable** passwords to generate a **high-entropy** session key

Intro of PAKE

- Applications
 - **Mutual authentication**
 - Alternative for computationally expensive authentication
- Common PAKE
 - EKE: Encrypted Key Exchange
 - SPEKE: Simple Password Exponential Key Exchange
 - J-PAKE: Password Authenticated Key Exchange by Juggling

Security Requirements

- **Off-line dictionary attack resistance**

It doesn't leak any info that allows attackers to perform offline-exhaustive search to find the password

- **On-line dictionary attack resistance**

An active attacker can only test one password per protocol

- **Forward secrecy**

The session keys still keep secure even the password is later leaked out

- **Known-session security**

If one session is compromised, other established session won't be affected

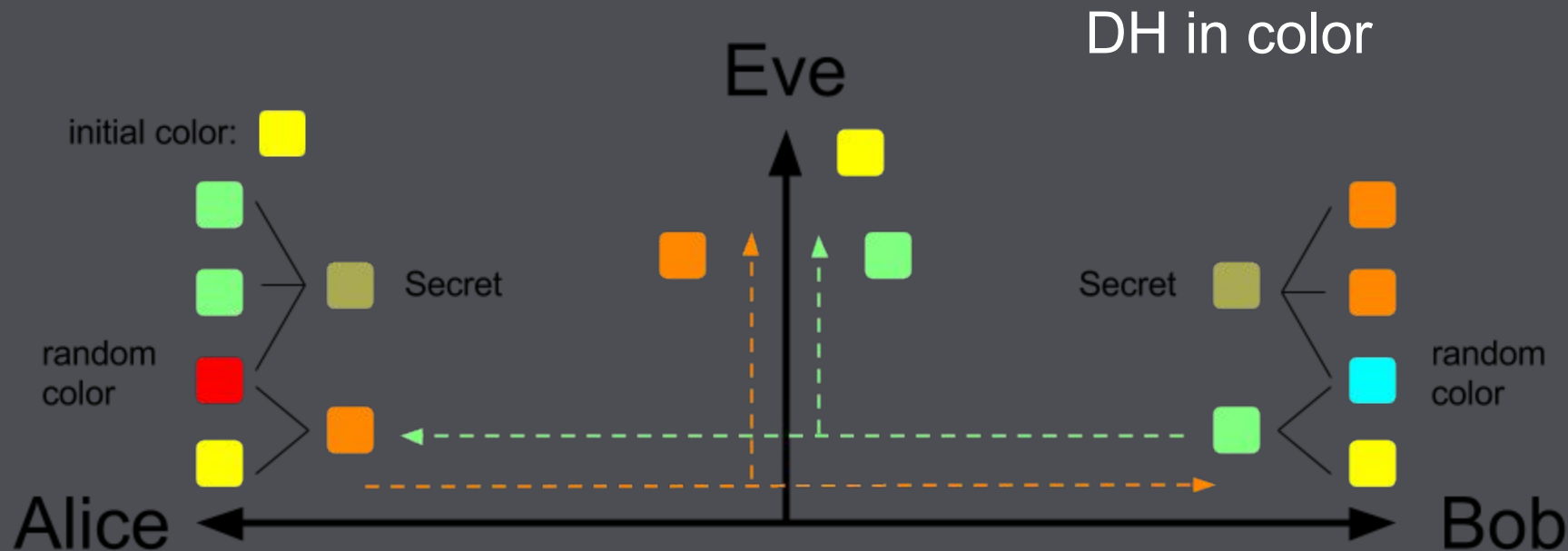
General Two-stage Framework

- **Key establishment**
 - Negotiate a session key for their communication
 - Common method is **Diffie–Hellman key exchange**
- **Key Confirmation**
 - Authenticate each other

Diffie-Hellman Key Exchange



Diffie-Hellman Key Exchange



Try yourself: <http://goo.gl/l52ecS>

Diffie-Hellman Key Exchange

multiplicative group G of integers modulo p , with generator g

DH in math

Eve

$$\begin{aligned}\text{Secret} &\equiv B^a \pmod{p} \\ &\equiv g^{ab} \pmod{p}\end{aligned}$$

Random
 $a \in [1, p)$

B

$$A \equiv g^a \pmod{p}$$

A

B

$$\begin{aligned}\text{Secret} &\equiv A^b \pmod{p} \\ &\equiv g^{ab} \pmod{p}\end{aligned}$$

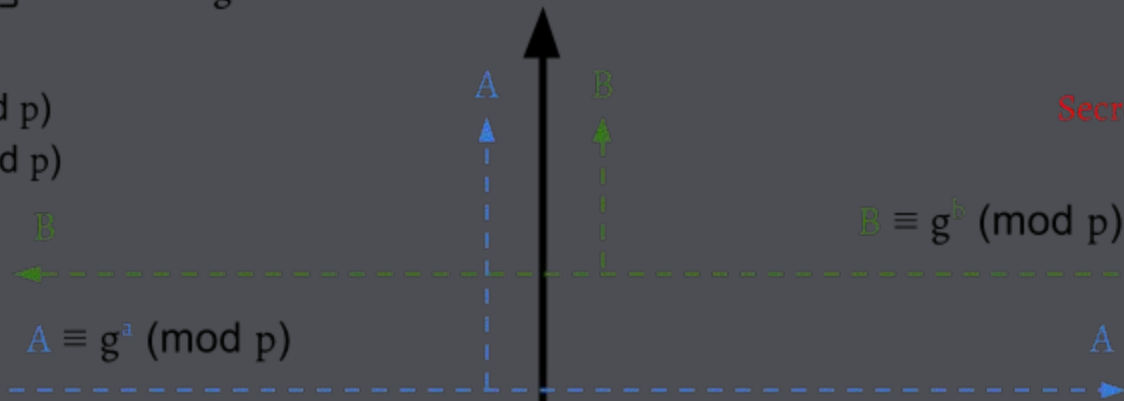
Random
 $b \in [1, p)$

$$B \equiv g^b \pmod{p}$$

A

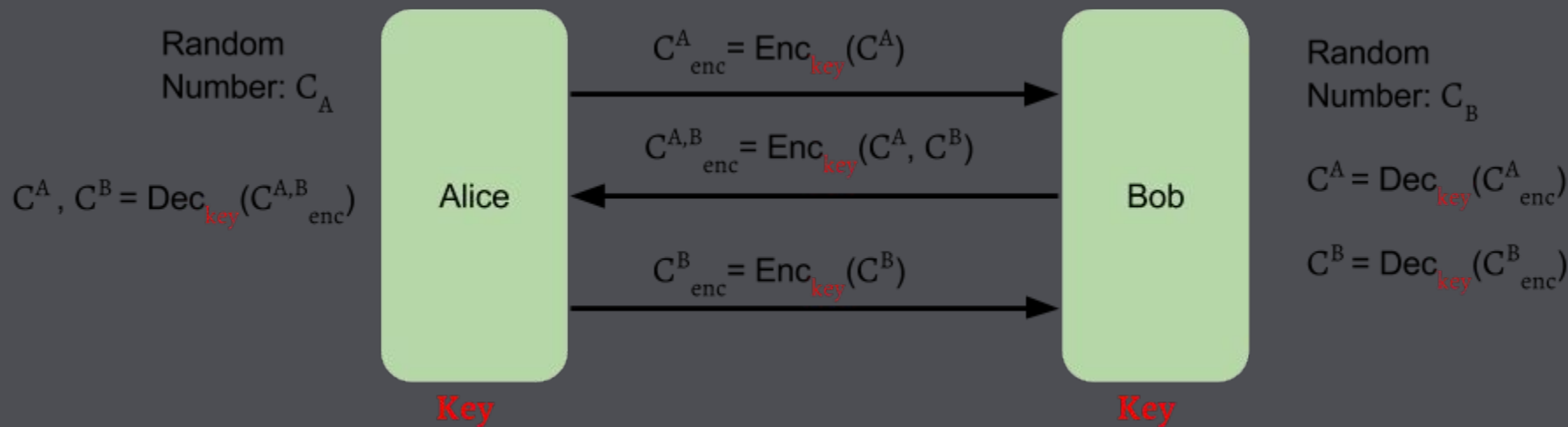
Alice

Bob



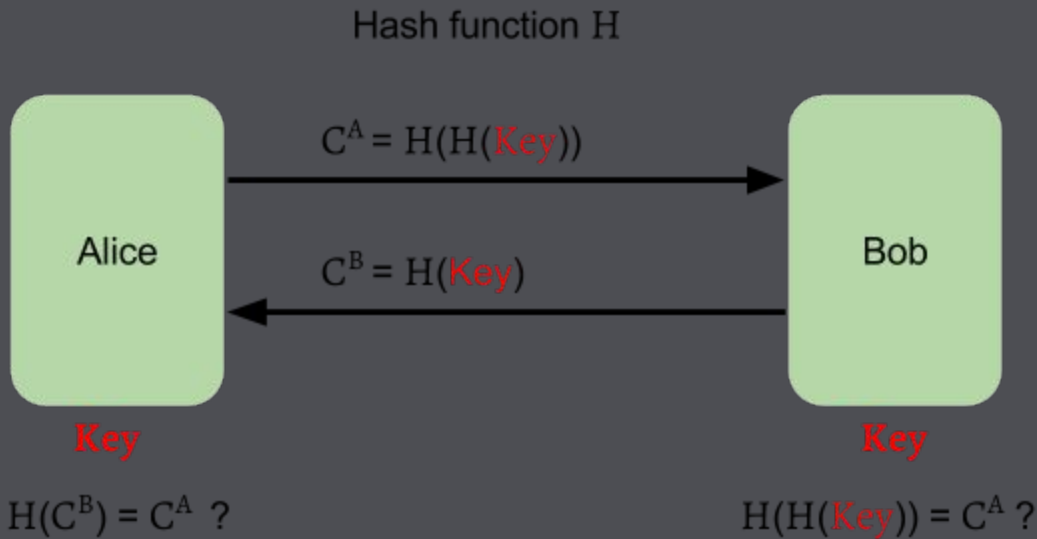
Key Confirmation

Challenge–Response Authentication



Key Confirmation

Hash–Key Authentication



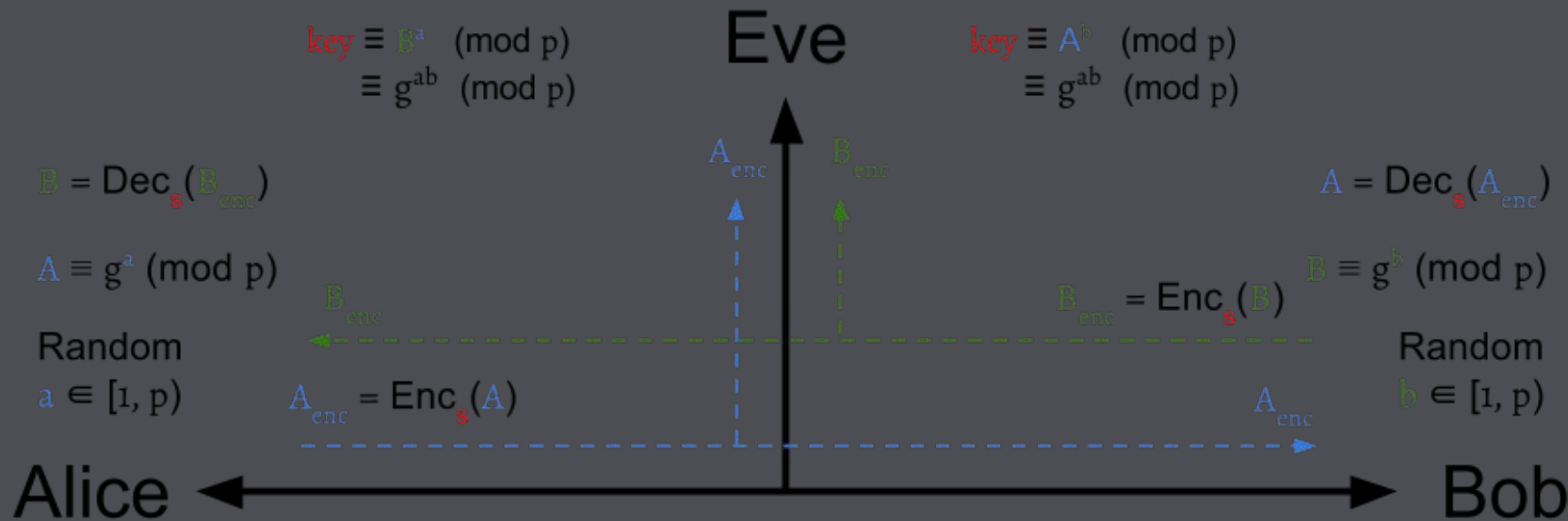
Encrypted Key Exchange

- Key establishment by DH
- But use password to encrypt/decrypt the public key instead of directly sending it

Encrypted Key Exchange

- multiplicative group G of **integers** modulo p , with generator g
- Shared password: **pwd**, Shared secret: $s = \text{Hash}(\text{pwd})$
- Encryption with key k : $\text{Enc}_k()$, Decryption with key k : $\text{Dec}_k()$

simplified version



Encrypted Key Exchange

- Drawbacks
 - It needs a very large exponent
 - It needs to choose modulo p carefully
 - If $p = 263 = (000000001\ 00000111)_2$, then group element must be in $[1, 262]$. We can guess the first seven bits in the first byte is all 0

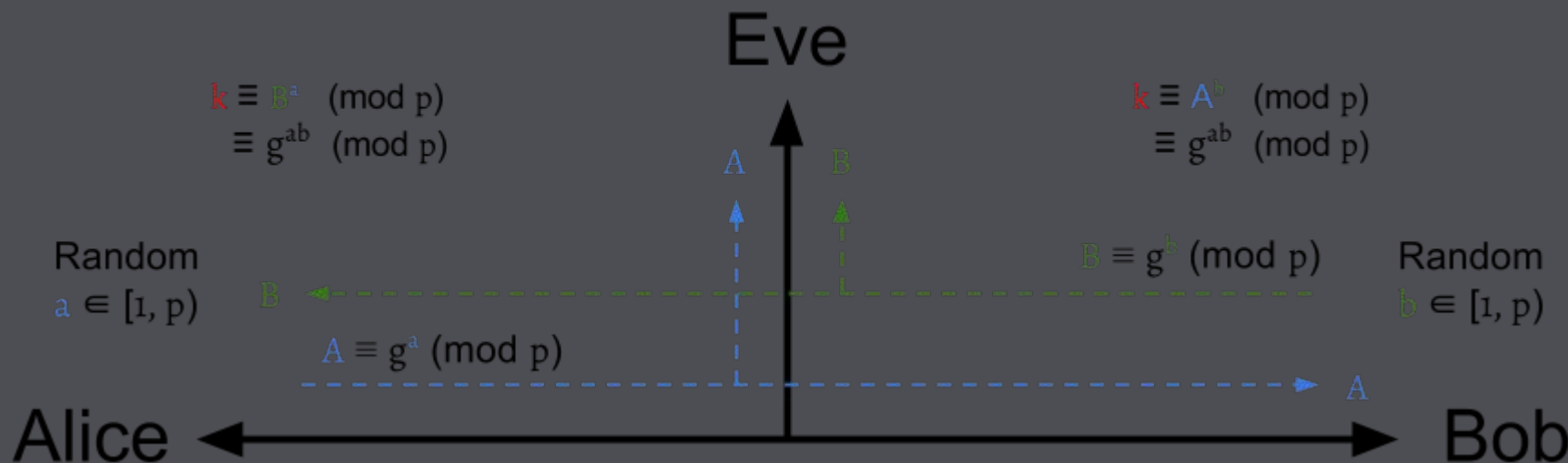
Simple Password Exponential Key Exchange

- Key establishment by DH
- But the group generator is derived by password instead
- The prime p must be a safe prime, $p = 2q + 1$, where q is also a prime.

Simple Password Exponential Key Exchange

- **Safe prime** p , Shared password: **pwd**
- $g \equiv \text{pwd}^2 \pmod{p}$

simplified version

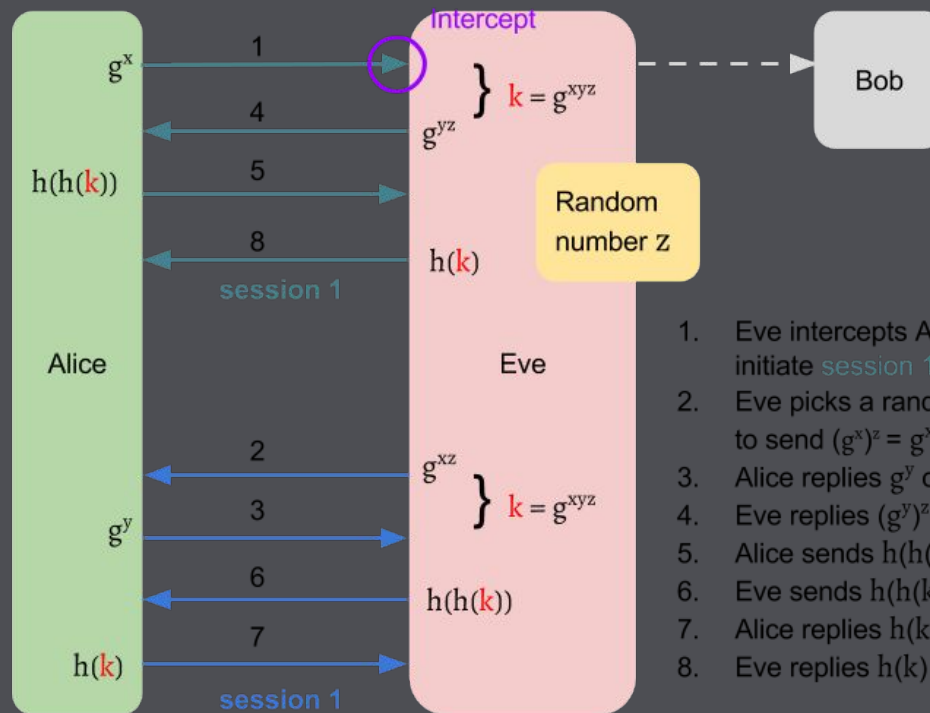


Simple Password Exponential Key Exchange

- Drawbacks
 - An attacker may test multiple password per protocol
 - $g \equiv (\text{pwd})^2 \pmod{p}$
 - $(q+k+1)^2 \equiv (q-k)^2 \pmod{p = 2q + 1}$
 - suppose $q = 11$, then
 - $k = 0: 11^2 \equiv 12^2 \equiv 6$
 - g is not 6, then pwd must not be 11 or 12
 - $k = 1: 10^2 \equiv 13^2 \equiv 8$
 - if g is not 8, then pwd must not be 10 or 13

Simple Password Exponential Key Exchange

Impersonation Attack



1. Eve intercepts Alice's g^x for Bob to initiate **session 1**
2. Eve picks a random z then pretends Bob to send $(g^x)^z = g^{xz}$ to initiate **session 2**
3. Alice replies g^y on **session 2**
4. Eve replies $(g^y)^z = g^{yz}$ on **session 1**
5. Alice sends $h(h(k))$ on **session 1**
6. Eve sends $h(h(k))$ on **session 2**
7. Alice replies $h(k)$ on **session 1**
8. Eve replies $h(k)$ on **session 2**



J-PAKE

Intro of J-PAKE

- Why we need J-PAKE?
 - EKE needs large exponents and may leak partial information about password
 - SPEKE allows an attacker tests multiple password in one protocol execution
 - EKE and SPEKE are **patented**
- Applications
 - Thread (IoT network protocol)
 - OpenSSH and OpenSSL
 - Firefox Sync
 - Palemoon sync(forked from Firefox)
- Zero-Knowledge Proof
 - Provides a valid knowledge proof of a discrete logarithm without revealing it

J-PAKE

- Group G with generator g of prime order q
- Shared secret: s
- ZKP_n : To prove knowledge of $N = g^n$, sends $\{ID, V = g^v, r = v - n \cdot h\}$, where ID is user identifier, $v \in [1, q - 1]$, and $h = \text{Hash}(g, V, N, ID)$

random:
 $x_1 \in [0, q-1]$,
 $x_2 \in [1, q-1]$

check: $g^{x_4} \neq 1$

$$A = (g^{x_1} \cdot g^{x_3} \cdot g^{x_4})^{x_2 \cdot s} \\ = g^{(x_1 + x_3 + x_4) \cdot x_2 \cdot s}$$

$$K = (B / (g^{x_4})^{x_2 \cdot s})^{x_2} \\ = (g^{(x_1 + x_3) \cdot x_4 \cdot s})^{x_2} \\ = g^{(x_1 + x_3) \cdot x_2 \cdot x_4 \cdot s}$$

Alice

$g^{x_1}, ZKP_{x_1}, g^{x_2}, ZKP_{x_2}$

$g^{x_3}, ZKP_{x_3}, g^{x_4}, ZKP_{x_4}$

$A, ZKP_{x_2 \cdot s}$

$B, ZKP_{x_4 \cdot s}$

Bob

random:
 $x_3 \in [0, q-1]$,
 $x_4 \in [1, q-1]$

check: $g^{x_2} \neq 1$

$$B = (g^{x_1} \cdot g^{x_2} \cdot g^{x_3})^{x_4 \cdot s} \\ = g^{(x_1 + x_2 + x_3) \cdot x_4 \cdot s}$$

$$K = (A / (g^{x_2})^{x_4 \cdot s})^{x_4} \\ = (g^{(x_1 + x_3) \cdot x_2 \cdot s})^{x_4} \\ = g^{(x_1 + x_3) \cdot x_2 \cdot x_4 \cdot s}$$

ZKP by Schnorr signature

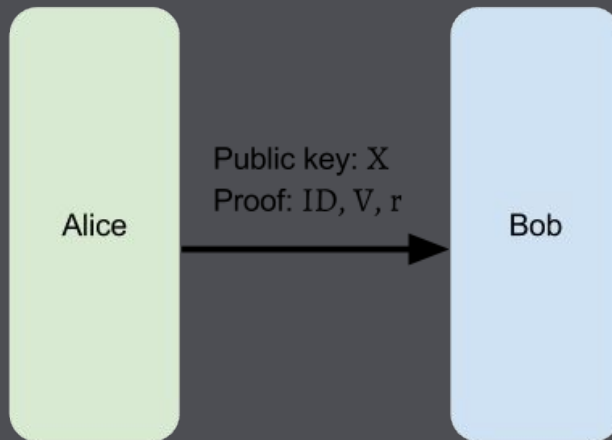
- Group G of prime order q with generator g (Thus $g^q \equiv 1$)
- Secure hash function H

Key Pair Generating

1. Pick **private key**:
random number x
2. Get **public key**: $X = g^x$

Proof of exponent x

1. Pick random number v
2. Compute $V = g^v$
3. $h = H(g, V, X, ID)$
4. $r = v - x \cdot h$



Verifying Proof

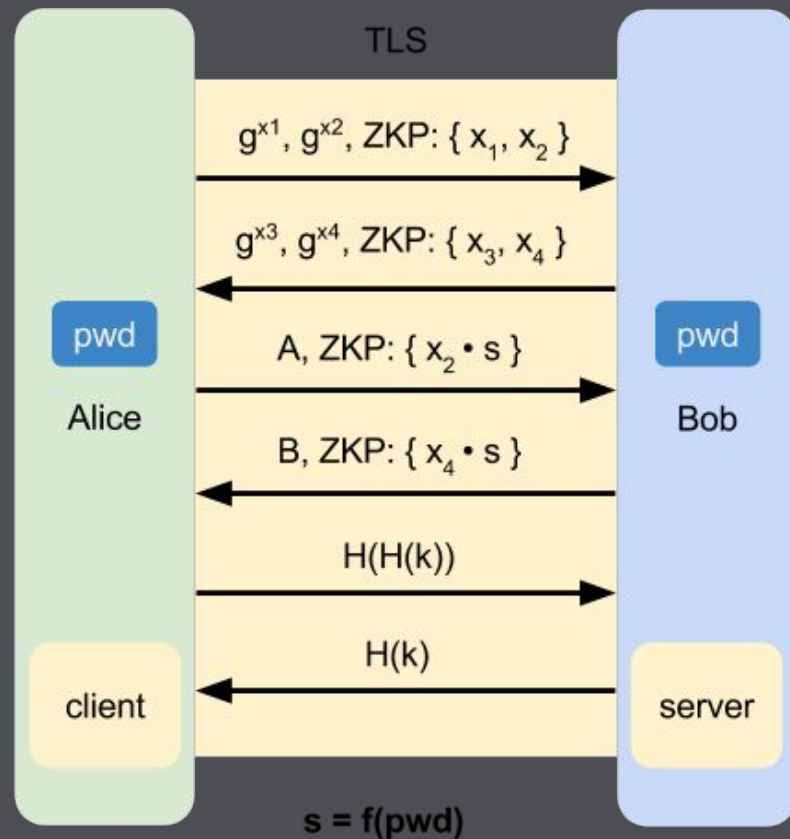
1. $h' = H(g, V, X, ID)$
 2. $V' = g^r \cdot X^{h'}$
 $= g^{v - xh} \cdot (g^x)^{h'}$
 $= g^{v + x(h' - h)}$
 3. Check $V' = V$
- (If $h' = h$, then $V' = V$)

- ID is a unique user identifier
- $r, h, h' \in \mathbb{Z}_q$, the set of congruence classes modulo q
- $x, v \in \mathbb{Z}_q^\times$, the multiplicative group of integers modulo q
- $X, V, V' \in G$

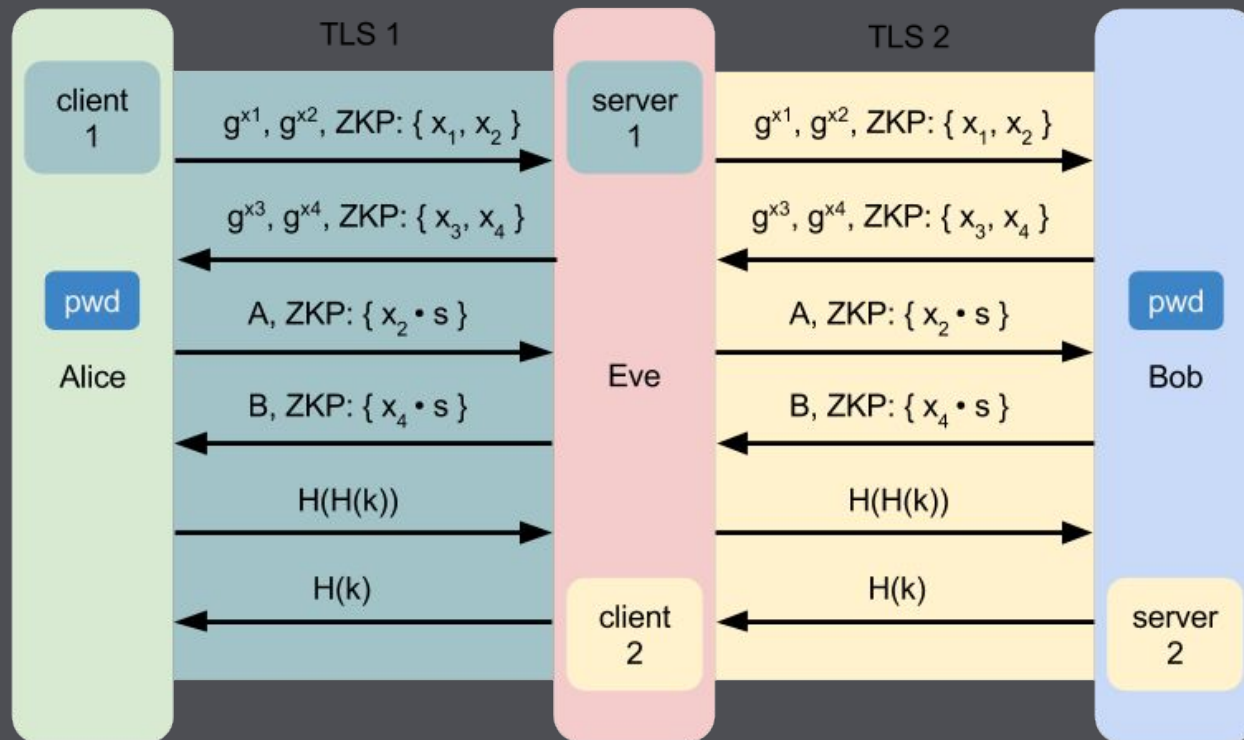


J-PAKE over TLS

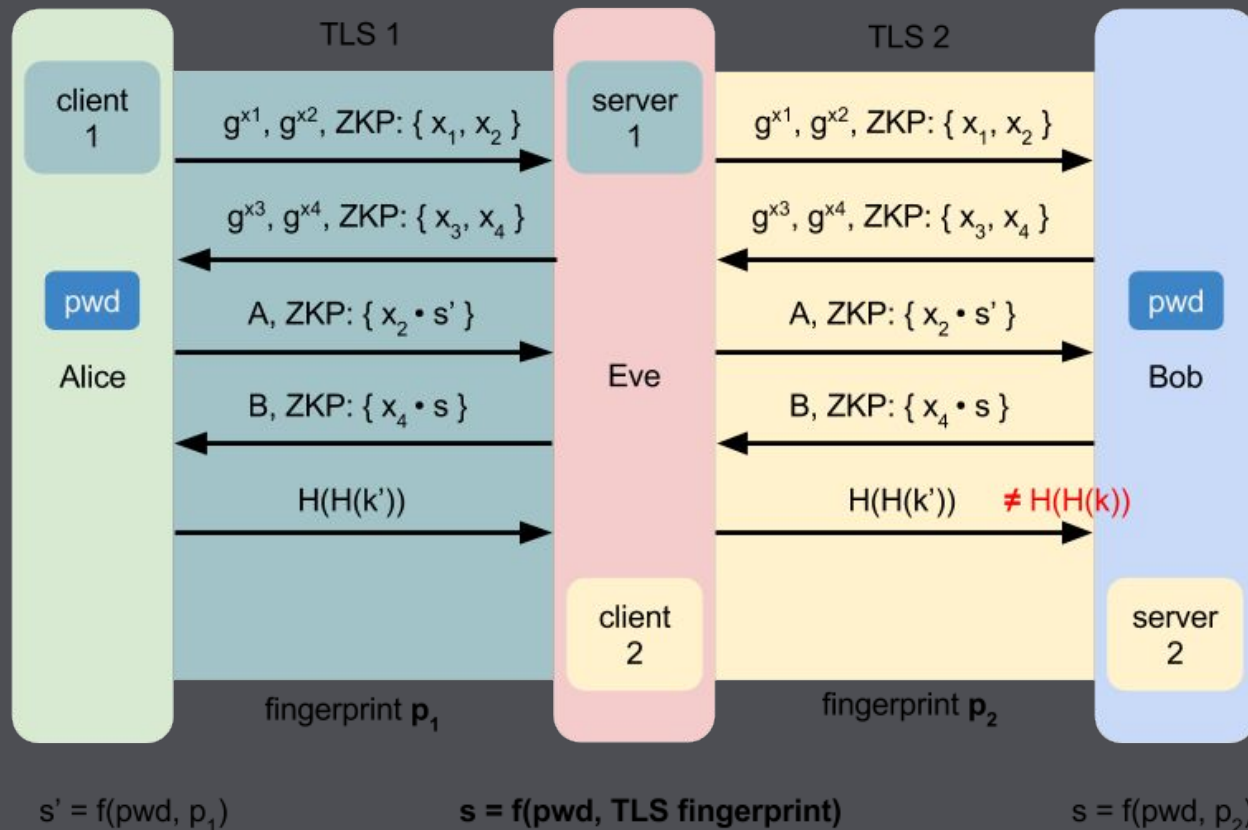
J-PAKE over TLS



J-PAKE over TLS



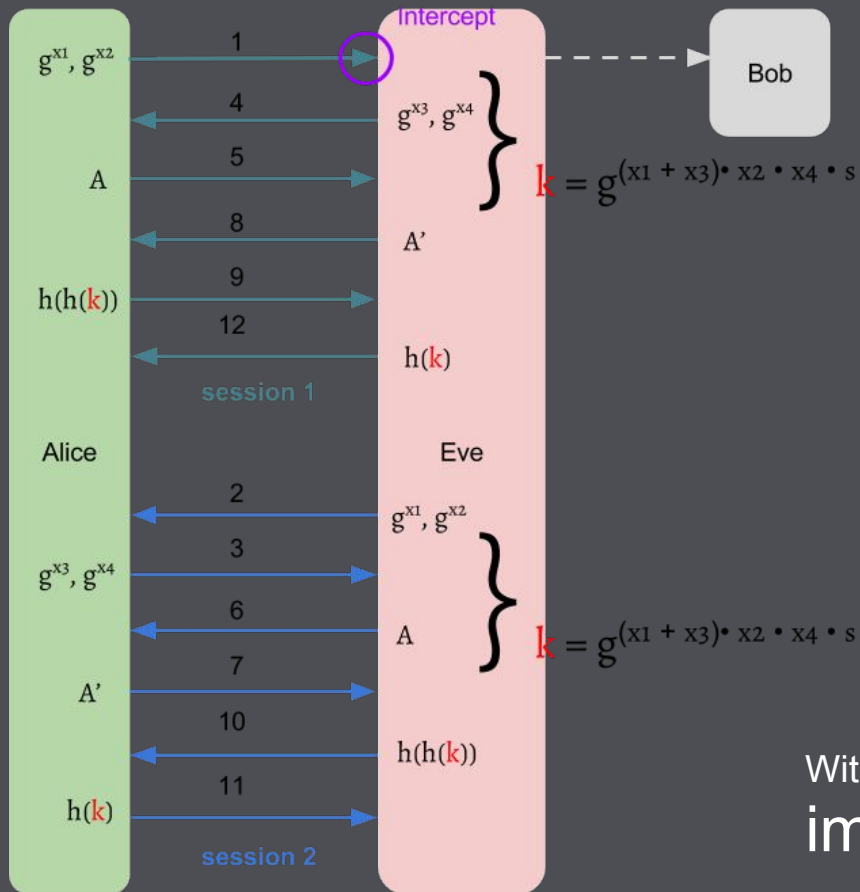
J-PAKE over TLS





Discussion

Why does J-PAKE need ZKP?



1. Eve intercepts Alice's g^{x_1}, g^{x_2} for Bob to initiate **session 1**
2. Eve sends g^{x_1}, g^{x_2} back to Alice to initiate **session 2**
3. Alice replies g^{x_3}, g^{x_4} on **session 2**
4. Eve sends g^{x_3}, g^{x_4} back on **session 1**
5. Alice sends A on **session 1**
6. Eve sends A back on **session 2**
7. Alice replies A' on **session 2**
8. Eve replies A' back on **session 1**
9. Alice sends $h(h(k))$ on **session 1**
10. Eve sends $h(h(k))$ on **session 2**
11. Eve replies $h(k)$ on **session 2**
12. Alice replies $h(k)$ on **session 1**

Without ZKP, J-PAKE will suffer
impersonation-attack

Why do we need TLS instead of using J-PAKE key directly?

- Save the effort to establish TCP channel and negotiate the encryption module

Why don't we just use password to authenticate each other?

- Password is human-memorable weak secret
- PAKE can keep safe of the established session

When do we use J-PAKE

- If the device is unable to operate large exponents
- If the network latency isn't too long

Why x_2 , x_4 can not be 0?

- If x_2 , x_4 , $s = 0$, then $K = 1$
- An attacker can intentionally choose $x_2 = 0$ or $x_4 = 0$ to get $K = 1$ even he doesn't know the password



See more here
