ECE351: Signals and Systems I - Fall 2023 - Dr. Thinh Nguyen Homework 5 Due 11/01/2023

1. Determine the DTFTs of the following signals:

(a)
$$x[n] = \left(\frac{3}{4}\right)^n u[n-4]$$

(b)
$$x[n] = a^{|n|} |a| < 1$$

(c)
$$x[n] = 2\delta[4 - 2n]$$

(d)
$$x[n] = \delta[n+4] + \delta[n+2] + \delta[n-2] - \delta[n-4]$$

(e)
$$x[n] = \begin{cases} \frac{1}{2} + \frac{1}{2}\cos(\frac{\pi}{N}n), & |n| \le N \\ 0, & \text{otherwise} \end{cases}$$

2. Determine the inverse DTFTs of the following frequency representations:

(a)
$$X(e^{j\Omega}) = \cos(2\Omega) + j\sin(2\Omega)$$

(b)
$$X(e^{j\Omega}) = \sin(\Omega) + \cos(\frac{\Omega}{2})$$

(c)
$$|X(e^{j\Omega})| = \begin{cases} 1, & \frac{\pi}{4} \le |\Omega| \le \frac{3\pi}{4} \\ 0, & \text{otherwise} \end{cases}$$

$$argX(e^{j\Omega}) = -4\Omega$$