# Package 'eSIR'

April 16, 2020

qh.eSIR	Extended state-space SIR with quarantine	
Index		
tvt.eSIR		
R topics docum	nented:	
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	ementation of extended state-space SIR models developed by school of Public Health.	
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Title Extended state-s	pace SIR models	
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## Description

Fit an extended state-space SIR model being reduced by in-home hospitalization.

qh.eSIR

#### **Usage**

```
qh.eSIR(Y, R, phi0 = NULL, change_time = NULL,
  begin_str = "01/13/2020", T_fin = 200, nchain = 4,
  nadapt = 10000, M = 500, thn = 10, nburnin = 200, dic = FALSE,
  death_in_R = 0.02, casename = "qh.eSIR", beta0 = 0.2586,
  gamma0 = 0.0821, R0 = beta0/gamma0, gamma0_sd = 0.1, R0_sd = 1,
  file_add = character(0), add_death = FALSE, save_files = FALSE,
  save_mcmc = FALSE, save_plot_data = FALSE, eps = 1e-10)
```

### **Arguments**

Y the time series of daily observed infected compartment proportions.

R the time series of daily observed removed compartment proportions, including

death and recovered.

phi0 a vector of values of the dirac delta function  $\phi_t$ . Each entry denotes the propor-

tion that will be qurantined at each change time point. Note that all the entries

lie between 0 and 1, its default is NULL.

change\_time the change points over time corresponding to phi0, to formulate the dirac delta

function  $\phi_t$ ; its defalt value is NULL.

begin\_str the character of starting time, the default is "01/13/2020".

T\_fin the end of follow-up time after the beginning date begin\_str, the default is 200.

nchain the number of MCMC chains generated by rjags, the default is 4.

nadapt the iteration number of adaptation in the MCMC. We recommend using at least

the default value 1e4 to obtained fully adapted chains.

M the number of draws in each chain, with no thinning. The default is M=5e2 but

suggest using 5e5.

thn the thinning interval between mixing. The total number of draws thus would

become round(M/thn)\*nchain. The default is 10.

nburnin the burn-in period. The default is 2e2 but suggest 2e5.

dic logical, whether compute the DIC (deviance information criterion) for model

selection.

death\_in\_R the numeric value of average of cumulative deaths in the removed compart-

ments. The default is 0.4 within Hubei and 0.02 outside Hubei.

casename the string of the job's name. The default is "qh.eSIR".

beta0 the hyperparameter of average transmission rate, the default is the one estimated

from the SARS first-month outbreak (0.2586).

gamma0 the hyperparameter of average removed rate, the default is the one estimated

from the SARS first-month outbreak (0.0821).

R0 the hyperparameter of the mean reproduction number R0. The default is thus

the ratio of beta0/gamma0, which can be specified directly.

gamma0\_sd the standard deviation for the prior distribution of the removed rate  $\gamma$ , the default

is 0.1.

R0\_sd the standard deviation for the prior disbution of R0, the default is 1.

file\_add the string to denote the location of saving output files and tables.

add\_death logical, whether add the approximate death curve to the plot, default is false.

save\_files logical, whether to save plots to file.

qh.eSIR 3

save\_mcmc

logical, whether save (TRUE) all the MCMC outputs or not (FALSE). The output file will be an .RData file named by the casename. We include arrays of prevalence values of the three compartments with their matrices of posterior draws up to the last date of the collected data as theta\_p[,,1] and afterwards as theta\_pp[,,1] for  $\theta_t^S$ , theta\_p[,,2] and theta\_pp[,,2] for  $\theta_t^R$ , and theta\_pp[,,3] and theta\_pp[,,3] for  $\theta_t^R$ . The posterior draws of the prevalence process of the quarantine compartment can be obtained via thetaQ\_p and thetaQ\_pp. Moreover, the input and predicted proportions Y, Y\_pp, R and R\_pp can also be retrieved. The prevalence and predicted proportion matrices have rows for MCMC replicates, and columns for days. The MCMC posterior draws of other parameters including beta, gamma, R0, and variance controllers k\_p, lambdaY\_p, lambdaR\_p are also available.

save\_plot\_data logical, whether save the plotting data or not.

a non-zero controller so that all the input Y and R values would be bounded above 0 (at least eps). Its default value is 1e-10

#### **Details**

eps

In this function we allow it to characterize time-varying proportions of susceptible due to government-enforced stringent in-home isolation. We expanded the SIR model by adding a quarantine compartment with a time-varying rate of quarantine  $\phi_t$ , the chance of a susceptible person being willing to take in-home isolation at time t.

#### Value

casename the predefined casename.

incidence\_mean mean cumulative incidence, the mean prevalence of cumulative confirmed cases

at the end of the study.

incidence\_ci 2.5%, 50%, and 97.5% quantiles of the incidences.

out\_table summary tables including the posterior mean of the prevalance processes of the 3 states compartments  $(\theta_t^S, \theta_t^I, \theta_t^R, \theta_t^H)$  at last date of data collected ((t') decided

by the lengths of your input data Y and R), and their respective credible inctervals (ci); the respective means and ci's of the reporduction number (R0), removed

rate  $(\gamma)$ , transmission rate  $(\beta)$ .

plot\_infection plot of summarizing and forecasting for the infection compartment, in which

the vertial blue line denotes the last date of data collected (t'), the vertial dark-gray line denotes the deacceleration point (first turning point) that the posterior mean first-derivative of infection prevalence  $\dot{\theta}_t^I$  achieves the maximum, the vertical purple line denotes the second turning point that the posterior mean first-derivative infection proportion  $\dot{\theta}_t^I$  equals zero, the darkgray line denotes the posterior mean of the infection prevalence  $\theta_t^I$  and the red line denotes its posterior

median.

plot\_removed plot of summarizing and forecasting for the removed compartment with lines

similar to those in the plot\_infection. The vertical lines are identical, but the horizontal mean and median correspond to the posterior mean and median of the removed process  $\theta_t^R$ . An additional line indicates the estimated death prevalence

from the input death\_in\_R.

spaghetti\_plot 20 randomly selected MCMC draws of the first-order derivative of the posterior prevalence of infection, namely  $\dot{\theta}_t^I$ . The black curve is the posterior mean of the derivative, and the vertical lines mark times of turning points corresponding

4 qh.eSIR

respectively to those shown in plot\_infection and plot\_removed. Moreover, the 95% credible intervals of these turning points are also highlighted by semi-transparent rectangles.

first\_tp\_mean

the date t at which  $\theta_t^I=0$ , calculated as the average of the time points with maximum posterior first-order derivatives  $\dot{\theta}_t^I$ ; this value may be slightly different from the one labeled by the "darkgreen" lines in the two plots plot\_infection and plot\_removed, which indicate the stationary point such that the first-order derivative of the averaged posterior of  $\theta_t^I$  reaches its maximum.

first\_tp\_mean

the date t at which  $\ddot{\theta}_t^I=0$ , calculated as the average of the time points with maximum posterior first-order derivatives  $\dot{\theta}_t^I$ ; this value may be slightly different from the one labeled by the "darkgreen" lines in the two plots plot\_infection and plot\_removed, which indicate the stationary point such that the first-order derivative of the averaged posterior of  $\theta_t^I$  reaches its maximum.

first\_tp\_ci

fwith first\_tp\_mean, it reports the corresponding credible interval and median.

second\_tp\_mean

the date t at which  $\theta_t^I=0$ , calculated as the average of the stationary points of all of posterior first-order derivatives  $\dot{\theta}_t^I$ ; this value may be slightly different from the one labeled by the "pruple" lines in the plots of plot\_infection and plot\_removed. The latter indicate stationary t at which the first-order derivative of the averaged posterior of  $\theta_t^I$  equals zero.

second\_tp\_ci

with second\_tp\_mean, it reports the corresponding credible interval and median.

dic\_val

the output of dic.samples() in dic.samples, computing deviance information criterion for model comparison.

## **Examples**

```
## Not run:
NI_complete <- c( 41,41,41,45,62,131,200,270,375,444,549, 729,
             1052,1423,2714,3554,4903,5806,7153,9074,11177,
             13522, 16678, 19665, 22112, 24953, 27100, 29631, 31728, 33366)
RI_complete <- c(1,1,7,10,14,20,25,31,34,45,55,71,94,121,152,213,
             252, 345, 417, 561, 650, 811, 1017, 1261, 1485, 1917, 2260,
             2725,3284,3754)
N=58.5e6
R <- RI_complete/N
Y <- NI_complete/N- R #Jan13->Feb 11
change_time <- c("01/23/2020","02/04/2020","02/08/2020")
phi0 <- c(0.1,0.4,0.4)
res.q \leftarrow qh.eSIR (Y,R,begin_str="01/13/2020",death_in_R = 0.4,
                  phi0=phi0,change_time=change_time,
                 casename="Hubei_q",save_files = T,save_mcmc = F,
                 M=5e2, nburnin = 2e2)
res.q$plot_infection
#res.q$plot_removed
res.noq <- qh.eSIR (Y,R,begin_str="01/13/2020",death_in_R = 0.4,
                     T_fin=200, casename="Hubei_noq",
                     M=5e2, nburnin = 2e2)
res.noq$plot_infection
## End(Not run)
```

raies	tvt.eSIR	Fit extended state-space SIR model with time-varying transmission rates
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## Description

Fit extended state-space SIR model with prespecified changes in the transmission rate, either stepwise or continuous, accomodating time-varying quaratine protocols.

## Usage

```
tvt.eSIR(Y, R, pi0 = NULL, change_time = NULL, exponential = FALSE,
  lambda0 = NULL, begin_str = "01/13/2020", T_fin = 200,
  nchain = 4, nadapt = 10000, M = 500, thn = 10, nburnin = 200,
  dic = FALSE, death_in_R = 0.02, beta0 = 0.2586, gamma0 = 0.0821,
  R0 = beta0/gamma0, gamma0_sd = 0.1, R0_sd = 1,
  casename = "tvt.eSIR", file_add = character(0), add_death = FALSE,
  save_files = FALSE, save_mcmc = FALSE, save_plot_data = FALSE,
  eps = 1e-10)
```

## **Arguments**

Υ	the time series of daily observed infected compartment proportions.
R	the time series of daily observed removed compartment proportions, including death and recovered.
pi0	the time-dependent transission rate modifier $\pi(t)$ between 0 and 1.
change_time	the change points over time for step function pi, defalt value is NULL.
exponential	logical, whether $\pi(t)$ is exponential $\exp(-\lambda_0 t)$ or not; the default is FALSE.
lambda0	the rate of decline in the exponential survival function in $\exp(-\lambda_0 t)$ .
begin_str	the character of starting time, the default is "01/13/2020".
T_fin	the end of follow-up time after the beginning date begin_str, the default is 200.
nchain	the number of MCMC chains generated by rjags, the default is 4.
nadapt	the iteration number of adaptation in the MCMC. We recommend using at least the default value 1e4 to obtained fully adapted chains.
М	the number of draws in each chain, with no thinning. The default is $M=5e2$ but suggest using $5e5$ .
thn	the thinning interval between mixing. The total number of draws thus would become round(M/thn)*nchain. The default is 10.
nburnin	the burn-in period. The default is 2e2 but suggest 2e5.
dic	logical, whether compute the DIC (deviance information criterion) for model selection.
death_in_R	the numeric value of average of cumulative deaths in the removed compartments. The default is 0.4 within Hubei and 0.02 outside Hubei.
beta0	the hyperparameter of average transmission rate, the default is the one estimated from the SARS first-month outbreak $(0.2586)$ .

gamma0 the hyperparameter of average removed rate, the default is the one estimated

from the SARS first-month outbreak (0.0821).

R0 the hyperparameter of the mean reproduction number R0. The default is thus

the ratio of beta0/gamma0, which can be specified directly.

gamma0\_sd the standard deviation for the prior distribution of the removed rate  $\gamma$ , the default

is 0.1.

R0\_sd the standard deviation for the prior disbution of R0, the default is 1.

casename the string of the job's name. The default is "tvt.eSIR".

file\_add the string to denote the location of saving output files and tables.

add\_death logical, whether add the approximate death curve to the plot, default is false.

save\_files logical, whether save (TRUE) results or not (FALSE). This enables to save sum-

mary tables, trace plots, and plots of the posterior means of the first-order deriva-

tives of the infection prevalence process  $\theta_t^I$ .

save\_mcmc logical, whether save (TRUE) all the MCMC outputs or not (FALSE). The out-

put file will be an .RData file named by the *casename*. We include arrays of prevalence values of the three compartments with their matrices of posterior draws up to the last date of the collected data as theta\_p[,,1] and afterwards as theta\_pp[,,1] for  $\theta_t^S$ , theta\_p[,,2] and theta\_pp[,,2] for  $\theta_t^I$ , and theta\_pp[,,3] and theta\_pp[,,3] for  $\theta_t^R$ . Moreover, the input and predicted proportions Y, Y\_pp, R and R\_pp can also be retrieved. The prevalence and predicted proportion matrices have rows for MCMC replicates, and columns for days. The MCMC posterior draws of other parameters including beta\_p, gamma\_p, R0\_p, and variance controllers k\_p, lambdaY\_p, lambdaR\_p are also

available.

save\_plot\_data logical, whether save the plotting data or not.

eps a non-zero controller so that all the input Y and R values would be bounded above

0 (at least eps). Its default value is 1e-10

save\_files logical, whether to save plots to file.

#### **Details**

We fit a state-space model with extended SIR, in which a time-varying transmission rate modifier  $\pi(t)$  (between 0 and 1) is introcuded to model. This allows us to accommodate quarantine protocol changes and ignored resources of hospitalization. The form of reducing rate may be a step-function with jomps at times of big policy changes or a smooth exponential survival function  $\exp(-\lambda_0 t)$ . The parameters of the function and change points, if any, should be predefined.

## Value

casename the predefined casename.

incidence\_mean mean cumulative incidence, the mean prevalence of cumulative confirmed cases

at the end of the study.

incidence\_ci 2.5%, 50%, and 97.5% quantiles of the incidences.

out\_table summary tables including the posterior mean of the prevalance processes of the

3 states compartments  $(\theta_t^S, \theta_t^I, \theta_t^R)$  at last date of data collected ((t') decided by the lengths of your input data Y and R), and their respective credible inctervals (ci); the respective means and ci's of the reporduction number (R0), removed

rate  $(\gamma)$ , transmission rate  $(\beta)$ .

plot\_infection plot of summarizing and forecasting for the infection compartment, in which the vertial blue line denotes the last date of data collected (t'), the vertial darkgray line denotes the deacceleration point (first turning point) that the posterior mean first-derivative of infection prevalence  $\dot{\theta}_t^I$  achieves the maximum, the vertical purple line denotes the second turning point that the posterior mean firstderivative infection proportion  $\dot{\theta}_t^I$  equals zero, the darkgray line denotes the posterior mean of the infection prevalence  $\theta_t^I$  and the red line denotes its posterior median.

plot\_removed

plot of summarizing and forecasting for the removed compartment with lines similar to those in the plot\_infection. The vertical lines are identical, but the horizontal mean and median correspond to the posterior mean and median of the removed process  $\theta_t^R$ . An additional line indicates the estimated death prevalence from the input death\_in\_R.

spaghetti\_plot

20 randomly selected MCMC draws of the first-order derivative of the posterior prevalence of infection, namely  $\dot{\theta}_t^I$ . The black curve is the posterior mean of the derivative, and the vertical lines mark times of turning points corresponding respectively to those shown in plot\_infection and plot\_removed. Moreover, the 95% credible intervals of these turning points are also highlighted by semitransparent rectangles.

first\_tp\_mean

the date t at which  $\ddot{\theta}_t^I = 0$ , calculated as the average of the time points with maximum posterior first-order derivatives  $\dot{\theta}_t^I$ ; this value may be slightly different from the one labeled by the "darkgreen" lines in the two plots plot\_infection and plot\_removed, which indicate the stationary point such that the first-order derivative of the averaged posterior of  $\theta_t^I$  reaches its maximum.

first\_tp\_ci

fwith first\_tp\_mean, it reports the corresponding credible interval and median.

second\_tp\_mean the date t at which  $\theta_I^I = 0$ , calculated as the average of the stationary points of all of posterior first-order derivatives  $\dot{\theta}_t^I$ ; this value may be slightly different from the one labeled by the "pruple" lines in the plots of plot\_infection and plot\_removed. The latter indicate stationary t at which the first-order derivative of the averaged posterior of  $\theta_t^I$  equals zero.

second\_tp\_ci

with second\_tp\_mean, it reports the corresponding credible interval and median.

dic\_val

the output of dic.samples() in dic.samples, computing deviance information criterion for model comparison.

## **Examples**

```
## Not run:
NI_complete <- c( 41,41,41,45,62,131,200,270,375,444,549, 729,
                   1052,1423,2714,3554,4903,5806,7153,9074,11177,
                13522, 16678, 19665, 22112, 24953, 27100, 29631, 31728, 33366)
RI_complete <- c(1,1,7,10,14,20,25,31,34,45,55,71,94,121,152,213,
                  252, 345, 417, 561, 650, 811, 1017, 1261, 1485, 1917, 2260,
                  2725,3284,3754)
N=58.5e6
R \leftarrow RI\_complete/N
Y <- NI_complete/N- R #Jan13->Feb 11
### Step function of pi(t)
change_time <- c("01/23/2020","02/04/2020","02/08/2020")
pi0 < -c(1.0, 0.9, 0.5, 0.1)
res.step <-tvt.eSIR(Y,R,begin_str="01/13/2020",death_in_R = 0.4,
         T_fin=200,pi0=pi0,change_time=change_time,dic=T,
```

```
casename="Hubei_step",save_files = T,
         save_mcmc=F,M=5e2,nburnin = 2e2)
res.step$plot_infection
res.step$plot_removed
res.step$dic_val
### continuous exponential function of pi(t)
res.exp <- tvt.eSIR(Y,R,begin_str="01/13/2020",death_in_R = 0.4,
           T_fin=200,exponential=TRUE,dic=F,lambda0=0.05,
           casename="Hubei_exp",save_files = F,save_mcmc=F,
           M=5e2, nburnin = 2e2)
res.exp$plot_infection
#res.exp$plot_removed
### without pi(t), the standard state-space SIR model without intervention
res.nopi <- tvt.eSIR(Y,R,begin_str="01/13/2020",death_in_R = 0.4,</pre>
                T_fin=200,casename="Hubei_nopi",save_files = F,
                M=5e2, nburnin = 2e2)
res.nopi$plot_infection
#res.nopi$plot_removed
## End(Not run)
```

## Index

```
dic.samples, 4, 7
qh.eSIR, 1
rjags, 2, 5
tvt.eSIR, 5
```