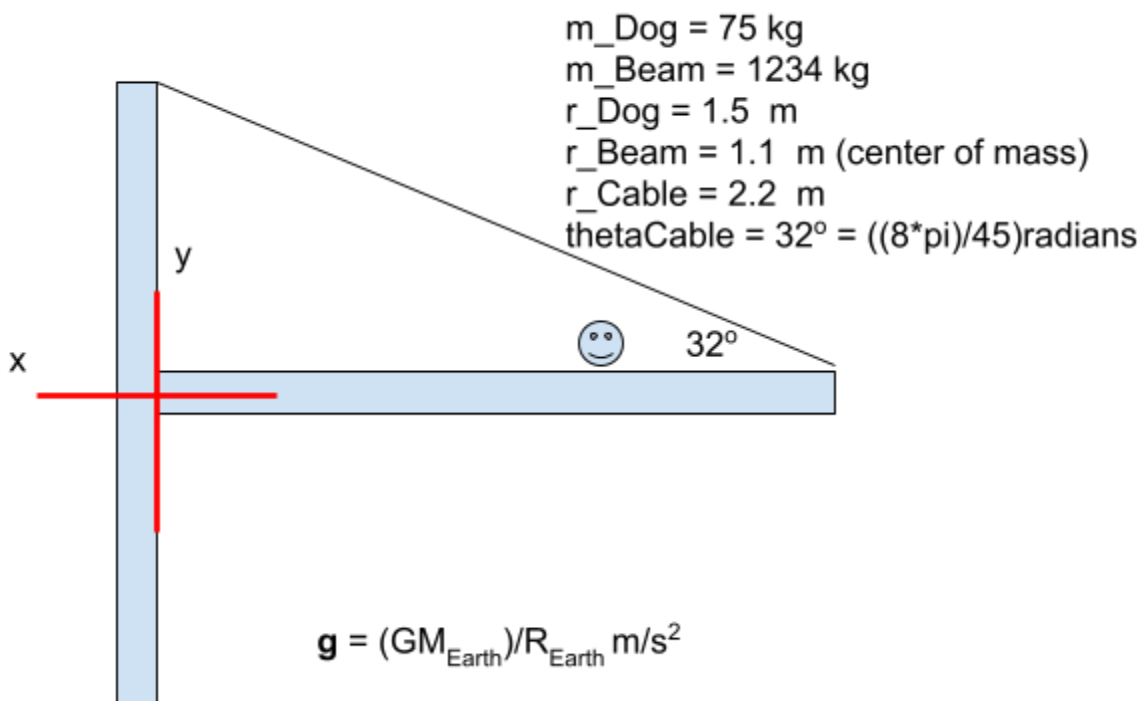


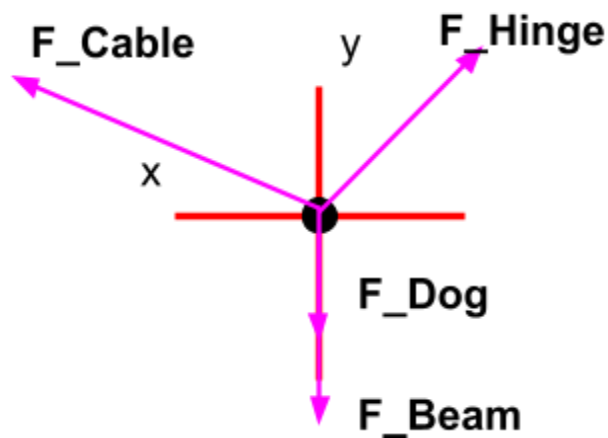
HIP 2

A 75kg dog sits down 1.5 meters of the way down a 2.2 meter long extended platform which is suspended from the end by a cable as shown. The platform has a mass of 1234kg. What is the Tension in the cable?

For this problem we assume that the beam, it's pivot point, the dog, and the cable are a closed system that are at static equilibrium - there is no acceleration occurring in the system. We will begin by drawing a picture of the scenario, and then creating a free body diagram with the coordinate system centered at the pivot point of the platform. Since this problem also includes rotational forces we will then draw a torque diagram. From here we will derive our equations and compute the answers.

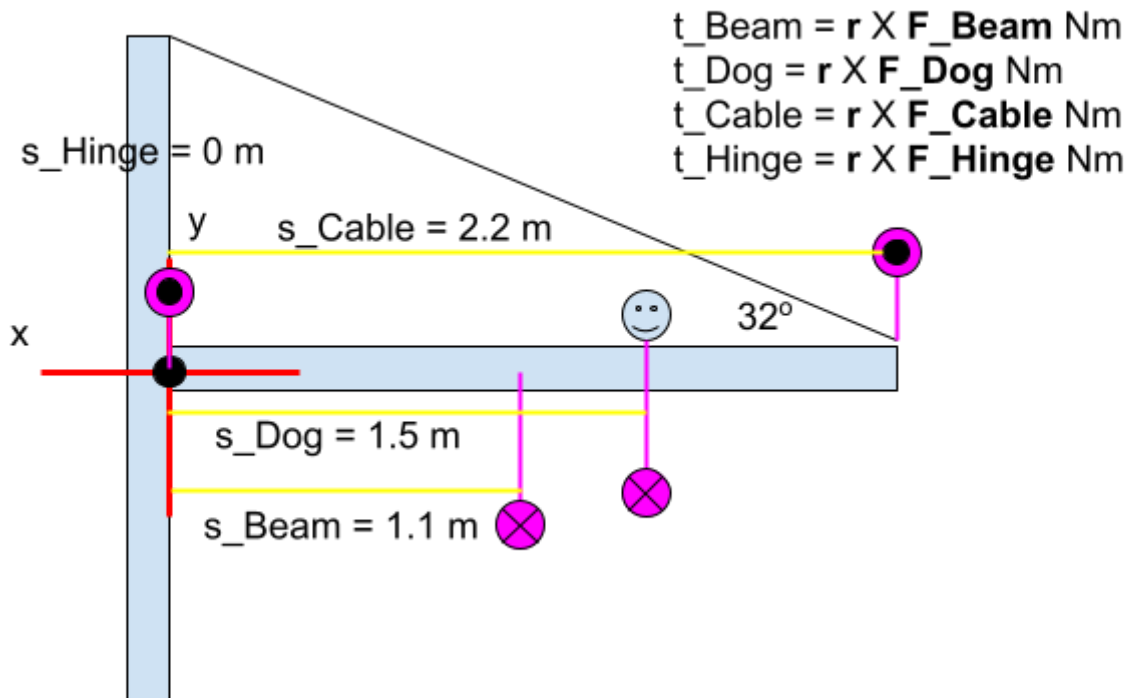


FBD of Pivot Point



$$\begin{aligned} F_{\text{Beam}} &= m_{\text{Beam}} \cdot g \text{ N} \\ F_{\text{Dog}} &= m_{\text{Dog}} \cdot g \text{ N} \\ F_{\text{Cable}} &= ? \text{ N} \\ F_{\text{Hinge}} &= ? \text{ N} \end{aligned}$$

Torque Diagram of Pivot Point



$$\begin{aligned} t_{\text{Beam}} &= r \times F_{\text{Beam}} \text{ Nm} \\ t_{\text{Dog}} &= r \times F_{\text{Dog}} \text{ Nm} \\ t_{\text{Cable}} &= r \times F_{\text{Cable}} \text{ Nm} \\ t_{\text{Hinge}} &= r \times F_{\text{Hinge}} \text{ Nm} \end{aligned}$$

Since we are assuming that the system is in static equilibrium we know that our sum of forces in the x and y directions will equal zero and we know that the sum of our torques will equal zero

$$\Sigma F_x = F_HingeMag*\cos(\theta_{Hinge}) + F_CableMag*\cos((8*\pi)/45) = 0 \text{ N}$$

$$\Sigma F_y = F_Dog + F_Beam + F_HingeMag*\sin(\theta_{Hinge}) + F_CableMag*\sin((8*\pi)/45) = 0 \text{ N}$$

$$\Sigma \tau = \tau_Dog + \tau_Beam + \tau_Cable + \tau_Hinge = 0 \text{ Nm}$$

Since we know that the hinge has a position vector of $\mathbf{s_Hinge} = \langle 0, 0, 0 \rangle$, if we attempt to find the torque caused by this force it will equal zero because taking the cross product of a zero vector will give us a zero vector.

$$\Sigma \tau = \tau_Dog + \tau_Beam + \tau_Cable + \tau_Hinge = 0 \text{ Nm} \rightarrow \tau_Dog + \tau_Beam + \tau_Cable = 0$$

$$\rightarrow \text{solve for } \tau_Cable \rightarrow \tau_Cable = -(\tau_Dog + \tau_Beam)$$

From this we can use the torque formula to find the magnitude of the force the cable is exerting and thus the tension on the cable.

$$|\tau_Cable| = |r_Cable| * F_CableMag * \sin\phi \rightarrow \text{solve for } F_CableMag \rightarrow F_CableMag = |\tau_Cable| / (|r_Cable| * \sin\phi)$$

$$F_CableMag = 1.23813e+4 \text{ N} \rightarrow 1.2e+4 \text{ N}$$

This answer seems reasonable. The net force in the y direction is approximately $-1.28e+4 \text{ N}$. Since the cable is acting at a longer lever length it is able to exert more torque for less force. The power of the force is reduced though due to the angle at which it is acting, but nevertheless, this answer seems reasonable.

Now we have the magnitude of the Force from the cable, which is the tension on the cable, our problem is solved.

We can use this to find the forces acting at the hinge.

$$\text{Forces at hinge on beam} = \langle 1.04999e+4, 6293.27, 0 \rangle \text{ N}$$

GlowScript 3.0 VPython

Begin by defining all of my variables. Begin with defining the scalars and then define the vectors

Scalars

$G = 6.67408 \times 10^{-11} \text{ Nm}^2/(\text{kg})^2$

$r_{\text{Earth}} = 6371000 \text{ m}$

$m_{\text{Earth}} = 5.9722 \times 10^{24} \text{ kg}$

$g = -(G \cdot m_{\text{Earth}}) / (r_{\text{Earth}}^2) \text{ m/s}^2$

$m_{\text{Dog}} = 75 \text{ kg}$

$m_{\text{Beam}} = 1234 \text{ kg}$

$r_{\text{Dog}} = 1.5 \text{ m}$

$r_{\text{Beam}} = 1.1 \text{ m}$ - The beam is 2.2 m long but since we assume the mass is evenly distributed across a perfectly even beam the center of mass will be 1.1 m

$r_{\text{Cable}} = 2.2 \text{ m}$ - Since the cable is attached at the very end of the beam, its distance from the pivot point is the length of the beam

$r_{\text{Hinge}} = 0 \text{ m}$

$\theta_{\text{Cable}} = (8\pi)/45 \text{ radians}$

Vectors

$\mathbf{s}_{\text{Dog}} = \text{vec}(r_{\text{Dog}}, 0, 0) \text{ m}$

$\mathbf{F}_{\text{Dog}} = \text{vec}(0, (m_{\text{Dog}} \cdot g), 0) \text{ N}$

$\mathbf{t}_{\text{Dog}} = \text{cross}(\mathbf{s}_{\text{Dog}}, \mathbf{F}_{\text{Dog}}) \text{ Nm}$

$\mathbf{s}_{\text{Beam}} = \text{vec}(r_{\text{Beam}}, 0, 0) \text{ m}$

$\mathbf{F}_{\text{Beam}} = \text{vec}(0, (m_{\text{Beam}} \cdot g), 0) \text{ N}$

$\mathbf{t}_{\text{Beam}} = \text{cross}(\mathbf{s}_{\text{Beam}}, \mathbf{F}_{\text{Beam}}) \text{ Nm}$

$\mathbf{s}_{\text{Hinge}} = \text{vec}(r_{\text{Hinge}}, 0, 0) \text{ m}$

$\mathbf{t}_{\text{NegBeam}} = \mathbf{t}_{\text{Dog}} + \mathbf{t}_{\text{Beam}} \text{ Nm}$

$\mathbf{s}_{\text{Cable}} = \text{vec}(r_{\text{Cable}}, 0, 0) \text{ m}$

Now that we know the net torque caused by the dog and the beam itself we can find the torque caused by the tension cable and from that the force in the cable itself.

$F_{\text{CableMag}} = (\text{mag}(\mathbf{t}_{\text{NegBeam}})) / (r_{\text{Cable}} \cdot \sin(\theta_{\text{Cable}})) \text{ N}$

$\mathbf{F}_{\text{Cable}} = \text{vec}((-F_{\text{CableMag}} \cdot \cos(\theta_{\text{Cable}})), (F_{\text{CableMag}} \cdot \sin(\theta_{\text{Cable}})), 0) \text{ N}$

$\mathbf{t}_{\text{Cable}} = \text{cross}(\mathbf{s}_{\text{Cable}}, \mathbf{F}_{\text{Cable}})$

$F_{\text{CableYaxis}} = \text{vec}(0, (F_{\text{CableMag}} \cdot \sin(\theta_{\text{Cable}})), 0) \text{ N}$

$\mathbf{F}_{\text{CableXaxis}} = \text{vec}((-F_{\text{CableMag}} \cdot \cos(\theta_{\text{Cable}})), 0, 0) \text{ N}$

Now that know the force vector the cable is exerting on the pivot point we can resolve the force of the hinge on the pivot point

$F_{\text{HingeYaxis}} = -1 \cdot (F_{\text{Beam}} + F_{\text{Dog}} + F_{\text{CableYaxis}}) \text{ N}$

$F_{\text{HingeXaxis}} = -1 \cdot (F_{\text{CableXaxis}}) \text{ N}$

$\mathbf{F}_{\text{Hinge}} = \text{vec}(\text{mag}(F_{\text{HingeXaxis}}), \text{mag}(F_{\text{HingeYaxis}}), 0) \text{ N}$

`print("Torque of dog on beam = ", \mathbf{t}_{Dog} , " Nm")`

```

print("Torque of beam on itself = ", t_Beam, " Nm")
print("Negative torque on beam = ", t_NegBeam, " Nm")
print("Magnitude of tension force on cable = ", F_CableMag, " N")
print("Tension on cable = ", F_Cable, " N")
print("Torque of cable on beam = ", t_Cable, " Nm")
print("Force at hinge on beam = ", F_Hinge, " N")

```

Torque of dog on beam = $\langle 0, 0, -1104.75 \rangle$ Nm

Torque of beam on itself = $\langle 0, 0, -1.33296e+4 \rangle$ Nm

Negative torque on beam = $\langle 0, 0, -1.44344e+4 \rangle$ Nm

Magnitude of tension force on cable = $1.23813e+4$ N

Tension on cable = $\langle -1.04999e+4, 6561.08, 0 \rangle$ N

Torque of cable on beam = $\langle 0, 0, 1.44344e+4 \rangle$ Nm

Forces at hinge on beam = $\langle 1.04999e+4, 6293.27, 0 \rangle$ N

Lecture Time: 11 am

Name: Christopher Hunt

CATEGORY	PLATINUM (1.5)	IMPROVED (1)	DEVELOPING (0.5)	POOR (0)
Statement and notation	Learning tool for our class is written	Problem is clearly presented for reader in words.	Problem is directly copied or is hard to read.	Problem is copied into some calculation.
	Sketch could be dropped into a novel as it stands.	A clear sketch, larger than a credit card, the problem set up with important data noted.	Some sketch of the problem.	Sketch?
Physics Tools	State physics tools are correlated to the exercise in textbook quality and quantity.	State physics tools are correlated to the exercise. Appropriate tools include: pictures, equations, observational laws utilized, etc...	Physics tools are correlated to the exercise.	Are a few equations written.
Final Solution Presentation	Is very clearly presented with no asides or annotations.	Is complete and clearly presented with no significant intuitive demands on the reader.	Solution I have to read between the lines.	Is a version of solution with only numbers present.
	Solution can serve as solution.	Sketch is larger than a credit card, notation is fluid, notation used is clear.	Figure the path of your solution with words.	Read it.
		Correctly given	Units & quantities are presented separately.	Units at the results.
Reasonableness			Close	Not reasonable.
Significant Figures		Sig Figs	Effort to use correct significant figures.	The number from the calculator.
Reasonableness	Is more than one type of reasonableness check.	Is clear rationale for appropriateness of solution in the setting.	That the answer is reasonable but isn't given any evidence.	Assessment.
Graded			Effort	Put your self-assessment in from mine by at least two steps.