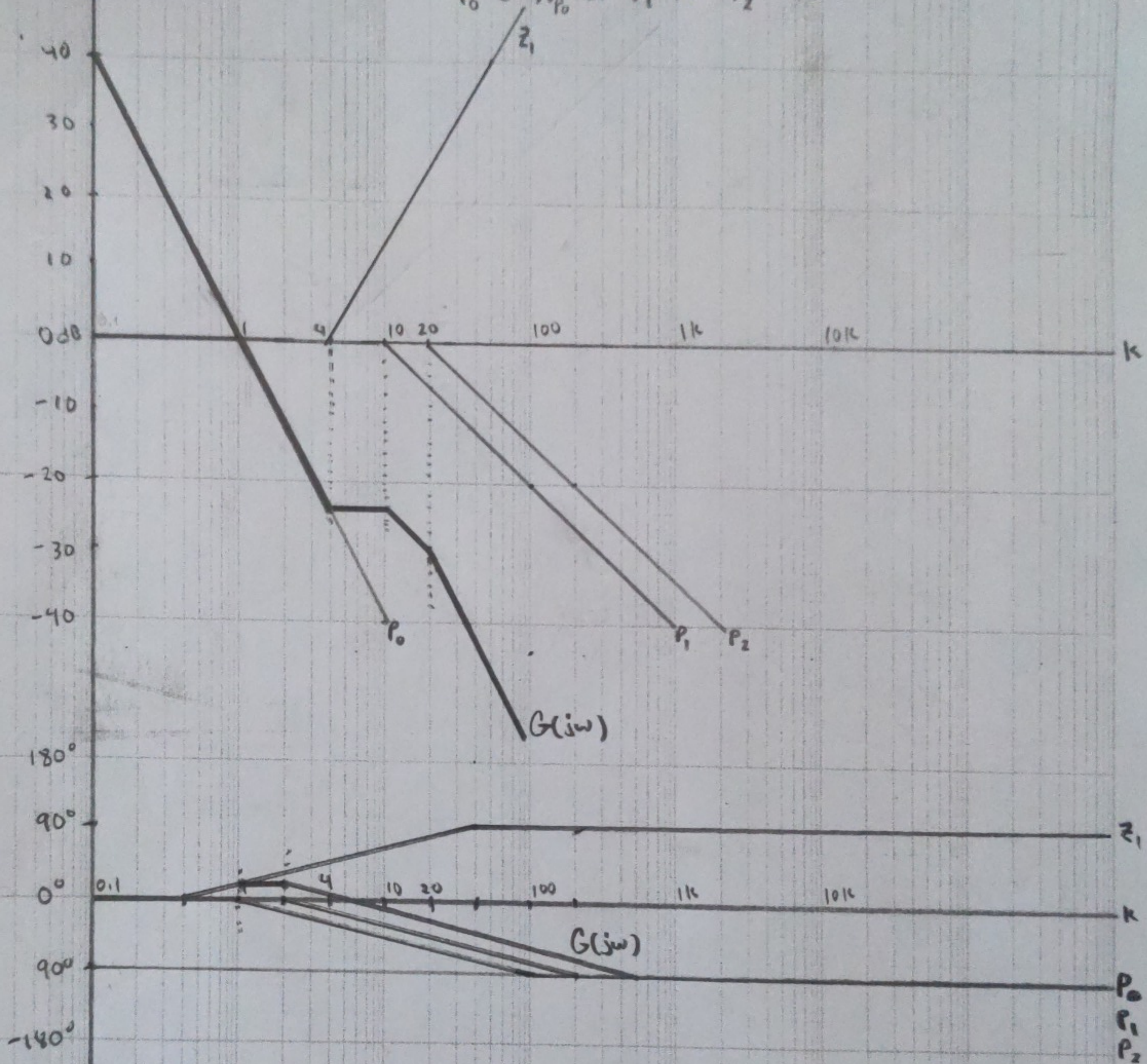


$$s=j\omega \quad G(s) = \frac{(s+4)^2}{s^2(\frac{s}{10}+1)(\frac{s}{20}+1)}$$

$$K = 20 \log_{10}(1) = 0 \text{ dB} \quad z_1 = 4 \quad N_{z_1} = 2$$

$$p_0 = 0 \quad N_{p_0} = 2 \quad p_1 = 10 \quad p_2 = 20$$





$$H(s) = \frac{30(s+10)}{s^2+3s+50}$$

$$s^2+3s+50$$

$$s^2+2\zeta\omega_n s+\omega_n^2$$

$$\omega_n^2 = 50$$

$$\omega_n = \sqrt{50}$$

$$2\zeta\omega_n = 3$$

$$\zeta = \frac{3}{2\omega_n}$$

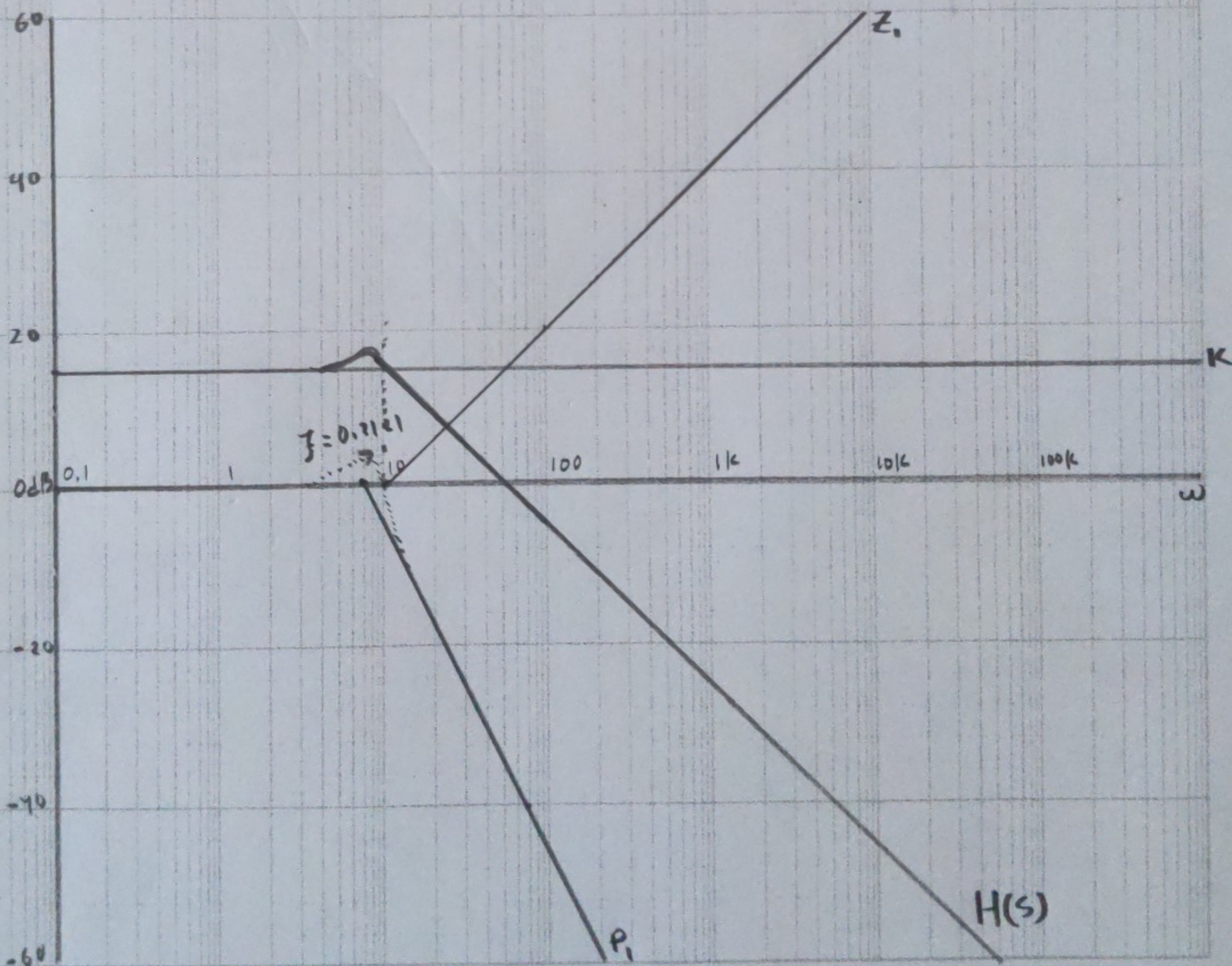
$$\zeta\omega_n = \alpha$$

$$\zeta = \frac{\alpha}{\omega_n} = \frac{3}{2\sqrt{50}} = 0.2121$$

$$H(s) = \frac{30(s+10)}{s^2+3s+50}$$

$$\rightarrow \frac{30 \cdot 10 \left(\frac{s}{10} + 1\right) \left(\frac{\omega_n^2}{\omega_n^2}\right)}{s^2 + 2\zeta\omega_n s + \omega_n^2} \rightarrow \frac{6\left(\frac{s}{10} + 1\right)}{s^2 + \frac{2\zeta s}{\omega_n} + 1}$$

$$K = 20 \log_{10}(6) = 15.6 \text{ dB} \quad Z_1 = 10 \quad P_1 = \sqrt{50} \approx 7$$

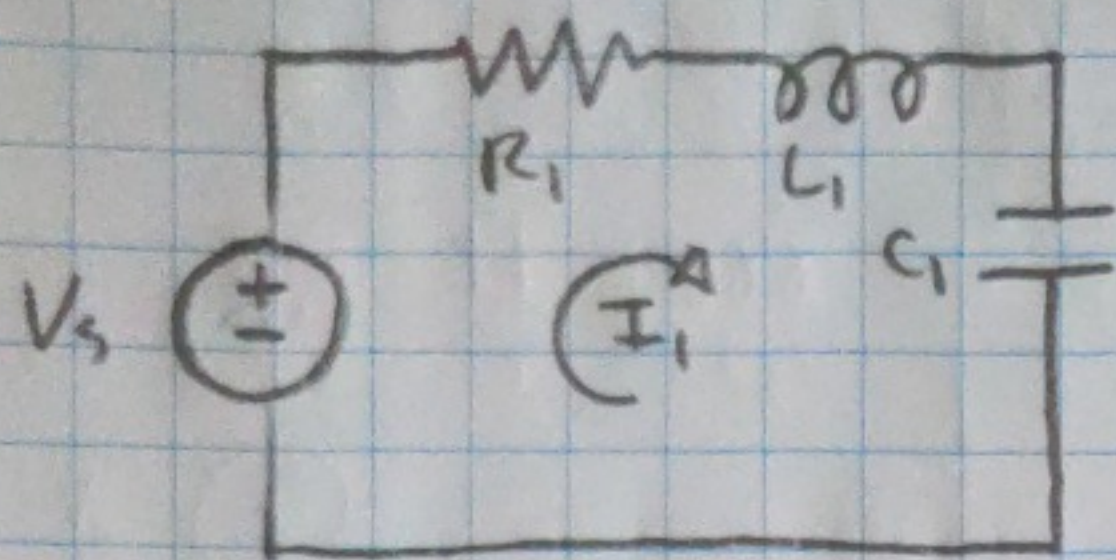




Chris Hunt

HW18

ENGR202

18.3) Find  $L_1$ ,  $Q$ , and  $B$  of the RLC circuit

$$\omega_0 = 6280 \text{ rad/s}$$

$$R_1 = 2.9 \Omega$$

$$C_1 = 47 \mu\text{F}$$

$$L_1 = ?$$

Find  $L_1$ )  $\omega_0 = \frac{1}{\sqrt{LC}} \text{ rad/s} \rightarrow L = \frac{1}{C\omega_0^2}$

$$L_1 = \frac{1}{47 \mu\text{F} \cdot 6280^2 \frac{\text{rad}^2}{\text{s}^2}} = \boxed{0.54 \text{ mH}}$$

Find  $Q$ )  $Q = \frac{\omega_0 L}{R} = \frac{1}{\omega_0 RC}$

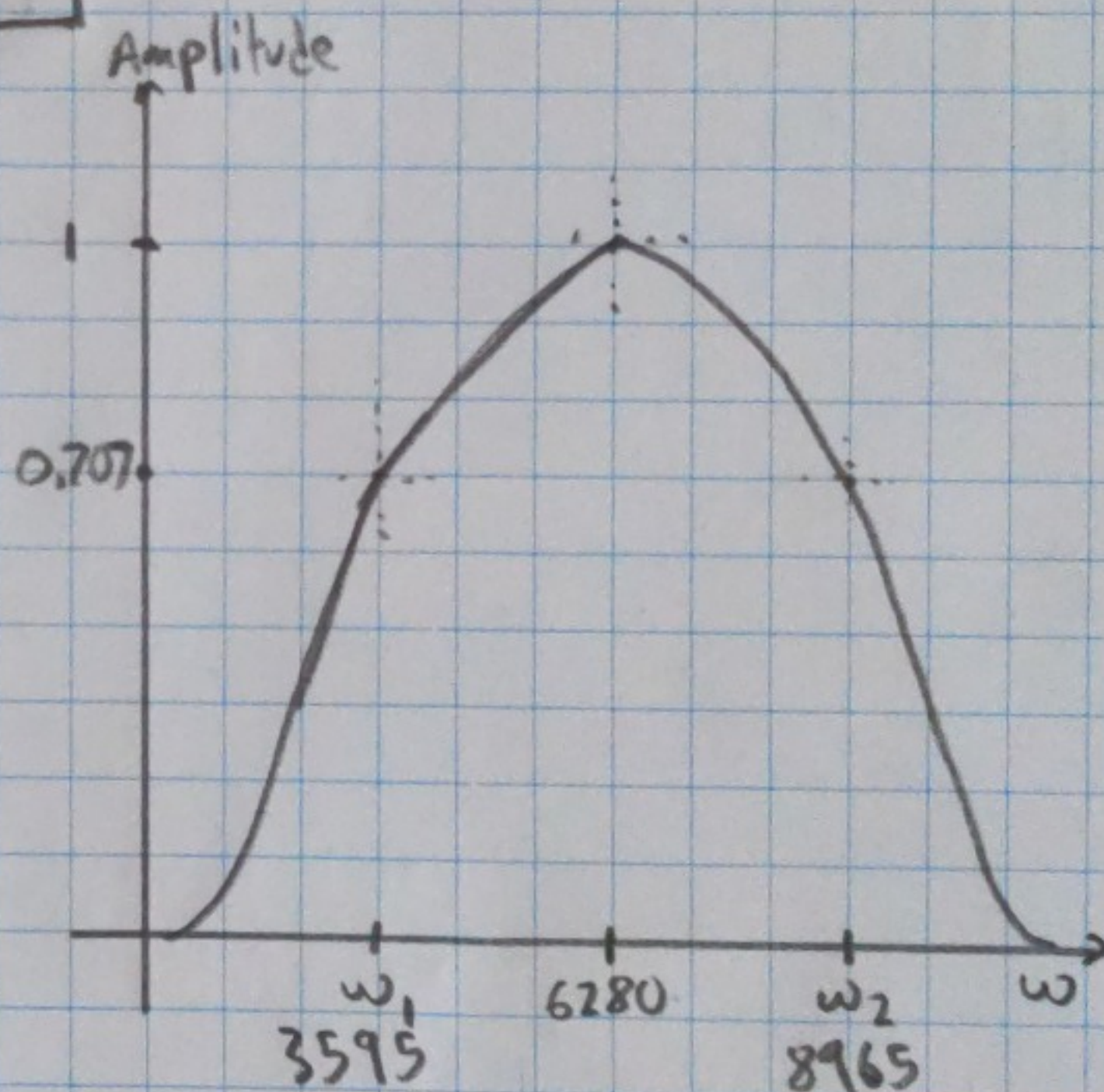
$$Q = \frac{6280 \frac{\text{rad}}{\text{s}} \cdot 0.54 \text{ mH}}{2.9 \Omega} = 1.17$$

Find  $B$ )  $B = \frac{R}{L} = \frac{\omega_0}{Q}$

$$B = \frac{2.9 \Omega}{0.54 \text{ mH}} = 5370 \text{ rad/s}$$

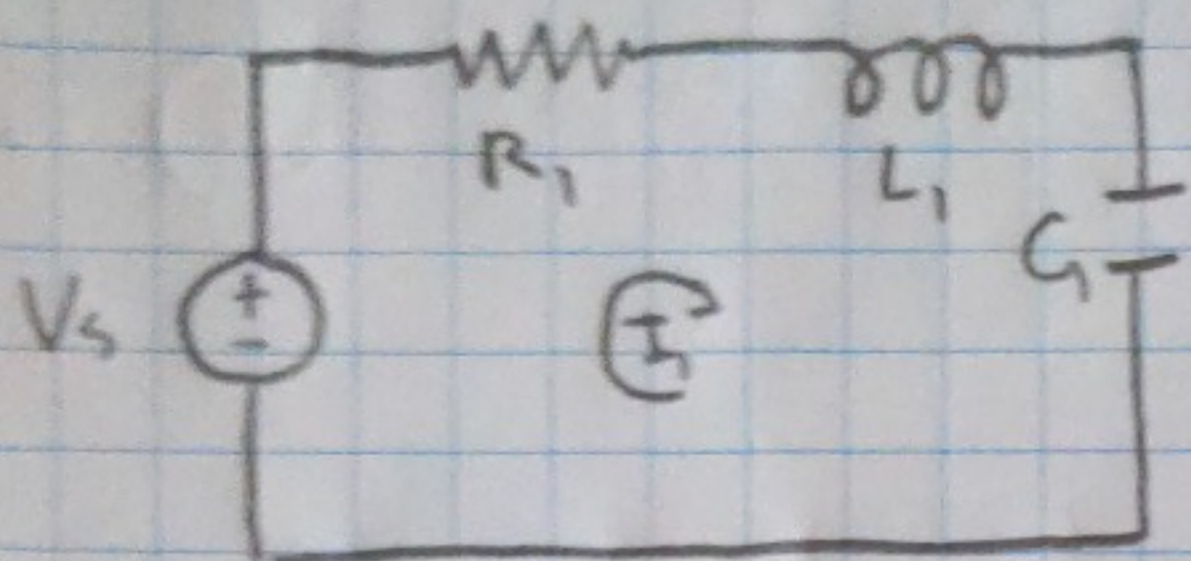
$$\omega_1 = 3595 \text{ rad/s}$$

$$\omega_2 = 8965 \text{ rad/s}$$





18.4) Find the values of  $L$ , and  $C$ , of a RLC circuit such that the circuit will be resonant at 100 kHz and have a bandwidth of 1 kHz



$$\omega_0 = 100 \text{ kHz} \cdot 2\pi \quad R_1 = 10 \Omega$$

$$B = 1 \text{ kHz}$$

$$C_1 = 1.59 \text{ nF}$$

$$L_1 = 1.59 \text{ nH}$$

$$\text{Find } L_1) \quad B = \frac{R}{L} \rightarrow L = \frac{R}{B}$$

$$L_1 = \frac{10 \Omega}{1 \text{ kHz} \cdot 2\pi} = \boxed{1.59 \text{ nH}}$$

$$\text{Find } C_1) \quad \omega_0 = \frac{1}{\sqrt{LC}} \rightarrow C = \frac{1}{L\omega_0^2}$$

$$C_1 = \frac{1}{1.59 \text{ nH} \cdot (100 \text{ kHz} \cdot 2\pi)^2} = \boxed{1.59 \text{ nF}}$$