Induction: A process of reasoning (arguing) which infers a general conclusion based on individual cases

Supervised (Inductive) Learning

The University of Texas at Dallas

Supervised Learning

• Given: Training examples $\langle \mathbf{x}, f(\mathbf{x}) \rangle$ for some unknown function f.

• Find: A good approximation to f.

Example Applications

Credit risk assessment

x: Properties of customer and proposed purchase.

 $f(\mathbf{x})$: Approve purchase or not.

• Disease diagnosis

x: Properties of patient (symptoms, lab tests)

 $f(\mathbf{x})$: Disease (or maybe, recommended therapy)

• Face recognition

x: Bitmap picture of person's face

 $f(\mathbf{x})$: Name of the person.

• Automatic Steering

x: Bitmap picture of road surface in front of car.

 $f(\mathbf{x})$: Degrees to turn the steering wheel.

Appropriate Applications for Supervised Learning

Situations where there is no human expert

x: Bond graph for a new molecule.

 $f(\mathbf{x})$: Predicted binding strength to AIDS protease molecule.

• Situations where humans can perform the task but can't describe how they do it.

x: Bitmap picture of hand-written character

 $f(\mathbf{x})$: Ascii code of the character

• Situations where the desired function is changing frequently

x: Description of stock prices and trades for last 10 days.

 $f(\mathbf{x})$: Recommended stock transactions

• Situations where each user needs a customized function f

x: Incoming email message.

 $f(\mathbf{x})$: Importance score for presenting to user (or deleting without presenting).

A learning problem!

X	0	X
0	X	0
0	X	X

X	0	X
X	X	0
X	0	0

$$f(x)=1$$

$$f(x)=0$$

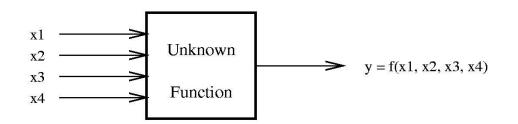
$$f(x)=?$$

If you prefer the training data in this form!

X1	X2	X3	X4	X5	X6	X7	X8	X9	f(x)
X	0	X	0	X	0	0	X	X	1
X	0	X	X	X	0	X	0	0	1
X	X	X	0	X	X	0	0	0	1
0	X	0	X	0	X	0	X	X	0
0	0	X	X	X	0	0	X	X	0
0	X	X	X	0	0	0	X	X	0
0	X	X	0	X	0	X	X	0	?

- x: a 9-dimensional vector
- f(x): a function or a program that takes the vector as input and outputs either a 0 or a 1
- **Task**: given the training examples, find a good approximation to f so that in future if you see an unseen vector "x" you will be able to figure out the value of f(x)

A Learning Problem



A simpler example for analysis!

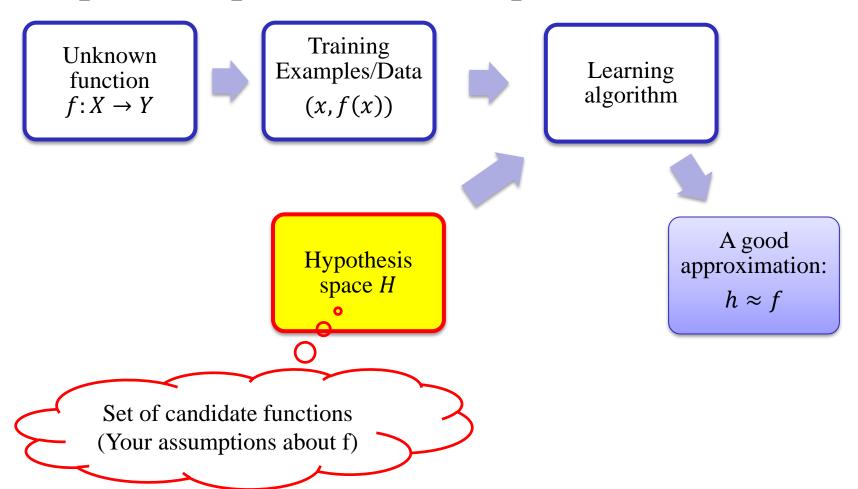
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Example	x_1	x_2	x_3		y
1	0	0	1	0	0
2	0			0	0
3	0	0	1	1	1
4	1	0	0	1	1
5	0		1	0	0
6	1	1	0	0	0
7	0	1	0	1	0

Classification problem

Given data or examples, find the function f?

How to find a good approximation to f?

• A possible/plausible technique



Hypothesis Spaces

• Complete Ignorance. There are $2^{16} = 65536$ possible boolean functions over four input features. We can't figure out which one is correct until we've seen every possible input-output pair. After 7 examples, we still have 2^9 possibilities.

You are assuming that the unknown function f could be any one of the 2¹⁶ functions!

x_1	x_2	x_3	x_4	y
0	0	0	0	?
0	0	0	1	?
0	0	1	0	0
0	0	1	1	1
0	1	0	0	0
0	1	0	1	0
0	1	1	0	0 ? ?
0	1	1	1	?
1	0	0	0	
1	0	0	1	1
1	0	1	0	1 ? ?
1	0	1	1	?
1	1	0	0	0
1	1	0	1	?
1	1	1	0	?
1	1	1	1	?

It turns out that out of the 2¹⁶ possible functions, 2⁹ classify all points in the training data correctly!

Hypothesis Spaces (2)

• Simple Rules. There are only 16 simple conjunctive rules.

You are assuming
•
that the unknown
function f could
be any one of the
16 conjunctive
rules!

Rule	Counterexample
$\Rightarrow y$	1
$x_1 \Rightarrow y$	3
$x_2 \Rightarrow y$	2
$x_3 \Rightarrow y$	1
$x_4 \Rightarrow y$	7
$x_1 \wedge x_2 \Rightarrow y$	3
$x_1 \wedge x_3 \Rightarrow y$	3
$x_1 \wedge x_4 \Rightarrow y$	3
$x_2 \wedge x_3 \Rightarrow y$	3
$x_2 \wedge x_4 \Rightarrow y$	3
$x_3 \wedge x_4 \Rightarrow y$	4
$x_1 \wedge x_2 \wedge x_3 \Rightarrow y$	3
$x_1 \wedge x_2 \wedge x_4 \Rightarrow y$	3
$x_1 \wedge x_3 \wedge x_4 \Rightarrow y$	3
$x_2 \wedge x_3 \wedge x_4 \Rightarrow y$	3
$x_1 \wedge x_2 \wedge x_3 \wedge x_4 \Rightarrow y$	3

Example	x_1	x_2	x_3	x_4	y
1	0	0	1	0	0
2	0	1	0	0	0
3	0	0	1	1	1
4	1	0	0	1	1
5	0	1	1	0	0
6	1	1	0	0	0
7	0	1	0	1	0

Unfortunately, none of them work

No simple rule explains the data. The same is true for simple clauses.

Hypothesis Space (3)

• m-of-n rules. There are 32 possible rules (includes simple conjunctions and clauses).

At least *m* of the *n* variables must be true

You are assuming that the unknown function f could be any one of the 32 m-of-n rules!

Only one of them, the one marked by "***" works!

	Counterexample				
variables	1-of	2-of	3-of	4-of	
$\overline{\{x_1\}}$	3	<u></u>	-	P 6	
$\{x_2\}$	2	<u> </u>	-	12—00	
$\{x_3\}$	1	=	T	¥	
$\{x_4\}$	7	S-1-30	-	n 0	
$\{x_1,x_2\}$	3	3	_	-	
$\{x_1,x_3\}$	4	3	-	-	
$\{x_1,x_4\}$	6	3	_	-	
$\{x_2,x_3\}$	2	3	_	-	
$\{x_2,x_4\}$	2	3	_		
$\{x_3,x_4\}$	4	4	_	-	
$\{x_1,x_2,x_3\}$	1	3	3	s—s	
$\{x_1,x_2,x_4\}$	2	3	3	# <u></u>	
$\{x_1,x_3,x_4\}$	1	***	3		
$\{x_2,x_3,x_4\}$	1	5	3	-	
$\{x_1,x_2,x_3,x_4\}$	1	5	3	3	

Example	x_1	x_2	x_3	x_4	y
1	0	0	1	0	0
2	0	1	0	0	0
3	0	0	1	1	1
4	1	0	0	1	1
5	0	1	1	0	0
6	1	1	0	0	0
7	0	1	0	1	0

Two Views of Learning

- Learning is the removal of our remaining uncertainty. Suppose we knew that the unknown function was an m-of-n boolean function, then we could use the training examples to infer which function it is.
- Learning requires guessing a good, small hypothesis class. We can start with a very small class and enlarge it until it contains an hypothesis that fits the data.

We could be wrong!

- Our prior knowledge might be wrong
- Our guess of the hypothesis class could be wrong

 The smaller the hypothesis class, the more likely we are wrong.

Example: $x_4 \wedge Oneof\{x_1, x_3\} \Rightarrow y$ is also consistent with the training data.

Example: $x_4 \wedge \neg x_2 \Rightarrow y$ is also consistent with the training data.

If either of these is the unknown function, then we will make errors when we are given new x values.

Two Strategies for Machine Learning

- Develop Languages for Expressing Prior Knowledge: Rule grammars and stochastic models.
- Develop Flexible Hypothesis Spaces: Nested collections of hypotheses. Decision trees, rules, neural networks, cases.

In either case:

• Develop Algorithms for Finding an Hypothesis that Fits the Data

Terminology

- Training example. An example of the form $\langle \mathbf{x}, f(\mathbf{x}) \rangle$.
- Target function (target concept). The true function f.
- **Hypothesis**. A proposed function h believed to be similar to f.
- Concept. A boolean function. Examples for which $f(\mathbf{x}) = 1$ are called **positive examples** or **positive instances** of the concept. Examples for which $f(\mathbf{x}) = 0$ are called **negative examples** or **negative instances**.
- Classifier. A discrete-valued function. The possible values $f(\mathbf{x}) \in \{1, \dots, K\}$ are called the classes or class labels.
- **Hypothesis Space**. The space of all hypotheses that can, in principle, be output by a learning algorithm.
- Version Space. The space of all hypotheses in the hypothesis space that have not yet been ruled out by a training example.

Key Issues in Machine Learning

- What are good hypothesis spaces?
 Which spaces have been useful in practical applications and why?
- What algorithms can work with these spaces?

 Are there general design principles for machine learning algorithms?
- How can we optimize accuracy on future data points? This is sometimes called the "problem of overfitting".
- How can we have confidence in the results?

 How much training data is required to find accurate hypotheses? (the *statistical question*)
- Are some learning problems computationally intractable? (the *computational question*)
- How can we formulate application problems as machine learning problems? (the *engineering question*)

Steps in Supervised Learning

1. Determine the representation for "x,f(x)" and determine what "x" to use

Feature Engineering

- 2. Gather a training set (not all data is kosher)

 Data Cleaning
- 3. Select a suitable evaluation method
- 4. Find a suitable learning algorithm among a plethora of available choices
 - Issues discussed on the previous slide

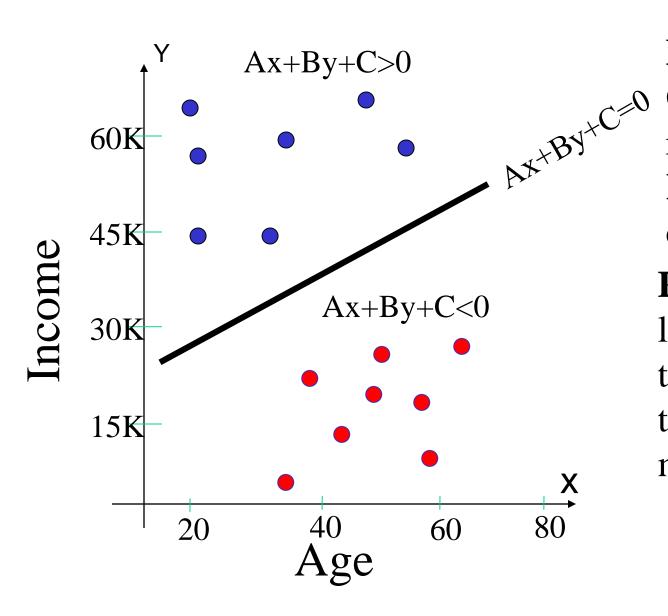
Feature Engineering is the Key

- Most effort in ML projects is constructing features
- Black art: Intuition, creativity required
 - Understand properties of the task at hand
 - How the features interact with or limit the algorithm you are using.
- ML is an iterative process
 - Try different types of features, experiment with each and then decide which feature set/algorithm combination to use

A sample machine learning Algorithm

- 2-way classification problem
 - +ve and -ve classes
- Representation: Lines (Ax+By=C)
 - Specifically
 - if Ax+By+C >0 then classify "+ve"
 - Else classify as "-ve"
- Evaluation: Number of mis-classified examples
- Optimization: An algorithm that searches for the three parameters: A, B and C.

Toy Example



Blue circles:

Good credit (low risk)

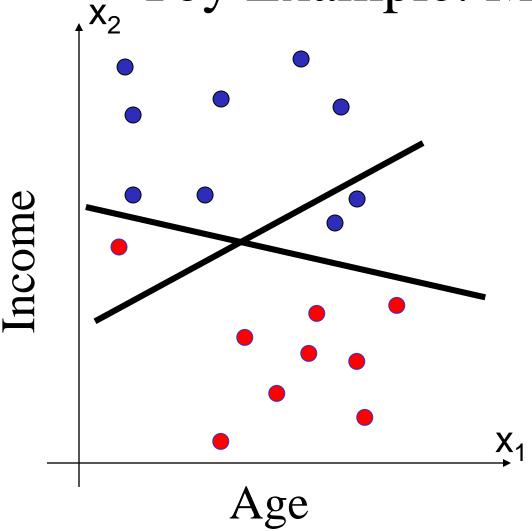
Red circles: Bad credit (high risk)

Problem: Fit a line that separates the two such that the error is minimized.

How do machine learners solve this problem?

- Try different lines until you find one that separates the data into two
- A more plausible alternative
 - Begin with a random line
 - Repeat until no errors
 - For each point
 - If the current line says +ve and point is –ve then decrease A, B and C
 - If the current line says —ve and the point is +ve then increase A, B, and C

Toy Example: More data



Blue circles: Good credit (low risk)
Red circles: Bad credit (high risk)

Problem: Fit a line that separates the two such that the error is minimized.

Learning = Representation + Evaluation + Optimization

Combinations of just three elements

Representation	Evaluation	Optimization
Instances	Accuracy	Greedy search
Hyperplanes	Precision/Recall	Branch & bound
Decision trees	Squared error	Gradient descent
Sets of rules	Likelihood	Quasi-Newton
Neural networks	Posterior prob.	Linear progr.
Graphical models	Margin	Quadratic progr.
Etc.	Etc.	Etc.