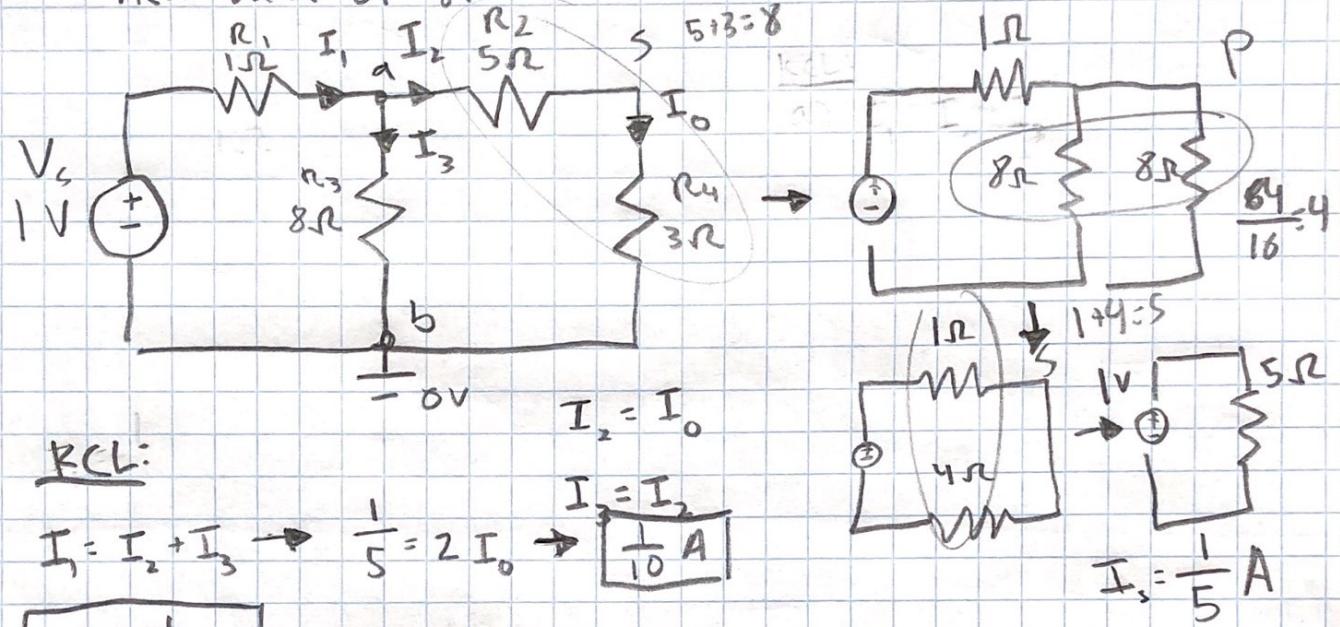


Chris Hunt

Homework 4

ENGR201

4.1) Find I_o , then increase V_s to 12V \rightarrow what is the new value of I_o ?

RCL:

$$I_1 = I_2 + I_3 \rightarrow \frac{1}{5} = 2 I_o \rightarrow I_o = \boxed{\frac{1}{10} A}$$

$$\boxed{I_o = \frac{1}{10} A}$$

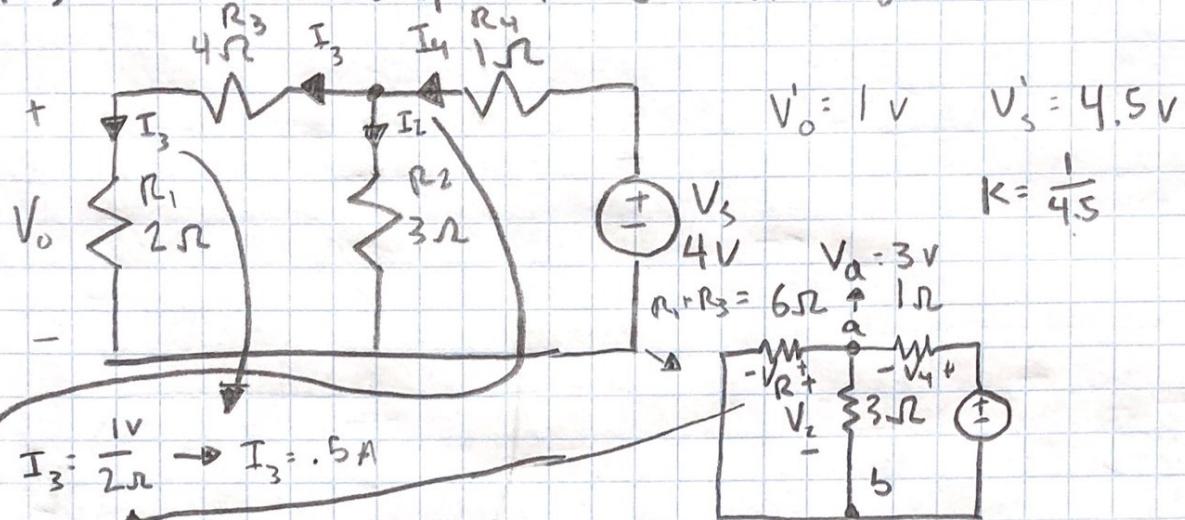
When V_s is increased to 12V I_o will increase proportionally due to linearity.

$$12 \cdot 1V = 12V \text{ therefore } 12 \cdot \frac{1}{10} A = \boxed{\frac{12}{10} A}$$

Chris Hunt

Homework 4

ENGR 201

4.2) Use the unit output method to find V_o 

$$I_3 = \frac{1V}{2\Omega} \rightarrow I_3 = .5A$$

$$V_2 = V_R = 6\Omega \cdot .5A = 3V = V_a$$

$$\Delta I_2 = \frac{3V}{3\Omega} = 1A$$

$$I_4 = I_3 + I_2 \rightarrow I_4 = 1.5A$$

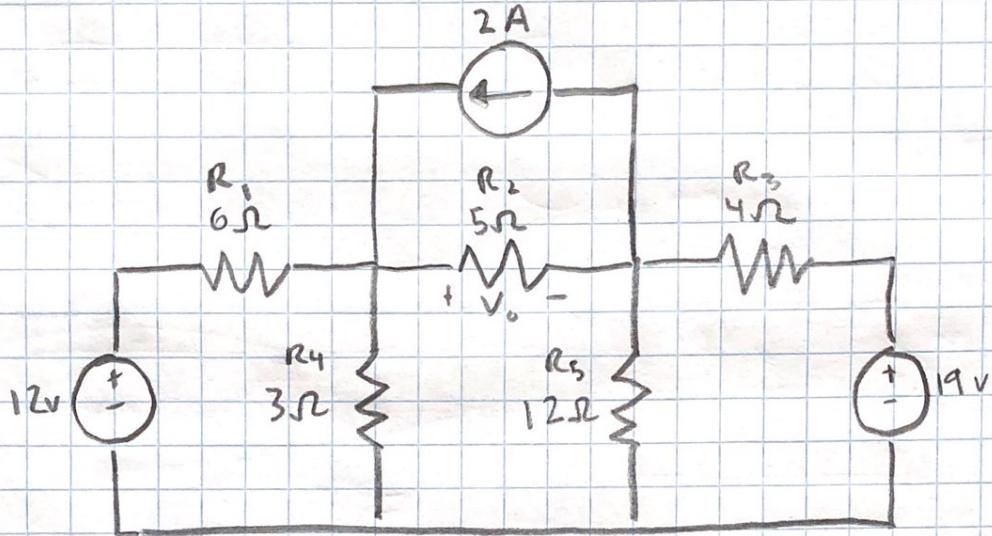
$$V_4 = 1.5A \cdot 1\Omega = 1.5V \rightarrow V'_s = V_a + V_4 \rightarrow V'_s = 4.5V$$

$$V_o = V_s \left(\frac{V'_o}{V'_s} \right) \rightarrow V_o = 4 \left(\frac{1}{4.5} \right) = \frac{4}{4.5} = .88V$$

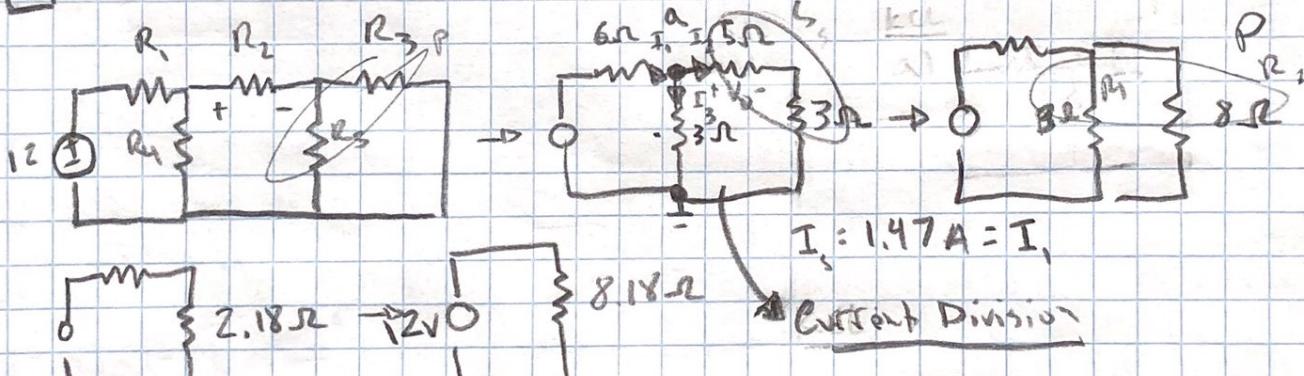
$$\boxed{V_o = .88V}$$

Chris Hunt

4.3) Find V_o using superposition



1

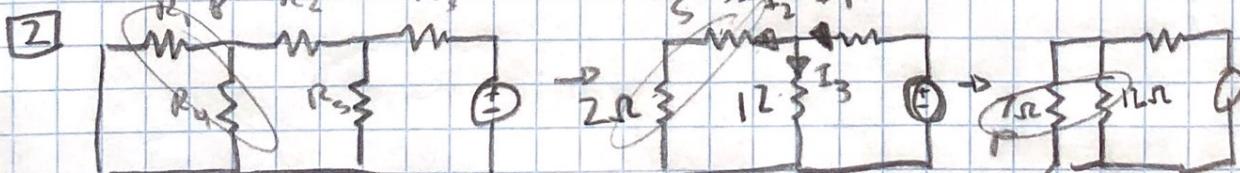


$$I_s = 1.47 A = I_1$$

Current Division

$$I_s = -3.54 \cdot 1.47 A$$

$$V_{o1} = 2.5 V \leftarrow V_{o1} = I_2 \cdot R_2 \leftarrow I_2 = 1.4 A$$

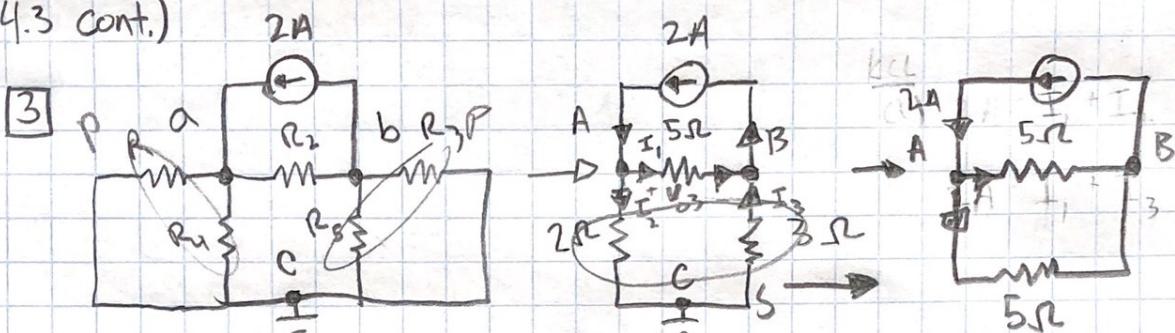


$$I_s = 2.256 \cdot I_1 \rightarrow I_2 = \frac{12}{19} \cdot I_1 = 1.425 A$$

$$V_{o2} = I_2 \cdot R_2 \rightarrow V_{o2} = 7.125 V$$

Chris Hunt

4.3 cont.)



Current Division

$$I_1 = \frac{R_2}{R_1 + R_2} \cdot I \rightarrow I_1 = \frac{1}{2}(2\text{A}) \rightarrow I_1 = 1\text{A}$$

$$V_{O3} = 1\text{A} \cdot 5\Omega \Rightarrow V_{O3} = 5\text{V}$$

Superposition:

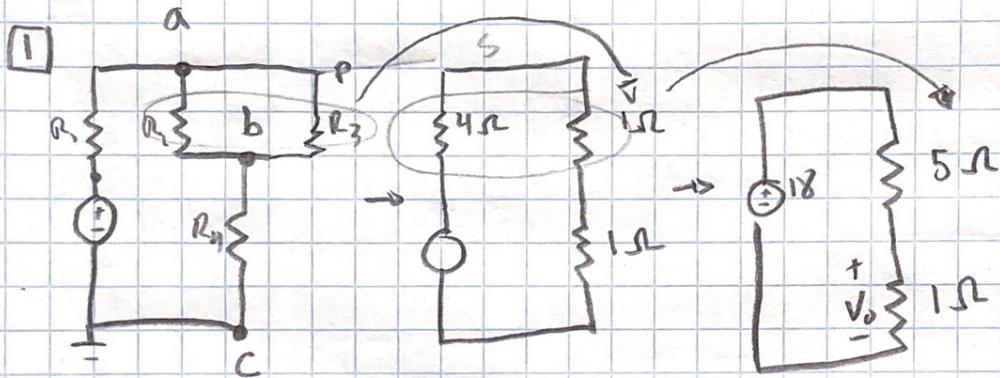
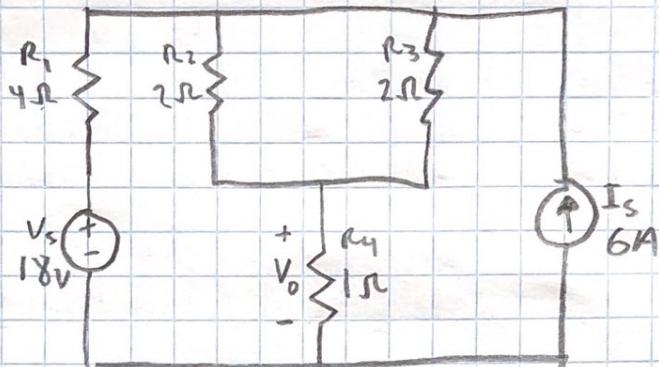
$$V_o = V_{o1} - V_{o2} + V_{o3}$$

$$V_o = 2\text{V} - 7.125\text{V} + 5\text{V} = -1.125\text{V}$$

$$\boxed{V_o = -1.125\text{V}}$$

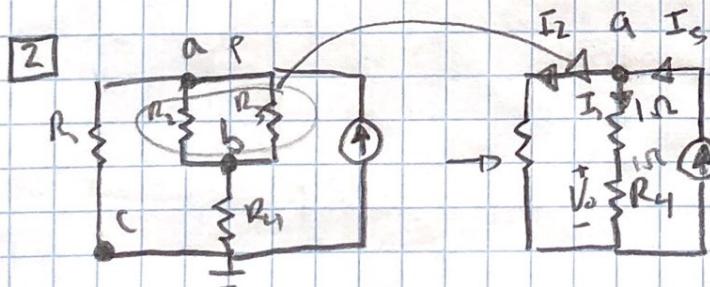
Chris Hunt

4.4) Find V_o



Voltage Division:

$$V_{o1} = \frac{1\Omega}{1+5\Omega} \cdot 18 \rightarrow V_{o1} = 3V$$



Current Division:

$$I_1 = \frac{4\Omega}{6\Omega} \cdot 6A$$

$$I_1 = 4A$$

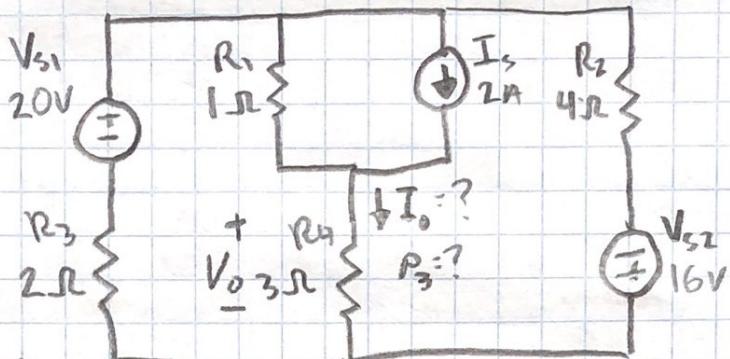
$$V_{o2} = 1\Omega \cdot 4A$$

$$V_{o2} = 4V$$

$$V_o = 3V + 4V \Rightarrow V_o = 7V$$

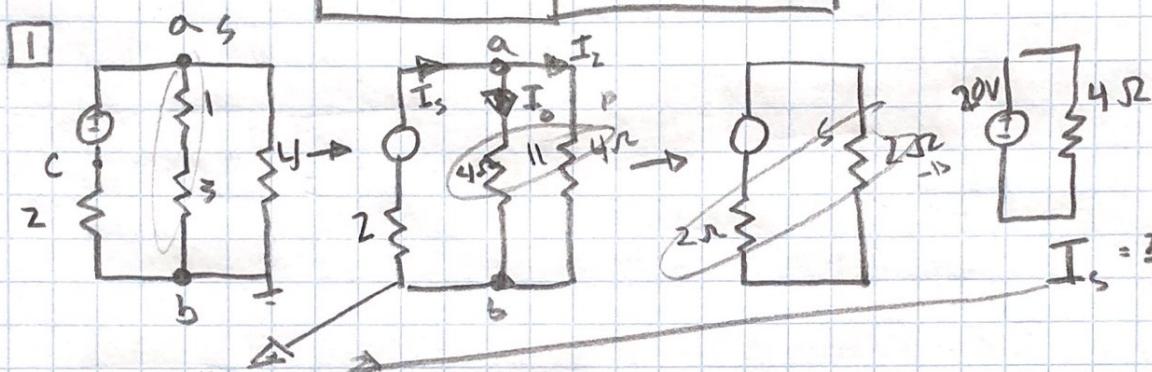
Chris Hunt

4.5)



Find I_o

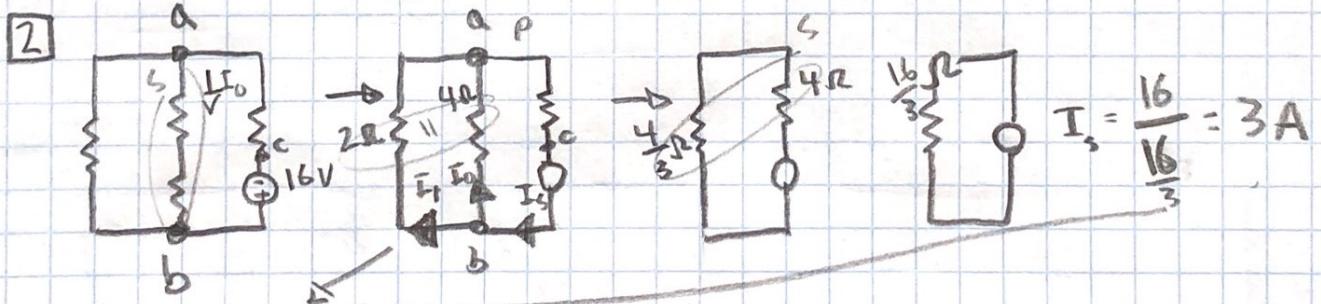
Find P_3



$$I_s = \frac{20V}{4\Omega} = 5A$$

Current Division:

$$I_o = 5 \cdot \frac{4}{8} \Rightarrow I_{o1} = 2.5A$$



$$I_s = \frac{16}{\frac{16}{3}} = 3A$$

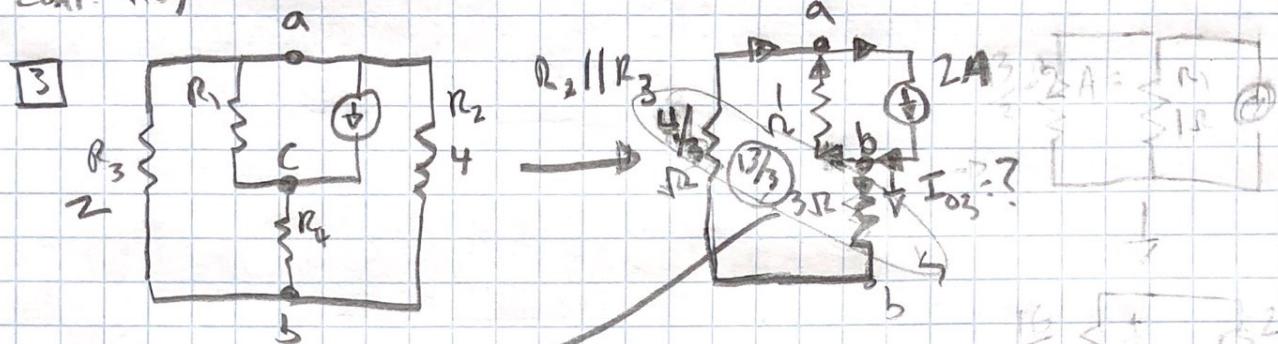
Current Division:

$$I_{o1} = \frac{2}{6} \cdot 3A \Rightarrow I_{o1} = 1A$$



Chris Hunt

cont. 4.S)



Current Division:

$$I_{03} = \frac{1}{13/3 \Omega} \cdot 2A \rightarrow I_{03} = 0.375A$$

$$I_o = I_{o1} - I_{o2} + I_{o3}$$

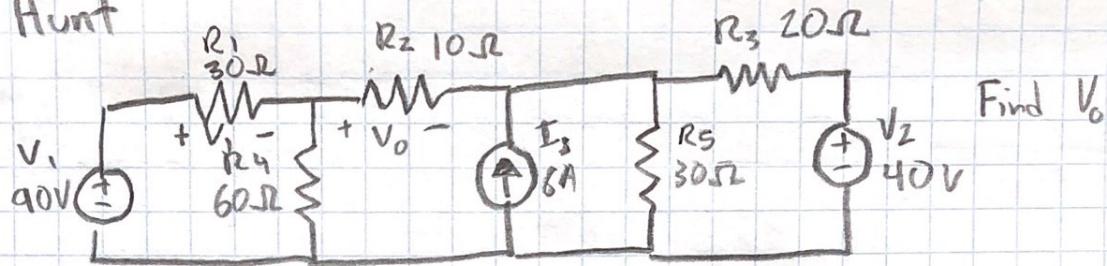
$$\boxed{I_o = 1.875A}$$

$$P = \frac{i^2}{G} = \frac{1.875^2}{1/3}$$

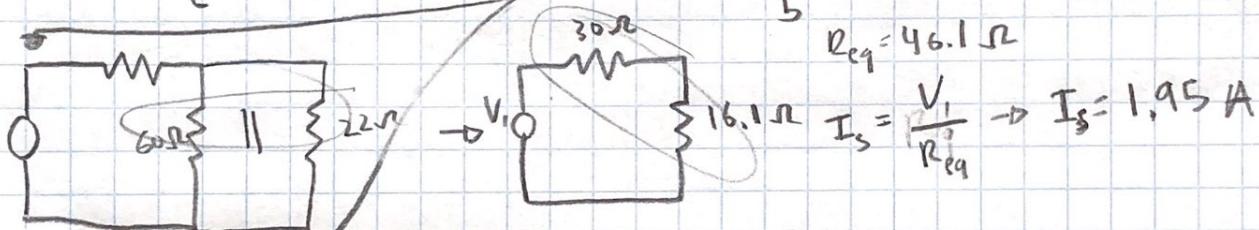
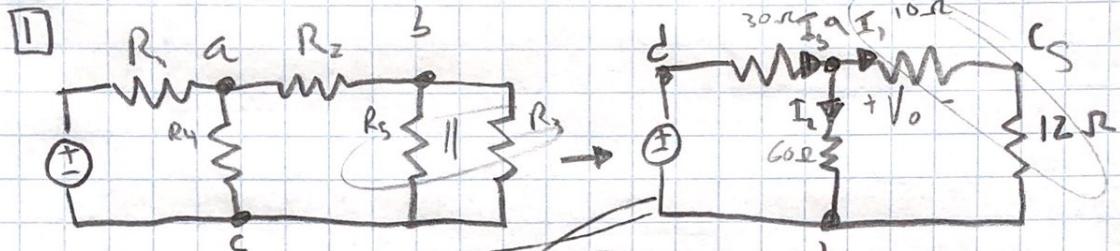
$$\boxed{P = 9.99 W}$$

Chris Hunt

4.6)

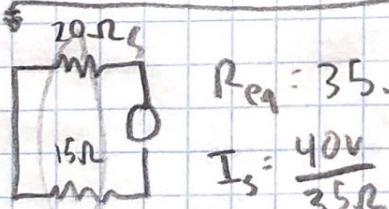
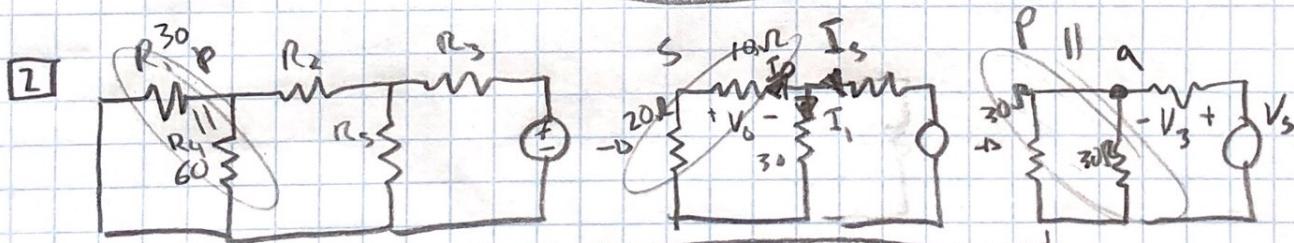


Find V_o



$$V_a = V_s - V_1 = 90V - (1.95 \cdot 30\Omega) = 31.43V$$

$$V_o = V_a \cdot \frac{10\Omega}{22\Omega} \rightarrow V_o = 14.29V$$



$$V_a = V_s - V_3$$

$$V_a = 40V - 22.86V$$

$$V_a = 17.14V$$

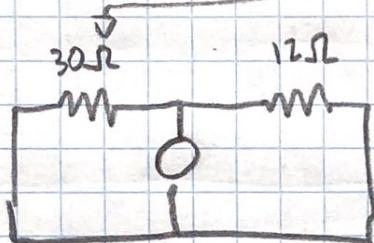
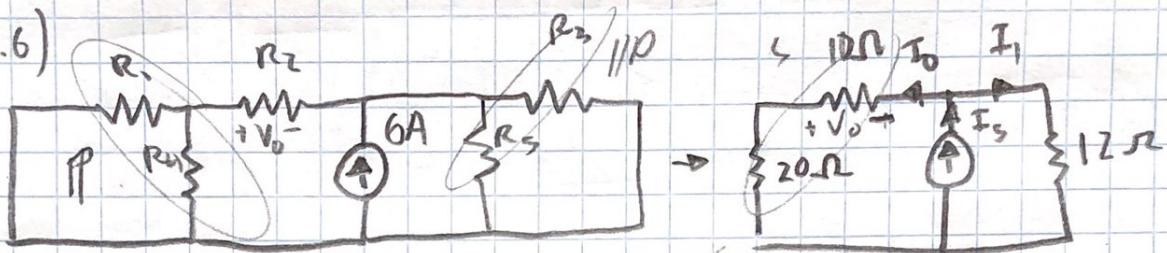
$$V_{o2} = V_a \cdot \frac{10\Omega}{30\Omega} \rightarrow V_{o2} = 5.71V$$



Chris Hunt

cont. 4.6)

3



Current Division

$$I_o = \frac{12}{42} \cdot 6A$$
$$I_o = 1.71 A$$

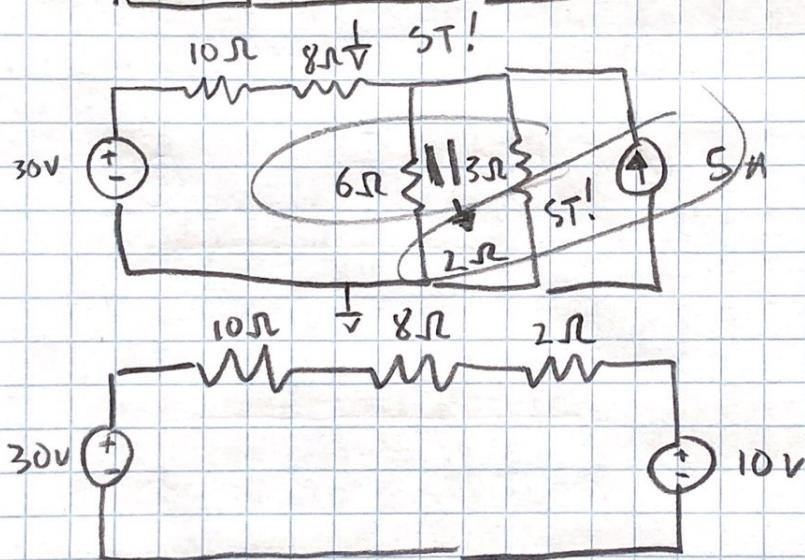
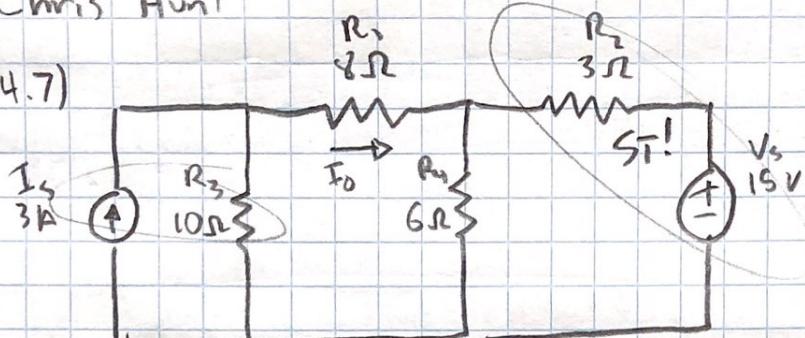
$$V_{o3} = 10\Omega \cdot 1.71 A$$
$$V_{o3} = 17.1 V$$

$$V_o = V_{o2} + V_{o3} - V_{o1}$$

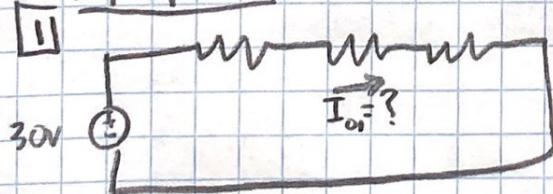
$$\boxed{V_o = -8.52 V}$$

Chris Hunt

4.7)

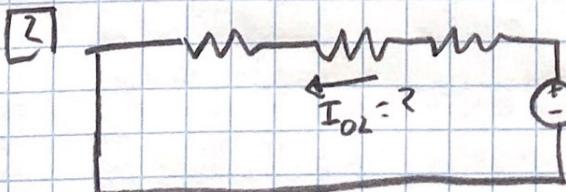


Superposition



$$R_{eq} = 10\Omega + 8\Omega + 2\Omega = 20\Omega$$

$$I_{o1} = \frac{30V}{20\Omega} \rightarrow I_{o1} = \frac{3}{2} A$$



$$I_{o2} = \frac{10V}{20\Omega} \rightarrow I_{o2} = -\frac{1}{2} A$$

$$I_o = \frac{3}{2} A - \frac{1}{2} A$$

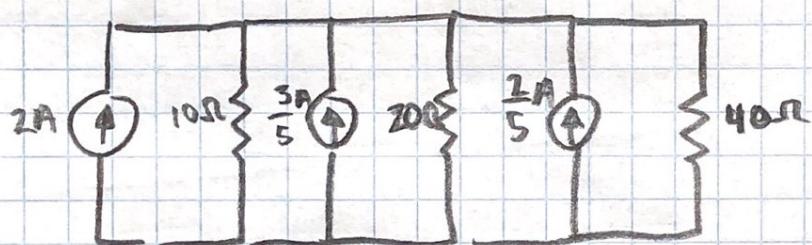
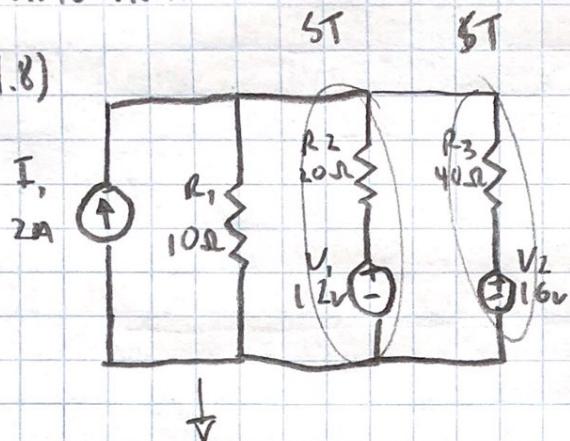
$$I_o = 1 A$$

$$P = \frac{I^2}{G} = \frac{I^2}{8}$$

$$P = 8 W$$

Chris Hunt

4.8)



$$\left(\frac{1}{R_{eq}} \right)^{-1} = \frac{1}{10} + \frac{1}{20} + \frac{1}{40} \rightarrow \frac{4}{40} + \frac{2}{40} + \frac{1}{40} \rightarrow \left(\frac{7}{40} \right)^{-1}$$

$$R_{eq} = \frac{40}{7} \Omega$$

Add all current sources in parallel

