

Homework 4

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OBJECTIVE: To build multiple linear regression and binary logistic regression models on the training data to predict the probability that: - a person will crash their car - the amount of money it will cost if the person does crash their car

1. DATA EXPLORATION

Explore, analyze and model a data set containing approximately 8000 records representing a customer at an auto insurance company. Each record has two response variables. The first response variable, TARGET_FLAG, is a 1 or a 0. A “1” means that the person was in a car crash. A zero means that the person was not in a car crash. The second response variable is TARGET_AMT. This value is zero if the person did not crash their car. But if they did crash their car, this number will be a value greater than zero.

VARIABLE NAME DEFINITION THEORETICAL EFFECT

- INDEX Identification Variable (do not use) None
- TARGET_FLAG Was Car in a crash? 1=YES 0=NO None
- TARGET_AMT If car was in a crash, what was the cost None
- AGE Age of Driver Very young people tend to be risky. Maybe very old people also.
- BLUEBOOK Value of Vehicle Unknown effect on probability of collision, but probably effect the payout if there is a crash
- CAR_AGE Vehicle Age Unknown effect on probability of collision, but probably effect the payout if there is a crash
- CAR_TYPE Type of Car Unknown effect on probability of collision, but probably effect the payout if there is a crash
- CAR_USE Vehicle Use Commercial vehicles are driven more, so might increase probability of collision
- CLM_FREQ # Claims (Past 5 Years) The more claims you filed in the past, the more you are likely to file in the future
- EDUCATION Max Education Level Unknown effect, but in theory more educated people tend to drive more safely
- HOMEKIDS # Children at Home Unknown effect
- HOME_VAL Home Value In theory, home owners tend to drive more responsibly
- INCOME Income In theory, rich people tend to get into fewer crashes
- JOB Job Category In theory, white collar jobs tend to be safer
- KIDSDRV # Driving Children When teenagers drive your car, you are more likely to get into crashes
- MSTATUS Marital Status In theory, married people drive more safely
- MVR PTS Motor Vehicle Record Points If you get lots of traffic tickets, you tend to get into more crashes
- OLDCLAIM Total Claims (Past 5 Years) If your total payout over the past five years was high, this suggests future payouts will be high
- PARENT1 Single Parent Unknown effect
- RED_CAR A Red Car Urban legend says that red cars (especially red sports cars) are more risky. Is that true?

- REVOKED License Revoked (Past 7 Years) If your license was revoked in the past 7 years, you probably are a more risky driver.
- SEX Gender Urban legend says that women have less crashes than men. Is that true?
- TIF Time in Force People who have been customers for a long time are usually more safe.
- TRAVTIME Distance to Work Long drives to work usually suggest greater risk
- URBANICITY Home/Work Area Unknown
- YOJ Years on Job People who stay at a job for a long time are usually more safe

2. DATA PREPARATION

```

train_df <- read.csv("https://raw.githubusercontent.com/Chung-Brandon/621-Data-Mining/refs/heads/main/in"
test_df <- read.csv("https://raw.githubusercontent.com/Chung-Brandon/621-Data-Mining/refs/heads/main/in"

# Clean column values and convert to appropriate data types
train_df <- train_df |>
  mutate(across(
    c(TARGET_FLAG, PARENT1, MSTATUS, SEX, EDUCATION, JOB, CAR_USE, CAR_TYPE, RED_CAR, REVOKED,  URBANIC
      ~ as.factor(gsub("z_|<", "", .x))
  )) |>
  mutate(across(
    c(INCOME, HOME_VAL, BLUEBOOK, OLDCLAIM),
    ~ as.numeric(gsub("[\\$,]", "", .x))
  ))

test_df <- test_df |>
  mutate(across(
    c(TARGET_FLAG, PARENT1, MSTATUS, SEX, EDUCATION, JOB, CAR_USE, CAR_TYPE, RED_CAR, REVOKED,  URBANIC
      ~ as.factor(gsub("z_|<", "", .x))
  )) |>
  mutate(across(
    c(INCOME, HOME_VAL, BLUEBOOK, OLDCLAIM),
    ~ as.numeric(gsub("[\\$,]", "", .x))
  ))

glimpse(train_df)

## #> #> Rows: 8,161
## #> #> Columns: 26
## #> #> $ INDEX      <int> 1, 2, 4, 5, 6, 7, 8, 11, 12, 13, 14, 15, 16, 17, 19, 20, 2~
## #> #> $ TARGET_FLAG <fct> 0, 0, 0, 0, 1, 0, 1, 1, 0, 1, 0, 0, 1, 1, 0, 0, 0, 0, 1~
## #> #> $ TARGET_AMT  <dbl> 0.000, 0.000, 0.000, 0.000, 0.000, 2946.000, 0.000, 4021.0~
## #> #> $ KIDSDRV     <int> 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0~
## #> #> $ AGE          <int> 60, 43, 35, 51, 50, 34, 54, 37, 34, 50, 53, 43, 55, 53, 45~
## #> #> $ HOMEKIDS    <int> 0, 0, 1, 0, 0, 1, 0, 2, 0, 0, 0, 0, 0, 0, 3, 0, 3, 2, 1~
## #> #> $ YOJ          <int> 11, 11, 10, 14, NA, 12, NA, 10, 7, 14, 5, 11, 11, 0, 1~
## #> #> $ INCOME       <dbl> 67349, 91449, 16039, NA, 114986, 125301, 18755, 107961, 62~
## #> #> $ PARENT1      <fct> No, No, No, No, Yes, No, No, No, No, No, No, N~
## #> #> $ HOME_VAL     <dbl> 0, 257252, 124191, 306251, 243925, 0, NA, 333680, 0, 0, 0, ~
## #> #> $ MSTATUS       <fct> No, No, Yes, Yes, Yes, No, Yes, Yes, No, No, Yes, Yes, ~
## #> #> $ SEX           <fct> M, M, F, M, F, F, M, F, M, F, F, M, F, F, F, F~
```

```

## $ EDUCATION <fct> PhD, High School, High School, High School, PhD, Bachelors-
## $ JOB <fct> Professional, Blue Collar, Clerical, Blue Collar, Doctor, ~
## $ TRAVTIME <int> 14, 22, 5, 32, 36, 46, 33, 44, 34, 48, 15, 36, 25, 64, 48, ~
## $ CAR_USE <fct> Private, Commercial, Private, Private, Private, Commercial-~
## $ BLUEBOOK <dbl> 14230, 14940, 4010, 15440, 18000, 17430, 8780, 16970, 1120~
## $ TIF <int> 11, 1, 4, 7, 1, 1, 1, 1, 7, 1, 7, 7, 6, 1, 6, 6, 7, 4, ~
## $ CAR_TYPE <fct> Minivan, Minivan, SUV, Minivan, SUV, Sports Car, SUV, Van, ~
## $ RED_CAR <fct> yes, yes, no, yes, no, no, no, yes, no, no, no, no, yes, y~
## $ OLDCLAIM <dbl> 4461, 0, 38690, 0, 19217, 0, 0, 2374, 0, 0, 0, 0, 0, 5028, 0, ~
## $ CLM_FREQ <int> 2, 0, 2, 0, 2, 0, 0, 1, 0, 0, 0, 0, 2, 0, 0, 0, 0, 0, 0, 0, 2~
## $ REVOKED <fct> No, No, No, No, Yes, No, No, Yes, No, No, No, Yes, No, ~
## $ MVR_PTS <int> 3, 0, 3, 0, 3, 0, 0, 10, 0, 1, 0, 0, 3, 3, 3, 0, 0, 0, 0, 0, ~
## $ CAR AGE <int> 18, 1, 10, 6, 17, 7, 1, 7, 1, 17, 11, 1, 9, 10, 5, 13, 16, ~
## $ URBANICITY <fct> Highly Urban/ Urban, Highly Urban/ Urban, Highly Urban/ Ur~

```

```
glimpse(test_df)
```

```

## Rows: 2,141
## Columns: 26

## $ INDEX <int> 3, 9, 10, 18, 21, 30, 31, 37, 39, 47, 60, 62, 63, 64, 68, ~
## $ TARGET_FLAG <fct> NA, ~
## $ TARGET_AMT <lgl> NA, ~
## $ KIDSDRV <int> 0, 1, 0, 0, 0, 0, 2, 0, 0, 0, 1, 0, 0, 0, 2, 0, 0, 0, ~
## $ AGE <int> 48, 40, 44, 35, 59, 46, 60, 54, 36, 50, 42, 41, 37, 36, 34~
## $ HOMEKIDS <int> 0, 1, 2, 2, 0, 0, 0, 2, 0, 0, 2, 2, 3, 3, 2, 2, 0, 0, 0~
## $ YOJ <int> 11, 11, 12, NA, 12, 14, 12, 12, 12, 8, NA, 7, 13, 12, 12, ~
## $ INCOME <dbl> 52881, 50815, 43486, 21204, 87460, NA, 37940, 33212, 13054~
## $ PARENT1 <fct> No, Yes, Yes, Yes, No, No, No, Yes, No, No, Yes, Yes, ~
## $ HOME_VAL <dbl> 0, 0, 0, 0, 0, 207519, 182739, 158432, 344195, 0, 176275, ~
## $ MSTATUS <fct> No, No, No, No, Yes, Yes, Yes, No, No, Yes, No, No, Ye~
## $ SEX <fct> M, M, F, M, M, M, F, M, F, F, M, F, F, M, M, F, F, M, F, F~
## $ EDUCATION <fct> Bachelors, High School, High School, High School, High Sch~
## $ JOB <fct> Manager, Manager, Blue Collar, Clerical, Manager, Professi~
## $ TRAVTIME <int> 26, 21, 30, 74, 45, 7, 16, 27, 5, 22, 24, 29, 62, 15, 26, ~
## $ CAR_USE <fct> Private, Private, Commercial, Private, Private, Commercial~
## $ BLUEBOOK <dbl> 21970, 18930, 5900, 9230, 15420, 25660, 11290, 24000, 2720~
## $ TIF <int> 1, 6, 10, 6, 1, 1, 4, 4, 4, 1, 1, 4, 6, 4, 5, 4, 6, 4, ~
## $ CAR_TYPE <fct> Van, Minivan, SUV, Pickup, Minivan, Panel Truck, Sports Ca~
## $ RED_CAR <fct> yes, no, no, no, yes, no, no, no, no, no, yes, no, no, ~
## $ OLDCLAIM <dbl> 0, 3295, 0, 0, 44857, 2119, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 2045, 0, ~
## $ CLM_FREQ <int> 0, 1, 0, 0, 2, 1, 0, 0, 0, 0, 0, 0, 0, 2, 0, 0, 1, 0, 2, 1~
## $ REVOKED <fct> No, No, No, Yes, No, No, No, No, No, Yes, No, No, ~
## $ MVR PTS <int> 2, 2, 0, 0, 4, 2, 0, 5, 0, 3, 2, 2, 0, 2, 0, 4, 8, 1, 2, 2~
## $ CAR AGE <int> 10, 1, 10, 4, 1, 12, 1, NA, 9, 1, 11, 1, NA, 16, 1, 4, NA, ~
## $ URBANICITY <fct> Highly Urban/ Urban, Highly Urban/ Urban, Highly Rural/ Ru~
```

```
train_df |>  
  summary() |>  
  kable() |>  
  kable_styling()
```

| INDEX | TARGET_FLAG | TARGET_AMT | KIDSDRIV | AGE | HOMEKIDS | YOJ |
|---------------|-------------|---------------|----------------|---------------|----------------|-----------------|
| Min. : 1 | 0:6008 | Min. : 0 | Min. :0.0000 | Min. :16.00 | Min. :0.0000 | Min. : 0.0000 |
| 1st Qu.: 2559 | 1:2153 | 1st Qu.: 0 | 1st Qu.:0.0000 | 1st Qu.:39.00 | 1st Qu.:0.0000 | 1st Qu.: 9.0000 |
| Median : 5133 | NA | Median : 0 | Median :0.0000 | Median :45.00 | Median :0.0000 | Median :1.0000 |
| Mean : 5152 | NA | Mean : 1504 | Mean :0.1711 | Mean :44.79 | Mean :0.7212 | Mean :10.0000 |
| 3rd Qu.: 7745 | NA | 3rd Qu.: 1036 | 3rd Qu.:0.0000 | 3rd Qu.:51.00 | 3rd Qu.:1.0000 | 3rd Qu.:1.0000 |
| Max. :10302 | NA | Max. :107586 | Max. :4.0000 | Max. :81.00 | Max. :5.0000 | Max. :23.0000 |
| NA | NA | NA | NA | NA's :6 | NA | NA's :454 |

Both datasets feature 26 variables; the training set contains 8161 observations and the testing set has 2141.

There are 5 columns contain missing data. Since AGE is only missing in 6 rows, those observations can be dropped. For the rest of the variables, we can impute missing data using the MICE package.

```
colSums(is.na(train_df))
```

```
##      INDEX TARGET_FLAG TARGET_AMT KIDSDRIV      AGE HOMEKIDS
##      0          0          0        0       6         0
##      YOJ      INCOME PARENT1 HOME_VAL MSTATUS      SEX
##      454      445        0        464        0         0
## EDUCATION     JOB TRAVTIME   CAR_USE BLUEBOOK      TIF
##      0          0          0        0       0         0
## CAR_TYPE    RED_CAR OLDCLAIM CLM_FREQ REVOKED MVR_PTS
##      0          0          0        0       0         0
## CAR_AGE URBANICITY
##      510        0
```

```
train_df_imp <- train_df |> drop_na(AGE)
train_df_imp <- complete(mice(train_df_imp, m = 1, method = "pmm", seed = 123))
```

```
##
## iter imp variable
## 1 1 YOJ INCOME HOME_VAL CAR_AGE
## 2 1 YOJ INCOME HOME_VAL CAR_AGE
## 3 1 YOJ INCOME HOME_VAL CAR_AGE
## 4 1 YOJ INCOME HOME_VAL CAR_AGE
## 5 1 YOJ INCOME HOME_VAL CAR_AGE
```

```
colSums(is.na(train_df_imp))
```

```
##      INDEX TARGET_FLAG TARGET_AMT KIDSDRIV      AGE HOMEKIDS
##      0          0          0        0       0         0
##      YOJ      INCOME PARENT1 HOME_VAL MSTATUS      SEX
##      0          0          0        0       0         0
## EDUCATION     JOB TRAVTIME   CAR_USE BLUEBOOK      TIF
##      0          0          0        0       0         0
## CAR_TYPE    RED_CAR OLDCLAIM CLM_FREQ REVOKED MVR_PTS
##      0          0          0        0       0         0
## CAR_AGE URBANICITY
##      0          0
```

The testing data also had missing data used mice a well to impute missing data without imputing data to the target variables. The target variables were turned to empty strings to avoid mice from filling in those variables.

```
# specify methods for each column
methVar <- make.method(test_df)

# set target columns to empty strings "" so mice will not touch them
methVar[methVar != ""] <- "pmm"
methVar["TARGET_FLAG"] <- ""
methVar["TARGET_AMT"] <- ""

imp <- (mice(test_df, m = 1, method = methVar, seed = 123))

## 
##   iter imp variable
##   1   1  AGE  YOJ  INCOME HOME_VAL CAR_AGE
##   2   1  AGE  YOJ  INCOME HOME_VAL CAR_AGE
##   3   1  AGE  YOJ  INCOME HOME_VAL CAR_AGE
##   4   1  AGE  YOJ  INCOME HOME_VAL CAR_AGE
##   5   1  AGE  YOJ  INCOME HOME_VAL CAR_AGE

## Warning: Number of logged events: 2

test_df_imp <- complete(imp)

test_df_imp$TARGET_AMT <- as.numeric(test_df$TARGET_AMT) #ensure the target variable is numeric

colSums(is.na(train_df_imp))

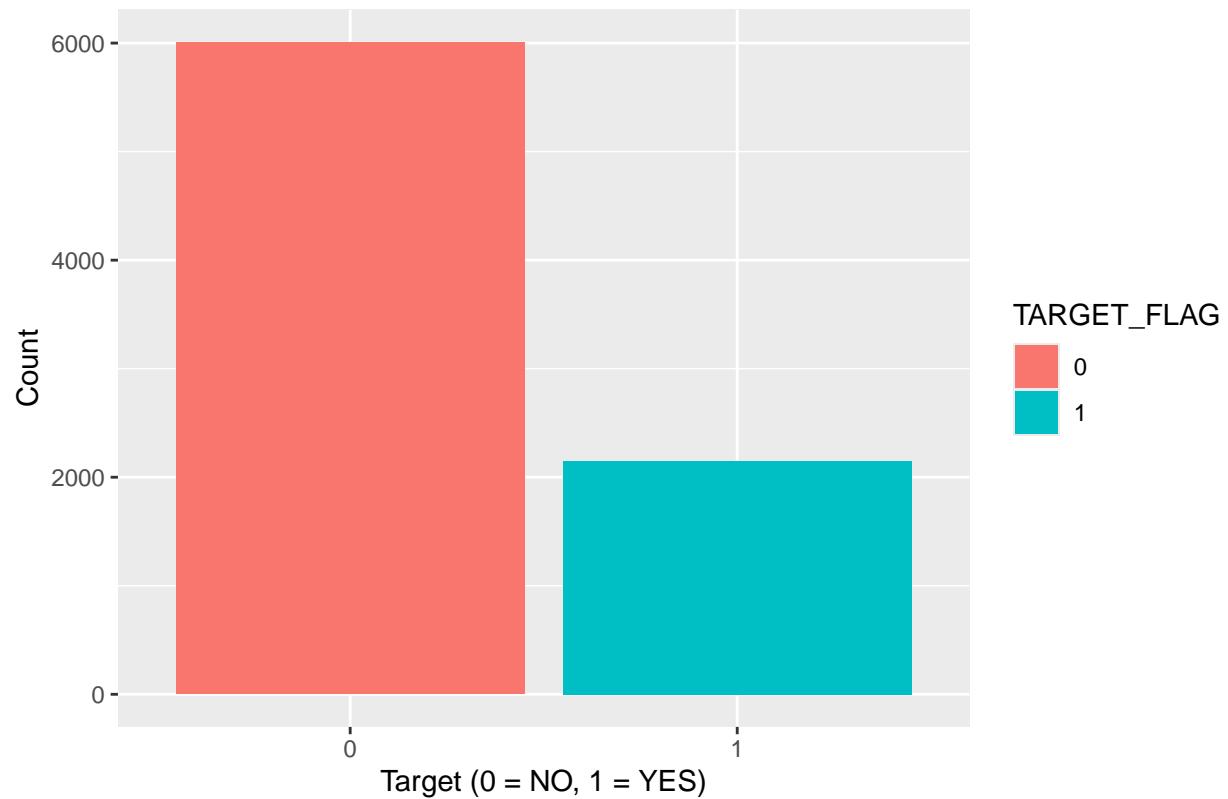
##      INDEX TARGET_FLAG TARGET_AMT KIDSDRV AGE HOMEKIDS
##      0          0        0        0    0        0
##      YOJ        INCOME PARENT1 HOME_VAL MSTATUS SEX
##      0          0        0        0    0        0
## EDUCATION     JOB TRAVTIME CAR_USE BLUEBOOK TIF
##      0          0        0        0    0        0
## CAR_TYPE RED_CAR OLDCLAIM CLM_FREQ REVOKED MVR PTS
##      0          0        0        0    0        0
## CAR_AGE URBANICITY
##      0          0
```

Distributions

Now we can visualize the distributions for our target variables in the training set.

```
ggplot(train_df_imp, aes(x = TARGET_FLAG, fill = TARGET_FLAG)) +
  geom_bar() +
  labs(
    title = "Distribution of Car Crash Involvement",
    x = "Target (0 = NO, 1 = YES)",
    y = "Count"
  )
```

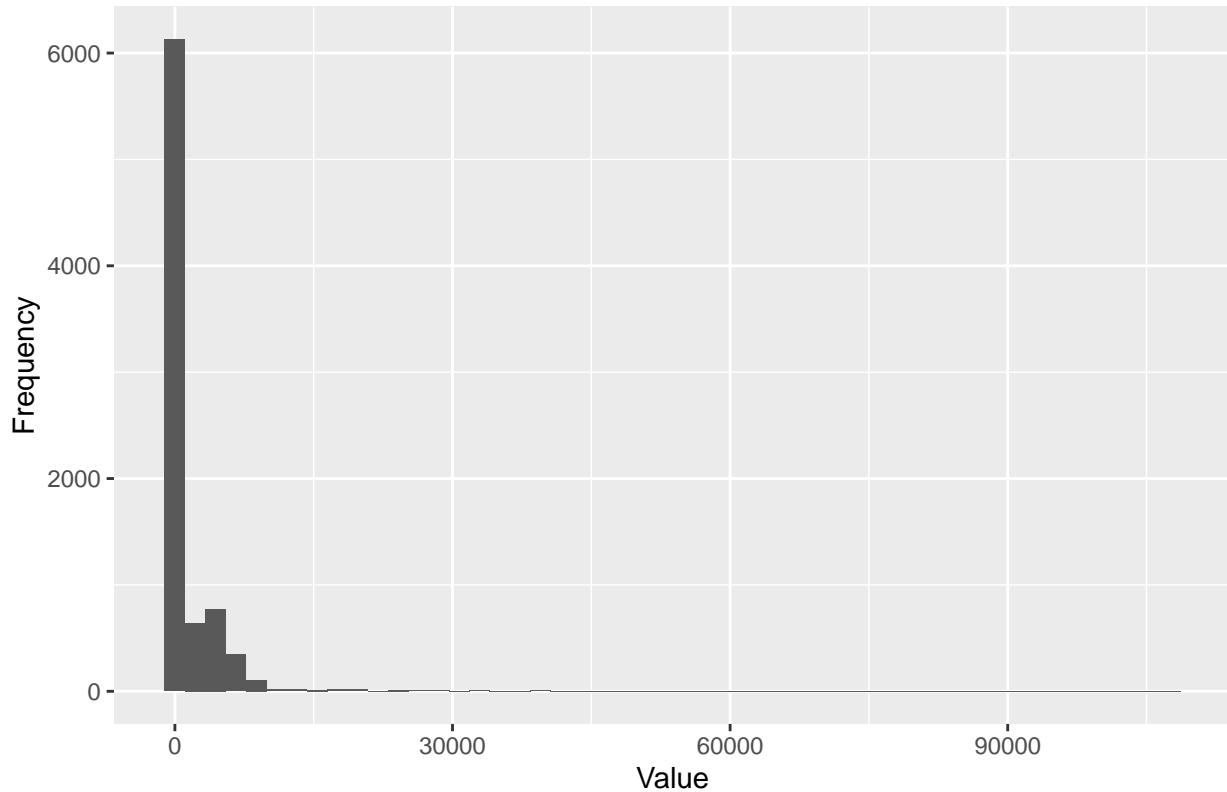
Distribution of Car Crash Involvement



- The distribution of TARGET_AMT is extremely right-skewed. - There are approximately 80% on the rows have a target amount of 0.

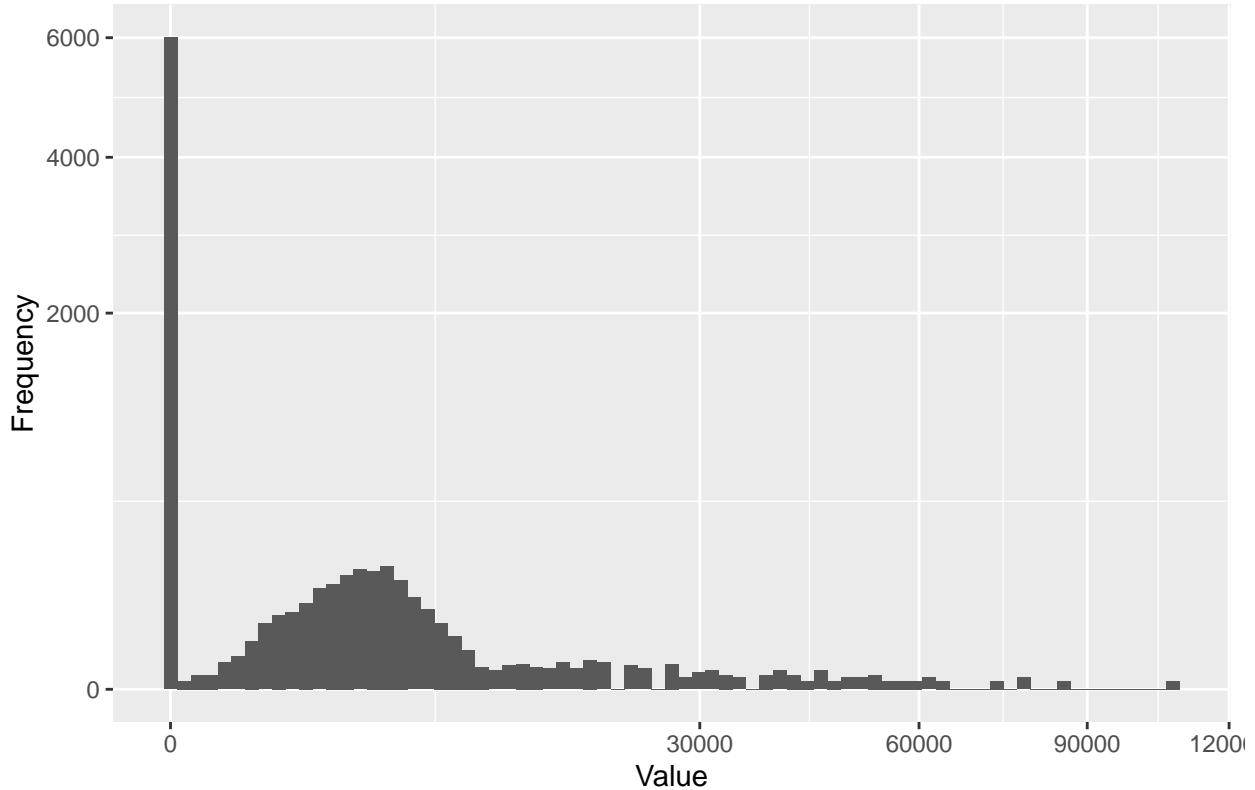
```
ggplot(train_df_imp, aes(x = TARGET_AMT)) +  
  geom_histogram(bins = 50) +  
  labs(title = "Distribution of Car Crash Costs", x = "Value", y = "Frequency")
```

Distribution of Car Crash Costs



```
ggplot(train_df_imp, aes(x = TARGET_AMT)) +
  geom_histogram(bins = 75) +
  scale_x_sqrt() +
  scale_y_sqrt() +
  labs(title = "Distribution of Car Crash Costs (Scaled)", x = "Value", y = "Frequency")
```

Distribution of Car Crash Costs (Scaled)



Distributions for some of the predictor variables can be seen below as well. - The distribution profile show specifically right skew with long tails in variables INCOME, OLDCLAIM, BLUEBOOK, HOME_VAL,TARGET_AMT.These variable contain many small values and a small number of extremely large values, this indicating the presence of outliers. - AGE, TRAVTIME, and YOJ are exhibit a mix of distribution shapes.

```
# Select numeric columns
num_vars <- train_df_imp |>
  as_tibble() |>
  dplyr::select(where(is.numeric)) |>
  dplyr::select(-any_of(c("target", "INDEX")))

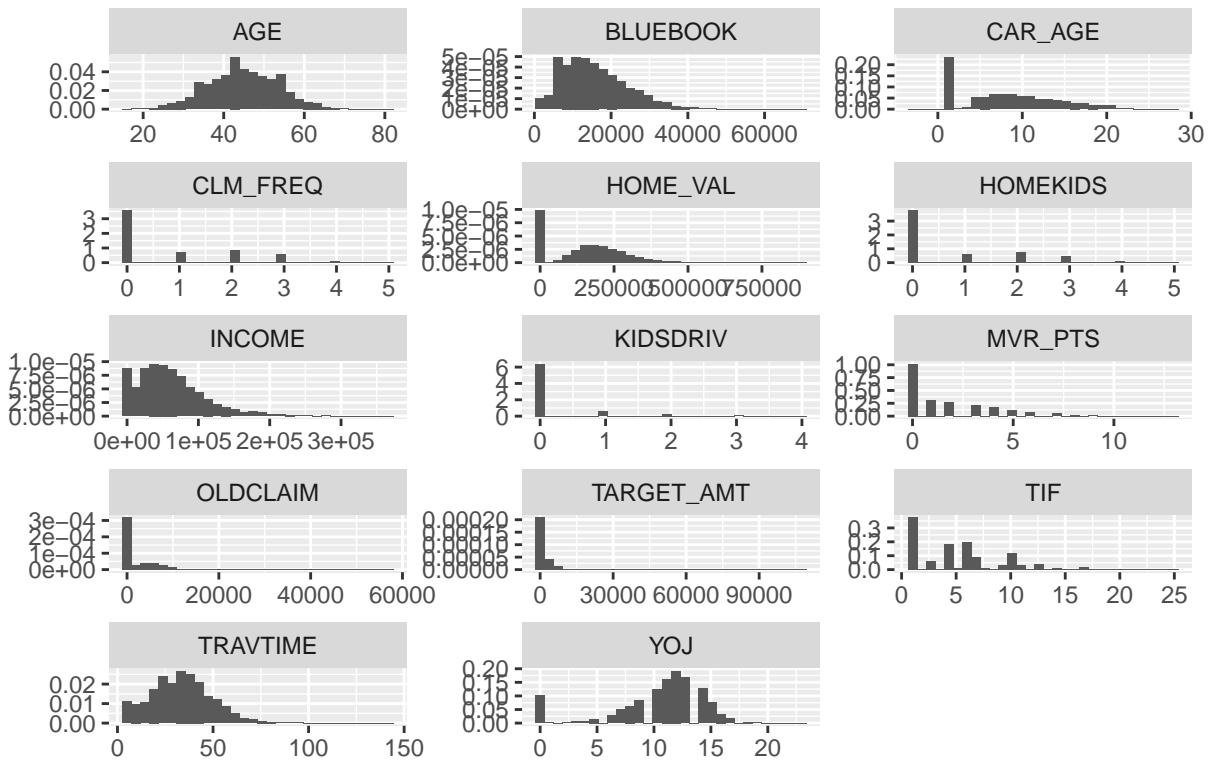
# Reshape to long format
long_df <- num_vars |>
  pivot_longer(cols = everything(), names_to = "variable", values_to = "value")

# Histograms
ggplot(long_df, aes(x = value)) +
  geom_histogram(aes(y = ..density..), bins = 30) +
  facet_wrap(~ variable, scales = "free", ncol = 3) +
  labs(title = "Distributions of Numeric Predictor Variables", y = "", x = "")

## Warning: The dot-dot notation (`..density..`) was deprecated in ggplot2 3.4.0.
## i Please use `after_stat(density)` instead.
## This warning is displayed once every 8 hours.
## Call `lifecycle::last_lifecycle_warnings()` to see where this warning was
```

```
## generated.
```

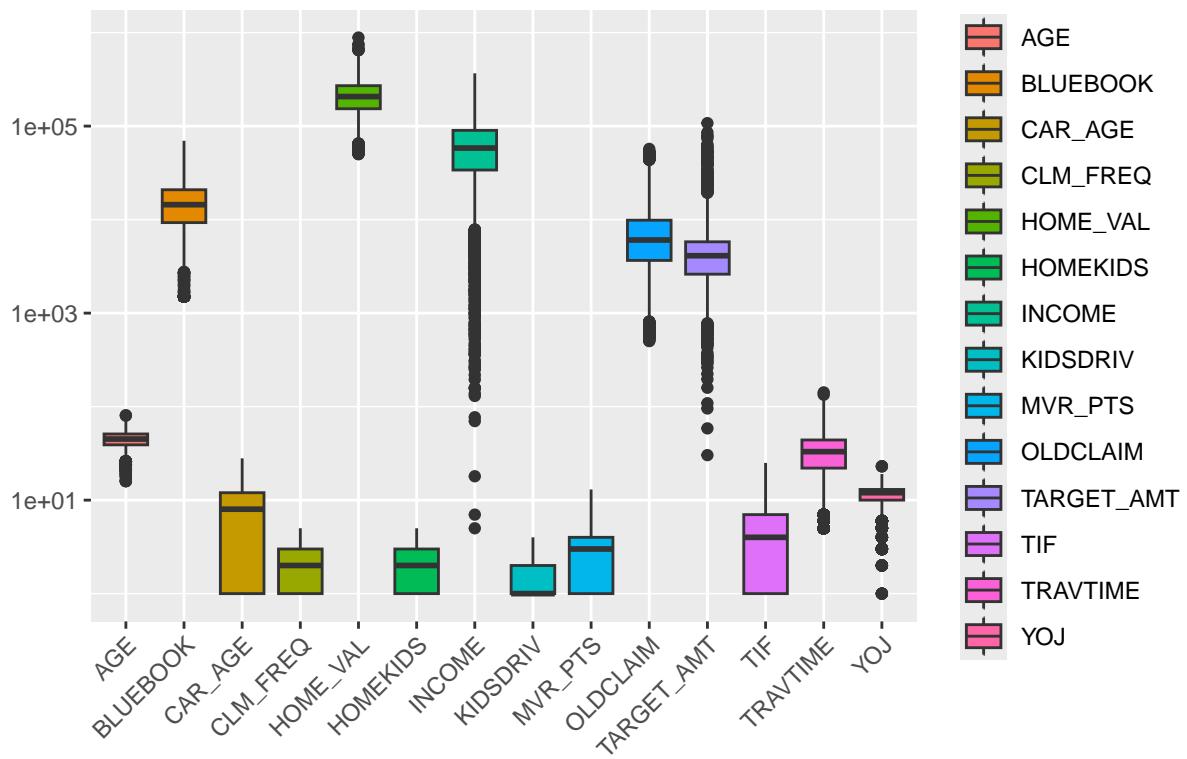
Distributions of Numeric Predictor Variables



- Several variables, such as INCOME, HOME_VAL, BLUEBOOK, and TARGET_AMT show a large spread and long right tails with many outliers, this is consistent with what was seen in the histograms above.
- In contrast, variables such as AGE, YOJ, and TIF exhibit more compact and symmetric distributions, with fewer extreme values.

```
# Box plots
ggplot(long_df, aes(x = variable, y = value, fill = variable)) +
  geom_boxplot() +
  scale_y_log10() +
  theme(axis.text.x = element_text(angle = 45, hjust = 1)) +
  labs(title = "Distributions of Numeric Predictor Variables (Scaled)", y = "", x = "")
```

Distributions of Numeric Predictor Variables (Scaled)



And here is a correlation matrix for the numeric variables.

- The correlation heatmap shows that most numeric predictor variables in the dataset have very weak linear relationships with one another. The majority of correlation values fall between -0.10 and 0.30 . This is helpful for regression modeling because it reduces instability in coefficient estimates.

A few moderate correlations appear:

- INCOME and HOME_VAL (0.58): Higher-income customers tend to live in higher-valued homes, which is expected.
- CLM_FREQ and OLDCLAIM (0.50): Customers with more past claims tend to have higher total past claim costs.
- HOME_VAL and BLUEBOOK (0.22): House value is weakly related to vehicle value.
- CAR_AGE and BLUEBOOK show a small negative correlation (-0.15): Newer cars tend to have higher value.

```
# Compute the correlation matrix
corr_matrix <- cor(num_vars)
corr_matrix[!is.finite(corr_matrix)] <- 0
hclust(as.dist(1 - corr_matrix))
```

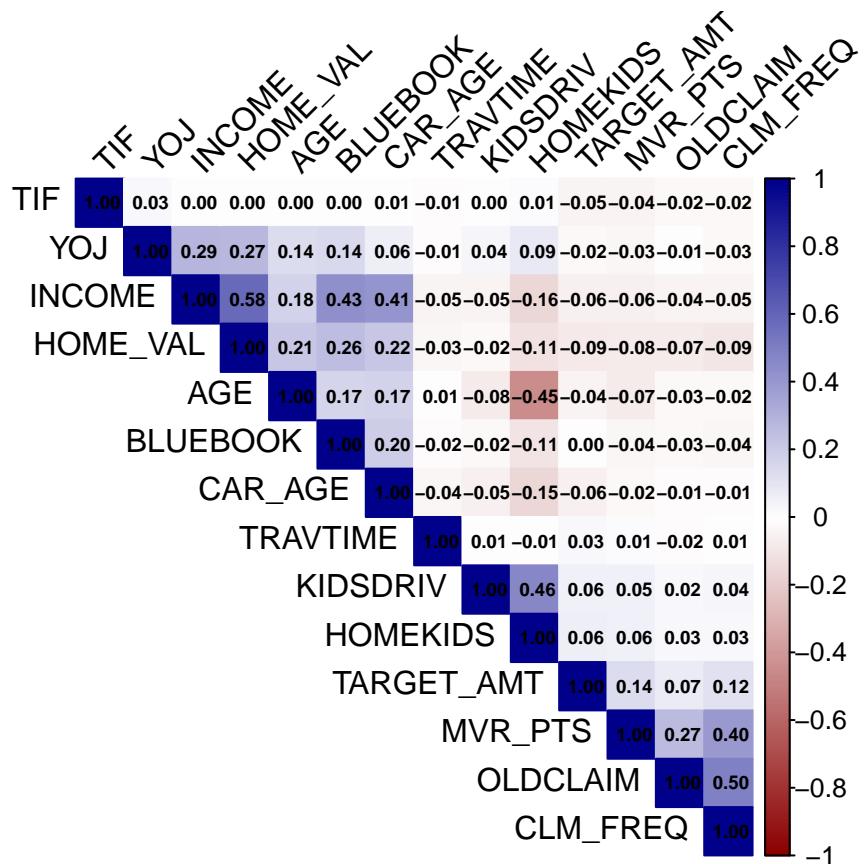
```
##
## Call:
```

```

## hclust(d = as.dist(1 - corr_matrix))
##
## Cluster method : complete
## Number of objects: 14

# Plot correlation heatmap
corrplot(
  corr_matrix,
  method = "color",
  type = "upper",
  order = "hclust",
  addCoef.col = "black",
  tl.col = "black",
  tl.srt = 45,
  number.cex = 0.6,
  col = colorRampPalette(c("darkred", "white", "darkblue"))(200)
)

```



```

# Get upper triangle of the correlation matrix
upper_tri <- upper.tri(corr_matrix)

# Find pairs with correlation > 0.8 (absolute)
high_corr_pairs <- which(abs(corr_matrix) > 0.8 & upper_tri, arr.ind = TRUE)

# Display variable pairs and their correlation

```

```

data.frame(
  Var1 = rownames(corr_matrix)[high_corr_pairs[, 1]],
  Var2 = colnames(corr_matrix)[high_corr_pairs[, 2]],
  Correlation = corr_matrix[high_corr_pairs]
)

## [1] Var1      Var2      Correlation
## <0 rows> (or 0-length row.names)

```

Describe how you have transformed the data by changing the original variables or creating new variables. If you did transform the data or create new variables, discuss why you did this. Here are some possible transformations. a. b. c. d. e. Fix missing values (maybe with a Mean or Median value) Create flags to suggest if a variable was missing Transform data by putting it into buckets Mathematical transforms such as log or square root (or use Box-Cox) Combine variables (such as ratios or adding or multiplying) to create new variables

Some numerical variables seemed to be skewed such as: “INCOME”, “TRAVTIME”, “OLDCLAIM”, “HOME_VAL” and “BLUEBOOK” were skewed to the right. Since right-skewed variables violate regression assumptions, we did a log transformation to make the variables normally distributed. We transformed skewed numeric variables that were not count variables. For the transformation we just added new variables just in case we wanted to use the non-transformed variable for modeling. The transformation can help reduces sensitivity to outliers and help to stabilizes variance.

```
Skewed_vars<- c("INCOME", "HOME_VAL", "BLUEBOOK", "OLDCLAIM", "TRAVTIME")
```

```
#Applied log transformation using log(x+1) to avoid log(0)
for(v in Skewed_vars){
  new_name<-paste0(v, "_LOG")
  train_df_imp[[new_name]]<-log(train_df_imp[[v]]+1)
}
```

```
#Also Applied transformation to test dataframe
for(v in Skewed_vars){
  new_name <- paste0(v, "_LOG")
  test_df_imp[[new_name]] <- log(test_df_imp[[v]] + 1)
}
```

Compartison graph

```

plot_list <- list()

for (v in Skewed_vars) {
  new_v <- paste0(v, "_LOG")

  p1 <- ggplot(train_df_imp, aes(x = .data[[v]])) +
    geom_histogram(aes(y = after_stat(density)), fill = "lightblue", color = "black", bins = 30) +
    ggttitle(paste0(v, " (Before Log)")) +
    theme_minimal()

  p2 <- ggplot(train_df_imp, aes(x = .data[[new_v]])) +
    geom_histogram(aes(y = after_stat(density)), fill = "lightgreen", color = "black", bins = 30) +
    ggttitle(paste0(v, " (After Log)")) +

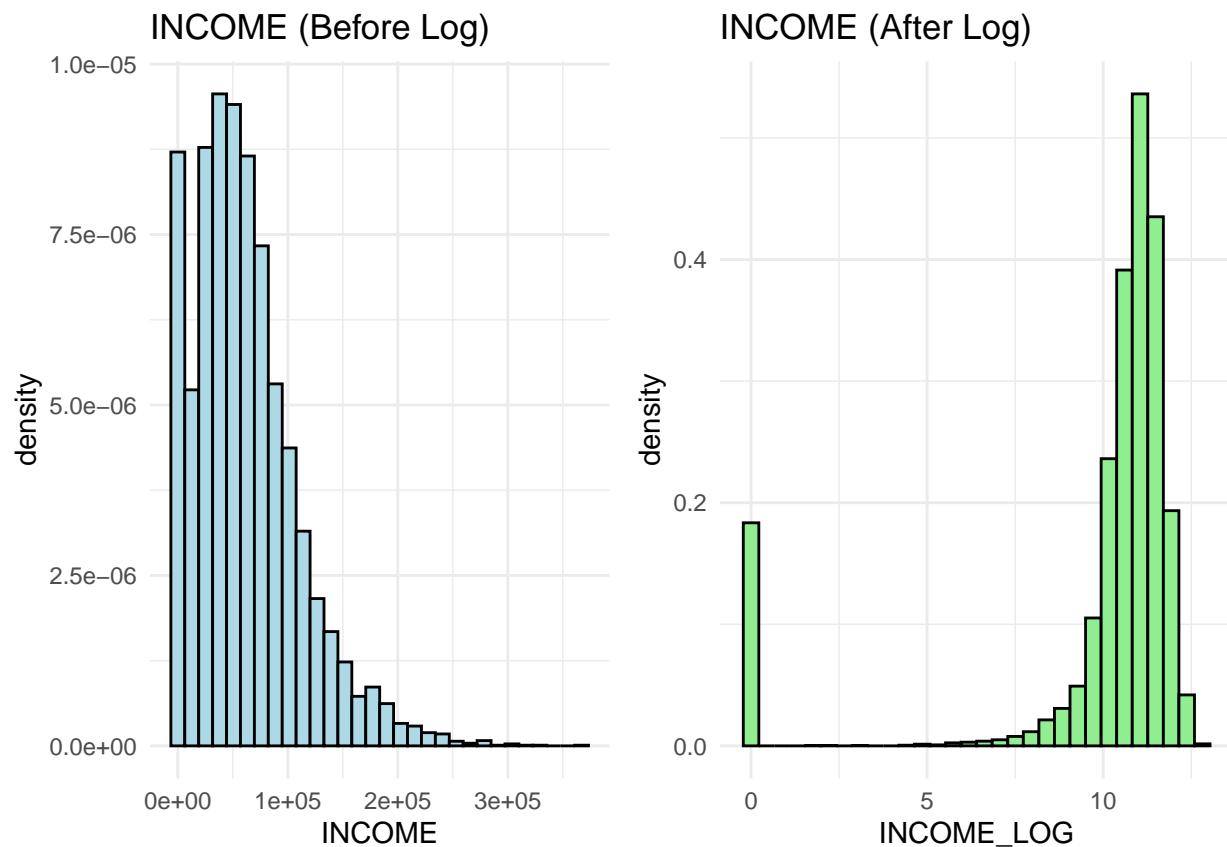
```

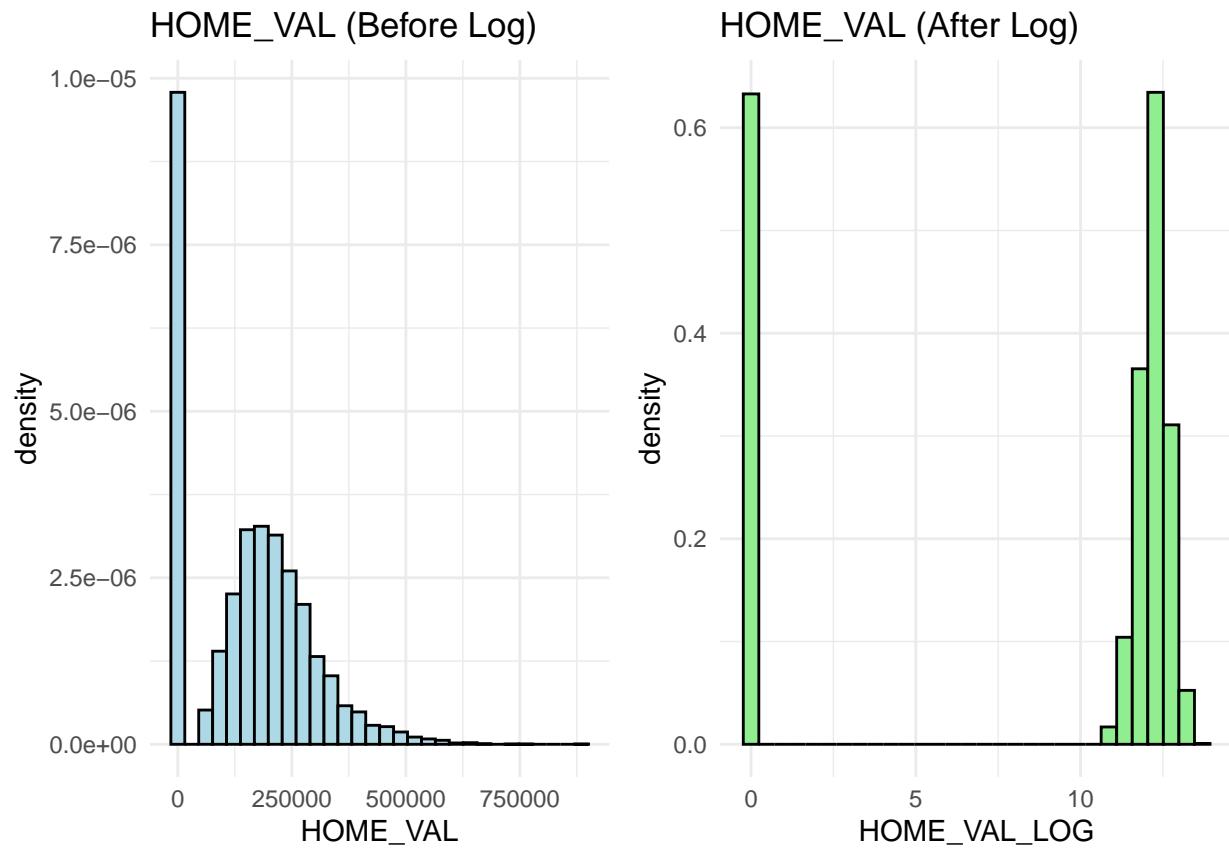
```

theme_minimal()

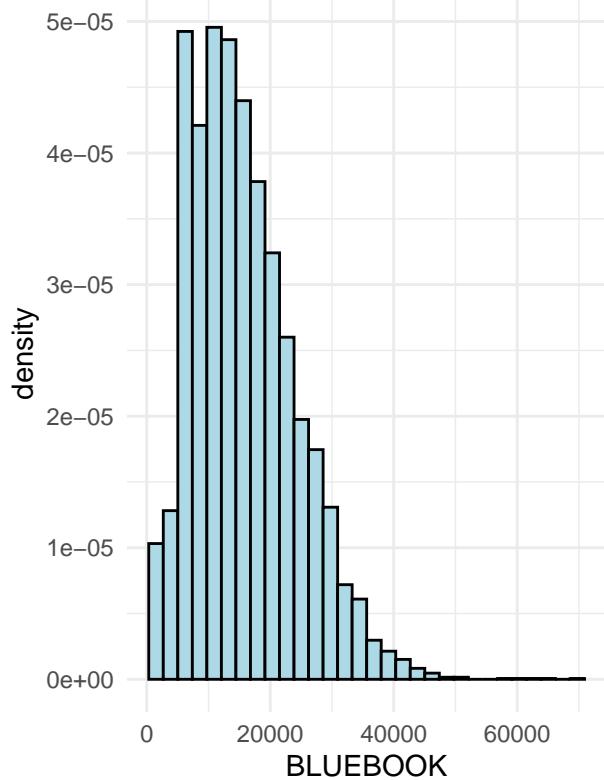
# Display graphs together
grid.arrange(p1, p2, ncol = 2)
}

```

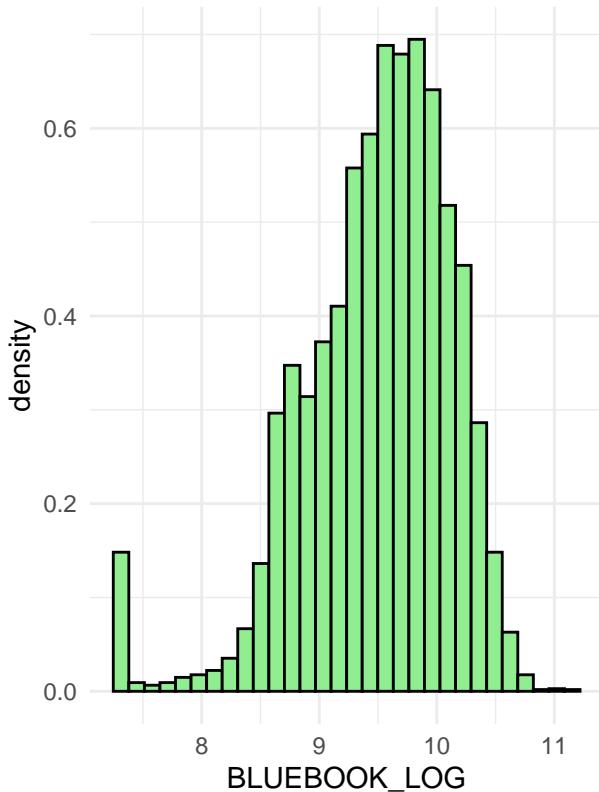


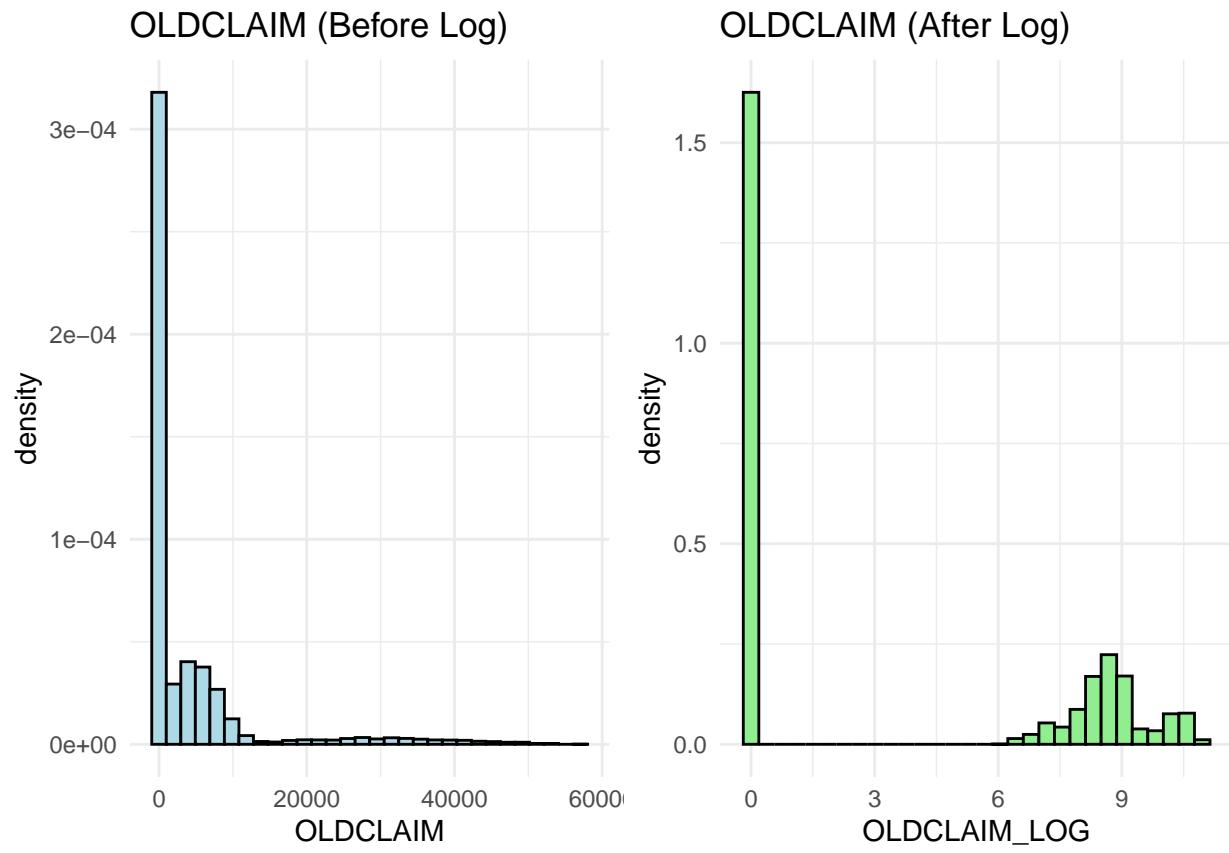


BLUEBOOK (Before Log)

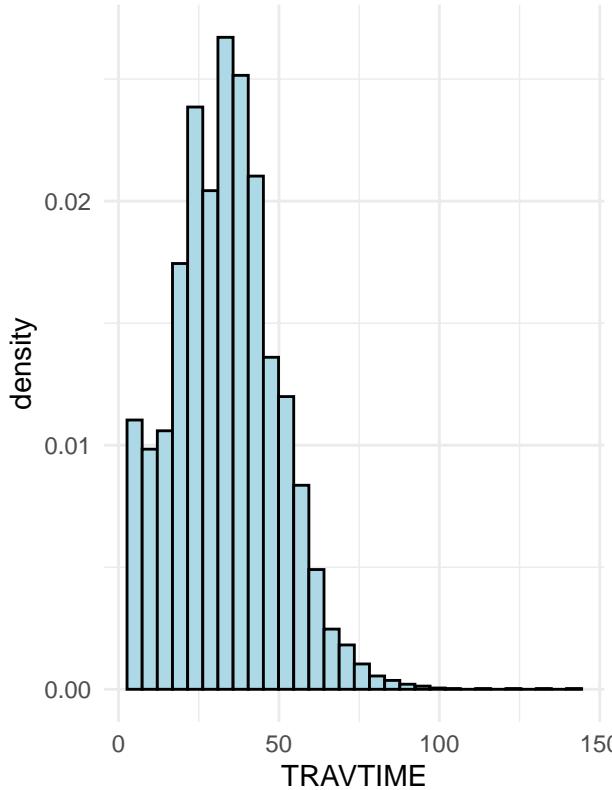


BLUEBOOK (After Log)

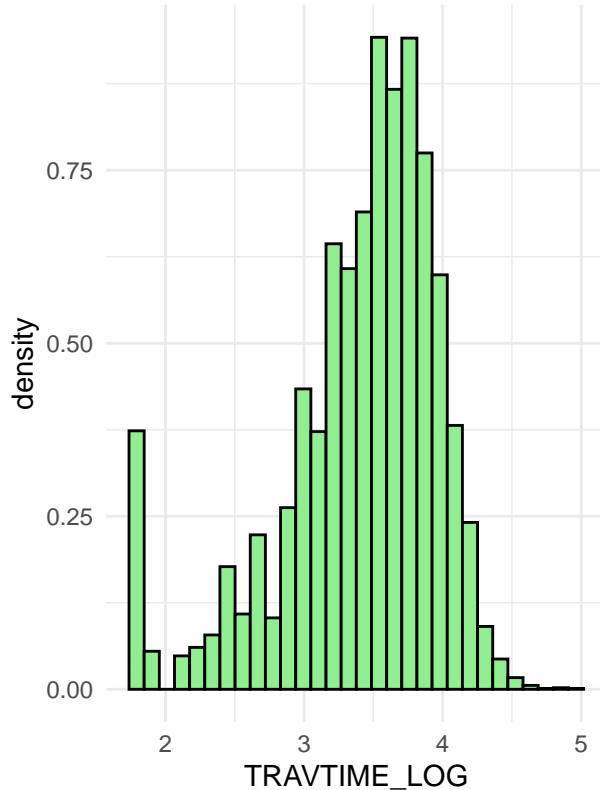




TRAVTIME (Before Log)



TRAVTIME (After Log)



3. BUILD MODELS

Using the training data set, build at least two different multiple linear regression models and three different binary logistic regression models, using different variables (or the same variables with different transformations). You may select the variables manually, use an approach such as Forward or Stepwise, use a different approach such as trees, or use a combination of techniques. Describe the techniques you used. If you manually selected a variable for inclusion into the model or exclusion into the model, indicate why this was done. Discuss the coefficients in the models, do they make sense? For example, if a person has a lot of traffic tickets, you would reasonably expect that person to have more car crashes. If the coefficient is negative (suggesting that the person is a safer driver), then that needs to be discussed. Are you keeping the model even though it is counter intuitive? Why? The boss needs to know.

The three logistic regression models built to predict Target flag (whether a person will crash their car), full logistic model with all predictors, reduced logistic model, and transformed logistic model; these models are different in complexity and interpretability which will allow us to compare performance and coefficients.

Logistic model for Target flag using all variables, as target flag is a binary variable. This model could be used for predicting crash probability. The coefficient show change in crash probability with each predictor, a positive coefficients means a higher crash probability and a negative coefficient would mean a lower crash probability. OLDClaim LOG and CLM FREQ had positive variables as expected but MVR PTS should have been positive as well, but it was skewed to the right and not transformed as it is a count variable.

```
# Removing Index from training and test data

train_df <- subset(train_df, select = -INDEX)
train_df_imp <- subset(train_df_imp, select = -INDEX)
```

```

test_df <- subset(test_df, select = -INDEX)

# Removing TARGET_AMT from data for logistic regression for TARGET_FLAG

train_df_log <- subset(train_df, select = -TARGET_AMT)
train_df_imp_log <- subset(train_df_imp, select = -TARGET_AMT)
test_df_log <- subset(test_df, select = -TARGET_AMT)

```

Logistic Model 1: All Predictors Without Transformed

To compare whether transformations materially improve interpretability or predictive accuracy. Log transformations were applied to reduce skewness (like OLDCLAIM, HOME VAL, BLUEBOOK), improving coefficient stability. CAR USE and CAR TYPE were included because exploratory analysis indicated differences in crash likelihood across usage categories and vehicle types. Based on these coefficient CLM_FREQ positively associated with crash probability and AGE, HOMEVAL, and BLUEBOOK negatively associated, suggesting older, wealthier drivers are safer. Also, the car type show the bigger the vechile the higher the probability the person will crash.

```

logist_model1 <- glm(
  TARGET_FLAG ~ . - INCOME_LOG - HOME_VAL_LOG - BLUEBOOK_LOG - OLDCLAIM_LOG - TRAVTIME_LOG,
  data = train_df_imp_log,
  family = binomial
)

summary(logist_model1)

## 
## Call:
## glm(formula = TARGET_FLAG ~ . - INCOME_LOG - HOME_VAL_LOG - BLUEBOOK_LOG -
##       OLDCLAIM_LOG - TRAVTIME_LOG, family = binomial, data = train_df_imp_log)
## 
## Coefficients:
##                               Estimate Std. Error z value Pr(>|z|)
## (Intercept)                -3.268e+00  3.381e-01 -9.664 < 2e-16 ***
## KIDSDRV                   3.911e-01  6.129e-02  6.380 1.77e-10 ***
## AGE                      -1.742e-03  4.033e-03 -0.432 0.665757
## HOMEKIDS                  4.357e-02  3.727e-02  1.169 0.242411
## YOJ                      -6.791e-03  8.485e-03 -0.800 0.423527
## INCOME                   -3.913e-06  1.127e-06 -3.473 0.000514 ***
## PARENT1Yes                 3.749e-01  1.098e-01  3.415 0.000639 ***
## HOME_VAL                  -1.201e-06  3.471e-07 -3.460 0.000540 ***
## MSTATUSYes                -5.036e-01  8.527e-02 -5.905 3.52e-09 ***
## SEXM                      9.099e-02  1.121e-01  0.812 0.417004
## EDUCATIONHigh School      3.876e-01  8.841e-02  4.384 1.16e-05 ***
## EDUCATIONMasters           9.824e-02  1.399e-01  0.702 0.482568
## EDUCATIONPhD               2.506e-01  1.806e-01  1.388 0.165272
## JOBBlue Collar             2.951e-01  1.853e-01  1.592 0.111284
## JOBClerical                 3.810e-01  1.972e-01  1.932 0.053379 .
## JOBDoctor                  -4.571e-01  2.671e-01 -1.711 0.087068 .
## JOBHome Maker               2.030e-01  2.113e-01  0.961 0.336651
## JOBLawyer                   9.662e-02  1.690e-01  0.572 0.567478
## JOBManager                 -5.613e-01  1.714e-01 -3.274 0.001059 **

```

```

## JOBProfessional          1.567e-01  1.783e-01  0.879  0.379617
## JOBStudent               1.849e-01  2.158e-01  0.857  0.391441
## TRAVTIME                 1.463e-02  1.883e-03  7.770  7.85e-15 ***
## CAR_USEPPrivate           -7.650e-01  8.743e-02  -8.750  < 2e-16 ***
## BLUEBOOK                  -2.018e-05  5.277e-06  -3.824  0.000131 ***
## TIF                        -5.559e-02  7.352e-03  -7.561  4.00e-14 ***
## CAR_TYPEPanel Truck        5.535e-01  1.605e-01  3.448  0.000565 ***
## CAR_TYPEPickup             5.546e-01  1.001e-01  5.542  2.99e-08 ***
## CAR_TYPESports Car         1.026e+00  1.299e-01  7.894  2.93e-15 ***
## CAR_TYPESUV                7.692e-01  1.113e-01  6.911  4.82e-12 ***
## CAR_TYPEVan                6.124e-01  1.261e-01  4.857  1.19e-06 ***
## RED_CARyes                 -2.376e-02  8.665e-02  -0.274  0.783958
## OLDCLAIM                   -1.412e-05  3.911e-06  -3.611  0.000306 ***
## CLM_FREQ                     1.968e-01  2.856e-02  6.891  5.56e-12 ***
## REVOKEDYes                  8.903e-01  9.133e-02  9.748  < 2e-16 ***
## MVR PTS                      1.132e-01  1.362e-02  8.307  < 2e-16 ***
## CAR AGE                      -5.609e-04  7.528e-03  -0.075  0.940598
## URBANICITYHighly Urban/ Urban  2.384e+00  1.128e-01  21.137  < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
## Null deviance: 9404.0  on 8154  degrees of freedom
## Residual deviance: 7289.3  on 8118  degrees of freedom
## AIC: 7363.3
##
## Number of Fisher Scoring iterations: 5

pred_probs <- predict(logist_model1, train_df_imp, type = "response")
pred_class <- ifelse(pred_probs > 0.5, 1, 0)

# Confusion matrix on training data
confusionMatrix(
  factor(pred_class),
  factor(train_df_imp$TARGET_FLAG),
  positive = "1"
)

## Confusion Matrix and Statistics
##
##             Reference
## Prediction      0      1
##               0 5545 1236
##               1  462  912
##
##             Accuracy : 0.7918
##             95% CI : (0.7828, 0.8006)
##   No Information Rate : 0.7366
##   P-Value [Acc > NIR] : < 2.2e-16
##
##             Kappa : 0.3932
##
##   Mcnemar's Test P-Value : < 2.2e-16

```

```

##          Sensitivity : 0.4246
##          Specificity  : 0.9231
##          Pos Pred Value : 0.6638
##          Neg Pred Value : 0.8177
##          Prevalence   : 0.2634
##          Detection Rate  : 0.1118
##          Detection Prevalence : 0.1685
##          Balanced Accuracy : 0.6738
##
##          'Positive' Class  : 1
##

```

Logistic Model 2: Reduced Predictors without Transformed

To compare the outcomes with the reduced transformed.

```
logist_model2 <- step(logist_model1, direction = "backward")
```

```

## Start:  AIC=7363.31
## TARGET_FLAG ~ (KIDSDRV + AGE + HOMEKIDS + YOJ + INCOME + PARENT1 +
##                 HOME_VAL + MSTATUS + SEX + EDUCATION + JOB + TRAVTIME + CAR_USE +
##                 BLUEBOOK + TIF + CAR_TYPE + RED_CAR + OLDCLAIM + CLM_FREQ +
##                 REVOKED + MVR PTS + CAR_AGE + URBANICITY + INCOME_LOG + HOME_VAL_LOG +
##                 BLUEBOOK_LOG + OLDCLAIM_LOG + TRAVTIME_LOG) - INCOME_LOG -
##                 HOME_VAL_LOG - BLUEBOOK_LOG - OLDCLAIM_LOG - TRAVTIME_LOG
##
##          Df Deviance    AIC
## - CAR_AGE     1  7289.3 7361.3
## - RED_CAR     1  7289.4 7361.4
## - AGE         1  7289.5 7361.5
## - YOJ         1  7290.0 7362.0
## - SEX         1  7290.0 7362.0
## - HOMEKIDS    1  7290.7 7362.7
## <none>        7289.3 7363.3
## - PARENT1     1  7301.0 7373.0
## - HOME_VAL    1  7301.3 7373.3
## - INCOME      1  7301.6 7373.6
## - OLDCLAIM    1  7302.6 7374.6
## - BLUEBOOK    1  7304.2 7376.2
## - EDUCATION    3  7310.4 7378.4
## - MSTATUS      1  7323.8 7395.8
## - KIDSDRV     1  7330.1 7402.1
## - CLM_FREQ     1  7336.2 7408.2
## - JOB          8  7350.5 7408.5
## - TIF          1  7348.6 7420.6
## - TRAVTIME     1  7349.9 7421.9
## - MVR PTS     1  7358.9 7430.9
## - CAR_USE      1  7367.2 7439.2
## - CAR_TYPE     5  7381.2 7445.2
## - REVOKED      1  7382.8 7454.8
## - URBANICITY   1  7934.5 8006.5
##
```

```

## Step: AIC=7361.32
## TARGET_FLAG ~ KIDSDRV + AGE + HOMEKIDS + YOJ + INCOME + PARENT1 +
##      HOME_VAL + MSTATUS + SEX + EDUCATION + JOB + TRAVTIME + CAR_USE +
##      BLUEBOOK + TIF + CAR_TYPE + RED_CAR + OLDCLAIM + CLM_FREQ +
##      REVOKED + MVR PTS + URBANICITY
##
##              Df Deviance    AIC
## - RED_CAR     1  7289.4 7359.4
## - AGE         1  7289.5 7359.5
## - YOJ         1  7290.0 7360.0
## - SEX         1  7290.0 7360.0
## - HOMEKIDS    1  7290.7 7360.7
## <none>        7289.3 7361.3
## - PARENT1     1  7301.0 7371.0
## - HOME_VAL    1  7301.3 7371.3
## - INCOME       1  7301.6 7371.6
## - OLDCLAIM     1  7302.6 7372.6
## - BLUEBOOK     1  7304.2 7374.2
## - EDUCATION    3  7313.9 7379.9
## - MSTATUS       1  7323.8 7393.8
## - KIDSDRV      1  7330.1 7400.1
## - CLM_FREQ     1  7336.2 7406.2
## - JOB          8  7350.5 7406.5
## - TIF          1  7348.6 7418.6
## - TRAVTIME     1  7349.9 7419.9
## - MVR PTS      1  7358.9 7428.9
## - CAR_USE       1  7367.3 7437.3
## - CAR_TYPE      5  7381.3 7443.3
## - REVOKED       1  7382.8 7452.8
## - URBANICITY   1  7934.6 8004.6
##
## Step: AIC=7359.39
## TARGET_FLAG ~ KIDSDRV + AGE + HOMEKIDS + YOJ + INCOME + PARENT1 +
##      HOME_VAL + MSTATUS + SEX + EDUCATION + JOB + TRAVTIME + CAR_USE +
##      BLUEBOOK + TIF + CAR_TYPE + OLDCLAIM + CLM_FREQ + REVOKED +
##      MVR PTS + URBANICITY
##
##              Df Deviance    AIC
## - AGE          1  7289.6 7357.6
## - SEX          1  7290.0 7358.0
## - YOJ          1  7290.0 7358.0
## - HOMEKIDS    1  7290.7 7358.7
## <none>        7289.4 7359.4
## - PARENT1     1  7301.1 7369.1
## - HOME_VAL    1  7301.3 7369.3
## - INCOME       1  7301.7 7369.7
## - OLDCLAIM     1  7302.7 7370.7
## - BLUEBOOK     1  7304.2 7372.2
## - EDUCATION    3  7314.1 7378.1
## - MSTATUS       1  7323.9 7391.9
## - KIDSDRV      1  7330.2 7398.2
## - CLM_FREQ     1  7336.2 7404.2
## - JOB          8  7350.7 7404.7
## - TIF          1  7348.7 7416.7

```

```

## - TRAVTIME      1    7350.0 7418.0
## - MVR_PTS       1    7358.9 7426.9
## - CAR_USE        1    7367.4 7435.4
## - CAR_TYPE       5    7381.5 7441.5
## - REVOKED        1    7382.9 7450.9
## - URBANICITY     1    7934.7 8002.7
##
## Step: AIC=7357.57
## TARGET_FLAG ~ KIDSDRV + HOMEKIDS + YOJ + INCOME + PARENT1 +
##           HOME_VAL + MSTATUS + SEX + EDUCATION + JOB + TRAVTIME + CAR_USE +
##           BLUEBOOK + TIF + CAR_TYPE + OLDCLAIM + CLM_FREQ + REVOKED +
##           MVR_PTS + URBANICITY
##
##              Df Deviance   AIC
## - SEX            1  7290.1 7356.1
## - YOJ            1  7290.4 7356.4
## <none>          7289.6 7357.6
## - HOMEKIDS       1  7291.6 7357.6
## - PARENT1        1  7301.7 7367.7
## - INCOME         1  7301.8 7367.8
## - HOME_VAL        1  7301.8 7367.8
## - OLDCLAIM        1  7302.9 7368.9
## - BLUEBOOK        1  7305.1 7371.1
## - EDUCATION       3  7314.2 7376.2
## - MSTATUS         1  7324.1 7390.1
## - KIDSDRV         1  7330.8 7396.8
## - CLM_FREQ        1  7336.3 7402.3
## - JOB             8  7351.5 7403.5
## - TIF             1  7348.8 7414.8
## - TRAVTIME        1  7350.0 7416.0
## - MVR_PTS         1  7359.4 7425.4
## - CAR_USE          1  7367.4 7433.4
## - CAR_TYPE         5  7381.5 7439.5
## - REVOKED         1  7383.1 7449.1
## - URBANICITY      1  7935.9 8001.9
##
## Step: AIC=7356.1
## TARGET_FLAG ~ KIDSDRV + HOMEKIDS + YOJ + INCOME + PARENT1 +
##           HOME_VAL + MSTATUS + EDUCATION + JOB + TRAVTIME + CAR_USE +
##           BLUEBOOK + TIF + CAR_TYPE + OLDCLAIM + CLM_FREQ + REVOKED +
##           MVR_PTS + URBANICITY
##
##              Df Deviance   AIC
## - YOJ            1  7290.9 7354.9
## - HOMEKIDS       1  7292.0 7356.0
## <none>          7290.1 7356.1
## - PARENT1        1  7302.1 7366.1
## - HOME_VAL        1  7302.2 7366.2
## - INCOME          1  7302.4 7366.4
## - OLDCLAIM        1  7303.4 7367.4
## - EDUCATION       3  7314.7 7374.7
## - BLUEBOOK        1  7312.2 7376.2
## - MSTATUS          1  7324.6 7388.6
## - KIDSDRV         1  7331.3 7395.3

```

```

## - CLM_FREQ    1  7336.9 7400.9
## - JOB         8  7351.8 7401.8
## - TIF         1  7349.4 7413.4
## - TRAVTIME   1  7350.7 7414.7
## - MVR_PTS    1  7359.8 7423.8
## - CAR_USE     1  7367.8 7431.8
## - REVOKED    1  7383.8 7447.8
## - CAR_TYPE    5  7398.4 7454.4
## - URBANICITY  1  7936.6 8000.6
##
## Step: AIC=7354.87
## TARGET_FLAG ~ KIDSDRV + HOMEKIDS + INCOME + PARENT1 + HOME_VAL +
##      MSTATUS + EDUCATION + JOB + TRAVTIME + CAR_USE + BLUEBOOK +
##      TIF + CAR_TYPE + OLDCALL + CLM_FREQ + REVOKED + MVR_PTS +
##      URBANICITY
##
##          Df Deviance   AIC
## - HOMEKIDS   1  7292.5 7354.5
## <none>        7290.9 7354.9
## - HOME_VAL   1  7303.1 7365.1
## - PARENT1    1  7303.1 7365.1
## - INCOME      1  7303.8 7365.8
## - OLDCALL    1  7304.3 7366.3
## - EDUCATION   3  7315.3 7373.3
## - BLUEBOOK    1  7313.3 7375.3
## - MSTATUS     1  7326.6 7388.6
## - KIDSDRV     1  7332.5 7394.5
## - CLM_FREQ    1  7337.8 7399.8
## - JOB         8  7352.2 7400.2
## - TIF         1  7350.3 7412.3
## - TRAVTIME   1  7351.2 7413.2
## - MVR_PTS    1  7361.2 7423.2
## - CAR_USE     1  7369.2 7431.2
## - REVOKED    1  7384.7 7446.7
## - CAR_TYPE    5  7399.5 7453.5
## - URBANICITY  1  7936.9 7998.9
##
## Step: AIC=7354.46
## TARGET_FLAG ~ KIDSDRV + INCOME + PARENT1 + HOME_VAL + MSTATUS +
##      EDUCATION + JOB + TRAVTIME + CAR_USE + BLUEBOOK + TIF + CAR_TYPE +
##      OLDCALL + CLM_FREQ + REVOKED + MVR_PTS + URBANICITY
##
##          Df Deviance   AIC
## <none>        7292.5 7354.5
## - INCOME       1  7305.0 7365.0
## - HOME_VAL    1  7305.2 7365.2
## - OLDCALL     1  7306.0 7366.0
## - EDUCATION    3  7317.2 7373.2
## - BLUEBOOK     1  7315.2 7375.2
## - PARENT1      1  7315.3 7375.3
## - MSTATUS      1  7326.8 7386.8
## - CLM_FREQ     1  7339.4 7399.4
## - JOB          8  7355.0 7401.0
## - KIDSDRV     1  7349.8 7409.8

```

```

## - TIF          1  7351.5 7411.5
## - TRAVTIME    1  7352.4 7412.4
## - MVR_PTS     1  7363.2 7423.2
## - CAR_USE      1  7370.5 7430.5
## - REVOKED     1  7387.1 7447.1
## - CAR_TYPE     5  7401.5 7453.5
## - URBANICITY   1  7938.6 7998.6

formula(logist_model2)

## TARGET_FLAG ~ KIDSDRV + INCOME + PARENT1 + HOME_VAL + MSTATUS +
##      EDUCATION + JOB + TRAVTIME + CAR_USE + BLUEBOOK + TIF + CAR_TYPE +
##      OLDCALL + CLM_FREQ + REVOKED + MVR_PTS + URBANICITY

pred_probs <- predict(logist_model2, train_df_imp, type = "response")
pred_class <- ifelse(pred_probs > 0.5, 1, 0)

# Confusion matrix on training data
confusionMatrix(
  factor(pred_class),
  factor(train_df_imp$TARGET_FLAG),
  positive = "1"
)

## Confusion Matrix and Statistics
##
##             Reference
## Prediction    0    1
##           0 5552 1246
##           1  455  902
##
##                 Accuracy : 0.7914
##                 95% CI : (0.7824, 0.8002)
## No Information Rate : 0.7366
## P-Value [Acc > NIR] : < 2.2e-16
##
##                 Kappa : 0.3904
##
## McNemar's Test P-Value : < 2.2e-16
##
##                 Sensitivity : 0.4199
##                 Specificity  : 0.9243
## Pos Pred Value : 0.6647
## Neg Pred Value : 0.8167
## Prevalence    : 0.2634
## Detection Rate : 0.1106
## Detection Prevalence : 0.1664
## Balanced Accuracy : 0.6721
##
## 'Positive' Class : 1
##

```

Logistic Model 3: All Predictors with Transformations

The baseline- logistic model uses all variables except Target amt, as it is defined for claimana and should be used to predict the likelihood someone would crash. This model could be used for predicting crash probability. The coefficient show change in crash probability with each predictor, a positive coefficients means a higher crash probability and a negative coefficient would mean a lower crash probability. MVR_PTS and CLM_FREQ had positive variables as expected.

```
logist_model3 <- glm(
  TARGET_FLAG ~ . - INCOME - HOME_VAL - BLUEBOOK - OLDCLAIM - TRAVTIME,
  data = train_df_imp_log,
  family = binomial
)

summary(logist_model3)

## 
## Call:
## glm(formula = TARGET_FLAG ~ . - INCOME - HOME_VAL - BLUEBOOK -
##     OLDCLAIM - TRAVTIME, family = binomial, data = train_df_imp_log)
## 
## Coefficients:
##                               Estimate Std. Error z value Pr(>|z|)
## (Intercept)                 -1.1558576  0.6723053 -1.719 0.085570 .
## KIDSDRV                      0.4126953  0.0614931  6.711 1.93e-11 ***
## AGE                          -0.0047765  0.0040649 -1.175 0.239970
## HOMEKIDS                     0.0148857  0.0376524  0.395 0.692587
## YOJ                          0.0292065  0.0107289  2.722 0.006484 **
## PARENT1Yes                   0.3724065  0.1098345  3.391 0.000697 ***
## MSTATUSYes                   -0.5013048  0.0878438 -5.707 1.15e-08 ***
## SEXM                         0.1243239  0.1083885  1.147 0.251373
## EDUCATIONHigh School          0.4325627  0.0876530  4.935 8.02e-07 ***
## EDUCATIONMasters              0.0532185  0.1403764  0.379 0.704604
## EDUCATIONPhD                  0.0496531  0.1761907  0.282 0.778086
## JOBBlue Collar                0.3866485  0.1842718  2.098 0.035883 *
## JOBClerical                   0.5101121  0.1937472  2.633 0.008467 **
## JOBDoctor                     -0.3924582  0.2642226 -1.485 0.137456
## JOBHome Maker                 0.0514228  0.2196766  0.234 0.814920
## JOBLawyer                      0.1788500  0.1679545  1.065 0.286934
## JOBManager                    -0.5048479  0.1699760 -2.970 0.002977 **
## JOBProfessional                0.2268496  0.1773153  1.279 0.200771
## JOBStudent                     -0.0836751  0.2254450 -0.371 0.710522
## CAR_USEPrivate                 -0.7692292  0.0877971 -8.761 < 2e-16 ***
## TIF                           -0.0533418  0.0073443 -7.263 3.79e-13 ***
## CAR_TYPEPanel Truck            0.4632667  0.1489124  3.111 0.001865 **
## CAR_TYPEPickup                 0.5895862  0.0999902  5.896 3.71e-09 ***
## CAR_TYPESports Car             1.0387666  0.1282857  8.097 5.62e-16 ***
## CAR_TYPESUV                    0.8136462  0.1078678  7.543 4.59e-14 ***
## CAR_TYPEVan                    0.6062681  0.1247455  4.860 1.17e-06 ***
## RED_CARYes                     -0.0314509  0.0866317 -0.363 0.716574
## CLM_FREQ                       0.0907825  0.0435077  2.087 0.036926 *
## REVOKEDYes                     0.7069977  0.0815059  8.674 < 2e-16 ***
## MVR PTS                        0.1027535  0.0140730  7.301 2.85e-13 ***
## CAR AGE                        -0.0005622  0.0075064 -0.075 0.940295
```

```

## URBANICITYHighly Urban/ Urban  2.3764133  0.1131900  20.995 < 2e-16 ***
## INCOME_LOG                      -0.1097580  0.0178294  -6.156 7.46e-10 ***
## HOME_VAL_LOG                     -0.0272343  0.0069209  -3.935 8.32e-05 ***
## BLUEBOOK_LOG                      -0.2936087  0.0592957  -4.952 7.36e-07 ***
## OLDCLAIM_LOG                      0.0222095  0.0124852   1.779 0.075263 .
## TRAVTIME_LOG                      0.4294576  0.0544868   7.882 3.23e-15 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##     Null deviance: 9404.0  on 8154  degrees of freedom
## Residual deviance: 7271.5  on 8118  degrees of freedom
## AIC: 7345.5
##
## Number of Fisher Scoring iterations: 5

pred_probs <- predict(logist_model3, train_df_imp, type = "response")
pred_class <- ifelse(pred_probs > 0.5, 1, 0)

# Confusion matrix on training data
confusionMatrix(
  factor(pred_class),
  factor(train_df_imp$TARGET_FLAG),
  positive = "1"
)

## Confusion Matrix and Statistics
##
##             Reference
## Prediction    0      1
##           0 5547 1237
##           1  460  911
##
##                 Accuracy : 0.7919
##                 95% CI : (0.7829, 0.8007)
##     No Information Rate : 0.7366
##     P-Value [Acc > NIR] : < 2.2e-16
##
##                 Kappa : 0.3932
##
##     Mcnemar's Test P-Value : < 2.2e-16
##
##                 Sensitivity : 0.4241
##                 Specificity  : 0.9234
##     Pos Pred Value : 0.6645
##     Neg Pred Value : 0.8177
##                 Prevalence : 0.2634
##     Detection Rate  : 0.1117
##     Detection Prevalence : 0.1681
##     Balanced Accuracy : 0.6738
##
##     'Positive' Class : 1
##

```

Logistic Model 4: Reduced Predictors with Transformations

Reduced logistic regression model with transformed variables. This model includes only a subset of variables chosen based on statistical significance and predictive relevance from Model 1. Many continuous predictors are log-transformed to reduce skewness and linearize relationships.

In the model, OLDCLAIM LOG is positively and highly significantly associated with the probability of a crash, indicating that larger prior claims increase risk. CLM FREQ shows a small positive association, but it is not statistically significant, so its effect is uncertain. Demographic and financial factors such as AGE, HOME VAL LOG, and BLUEBOOK LOG are negatively associated with crash probability, suggesting that older and wealthier drivers tend to be safer. Regarding vehicle type, most larger vehicles—such as SUVs, pickups, vans, and panel trucks—are associated with higher crash probability compared to the reference category. Sports cars also have the highest positive coefficient, likely reflecting riskier driving behavior rather than vehicle size alone. Overall, the model indicates that prior claims, driver age, wealth, vehicle use, and type are important predictors of crash likelihood.

```
logist_model4 <- step(logist_model3, direction = "backward")  
  
## Start: AIC=7345.54  
## TARGET_FLAG ~ (KIDSDRV + AGE + HOMEKIDS + YOJ + INCOME + PARENT1 +  
##     HOME_VAL + MSTATUS + SEX + EDUCATION + JOB + TRAVTIME + CAR_USE +  
##     BLUEBOOK + TIF + CAR_TYPE + RED_CAR + OLDCLAIM + CLM_FREQ +  
##     REVOKED + MVR PTS + CAR_AGE + URBANICITY + INCOME_LOG + HOME_VAL_LOG +  
##     BLUEBOOK_LOG + OLDCLAIM_LOG + TRAVTIME_LOG) - INCOME - HOME_VAL -  
##     BLUEBOOK - OLDCLAIM - TRAVTIME  
##  
##          Df Deviance    AIC  
## - CAR_AGE      1   7271.5 7343.5  
## - RED_CAR      1   7271.7 7343.7  
## - HOMEKIDS     1   7271.7 7343.7  
## - SEX          1   7272.9 7344.9  
## - AGE          1   7272.9 7344.9  
## <none>        7271.5 7345.5  
## - OLDCLAIM_LOG 1   7274.7 7346.7  
## - CLM_FREQ     1   7275.9 7347.9  
## - YOJ          1   7279.0 7351.0  
## - PARENT1      1   7283.1 7355.1  
## - HOME_VAL_LOG 1   7287.1 7359.1  
## - EDUCATION     3   7296.1 7364.1  
## - BLUEBOOK_LOG  1   7295.9 7367.9  
## - MSTATUS       1   7303.7 7375.7  
## - INCOME_LOG    1   7309.9 7381.9  
## - KIDSDRV       1   7316.6 7388.6  
## - MVR PTS      1   7325.3 7397.3  
## - TIF          1   7326.2 7398.2  
## - JOB          8   7349.8 7407.8  
## - TRAVTIME_LOG  1   7336.5 7408.5  
## - REVOKED      1   7345.5 7417.5  
## - CAR_USE       1   7349.7 7421.7  
## - CAR_TYPE      5   7365.6 7429.6  
## - URBANICITY    1   7903.3 7975.3  
##  
## Step: AIC=7343.55  
## TARGET_FLAG ~ KIDSDRV + AGE + HOMEKIDS + YOJ + PARENT1 + MSTATUS +
```

```

##      SEX + EDUCATION + JOB + CAR_USE + TIF + CAR_TYPE + RED_CAR +
##      CLM_FREQ + REVOKED + MVR PTS + URBANICITY + INCOME_LOG +
##      HOME_VAL_LOG + BLUEBOOK_LOG + OLDCLAIM_LOG + TRAVTIME_LOG
##
##              Df Deviance    AIC
## - RED_CAR      1  7271.7 7341.7
## - HOMEKIDS     1  7271.7 7341.7
## - SEX          1  7272.9 7342.9
## - AGE          1  7272.9 7342.9
## <none>        7271.5 7343.5
## - OLDCLAIM_LOG 1  7274.7 7344.7
## - CLM_FREQ     1  7275.9 7345.9
## - YOJ          1  7279.0 7349.0
## - PARENT1      1  7283.1 7353.1
## - HOME_VAL_LOG 1  7287.1 7357.1
## - BLUEBOOK_LOG 1  7295.9 7365.9
## - EDUCATION     3  7301.8 7367.8
## - MSTATUS       1  7303.7 7373.7
## - INCOME_LOG    1  7310.0 7380.0
## - KIDSDRV       1  7316.6 7386.6
## - MVR PTS      1  7325.3 7395.3
## - TIF          1  7326.2 7396.2
## - JOB          8   7349.8 7405.8
## - TRAVTIME_LOG 1  7336.6 7406.6
## - REVOKED      1  7345.5 7415.5
## - CAR_USE       1  7349.8 7419.8
## - CAR_TYPE      5   7365.7 7427.7
## - URBANICITY    1  7903.4 7973.4
##
## Step: AIC=7341.68
## TARGET_FLAG ~ KIDSDRV + AGE + HOMEKIDS + YOJ + PARENT1 + MSTATUS +
##      SEX + EDUCATION + JOB + CAR_USE + TIF + CAR_TYPE + CLM_FREQ +
##      REVOKED + MVR PTS + URBANICITY + INCOME_LOG + HOME_VAL_LOG +
##      BLUEBOOK_LOG + OLDCLAIM_LOG + TRAVTIME_LOG
##
##              Df Deviance    AIC
## - HOMEKIDS     1  7271.8 7339.8
## - SEX          1  7272.9 7340.9
## - AGE          1  7273.0 7341.0
## <none>        7271.7 7341.7
## - OLDCLAIM_LOG 1  7274.9 7342.9
## - CLM_FREQ     1  7276.0 7344.0
## - YOJ          1  7279.1 7347.1
## - PARENT1      1  7283.3 7351.3
## - HOME_VAL_LOG 1  7287.2 7355.2
## - BLUEBOOK_LOG 1  7295.9 7363.9
## - EDUCATION     3  7302.0 7366.0
## - MSTATUS       1  7303.8 7371.8
## - INCOME_LOG    1  7310.0 7378.0
## - KIDSDRV       1  7316.9 7384.9
## - MVR PTS      1  7325.4 7393.4
## - TIF          1  7326.3 7394.3
## - JOB          8   7350.1 7404.1
## - TRAVTIME_LOG 1  7336.7 7404.7

```

```

## - REVOKED      1  7345.7 7413.7
## - CAR_USE       1  7350.0 7418.0
## - CAR_TYPE       5  7366.0 7426.0
## - URBANICITY     1  7903.4 7971.4
##
## Step: AIC=7339.83
## TARGET_FLAG ~ KIDSDRV + AGE + YOJ + PARENT1 + MSTATUS + SEX +
##   EDUCATION + JOB + CAR_USE + TIF + CAR_TYPE + CLM_FREQ + REVOKED +
##   MVR PTS + URBANICITY + INCOME_LOG + HOME_VAL_LOG + BLUEBOOK_LOG +
##   OLDCLAIM_LOG + TRAVTIME_LOG
##
##             Df Deviance    AIC
## - SEX          1  7273.0 7339.0
## <none>           7271.8 7339.8
## - AGE          1  7273.9 7339.9
## - OLDCLAIM_LOG 1  7275.0 7341.0
## - CLM_FREQ      1  7276.1 7342.1
## - YOJ          1  7280.4 7346.4
## - PARENT1      1  7287.2 7353.2
## - HOME_VAL_LOG 1  7287.4 7353.4
## - BLUEBOOK_LOG 1  7296.1 7362.1
## - EDUCATION     3  7302.2 7364.2
## - MSTATUS        1  7304.5 7370.5
## - INCOME_LOG     1  7311.6 7377.6
## - MVR PTS       1  7325.5 7391.5
## - TIF          1  7326.4 7392.4
## - KIDSDRV        1  7330.0 7396.0
## - JOB           8  7350.3 7402.3
## - TRAVTIME_LOG   1  7336.7 7402.7
## - REVOKED       1  7346.0 7412.0
## - CAR_USE        1  7350.1 7416.1
## - CAR_TYPE       5  7366.4 7424.4
## - URBANICITY     1  7903.5 7969.5
##
## Step: AIC=7339.04
## TARGET_FLAG ~ KIDSDRV + AGE + YOJ + PARENT1 + MSTATUS + EDUCATION +
##   JOB + CAR_USE + TIF + CAR_TYPE + CLM_FREQ + REVOKED + MVR PTS +
##   URBANICITY + INCOME_LOG + HOME_VAL_LOG + BLUEBOOK_LOG + OLDCLAIM_LOG +
##   TRAVTIME_LOG
##
##             Df Deviance    AIC
## - AGE          1  7274.8 7338.8
## <none>           7273.0 7339.0
## - OLDCLAIM_LOG 1  7276.2 7340.2
## - CLM_FREQ      1  7277.4 7341.4
## - YOJ          1  7281.6 7345.6
## - PARENT1      1  7288.2 7352.2
## - HOME_VAL_LOG 1  7288.4 7352.4
## - EDUCATION     3  7303.5 7363.5
## - BLUEBOOK_LOG 1  7305.3 7369.3
## - MSTATUS        1  7305.9 7369.9
## - INCOME_LOG     1  7312.9 7376.9
## - MVR PTS       1  7326.6 7390.6
## - TIF          1  7327.5 7391.5

```

```

## - KIDSDRV      1  7330.8 7394.8
## - JOB          8  7351.4 7401.4
## - TRAVTIME_LOG 1  7338.1 7402.1
## - REVOKED      1  7347.5 7411.5
## - CAR_USE       1  7351.0 7415.0
## - CAR_TYPE      5  7383.1 7439.1
## - URBANICITY    1  7905.0 7969.0
##
## Step: AIC=7338.76
## TARGET_FLAG ~ KIDSDRV + YOJ + PARENT1 + MSTATUS + EDUCATION +
##   JOB + CAR_USE + TIF + CAR_TYPE + CLM_FREQ + REVOKED + MVR PTS +
##   URBANICITY + INCOME_LOG + HOME_VAL_LOG + BLUEBOOK_LOG + OLDCLAIM_LOG +
##   TRAVTIME_LOG
##
##             Df Deviance     AIC
## <none>            7274.8 7338.8
## - OLDCLAIM_LOG  1  7278.0 7340.0
## - CLM_FREQ       1  7279.0 7341.0
## - YOJ            1  7282.4 7344.4
## - HOME_VAL_LOG   1  7290.6 7352.6
## - PARENT1        1  7295.3 7357.3
## - EDUCATION       3  7305.6 7363.6
## - MSTATUS         1  7306.6 7368.6
## - BLUEBOOK_LOG   1  7309.0 7371.0
## - INCOME_LOG      1  7313.5 7375.5
## - TIF             1  7329.0 7391.0
## - MVR PTS         1  7329.2 7391.2
## - KIDSDRV         1  7332.2 7394.2
## - TRAVTIME_LOG    1  7339.3 7401.3
## - JOB             8  7354.8 7402.8
## - REVOKED         1  7349.6 7411.6
## - CAR_USE          1  7352.3 7414.3
## - CAR_TYPE         5  7383.8 7437.8
## - URBANICITY       1  7908.6 7970.6

formula(logist_model4)

## TARGET_FLAG ~ KIDSDRV + YOJ + PARENT1 + MSTATUS + EDUCATION +
##   JOB + CAR_USE + TIF + CAR_TYPE + CLM_FREQ + REVOKED + MVR PTS +
##   URBANICITY + INCOME_LOG + HOME_VAL_LOG + BLUEBOOK_LOG + OLDCLAIM_LOG +
##   TRAVTIME_LOG

summary(logist_model4)

##
## Call:
## glm(formula = TARGET_FLAG ~ KIDSDRV + YOJ + PARENT1 + MSTATUS +
##   EDUCATION + JOB + CAR_USE + TIF + CAR_TYPE + CLM_FREQ + REVOKED +
##   MVR PTS + URBANICITY + INCOME_LOG + HOME_VAL_LOG + BLUEBOOK_LOG +
##   OLDCLAIM_LOG + TRAVTIME_LOG, family = binomial, data = train_df_imp_log)
##
## Coefficients:
##                                         Estimate Std. Error z value Pr(>|z|)

```

```

## (Intercept) -1.024284 0.607345 -1.686 0.091701 .
## KIDSDRV 0.420756 0.055264 7.614 2.67e-14 ***
## YOJ 0.028332 0.010262 2.761 0.005768 **
## PARENT1Yes 0.430005 0.094935 4.529 5.91e-06 ***
## MSTATUSYes -0.484854 0.085329 -5.682 1.33e-08 ***
## EDUCATIONHigh School 0.437975 0.080283 5.455 4.89e-08 ***
## EDUCATIONMasters 0.043986 0.134407 0.327 0.743470
## EDUCATIONPhD 0.025534 0.171478 0.149 0.881630
## JOBBlue Collar 0.389370 0.184185 2.114 0.034514 *
## JOBClerical 0.518526 0.193583 2.679 0.007394 **
## JOBDoctor -0.398345 0.263824 -1.510 0.131073
## JOBHome Maker 0.031617 0.218758 0.145 0.885081
## JOBLawyer 0.165509 0.167695 0.987 0.323660
## JOBManager -0.514913 0.169772 -3.033 0.002422 **
## JOBProfessional 0.218896 0.177198 1.235 0.216711
## JOBStudent -0.072148 0.225065 -0.321 0.748540
## CAR_USEPrivate -0.764788 0.087658 -8.725 < 2e-16 ***
## TIF -0.053147 0.007341 -7.240 4.50e-13 ***
## CAR_TYPEPanel Truck 0.511876 0.142608 3.589 0.000331 ***
## CAR_TYPEPickup 0.588641 0.099871 5.894 3.77e-09 ***
## CAR_TYPESports Car 0.957686 0.108213 8.850 < 2e-16 ***
## CAR_TYPE SUV 0.741755 0.085908 8.634 < 2e-16 ***
## CAR_TYPEVan 0.639808 0.121348 5.273 1.35e-07 ***
## CLM_FREQ 0.089786 0.043487 2.065 0.038955 *
## REVOKEDYes 0.710936 0.081472 8.726 < 2e-16 ***
## MVR PTS 0.103327 0.014058 7.350 1.98e-13 ***
## URBANICITYHighly Urban/ Urban 2.380316 0.113242 21.020 < 2e-16 ***
## INCOME_LOG -0.108636 0.017575 -6.181 6.36e-10 ***
## HOME_VAL_LOG -0.027417 0.006915 -3.965 7.34e-05 ***
## BLUEBOOK_LOG -0.323606 0.055087 -5.874 4.24e-09 ***
## OLDCLAIM_LOG 0.022491 0.012480 1.802 0.071519 .
## TRAVTIME_LOG 0.427533 0.054439 7.853 4.05e-15 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
## Null deviance: 9404.0 on 8154 degrees of freedom
## Residual deviance: 7274.8 on 8123 degrees of freedom
## AIC: 7338.8
##
## Number of Fisher Scoring iterations: 5

pred_probs <- predict(logist_model4, train_df_imp, type = "response")
pred_class <- ifelse(pred_probs > 0.5, 1, 0)

# Confusion matrix on training data
confusionMatrix(
  factor(pred_class),
  factor(train_df_imp$TARGET_FLAG),
  positive = "1"
)

## Confusion Matrix and Statistics

```

```

##          Reference
## Prediction 0 1
##          0 5550 1243
##          1 457 905
##
##          Accuracy : 0.7915
##          95% CI : (0.7826, 0.8003)
##          No Information Rate : 0.7366
##          P-Value [Acc > NIR] : < 2.2e-16
##
##          Kappa : 0.3912
##
## McNemar's Test P-Value : < 2.2e-16
##
##          Sensitivity : 0.4213
##          Specificity : 0.9239
##          Pos Pred Value : 0.6645
##          Neg Pred Value : 0.8170
##          Prevalence : 0.2634
##          Detection Rate : 0.1110
##          Detection Prevalence : 0.1670
##          Balanced Accuracy : 0.6726
##
##          'Positive' Class : 1
##

```

Linear Model 1: All Predictors Without Transformed

To make predictions on claim amount, this model would be the baseline.

```
# Removing TARGET_FLAG from training and testing data for linear modeling of TARGET_AMT
```

```
train_df_imp_lin <- subset(train_df_imp, select = -TARGET_FLAG)
test_df_lin <- subset(test_df, select = -TARGET_FLAG)
```

```
linear_model1 <- lm(TARGET_AMT ~ . - INCOME_LOG - HOME_VAL_LOG - BLUEBOOK_LOG - OLDCLAIM_LOG - TRAVTIME_LOG)
```

```
summary(linear_model1)
```

```
##
## Call:
## lm(formula = TARGET_AMT ~ . - INCOME_LOG - HOME_VAL_LOG - BLUEBOOK_LOG -
##     OLDCLAIM_LOG - TRAVTIME_LOG, data = train_df_imp_lin)
##
## Residuals:
##      Min      1Q Median      3Q      Max
## -5817   -1701    -767    351  103812
##
## Coefficients:
##             Estimate Std. Error t value Pr(>|t|)    
## (Intercept) -6.082e+02  5.640e+02 -1.078 0.280881  
## KIDSDRV      3.160e+02  1.133e+02   2.790 0.005282 **
```

```

## AGE          4.966e+00  7.089e+00  0.700  0.483637
## HOMEKIDS    7.772e+01  6.553e+01  1.186  0.235681
## YOJ         -3.455e+00  1.489e+01  -0.232  0.816450
## INCOME      -5.407e-03  1.897e-03  -2.851  0.004369 **
## PARENT1Yes   5.719e+02  2.023e+02  2.827  0.004706 **
## HOME_VAL     -5.628e-04  6.066e-04  -0.928  0.353516
## MSTATUSYes   -5.701e+02  1.481e+02  -3.849  0.000120 ***
## SEXM         3.719e+02  1.840e+02  2.021  0.043281 *
## EDUCATIONHigh School 1.779e+02  1.549e+02  1.148  0.250877
## EDUCATIONMasters 2.901e+02  2.242e+02  1.294  0.195783
## EDUCATIONPhD  6.117e+02  2.915e+02  2.099  0.035878 *
## JOBBlue Collar 4.971e+02  3.212e+02  1.547  0.121782
## JOBCLerical   4.859e+02  3.421e+02  1.420  0.155591
## JOBDoctor     -5.329e+02  4.083e+02  -1.305  0.191808
## JOBHome Maker 2.523e+02  3.669e+02  0.688  0.491632
## JOBLawyer     2.049e+02  2.949e+02  0.695  0.487205
## JOBManager    -5.001e+02  2.880e+02  -1.736  0.082559 .
## JOBProfessional 4.309e+02  3.084e+02  1.397  0.162436
## JOBStudent    2.106e+02  3.761e+02  0.560  0.575560
## TRAVTIME      1.197e+01  3.223e+00  3.713  0.000207 ***
## CAR_USEPrivate -7.603e+02  1.578e+02  -4.819  1.47e-06 ***
## BLUEBOOK      1.561e-02  8.647e-03  1.806  0.071014 .
## TIF           -4.825e+01  1.219e+01  -3.959  7.59e-05 ***
## CAR_TYPEPanel Truck 2.829e+02  2.761e+02  1.025  0.305495
## CAR_TYPEPickup 3.864e+02  1.697e+02  2.278  0.022763 *
## CAR_TYPESports Car 1.020e+03  2.179e+02  4.681  2.90e-06 ***
## CAR_TYPESUV   7.502e+02  1.794e+02  4.182  2.92e-05 ***
## CAR_TYPEVan   5.233e+02  2.125e+02  2.462  0.013818 *
## RED_CARyes   -5.254e+01  1.495e+02  -0.351  0.725226
## OLDCLAIM     -1.060e-02  7.438e-03  -1.424  0.154355
## CLM_FREQ      1.394e+02  5.510e+01  2.530  0.011426 *
## REVOKEDYes   5.493e+02  1.736e+02  3.165  0.001557 **
## MVR_PTS       1.748e+02  2.594e+01  6.739  1.70e-11 ***
## CAR_AGE        -2.389e+01  1.273e+01  -1.877  0.060549 .
## URBANICITYHighly Urban/ Urban 1.662e+03  1.395e+02  11.919 < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 4545 on 8118 degrees of freedom
## Multiple R-squared:  0.07117,   Adjusted R-squared:  0.06706
## F-statistic: 17.28 on 36 and 8118 DF,  p-value: < 2.2e-16

```

Linear Model 2: Reduced Predictors Without Transformed

```

linear_model2<- step(linear_model1, direction = "backward")

## Start:  AIC=137394.9
## TARGET_AMT ~ (KIDSDRIV + AGE + HOMEKIDS + YOJ + INCOME + PARENT1 +
##                HOME_VAL + MSTATUS + SEX + EDUCATION + JOB + TRAVTIME + CAR_USE +
##                BLUEBOOK + TIF + CAR_TYPE + RED_CAR + OLDCLAIM + CLM_FREQ +
##                REVOKED + MVR_PTS + CAR_AGE + URBANICITY + INCOME_LOG + HOME_VAL_LOG +
##                BLUEBOOK_LOG + OLDCLAIM_LOG + TRAVTIME_LOG) - INCOME_LOG -

```

```

##      HOME_VAL_LOG - BLUEBOOK_LOG - OLDCLAIM_LOG - TRAVTIME_LOG
##
##          Df  Sum of Sq      RSS      AIC
## - YOJ      1  1112829 1.6767e+11 137393
## - RED_CAR   1  2551742 1.6767e+11 137393
## - AGE       1 10134704 1.6768e+11 137393
## - HOME_VAL   1 17780701 1.6768e+11 137394
## - HOMEKIDS   1 29048453 1.6770e+11 137394
## - EDUCATION   3 116858515 1.6778e+11 137395
## <none>           1.6767e+11 137395
## - OLDCLAIM   1 41907585 1.6771e+11 137395
## - BLUEBOOK   1 67337122 1.6773e+11 137396
## - CAR_AGE     1 72768597 1.6774e+11 137396
## - SEX         1 84384775 1.6775e+11 137397
## - CLM_FREQ    1 132199902 1.6780e+11 137399
## - KIDSDRIV    1 160778001 1.6783e+11 137401
## - PARENT1     1 165098600 1.6783e+11 137401
## - INCOME      1 167882584 1.6783e+11 137401
## - REVOKED     1 206871090 1.6787e+11 137403
## - TRAVTIME     1 284669259 1.6795e+11 137407
## - MSTATUS      1 305920949 1.6797e+11 137408
## - TIF          1 323724741 1.6799e+11 137409
## - JOB          8 635092840 1.6830e+11 137410
## - CAR_TYPE     5 607765851 1.6827e+11 137414
## - CAR_USE       1 479609362 1.6815e+11 137416
## - MVR PTS      1 937963469 1.6861e+11 137438
## - URBANICITY   1 2934277503 1.7060e+11 137534
##
## Step: AIC=137393
## TARGET_AMT ~ KIDSDRIV + AGE + HOMEKIDS + INCOME + PARENT1 + HOME_VAL +
##             MSTATUS + SEX + EDUCATION + JOB + TRAVTIME + CAR_USE + BLUEBOOK +
##             TIF + CAR_TYPE + RED_CAR + OLDCLAIM + CLM_FREQ + REVOKED +
##             MVR PTS + CAR_AGE + URBANICITY
##
##          Df  Sum of Sq      RSS      AIC
## - RED_CAR     1  2583649 1.6767e+11 137391
## - AGE         1  9246605 1.6768e+11 137391
## - HOME_VAL    1 17732411 1.6769e+11 137392
## - HOMEKIDS    1 27939582 1.6770e+11 137392
## - EDUCATION    3 117385626 1.6779e+11 137393
## <none>           1.6767e+11 137393
## - OLDCLAIM    1 42175316 1.6771e+11 137393
## - BLUEBOOK    1 67197994 1.6774e+11 137394
## - CAR_AGE      1 72668804 1.6774e+11 137394
## - SEX          1 84491243 1.6775e+11 137395
## - CLM_FREQ     1 132504760 1.6780e+11 137397
## - KIDSDRIV    1 162755347 1.6783e+11 137399
## - PARENT1     1 165441550 1.6783e+11 137399
## - INCOME      1 171214430 1.6784e+11 137399
## - REVOKED     1 207222948 1.6788e+11 137401
## - TRAVTIME     1 284272996 1.6795e+11 137405
## - MSTATUS      1 312435644 1.6798e+11 137406
## - TIF          1 324212833 1.6799e+11 137407
## - JOB          8 635159796 1.6830e+11 137408

```

```

## - CAR_TYPE      5  609771449 1.6828e+11 137413
## - CAR_USE       1  481219501 1.6815e+11 137414
## - MVR PTS      1  939631112 1.6861e+11 137437
## - URBANICITY    1  2933248642 1.7060e+11 137532
##
## Step: AIC=137391.1
## TARGET_AMT ~ KIDSDRV + AGE + HOMEKIDS + INCOME + PARENT1 + HOME_VAL +
##             MSTATUS + SEX + EDUCATION + JOB + TRAVTIME + CAR_USE + BLUEBOOK +
##             TIF + CAR_TYPE + OLDCLAIM + CLM_FREQ + REVOKED + MVR PTS +
##             CAR_AGE + URBANICITY
##
##              Df  Sum of Sq      RSS     AIC
## - AGE           1   9432621 1.6768e+11 137390
## - HOME_VAL      1   17243154 1.6769e+11 137390
## - HOMEKIDS      1   27817519 1.6770e+11 137390
## - EDUCATION     3   117858154 1.6779e+11 137391
## <none>          1   1.6767e+11 137391
## - OLDCLAIM      1   42307629 1.6771e+11 137391
## - BLUEBOOK      1   67967365 1.6774e+11 137392
## - CAR_AGE        1   73040376 1.6774e+11 137393
## - SEX            1   91511213 1.6776e+11 137394
## - CLM_FREQ       1   132172012 1.6780e+11 137396
## - KIDSDRV        1   163544918 1.6783e+11 137397
## - PARENT1        1   165875106 1.6784e+11 137397
## - INCOME         1   171800351 1.6784e+11 137397
## - REVOKED        1   207303164 1.6788e+11 137399
## - TRAVTIME       1   283655873 1.6795e+11 137403
## - MSTATUS         1   312660009 1.6798e+11 137404
## - TIF             1   323843383 1.6799e+11 137405
## - JOB             8   636677616 1.6831e+11 137406
## - CAR_TYPE        5   611689334 1.6828e+11 137411
## - CAR_USE         1   480965539 1.6815e+11 137412
## - MVR PTS         1   939514216 1.6861e+11 137435
## - URBANICITY      1   2931769825 1.7060e+11 137530
##
## Step: AIC=137389.5
## TARGET_AMT ~ KIDSDRV + HOMEKIDS + INCOME + PARENT1 + HOME_VAL +
##             MSTATUS + SEX + EDUCATION + JOB + TRAVTIME + CAR_USE + BLUEBOOK +
##             TIF + CAR_TYPE + OLDCLAIM + CLM_FREQ + REVOKED + MVR PTS +
##             CAR_AGE + URBANICITY
##
##              Df  Sum of Sq      RSS     AIC
## - HOME_VAL       1   15430964 1.6770e+11 137388
## - HOMEKIDS       1   20091357 1.6770e+11 137389
## - EDUCATION      3   121203600 1.6780e+11 137389
## <none>           1   1.6768e+11 137390
## - OLDCLAIM        1   42187435 1.6772e+11 137390
## - CAR_AGE         1   72799224 1.6775e+11 137391
## - BLUEBOOK        1   76871033 1.6776e+11 137391
## - SEX             1   99265586 1.6778e+11 137392
## - CLM_FREQ        1   133388848 1.6781e+11 137394
## - PARENT1         1   159916441 1.6784e+11 137395
## - INCOME          1   176719999 1.6786e+11 137396
## - KIDSDRV         1   181442153 1.6786e+11 137396

```

```

## - REVOKED      1  206197630 1.6789e+11 137398
## - TRAVTIME     1  284883156 1.6797e+11 137401
## - MSTATUS      1  311954623 1.6799e+11 137403
## - TIF          1  323108458 1.6800e+11 137403
## - JOB          8   631398802 1.6831e+11 137404
## - CAR_TYPE      5   629558850 1.6831e+11 137410
## - CAR_USE       1   482469176 1.6816e+11 137411
## - MVR_PTS       1   933474247 1.6861e+11 137433
## - URBANICITY    1  2926209016 1.7061e+11 137529
##
## Step: AIC=137388.3
## TARGET_AMT ~ KIDSDRV + HOMEKIDS + INCOME + PARENT1 + MSTATUS +
##             SEX + EDUCATION + JOB + TRAVTIME + CAR_USE + BLUEBOOK + TIF +
##             CAR_TYPE + OLDCLAIM + CLM_FREQ + REVOKED + MVR_PTS + CAR_AGE +
##             URBANICITY
##
##              Df  Sum of Sq      RSS      AIC
## - HOMEKIDS      1   22289847 1.6772e+11 137387
## <none>                  1.6770e+11 137388
## - EDUCATION     3   123896326 1.6782e+11 137388
## - OLDCLAIM      1   42025960 1.6774e+11 137388
## - CAR_AGE       1   70509464 1.6777e+11 137390
## - BLUEBOOK      1   76665722 1.6777e+11 137390
## - SEX           1   97804438 1.6779e+11 137391
## - CLM_FREQ      1   136571590 1.6783e+11 137393
## - PARENT1       1   154935616 1.6785e+11 137394
## - KIDSDRV       1   181200540 1.6788e+11 137395
## - REVOKED       1   208207491 1.6790e+11 137396
## - TRAVTIME      1   286690985 1.6798e+11 137400
## - INCOME        1   296728586 1.6799e+11 137401
## - TIF           1   323387309 1.6802e+11 137402
## - JOB           8   623642849 1.6832e+11 137403
## - CAR_TYPE      5   626421056 1.6832e+11 137409
## - CAR_USE       1   482234372 1.6818e+11 137410
## - MSTATUS        1   548908441 1.6824e+11 137413
## - MVR_PTS       1   936347461 1.6863e+11 137432
## - URBANICITY    1  2925421152 1.7062e+11 137527
##
## Step: AIC=137387.4
## TARGET_AMT ~ KIDSDRV + INCOME + PARENT1 + MSTATUS + SEX + EDUCATION +
##             JOB + TRAVTIME + CAR_USE + BLUEBOOK + TIF + CAR_TYPE + OLDCLAIM +
##             CLM_FREQ + REVOKED + MVR_PTS + CAR_AGE + URBANICITY
##
##              Df  Sum of Sq      RSS      AIC
## - EDUCATION     3   122723668 1.6784e+11 137387
## <none>                  1.6772e+11 137387
## - OLDCLAIM      1   41734993 1.6776e+11 137387
## - CAR_AGE       1   71509300 1.6779e+11 137389
## - BLUEBOOK      1   73274972 1.6779e+11 137389
## - SEX           1   92981999 1.6781e+11 137390
## - CLM_FREQ      1   136657162 1.6785e+11 137392
## - REVOKED       1   210218593 1.6793e+11 137396
## - PARENT1       1   278222687 1.6800e+11 137399
## - KIDSDRV       1   281565317 1.6800e+11 137399

```

```

## - TRAVTIME      1  284231927 1.6800e+11 137399
## - INCOME        1  293171568 1.6801e+11 137400
## - TIF           1  320101852 1.6804e+11 137401
## - JOB           8   631327071 1.6835e+11 137402
## - CAR_TYPE       5   625999868 1.6834e+11 137408
## - CAR_USE        1   479341033 1.6820e+11 137409
## - MSTATUS        1   530362886 1.6825e+11 137411
## - MVR_PTS        1   940827635 1.6866e+11 137431
## - URBANICITY     1  2926016969 1.7064e+11 137526
##
## Step: AIC=137387.3
## TARGET_AMT ~ KIDSDRV + INCOME + PARENT1 + MSTATUS + SEX + JOB +
##             TRAVTIME + CAR_USE + BLUEBOOK + TIF + CAR_TYPE + OLDCALLM +
##             CLM_FREQ + REVOKED + MVR_PTS + CAR_AGE + URBANICITY
##
##              Df  Sum of Sq      RSS      AIC
## <none>                   1.6784e+11 137387
## - OLDCALLM      1   41654117 1.6788e+11 137387
## - BLUEBOOK       1   71628045 1.6791e+11 137389
## - SEX            1   87070026 1.6793e+11 137390
## - CAR_AGE        1   90325552 1.6793e+11 137390
## - CLM_FREQ        1  137391230 1.6798e+11 137392
## - REVOKED        1   212478648 1.6805e+11 137396
## - INCOME          1   270824651 1.6811e+11 137398
## - PARENT1         1   271187980 1.6811e+11 137399
## - TRAVTIME        1   276704526 1.6812e+11 137399
## - KIDSDRV         1   282924792 1.6812e+11 137399
## - TIF             1   314920711 1.6816e+11 137401
## - JOB             8   621015876 1.6846e+11 137401
## - CAR_USE          1   454348561 1.6829e+11 137407
## - CAR_TYPE         5   629496006 1.6847e+11 137408
## - MSTATUS          1   528346071 1.6837e+11 137411
## - MVR_PTS          1   944263934 1.6878e+11 137431
## - URBANICITY       1  2920994033 1.7076e+11 137526

```

```
summary(linear_model2)
```

```

##
## Call:
## lm(formula = TARGET_AMT ~ KIDSDRV + INCOME + PARENT1 + MSTATUS +
##      SEX + JOB + TRAVTIME + CAR_USE + BLUEBOOK + TIF + CAR_TYPE +
##      OLDCALLM + CLM_FREQ + REVOKED + MVR_PTS + CAR_AGE + URBANICITY,
##      data = train_df_imp_lin)
##
## Residuals:
##    Min      1Q  Median      3Q     Max
## -5804   -1693   -763    333  103735
##
## Coefficients:
##                               Estimate Std. Error t value Pr(>|t|)
## (Intercept)                -8.933e+01  4.459e+02 -0.200 0.841209
## KIDSDRV                     3.780e+02  1.021e+02  3.701 0.000216 ***
## INCOME                      -5.698e-03  1.573e-03 -3.621 0.000295 ***
## PARENT1Yes                  6.411e+02  1.769e+02  3.623 0.000292 ***

```

```

## MSTATUSYes          -6.038e+02  1.194e+02 -5.058 4.34e-07 ***
## SEXM               3.303e+02  1.609e+02  2.053 0.040088 *
## JOBBBlue Collar   2.505e+02  2.710e+02  0.924 0.355299
## JOBClerical        2.751e+02  2.982e+02  0.923 0.356253
## JOBDoctor          -3.415e+02  3.768e+02 -0.906 0.364787
## JOBHome Maker     1.016e+02  3.392e+02  0.299 0.764650
## JOBLawyer          1.147e+02  2.876e+02  0.399 0.690025
## JOBManager         -7.109e+02  2.683e+02 -2.649 0.008081 **
## JOBProfessional    1.166e+02  2.688e+02  0.434 0.664480
## JOBStudent         7.334e+01  3.312e+02  0.221 0.824733
## TRAVTIME           1.179e+01  3.221e+00  3.660 0.000254 ***
## CAR_USEPrivate     -7.362e+02  1.570e+02 -4.690 2.77e-06 ***
## BLUEBOOK            1.592e-02  8.547e-03  1.862 0.062608 .
## TIF                -4.755e+01  1.218e+01 -3.905 9.51e-05 ***
## CAR_TYPEPanel Truck 3.049e+02  2.750e+02  1.108 0.267703
## CAR_TYPEPickup     4.033e+02  1.694e+02  2.381 0.017305 *
## CAR_TYPESports Car 1.034e+03  2.164e+02  4.778 1.80e-06 ***
## CAR_TYPESUV         7.565e+02  1.785e+02  4.239 2.27e-05 ***
## CAR_TYPEVan         5.318e+02  2.122e+02  2.506 0.012239 *
## OLDCLAIM            -1.056e-02 7.435e-03 -1.420 0.155617
## CLM_FREQ            1.420e+02  5.506e+01  2.579 0.009923 **
## REVOKEDYes          5.564e+02  1.735e+02  3.207 0.001345 **
## MVR PTS             1.752e+02  2.590e+01  6.761 1.46e-11 ***
## CAR AGE              -2.311e+01 1.105e+01 -2.091 0.036541 *
## URBANICITYHighly Urban/ Urban 1.658e+03  1.394e+02  11.892 < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 4545 on 8126 degrees of freedom
## Multiple R-squared:  0.07021,    Adjusted R-squared:  0.06701
## F-statistic: 21.92 on 28 and 8126 DF,  p-value: < 2.2e-16

```

```
formula(linear_model2)
```

```

## TARGET_AMT ~ KIDSDRV + INCOME + PARENT1 + MSTATUS + SEX + JOB +
##      TRAVTIME + CAR_USE + BLUEBOOK + TIF + CAR_TYPE + OLDCLAIM +
##      CLM_FREQ + REVOKED + MVR PTS + CAR AGE + URBANICITY

```

Linear Model 3: All Predictors With Transformed

For comparsion with models that have non tranformed variables

```

linear_model3 <- lm(TARGET_AMT ~ . - INCOME - HOME_VAL - BLUEBOOK - OLDCLAIM - TRAVTIME, data = train_df)

summary(linear_model3)

```

```

##
## Call:
## lm(formula = TARGET_AMT ~ . - INCOME - HOME_VAL - BLUEBOOK -
##      OLDCLAIM - TRAVTIME, data = train_df_imp_lin)
##
## Residuals:

```

```

##      Min     1Q Median     3Q    Max
## -5489 -1687   -769    354 104037
##
## Coefficients:
##                               Estimate Std. Error t value Pr(>|t|)
## (Intercept)             -2295.993   1165.409 -1.970 0.048859 *
## KIDSDRV                  327.894    113.370   2.892 0.003835 **
## AGE                      3.019     7.112   0.425 0.671193
## HOMEKIDS                 53.903    66.165   0.815 0.415275
## YOJ                      22.774    18.293   1.245 0.213184
## PARENT1Yes                578.177   201.936   2.863 0.004205 **
## MSTATUSYes               -553.242   151.997  -3.640 0.000275 ***
## SEXM                      376.046   179.431   2.096 0.036134 *
## EDUCATIONHigh School       237.207   153.304   1.547 0.121831
## EDUCATIONMasters           238.780   224.016   1.066 0.286498
## EDUCATIONPhD                375.478   281.682   1.333 0.182574
## JOBBlue Collar              595.661   319.693   1.863 0.062466 .
## JOBCLerical                  660.500   336.428   1.963 0.049649 *
## JOBDoctor                   -508.220   408.302  -1.245 0.213272
## JOBHome Maker                291.881   372.939   0.783 0.433855
## JOBLawyer                     267.343   294.391   0.908 0.363841
## JOBManager                   -449.145   287.699  -1.561 0.118524
## JOBProfessional                502.263   307.661   1.633 0.102608
## JOBStudent                     132.249   393.723   0.336 0.736959
## CAR_USEPrivate                -756.953   157.833  -4.796 1.65e-06 ***
## TIF                         -47.111    12.190  -3.865 0.000112 ***
## CAR_TYPEPanel Truck            297.467   260.603   1.141 0.253713
## CAR_TYPEPickup                 402.999   169.365   2.379 0.017361 *
## CAR_TYPESports Car             1020.824   216.043   4.725 2.34e-06 ***
## CAR_TYPESUV                    751.632   174.245   4.314 1.62e-05 ***
## CAR_TYPEVan                     503.726   211.540   2.381 0.017278 *
## RED_CARyes                     -58.047   149.476  -0.388 0.697775
## CLM_FREQ                        67.217    85.752   0.784 0.433144
## REVOKEDYes                      424.791   156.756   2.710 0.006745 **
## MVR PTS                          169.384   26.678   6.349 2.28e-10 ***
## CAR_AGE                           -23.956   12.726  -1.882 0.059808 .
## URBANICITYHighly Urban/ Urban    1636.301   139.949  11.692 < 2e-16 ***
## INCOME_LOG                       -89.452    30.947  -2.890 0.003857 **
## HOME_VAL_LOG                      -16.205   12.609  -1.285 0.198768
## BLUEBOOK_LOG                      163.858   103.035   1.590 0.111806
## OLDCLAIM_LOG                      13.723    24.147   0.568 0.569837
## TRAVTIME_LOG                      335.287   89.168   3.760 0.000171 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 4546 on 8118 degrees of freedom
## Multiple R-squared:  0.07061,    Adjusted R-squared:  0.06649
## F-statistic: 17.13 on 36 and 8118 DF,  p-value: < 2.2e-16

```

Linear Model 4: Reduced Predictors With Transformed

```

linear_model4 <- step(linear_model3, direction = "backward")

## Start: AIC=137399.8
## TARGET_AMT ~ (KIDSDRV + AGE + HOMEKIDS + YOJ + INCOME + PARENT1 +
##               HOME_VAL + MSTATUS + SEX + EDUCATION + JOB + TRAVTIME + CAR_USE +
##               BLUEBOOK + TIF + CAR_TYPE + RED_CAR + OLDCALL + CLM_FREQ +
##               REVOKED + MVR_PTS + CAR_AGE + URBANICITY + INCOME_LOG + HOME_VAL_LOG +
##               BLUEBOOK_LOG + OLDCALL_LOG + TRAVTIME_LOG) - INCOME - HOME_VAL -
##               BLUEBOOK - OLDCALL - TRAVTIME
##
##          Df  Sum of Sq    RSS    AIC
## - EDUCATION   3  83764537 1.6785e+11 137398
## - RED_CAR     1   3116619 1.6777e+11 137398
## - AGE         1   3724528 1.6777e+11 137398
## - OLDCALL_LOG 1   6674831 1.6778e+11 137398
## - CLM_FREQ    1   12698169 1.6778e+11 137398
## - HOMEKIDS    1   13716509 1.6778e+11 137399
## - YOJ         1   32030904 1.6780e+11 137399
## - HOME_VAL_LOG 1   34133834 1.6780e+11 137399
## <none>           1.6777e+11 137400
## - BLUEBOOK_LOG 1   52266252 1.6782e+11 137400
## - CAR_AGE      1   73234748 1.6784e+11 137401
## - SEX          1   90771157 1.6786e+11 137402
## - REVOKED      1   151762251 1.6792e+11 137405
## - PARENT1      1   169416146 1.6794e+11 137406
## - INCOME_LOG    1   172663430 1.6794e+11 137406
## - KIDSDRV       1   172875568 1.6794e+11 137406
## - MSTATUS        1   273793538 1.6804e+11 137411
## - TRAVTIME_LOG  1   292195343 1.6806e+11 137412
## - TIF          1   308685747 1.6808e+11 137413
## - CAR_TYPE      5   609247307 1.6838e+11 137419
## - JOB          8   748968743 1.6852e+11 137420
## - CAR_USE       1   475337908 1.6824e+11 137421
## - MVR_PTS       1   833078192 1.6860e+11 137438
## - URBANICITY    1   2825204941 1.7059e+11 137534
##
## Step: AIC=137397.9
## TARGET_AMT ~ KIDSDRV + AGE + HOMEKIDS + YOJ + PARENT1 + MSTATUS +
##               SEX + JOB + CAR_USE + TIF + CAR_TYPE + RED_CAR + CLM_FREQ +
##               REVOKED + MVR_PTS + CAR_AGE + URBANICITY + INCOME_LOG + HOME_VAL_LOG +
##               BLUEBOOK_LOG + OLDCALL_LOG + TRAVTIME_LOG
##
##          Df  Sum of Sq    RSS    AIC
## - RED_CAR      1   3598045 1.6786e+11 137396
## - AGE          1   4654470 1.6786e+11 137396
## - OLDCALL_LOG 1   6718740 1.6786e+11 137396
## - CLM_FREQ     1   12585069 1.6786e+11 137397
## - HOMEKIDS     1   13877963 1.6787e+11 137397
## - YOJ          1   33923562 1.6789e+11 137398
## - HOME_VAL_LOG 1   38252754 1.6789e+11 137398
## <none>           1.6785e+11 137398
## - BLUEBOOK_LOG 1   49228358 1.6790e+11 137398
## - SEX          1   86572738 1.6794e+11 137400

```

```

## - CAR_AGE      1 121470587 1.6797e+11 137402
## - REVOKED     1 153844373 1.6801e+11 137403
## - PARENT1      1 166003727 1.6802e+11 137404
## - KIDSDRV      1 173689080 1.6803e+11 137404
## - INCOME_LOG    1 183979035 1.6804e+11 137405
## - MSTATUS       1 266455930 1.6812e+11 137409
## - TRAVTIME_LOG   1 284014359 1.6814e+11 137410
## - TIF           1 303762559 1.6816e+11 137411
## - CAR_TYPE      5 609946016 1.6846e+11 137417
## - CAR_USE        1 447327201 1.6830e+11 137418
## - JOB            8 847504748 1.6870e+11 137423
## - MVR_PTS        1 833642710 1.6869e+11 137436
## - URBANICITY     1 2819644634 1.7067e+11 137532
##
## Step: AIC=137396.1
## TARGET_AMT ~ KIDSDRV + AGE + HOMEKIDS + YOJ + PARENT1 + MSTATUS +
##             SEX + JOB + CAR_USE + TIF + CAR_TYPE + CLM_FREQ + REVOKED +
##             MVR_PTS + CAR_AGE + URBANICITY + INCOME_LOG + HOME_VAL_LOG +
##             BLUEBOOK_LOG + OLDCLAIM_LOG + TRAVTIME_LOG
##
##              Df  Sum of Sq      RSS      AIC
## - AGE           1  4867735 1.6786e+11 137394
## - OLDCLAIM_LOG  1  6813624 1.6786e+11 137394
## - CLM_FREQ      1 12371730 1.6787e+11 137395
## - HOMEKIDS      1 13826346 1.6787e+11 137395
## - YOJ            1 33554295 1.6789e+11 137396
## - HOME_VAL_LOG   1 37636262 1.6789e+11 137396
## <none>          1 1.6786e+11 137396
## - BLUEBOOK_LOG   1 49866193 1.6791e+11 137397
## - SEX            1 92176080 1.6795e+11 137399
## - CAR_AGE        1 122188318 1.6798e+11 137400
## - REVOKED        1 153732425 1.6801e+11 137402
## - PARENT1        1 166621510 1.6802e+11 137402
## - KIDSDRV        1 174572217 1.6803e+11 137403
## - INCOME_LOG      1 183240986 1.6804e+11 137403
## - MSTATUS         1 266262583 1.6812e+11 137407
## - TRAVTIME_LOG    1 283166674 1.6814e+11 137408
## - TIF            1 303349198 1.6816e+11 137409
## - CAR_TYPE        5 611947046 1.6847e+11 137416
## - CAR_USE         1 446914288 1.6830e+11 137416
## - JOB             8 849536593 1.6871e+11 137421
## - MVR_PTS         1 833232415 1.6869e+11 137434
## - URBANICITY      1 2817725753 1.7067e+11 137530
##
## Step: AIC=137394.3
## TARGET_AMT ~ KIDSDRV + HOMEKIDS + YOJ + PARENT1 + MSTATUS +
##             SEX + JOB + CAR_USE + TIF + CAR_TYPE + CLM_FREQ + REVOKED +
##             MVR_PTS + CAR_AGE + URBANICITY + INCOME_LOG + HOME_VAL_LOG +
##             BLUEBOOK_LOG + OLDCLAIM_LOG + TRAVTIME_LOG
##
##              Df  Sum of Sq      RSS      AIC
## - OLDCLAIM_LOG   1  6820600 1.6787e+11 137393
## - HOMEKIDS        1  9639346 1.6787e+11 137393
## - CLM_FREQ        1 12499280 1.6787e+11 137393

```

```

## - HOME_VAL_LOG 1 36939207 1.6790e+11 137394
## <none> 1 1.6786e+11 137394
## - YOJ 1 41416724 1.6790e+11 137394
## - BLUEBOOK_LOG 1 54966017 1.6792e+11 137395
## - SEX 1 96908236 1.6796e+11 137397
## - CAR_AGE 1 121058293 1.6798e+11 137398
## - REVOKED 1 152980168 1.6801e+11 137400
## - PARENT1 1 162936018 1.6802e+11 137400
## - KIDSDRV 1 190539013 1.6805e+11 137402
## - INCOME_LOG 1 193861072 1.6805e+11 137402
## - MSTATUS 1 265962239 1.6813e+11 137405
## - TRAVTIME_LOG 1 283322006 1.6814e+11 137406
## - TIF 1 303072148 1.6816e+11 137407
## - CAR_USE 1 448751128 1.6831e+11 137414
## - CAR_TYPE 5 625784271 1.6849e+11 137415
## - JOB 8 844835231 1.6871e+11 137419
## - MVR PTS 1 829618807 1.6869e+11 137433
## - URBANICITY 1 2813937018 1.7067e+11 137528
##
## Step: AIC=137392.6
## TARGET_AMT ~ KIDSDRV + HOMEKIDS + YOJ + PARENT1 + MSTATUS +
##      SEX + JOB + CAR_USE + TIF + CAR_TYPE + CLM_FREQ + REVOKED +
##      MVR PTS + CAR_AGE + URBANICITY + INCOME_LOG + HOME_VAL_LOG +
##      BLUEBOOK_LOG + TRAVTIME_LOG
##
##          Df  Sum of Sq      RSS     AIC
## - HOMEKIDS 1  9915206 1.6788e+11 137391
## - HOME_VAL_LOG 1  37375762 1.6791e+11 137392
## <none> 1 1.6787e+11 137393
## - YOJ 1  41903117 1.6791e+11 137393
## - BLUEBOOK_LOG 1  55273914 1.6792e+11 137393
## - SEX 1  97192211 1.6796e+11 137395
## - CLM_FREQ 1  99266117 1.6797e+11 137395
## - CAR_AGE 1  121691454 1.6799e+11 137397
## - PARENT1 1  162483609 1.6803e+11 137399
## - REVOKED 1  165851175 1.6803e+11 137399
## - KIDSDRV 1  190523133 1.6806e+11 137400
## - INCOME_LOG 1  193767962 1.6806e+11 137400
## - MSTATUS 1  266847149 1.6813e+11 137404
## - TRAVTIME_LOG 1  282849713 1.6815e+11 137404
## - TIF 1  304191130 1.6817e+11 137405
## - CAR_USE 1  450314331 1.6832e+11 137412
## - CAR_TYPE 5  630032122 1.6850e+11 137413
## - JOB 8  848903491 1.6872e+11 137418
## - MVR PTS 1  923088612 1.6879e+11 137435
## - URBANICITY 1  2885568697 1.7075e+11 137530
##
## Step: AIC=137391.1
## TARGET_AMT ~ KIDSDRV + YOJ + PARENT1 + MSTATUS + SEX + JOB +
##      CAR_USE + TIF + CAR_TYPE + CLM_FREQ + REVOKED + MVR PTS +
##      CAR_AGE + URBANICITY + INCOME_LOG + HOME_VAL_LOG + BLUEBOOK_LOG +
##      TRAVTIME_LOG
##
##          Df  Sum of Sq      RSS     AIC

```

```

## - HOME_VAL_LOG 1 38160904 1.6792e+11 137391
## <none> 1 1.6788e+11 137391
## - YOJ 1 51182838 1.6793e+11 137392
## - BLUEBOOK_LOG 1 53591657 1.6793e+11 137392
## - SEX 1 94029600 1.6797e+11 137394
## - CLM_FREQ 1 99289987 1.6798e+11 137394
## - CAR_AGE 1 123231789 1.6800e+11 137395
## - REVOKED 1 167278023 1.6804e+11 137397
## - INCOME_LOG 1 204064662 1.6808e+11 137399
## - MSTATUS 1 257057257 1.6813e+11 137402
## - PARENT1 1 259900760 1.6814e+11 137402
## - KIDSDRV 1 270503381 1.6815e+11 137402
## - TRAVTIME_LOG 1 280611051 1.6816e+11 137403
## - TIF 1 302329138 1.6818e+11 137404
## - CAR_USE 1 449130706 1.6833e+11 137411
## - CAR_TYPE 5 630020938 1.6851e+11 137412
## - JOB 8 860804920 1.6874e+11 137417
## - MVR PTS 1 926462842 1.6880e+11 137434
## - URBANICITY 1 2885886068 1.7076e+11 137528
##
## Step: AIC=137391
## TARGET_AMT ~ KIDSDRV + YOJ + PARENT1 + MSTATUS + SEX + JOB +
##     CAR_USE + TIF + CAR_TYPE + CLM_FREQ + REVOKED + MVR PTS +
##     CAR_AGE + URBANICITY + INCOME_LOG + BLUEBOOK_LOG + TRAVTIME_LOG
##
##             Df Sum of Sq      RSS      AIC
## <none> 1.6792e+11 137391
## - YOJ 1 51807582 1.6797e+11 137392
## - BLUEBOOK_LOG 1 52809358 1.6797e+11 137392
## - SEX 1 91596369 1.6801e+11 137393
## - CLM_FREQ 1 103056765 1.6802e+11 137394
## - CAR_AGE 1 122757775 1.6804e+11 137395
## - REVOKED 1 170913939 1.6809e+11 137397
## - INCOME_LOG 1 213579483 1.6813e+11 137399
## - PARENT1 1 259169748 1.6817e+11 137402
## - KIDSDRV 1 273899405 1.6819e+11 137402
## - TRAVTIME_LOG 1 284181817 1.6820e+11 137403
## - TIF 1 303740963 1.6822e+11 137404
## - CAR_USE 1 446353873 1.6836e+11 137411
## - CAR_TYPE 5 628972873 1.6854e+11 137411
## - JOB 8 841952714 1.6876e+11 137416
## - MSTATUS 1 564089417 1.6848e+11 137416
## - MVR PTS 1 935911078 1.6885e+11 137434
## - URBANICITY 1 2880984646 1.7080e+11 137528

```

```
summary(linear_model4)
```

```

##
## Call:
## lm(formula = TARGET_AMT ~ KIDSDRV + YOJ + PARENT1 + MSTATUS +
##     SEX + JOB + CAR_USE + TIF + CAR_TYPE + CLM_FREQ + REVOKED +
##     MVR PTS + CAR_AGE + URBANICITY + INCOME_LOG + BLUEBOOK_LOG +
##     TRAVTIME_LOG, data = train_df_imp_lin)
##
```

```

## Residuals:
##      Min     1Q Median     3Q    Max
## -5482 -1681   -766    343 103878
##
## Coefficients:
##                               Estimate Std. Error t value Pr(>|t|)
## (Intercept)                 -1865.26   1128.94 -1.652 0.098527 .
## KIDSDRV                      372.21    102.23  3.641 0.000274 ***
## YOJ                           27.76     17.53  1.583 0.113370
## PARENT1Yes                   628.53    177.48  3.541 0.000400 ***
## MSTATUSYes                  -637.96   122.10 -5.225 1.79e-07 ***
## SEXM                          327.41    155.51  2.105 0.035288 *
## JOBBlue Collar                452.19    262.54  1.722 0.085037 .
## JOBClerical                   543.91    282.07  1.928 0.053853 .
## JOBDoctor                     -436.83   375.63 -1.163 0.244894
## JOBHome Maker                 149.56    347.45  0.430 0.666872
## JOBLawyer                     213.74    285.85  0.748 0.454641
## JOBManager                    -608.01   266.42 -2.282 0.022506 *
## JOBProfessional                268.52    264.74  1.014 0.310476
## JOBStudent                    115.69    339.91  0.340 0.733599
## CAR_USEPrivate                 -729.72   157.01 -4.648 3.41e-06 ***
## TIF                           -46.70     12.18 -3.834 0.000127 ***
## CAR_TYPEPanel Truck            328.88    259.89  1.265 0.205743
## CAR_TYPEPickup                 417.35    169.09  2.468 0.013599 *
## CAR_TYPESports Car             1028.57   214.64  4.792 1.68e-06 ***
## CAR_TYPESUV                    755.38    173.46  4.355 1.35e-05 ***
## CAR_TYPEVan                    519.52    211.26  2.459 0.013950 *
## CLM_FREQ                       109.11     48.86  2.233 0.025562 *
## REVOKEDYes                     445.86   155.03  2.876 0.004039 **
## MVR PTS                        173.79     25.82  6.730 1.81e-11 ***
## CAR AGE                         -26.74    10.97 -2.437 0.014817 *
## URBANICITYHighly Urban/ Urban 1639.98   138.89 11.808 < 2e-16 ***
## INCOME_LOG                      -97.73    30.40 -3.215 0.001310 **
## BLUEBOOK_LOG                    162.97    101.94  1.599 0.109942
## TRAVTIME_LOG                   330.33    89.07  3.708 0.000210 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 4546 on 8126 degrees of freedom
## Multiple R-squared:  0.0698, Adjusted R-squared:  0.06659
## F-statistic: 21.78 on 28 and 8126 DF,  p-value: < 2.2e-16

```

```
formula(linear_model4)
```

```

## TARGET_AMT ~ KIDSDRV + YOJ + PARENT1 + MSTATUS + SEX + JOB +
##      CAR_USE + TIF + CAR_TYPE + CLM_FREQ + REVOKED + MVR PTS +
##      CAR AGE + URBANICITY + INCOME_LOG + BLUEBOOK_LOG + TRAVTIME_LOG

```

4. SELECT MODELS

Decide on the criteria for selecting the best multiple linear regression model and the best binary logistic regression model. Will you select models with slightly worse performance if it makes more sense or is more parsimonious? Discuss why you selected your models. For the multiple linear regression model, will you use

a metric such as Adjusted R2, RMSE, etc.? Be sure to explain how you can make inferences from the model, discuss multi-collinearity issues (if any), and discuss other relevant model output. Using the training data set, evaluate the multiple linear regression model based on (a) mean squared error, (b) R2, (c) F-statistic, and (d) residual plots. For the binary logistic regression model, will you use a metric such as log likelihood, AIC, ROC curve, etc.? Using the training data set, evaluate the binary logistic regression model based on (a) accuracy, (b) classification error rate, (c) precision, (d) sensitivity, (e) specificity, (f) F1 score, (g) AUC, and (h) confusion matrix. Make predictions using the evaluation data set.

Assessing Logistic Models

Our logistic regression model 1 the model with all variables (except target amt) with log transformation. This model was the best choice, as the accuracy difference amog the other models were minimal, it had the highest accuracy, the highest sensitivity, meaning it was slightly better at correctly identifying positive cases. This is important in situations where detecting positive is more critical than minimizing false positives. Although its AIC (7345.540) is slightly higher than some reduced models, the trade-off in favor of sensitivity justifies choosing Full Log in this context. Therefore, Full Log provides a good balance between performance and the practical goal of maximizing true positive detection.

```
compare_logistic_models <- function(models, data, response_var, threshold = 0.5) {

  results <- data.frame(
    Model = character(),
    AIC = numeric(),
    Accuracy = numeric(),
    Sensitivity = numeric(),
    Specificity = numeric(),
    stringsAsFactors = FALSE
  )

  for (i in seq_along(models)) {
    model <- models[[i]]
    model_name <- names(models)[i]

    # Predicted probabilities
    probs <- predict(model, newdata = data, type = "response")
    preds <- factor(ifelse(probs > threshold, 1, 0), levels = c(0, 1))

    # Actual values
    actual <- factor(data[[response_var]], levels = c(0, 1))

    # Confusion matrix
    cm <- confusionMatrix(as.factor(preds), as.factor(actual), positive = "1")

    # Append results
    results <- rbind(results, data.frame(
      Model = model_name,
      AIC = AIC(model),
      Accuracy = cm$overall["Accuracy"],
      Sensitivity = cm$byClass["Sensitivity"],
      Specificity = cm$byClass["Specificity"]
    )))
  }
}
```

```

    }

    return(results)
}

models <- list(
  Full_Log = logist_model3,
  Full_NoLog = logist_model1,
  Reduced_Log = logist_model4,
  Reduced_NoLog = logist_model2
)

compare_logistic_models(models, train_df_imp_log, response_var = "TARGET_FLAG")

##           Model      AIC Accuracy Sensitivity Specificity
## Accuracy     Full_Log 7345.540 0.7919068  0.4241155  0.9234227
## Accuracy1   Full_NoLog 7363.311 0.7917842  0.4245810  0.9230897
## Accuracy2   Reduced_Log 7338.760 0.7915389  0.4213222  0.9239221
## Accuracy3   Reduced_NoLog 7354.455 0.7914163  0.4199255  0.9242550

```

Assessing Linear Models

Our linear model 2, the reduced model without transformed data performed the best with AIC and only very slightly worse on Rsquared.

```

model_comparison <- data.frame(
  Model = c("linear_model1", "linear_model2", "linear_model3", "linear_model4"),
  AIC = c(
    AIC(linear_model1),
    AIC(linear_model2),
    AIC(linear_model3),
    AIC(linear_model4)
  ),
  Adjusted_R2 = c(
    summary(linear_model1)$adj.r.squared,
    summary(linear_model2)$adj.r.squared,
    summary(linear_model3)$adj.r.squared,
    summary(linear_model4)$adj.r.squared
  )
)

print(model_comparison)

##           Model      AIC Adjusted_R2
## 1 linear_model1 160539.8  0.06705563
## 2 linear_model2 160532.2  0.06700925
## 3 linear_model3 160544.7  0.06649053
## 4 linear_model4 160535.9  0.06659172

```

Predictions

Predictions were made and saved to csv “Homework 4 Predictions”. Logistic regression model 3 was used to predict car crash in variable TARGET_FLAG, and multiple linear regression model 2 was used to predict amount of claim for the car crash in variable TARGET_AMT. Multiple linear regression was only used on observations in the test data where our logistic regression predicts a car crash. Observations where there is not a predicted car crash defaults to a 0\$ claim in TARGET_AMT.

```
# Generate predicted probabilities
probs <- predict(logist_model3, newdata = test_df_imp, type = "response")

# Convert to binary predictions using a threshold (e.g., 0.5)
preds <- ifelse(probs > 0.5, 1, 0)

# Add predictions to your test data frame
test_df_imp$TARGET_FLAG <- preds

pred_probs <- predict(logist_model3, train_df_imp, type = "response")
pred_class <- ifelse(pred_probs > 0.5, 1, 0)

# Confusion matrix on training data
confusionMatrix(
  factor(pred_class),
  factor(train_df_imp$TARGET_FLAG),
  positive = "1"
)

## Confusion Matrix and Statistics
##
##             Reference
## Prediction      0      1
##           0 5547 1237
##           1   460   911
##
##                   Accuracy : 0.7919
##                   95% CI : (0.7829, 0.8007)
##       No Information Rate : 0.7366
##       P-Value [Acc > NIR] : < 2.2e-16
##
##                   Kappa : 0.3932
##
## Mcnemar's Test P-Value : < 2.2e-16
##
##                   Sensitivity : 0.4241
##                   Specificity : 0.9234
##       Pos Pred Value : 0.6645
##       Neg Pred Value : 0.8177
##                   Prevalence : 0.2634
##       Detection Rate : 0.1117
## Detection Prevalence : 0.1681
##       Balanced Accuracy : 0.6738
##
##       'Positive' Class : 1
##
```



```

## [1481] 0 0 0 0 0 0 0 0 1 0 0 1 0 0 1 0 0 0 0 0 0 0 0 1 0 0 1 0 0 0 0 0 0 0 0 0 0
## [1518] 1 0 0 0 0 0 1 0 0 0 0 1 1 0 0 0 0 0 0 0 0 0 1 1 0 0 0 0 1 0 0 0 0 0 0 0 1
## [1555] 0 0 0 0 0 0 0 1 0 0 1 0 0 0 0 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
## [1592] 1 0 0 0 0 0 0 0 0 0 0 0 0 1 0 1 0 0 0 1 0 0 0 0 0 1 0 1 0 0 1 0 1 0 0 0 0
## [1629] 0 1 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 0 0 0 0 1 0 0 0 0 1 0 0 0 0 1 1 1 1
## [1666] 0 0 0 1 0 1 0 1 0 0 0 0 0 0 0 0 0 1 1 0 0 0 0 0 0 0 0 0 0 0 0 1 0 1 1 0 1 0
## [1703] 0 1 0 0 1 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 0 0 0 0 0 0 0 0 0 0
## [1740] 0 1 0 0 0 0 0 0 0 1 0 0 0 0 1 0 0 0 0 0 0 1 0 0 0 0 1 0 0 0 0 0 0 0 0 1 0 0
## [1777] 1 0 0 0 0 0 0 0 0 0 0 0 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 1 0 0 0 1
## [1814] 0 1 0 0 0 0 0 0 0 0 0 0 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0 1 0 1 0 0 0 0 0 0 0 0 0
## [1851] 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 0 0 0 0 0 0 1 0 0 0 0 0 0 0 0 0 0 0
## [1888] 0 0 0 0 0 0 0 0 0 0 0 0 0 1 0 0 0 0 0 0 0 0 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
## [1925] 0 0 0 0 0 0 0 0 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0 1 0 1 0 0 0 0 0 0 0 0 0 0 0 0 1
## [1962] 0 0 0 0 0 0 0 0 0 0 0 0 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 0 1 1 1 0 0 0 1
## [1999] 0 0 1 0 1 0 1 0 0 0 0 0 0 1 0 1 0 0 0 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 0 0 0 1
## [2036] 0 0 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 0 0 0 0 0 0 0 0 1 0 0 0 0 1 0 0 0 0
## [2073] 1 0 0 0 1 0 0 1 0 0 0 0 0 0 0 0 1 0 1 0 0 0 0 0 1 0 0 1 1 1 1 0 0 0 1 0 0
## [2110] 0 1 0 0 0 0 0 0 0 1 0 0 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
```

`testdf_predictions$TARGET_AMT`

| | [1] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|-------|-------|
| ## [9] | 0.000 | 0.000 | 0.000 | 0.000 | 4346.342 | 0.000 | 0.000 | 3360.126 | | | |
| ## [17] | 3414.275 | 0.000 | 2515.321 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | |
| ## [25] | 0.000 | 0.000 | 0.000 | 3309.341 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | |
| ## [33] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 3084.804 | | | |
| ## [41] | 0.000 | 0.000 | 0.000 | 3423.893 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | |
| ## [49] | 0.000 | 2740.136 | 0.000 | 0.000 | 4109.158 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | |
| ## [57] | 0.000 | 0.000 | 0.000 | 2287.818 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | |
| ## [65] | 0.000 | 1574.911 | 4013.430 | 3710.800 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | |
| ## [73] | 3318.909 | 0.000 | 3345.358 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | |
| ## [81] | 2357.352 | 0.000 | 0.000 | 0.000 | 0.000 | 3430.573 | 0.000 | 0.000 | 0.000 | 0.000 | |
| ## [89] | 0.000 | 3934.113 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | |
| ## [97] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 3310.991 | 3535.094 | | |
| ## [105] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 2956.188 | 0.000 | | |
| ## [113] | 0.000 | 0.000 | 3069.187 | 0.000 | 0.000 | 3102.105 | 1840.159 | 0.000 | | | |
| ## [121] | 0.000 | 3459.670 | 2666.295 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | |
| ## [129] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | |
| ## [137] | 4119.037 | 3553.831 | 0.000 | 0.000 | 0.000 | 3699.183 | 0.000 | 0.000 | 0.000 | 0.000 | |
| ## [145] | 0.000 | 2903.229 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | |
| ## [153] | 4322.071 | 0.000 | 0.000 | 2189.982 | 0.000 | 0.000 | 2265.982 | 0.000 | | | |
| ## [161] | 0.000 | 0.000 | 0.000 | 0.000 | 4904.801 | 0.000 | 0.000 | 0.000 | 0.000 | | |
| ## [169] | 0.000 | 0.000 | 0.000 | 3222.693 | 0.000 | 4176.113 | 0.000 | 0.000 | | | |
| ## [177] | 3528.219 | 3174.611 | 4146.255 | 3050.563 | 3254.074 | 0.000 | 0.000 | 0.000 | 0.000 | | |
| ## [185] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 2164.372 | 3248.140 | | | |
| ## [193] | 0.000 | 0.000 | 0.000 | 2341.528 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | | |
| ## [201] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 4190.535 | 0.000 | | |
| ## [209] | 0.000 | 0.000 | 0.000 | 0.000 | 2977.801 | 2955.963 | 0.000 | 0.000 | | | |
| ## [217] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | | |
| ## [225] | 0.000 | 0.000 | 3358.296 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | | |
| ## [233] | 3694.071 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 3818.680 | | |
| ## [241] | 0.000 | 0.000 | 3959.213 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | | |
| ## [249] | 0.000 | 2488.343 | 0.000 | 2668.967 | 0.000 | 0.000 | 1694.036 | 0.000 | | | |
| ## [257] | 0.000 | 0.000 | 2629.215 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | | |

| | | | | | | | | | |
|----|-------|----------|----------|----------|----------|----------|----------|----------|----------|
| ## | [265] | 0.000 | 0.000 | 0.000 | 0.000 | 4793.566 | 0.000 | 2521.215 | 0.000 |
| ## | [273] | 0.000 | 2716.135 | 0.000 | 0.000 | 3951.662 | 0.000 | 0.000 | 0.000 |
| ## | [281] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 2266.173 | 0.000 | 0.000 |
| ## | [289] | 2008.997 | 3633.614 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## | [297] | 0.000 | 3154.918 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## | [305] | 0.000 | 0.000 | 0.000 | 2165.967 | 0.000 | 0.000 | 4210.164 | 0.000 |
| ## | [313] | 0.000 | 4742.237 | 0.000 | 0.000 | 0.000 | 0.000 | 2767.508 | 0.000 |
| ## | [321] | 0.000 | 2739.156 | 0.000 | 0.000 | 3620.464 | 0.000 | 0.000 | 0.000 |
| ## | [329] | 0.000 | 0.000 | 0.000 | 0.000 | 3867.975 | 0.000 | 0.000 | 0.000 |
| ## | [337] | 0.000 | 0.000 | 0.000 | 0.000 | 2628.751 | 0.000 | 0.000 | 3237.668 |
| ## | [345] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## | [353] | 4182.229 | 4268.812 | 0.000 | 2683.003 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## | [361] | 3072.300 | 0.000 | 0.000 | 2598.351 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## | [369] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 2710.464 |
| ## | [377] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## | [385] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 2344.299 | 0.000 | 0.000 |
| ## | [393] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## | [401] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## | [409] | 0.000 | 0.000 | 0.000 | 3184.381 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## | [417] | 0.000 | 0.000 | 0.000 | 0.000 | 2902.198 | 3769.647 | 4420.564 | 0.000 |
| ## | [425] | 0.000 | 0.000 | 0.000 | 0.000 | 2733.449 | 0.000 | 0.000 | 0.000 |
| ## | [433] | 0.000 | 0.000 | 0.000 | 4091.925 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## | [441] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## | [449] | 3073.991 | 3877.864 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 2741.662 |
| ## | [457] | 0.000 | 4700.213 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## | [465] | 0.000 | 0.000 | 4204.309 | 2240.163 | 0.000 | 0.000 | 0.000 | 3412.091 |
| ## | [473] | 0.000 | 0.000 | 0.000 | 0.000 | 3493.719 | 4141.819 | 0.000 | 0.000 |
| ## | [481] | 0.000 | 0.000 | 0.000 | 0.000 | 3520.683 | 2768.192 | 0.000 | 0.000 |
| ## | [489] | 0.000 | 3978.810 | 2991.445 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## | [497] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 3420.266 | 0.000 |
| ## | [505] | 3883.747 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## | [513] | 0.000 | 0.000 | 0.000 | 0.000 | 3340.964 | 3040.315 | 0.000 | 3010.149 |
| ## | [521] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## | [529] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## | [537] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## | [545] | 0.000 | 0.000 | 0.000 | 4687.548 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## | [553] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## | [561] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 5514.220 | 0.000 |
| ## | [569] | 0.000 | 3139.104 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## | [577] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 2705.559 | 0.000 | 3216.993 |
| ## | [585] | 0.000 | 0.000 | 0.000 | 0.000 | 3616.528 | 0.000 | 0.000 | 0.000 |
| ## | [593] | 0.000 | 0.000 | 2614.935 | 2458.293 | 2877.629 | 0.000 | 0.000 | 2138.643 |
| ## | [601] | 2722.592 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 3791.845 | 0.000 |
| ## | [609] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## | [617] | 0.000 | 0.000 | 0.000 | 3657.614 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## | [625] | 0.000 | 4320.423 | 3039.101 | 0.000 | 0.000 | 3143.036 | 0.000 | 0.000 |
| ## | [633] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 2975.074 | 0.000 | 0.000 |
| ## | [641] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 2980.049 | 0.000 | 0.000 |
| ## | [649] | 0.000 | 0.000 | 0.000 | 0.000 | 3441.578 | 0.000 | 0.000 | 0.000 |
| ## | [657] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## | [665] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 2821.537 |
| ## | [673] | 2947.197 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## | [681] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## | [689] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |

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|----|--------|----------|----------|----------|----------|----------|----------|----------|----------|
| ## | [697] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## | [705] | 0.000 | 0.000 | 0.000 | 4107.645 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## | [713] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## | [721] | 2515.978 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## | [729] | 0.000 | 0.000 | 2347.332 | 3011.205 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## | [737] | 0.000 | 0.000 | 0.000 | 0.000 | 2975.883 | 0.000 | 3233.931 | 0.000 |
| ## | [745] | 0.000 | 0.000 | 3440.390 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## | [753] | 0.000 | 2830.301 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## | [761] | 0.000 | 3955.387 | 0.000 | 3108.785 | 2442.731 | 3185.649 | 0.000 | 0.000 |
| ## | [769] | 0.000 | 0.000 | 0.000 | 2704.319 | 0.000 | 3712.839 | 0.000 | 0.000 |
| ## | [777] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 4219.961 | 0.000 | 0.000 |
| ## | [785] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## | [793] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 2769.601 | 3412.353 | 0.000 |
| ## | [801] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## | [809] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## | [817] | 0.000 | 3367.857 | 3093.542 | 0.000 | 2776.364 | 0.000 | 0.000 | 0.000 |
| ## | [825] | 2940.732 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## | [833] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## | [841] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## | [849] | 3961.017 | 3381.752 | 3231.657 | 0.000 | 0.000 | 0.000 | 2516.375 | 0.000 |
| ## | [857] | 0.000 | 0.000 | 4049.653 | 0.000 | 0.000 | 3051.534 | 0.000 | 0.000 |
| ## | [865] | 0.000 | 0.000 | 3838.369 | 0.000 | 0.000 | 3284.558 | 0.000 | 3452.100 |
| ## | [873] | 0.000 | 4486.066 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## | [881] | 0.000 | 0.000 | 0.000 | 0.000 | 2919.781 | 0.000 | 3942.148 | 0.000 |
| ## | [889] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## | [897] | 0.000 | 0.000 | 2231.554 | 0.000 | 0.000 | 0.000 | 3997.104 | 0.000 |
| ## | [905] | 0.000 | 0.000 | 3275.490 | 0.000 | 0.000 | 0.000 | 3948.241 | 0.000 |
| ## | [913] | 0.000 | 0.000 | 0.000 | 0.000 | 4696.655 | 2603.120 | 0.000 | 0.000 |
| ## | [921] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## | [929] | 3121.541 | 0.000 | 0.000 | 4391.628 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## | [937] | 0.000 | 0.000 | 0.000 | 0.000 | 3807.007 | 0.000 | 2112.229 | 0.000 |
| ## | [945] | 3035.707 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## | [953] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## | [961] | 2181.017 | 0.000 | 0.000 | 0.000 | 0.000 | 3541.376 | 0.000 | 0.000 |
| ## | [969] | 0.000 | 0.000 | 3164.032 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## | [977] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 3593.193 | 2637.747 |
| ## | [985] | 3134.431 | 2692.620 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## | [993] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## | [1001] | 0.000 | 4381.639 | 2982.583 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## | [1009] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## | [1017] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 3587.903 | 0.000 |
| ## | [1025] | 3409.510 | 3295.644 | 2021.219 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## | [1033] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## | [1041] | 0.000 | 1886.266 | 1690.410 | 0.000 | 3709.535 | 0.000 | 0.000 | 0.000 |
| ## | [1049] | 2451.514 | 0.000 | 0.000 | 0.000 | 3006.525 | 0.000 | 0.000 | 0.000 |
| ## | [1057] | 0.000 | 0.000 | 2371.307 | 2903.436 | 0.000 | 3185.622 | 0.000 | 0.000 |
| ## | [1065] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 2304.252 | 0.000 | 0.000 |
| ## | [1073] | 0.000 | 4290.718 | 0.000 | 0.000 | 0.000 | 0.000 | 3027.488 | 0.000 |
| ## | [1081] | 3596.314 | 3078.302 | 0.000 | 0.000 | 2247.397 | 4343.952 | 0.000 | 0.000 |
| ## | [1089] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## | [1097] | 0.000 | 0.000 | 0.000 | 3346.956 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## | [1105] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 1601.949 | 2790.555 | 0.000 |
| ## | [1113] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 4471.567 | 0.000 | 0.000 |
| ## | [1121] | 0.000 | 1988.596 | 0.000 | 0.000 | 0.000 | 0.000 | 4673.711 | 0.000 |

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| ## [1129] | 0.000 | 0.000 | 0.000 | 0.000 | 3295.311 | 0.000 | 0.000 | 0.000 |
| ## [1137] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## [1145] | 3025.576 | 0.000 | 0.000 | 3973.971 | 0.000 | 0.000 | 0.000 | 4317.051 |
| ## [1153] | 0.000 | 0.000 | 3562.331 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## [1161] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## [1169] | 0.000 | 0.000 | 1913.090 | 0.000 | 0.000 | 3522.103 | 0.000 | 0.000 |
| ## [1177] | 0.000 | 0.000 | 0.000 | 3519.685 | 0.000 | 3685.170 | 0.000 | 0.000 |
| ## [1185] | 3734.497 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## [1193] | 0.000 | 2915.425 | 0.000 | 0.000 | 0.000 | 0.000 | 2519.349 | 0.000 |
| ## [1201] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 2477.787 | 0.000 |
| ## [1209] | 0.000 | 0.000 | 0.000 | 0.000 | 3874.528 | 0.000 | 0.000 | 0.000 |
| ## [1217] | 3073.224 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 3977.356 | 0.000 |
| ## [1225] | 2601.493 | 0.000 | 0.000 | 0.000 | 0.000 | 3734.712 | 0.000 | 0.000 |
| ## [1233] | 0.000 | 3402.848 | 0.000 | 0.000 | 0.000 | 3784.917 | 0.000 | 0.000 |
| ## [1241] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 4391.160 | 0.000 | 0.000 |
| ## [1249] | 0.000 | 0.000 | 0.000 | 3790.210 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## [1257] | 3721.544 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 3537.800 |
| ## [1265] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## [1273] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## [1281] | 3158.783 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 2408.281 | 0.000 |
| ## [1289] | 0.000 | 0.000 | 3556.992 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## [1297] | 0.000 | 0.000 | 3330.694 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## [1305] | 0.000 | 0.000 | 2942.387 | 0.000 | 0.000 | 3307.941 | 0.000 | 0.000 |
| ## [1313] | 4462.081 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 3811.096 |
| ## [1321] | 0.000 | 0.000 | 2946.312 | 0.000 | 0.000 | 2808.463 | 0.000 | 0.000 |
| ## [1329] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## [1337] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 2524.099 | 0.000 | 0.000 |
| ## [1345] | 3786.703 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 2604.646 |
| ## [1353] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## [1361] | 0.000 | 0.000 | 4059.667 | 0.000 | 0.000 | 0.000 | 2962.060 | 2500.707 |
| ## [1369] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## [1377] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 3368.029 | 0.000 | 0.000 |
| ## [1385] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 3210.848 | 2645.135 |
| ## [1393] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## [1401] | 0.000 | 0.000 | 3853.971 | 2206.858 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## [1409] | 0.000 | 3189.211 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## [1417] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 4638.128 | 2231.716 | 0.000 |
| ## [1425] | 0.000 | 4747.953 | 0.000 | 0.000 | 2179.216 | 0.000 | 0.000 | 0.000 |
| ## [1433] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 2428.047 | 0.000 | 0.000 |
| ## [1441] | 0.000 | 3510.759 | 0.000 | 0.000 | 0.000 | 2829.904 | 0.000 | 0.000 |
| ## [1449] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## [1457] | 3555.280 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## [1465] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## [1473] | 0.000 | 0.000 | 0.000 | 2178.332 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## [1481] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## [1489] | 3501.311 | 0.000 | 0.000 | 3161.067 | 0.000 | 0.000 | 3711.656 | 0.000 |
| ## [1497] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 3597.845 |
| ## [1505] | 0.000 | 0.000 | 3137.129 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## [1513] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 1817.183 | 0.000 | 0.000 |
| ## [1521] | 0.000 | 0.000 | 0.000 | 2016.923 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## [1529] | 2657.317 | 3161.089 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## [1537] | 0.000 | 0.000 | 3619.778 | 3945.420 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## [1545] | 3103.711 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## [1553] | 0.000 | 3033.896 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |

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| ## [1561] | 0.000 | 3062.007 | 0.000 | 0.000 | 4534.045 | 0.000 | 0.000 | 0.000 |
| ## [1569] | 0.000 | 0.000 | 2779.412 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## [1577] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## [1585] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 4004.899 |
| ## [1593] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## [1601] | 0.000 | 0.000 | 0.000 | 3255.657 | 0.000 | 4195.879 | 0.000 | 0.000 |
| ## [1609] | 0.000 | 4081.018 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 2691.572 |
| ## [1617] | 0.000 | 2999.243 | 0.000 | 0.000 | 2693.528 | 0.000 | 3383.426 | 0.000 |
| ## [1625] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 4419.178 | 0.000 | 3129.360 |
| ## [1633] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## [1641] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## [1649] | 0.000 | 2455.384 | 0.000 | 0.000 | 0.000 | 0.000 | 3177.257 | 0.000 |
| ## [1657] | 0.000 | 0.000 | 0.000 | 0.000 | 2336.781 | 3839.072 | 2756.927 | 3871.550 |
| ## [1665] | 5293.727 | 0.000 | 0.000 | 0.000 | 4162.510 | 0.000 | 2933.068 | 0.000 |
| ## [1673] | 3520.379 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## [1681] | 0.000 | 3693.396 | 3202.301 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## [1689] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 3065.616 |
| ## [1697] | 0.000 | 2756.420 | 4134.429 | 0.000 | 2580.138 | 0.000 | 0.000 | 1361.694 |
| ## [1705] | 0.000 | 0.000 | 3332.846 | 0.000 | 4243.905 | 0.000 | 0.000 | 0.000 |
| ## [1713] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## [1721] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## [1729] | 3637.484 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## [1737] | 0.000 | 0.000 | 0.000 | 0.000 | 4570.431 | 0.000 | 0.000 | 0.000 |
| ## [1745] | 0.000 | 0.000 | 0.000 | 0.000 | 2629.770 | 0.000 | 0.000 | 0.000 |
| ## [1753] | 0.000 | 3039.880 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## [1761] | 3852.260 | 0.000 | 0.000 | 0.000 | 0.000 | 3742.656 | 0.000 | 0.000 |
| ## [1769] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 4178.757 | 0.000 | 0.000 |
| ## [1777] | 2585.026 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## [1785] | 0.000 | 0.000 | 0.000 | 0.000 | 3280.636 | 0.000 | 0.000 | 0.000 |
| ## [1793] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## [1801] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 3155.765 | 3387.546 |
| ## [1809] | 0.000 | 0.000 | 0.000 | 0.000 | 2351.594 | 0.000 | 1871.423 | 0.000 |
| ## [1817] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## [1825] | 0.000 | 3632.162 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## [1833] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 4363.327 | 0.000 | 3431.554 |
| ## [1841] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## [1849] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## [1857] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## [1865] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 3068.884 | 0.000 |
| ## [1873] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 3668.838 | 0.000 | 0.000 |
| ## [1881] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## [1889] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## [1897] | 0.000 | 0.000 | 0.000 | 2510.126 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## [1905] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 3953.076 | 0.000 | 0.000 |
| ## [1913] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## [1921] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## [1929] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 3472.979 | 0.000 | 0.000 |
| ## [1937] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## [1945] | 0.000 | 0.000 | 3043.451 | 0.000 | 2573.287 | 0.000 | 0.000 | 0.000 |
| ## [1953] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## [1961] | 3855.575 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## [1969] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 3252.756 | 0.000 | 0.000 |
| ## [1977] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| ## [1985] | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 2403.709 | 0.000 | 3311.629 |

```

## [1993] 3486.338 3299.985    0.000    0.000    0.000 4390.028    0.000    0.000
## [2001] 2770.952    0.000 3559.453    0.000 3006.626    0.000    0.000    0.000
## [2009]    0.000    0.000 2095.736    0.000 5387.863    0.000    0.000    0.000
## [2017]    0.000 3104.122    0.000    0.000    0.000    0.000    0.000    0.000
## [2025]    0.000    0.000    0.000    0.000    0.000 2806.144    0.000    0.000
## [2033]    0.000    0.000 2950.330    0.000    0.000    0.000 2551.447    0.000
## [2041]    0.000    0.000    0.000    0.000    0.000    0.000    0.000    0.000
## [2049]    0.000    0.000    0.000    0.000    0.000    0.000 3217.130    0.000
## [2057]    0.000    0.000    0.000    0.000    0.000    0.000 2067.641    0.000
## [2065]    0.000    0.000    0.000 4185.271    0.000    0.000    0.000    0.000
## [2073] 3413.971    0.000    0.000    0.000 3636.778    0.000    0.000 4914.937
## [2081]    0.000    0.000    0.000    0.000    0.000    0.000    0.000 2776.496
## [2089]    0.000 2855.831    0.000    0.000    0.000    0.000    0.000 3021.110
## [2097]    0.000    0.000 3832.960 2675.241 3246.550 1560.755 4739.731    0.000
## [2105]    0.000    0.000 2799.317    0.000    0.000    0.000 4245.857    0.000
## [2113]    0.000    0.000    0.000    0.000    0.000    0.000 5148.513    0.000
## [2121]    0.000    0.000 3880.107    0.000    0.000    0.000    0.000    0.000
## [2129]    0.000    0.000    0.000    0.000    0.000    0.000    0.000    0.000
## [2137]    0.000    0.000    0.000    0.000    0.000    0.000    0.000    0.000

```

```

# writing predictions to csv

write.csv(testdf_predictions, "Homework 4 Predictions")

```