

# CS3200: Computer Networks

## Lecture 35

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# Public-Key Algorithms

- Distributing the keys has always been the weakest link in most cryptosystems.
- Keys had to be protected from theft, but they also had to be distributed, so they could not be locked in a bank vault.
- In 1976, two researchers at Stanford University, Diffie and Hellman (1976), proposed a radically new kind of cryptosystem, one in which the encryption and decryption keys were so different that the decryption key could not feasibly be derived from the encryption key

# Public-Key Algorithms

In their proposal, the (keyed) encryption algorithm,  $E$ , and the (keyed) decryption algorithm,  $D$ , had to meet three requirements.

- $D(E(P)) = P$
- It is exceedingly difficult to deduce  $D$  from  $E$ .
- $E$  cannot be broken by a chosen plaintext attack.

Public-key cryptography requires each user to have two keys: **a public key**, used by the entire world for encrypting messages to be sent to that user, and **a private key**, which the user needs for decrypting messages.

- One good method was discovered by a group at M.I.T. (Rivest et al., 1978). It is known by the initials of the three discoverers (Rivest, Shamir, Adleman): **RSA**
- It has survived all attempts to break it for more than 30 years and is considered very strong.
- Its major disadvantage is that it requires keys of at least 1024 bits for good security (versus 128 bits for symmetric-key algorithms), which makes it quite slow.

The RSA method is based on some principles from number theory. We will now summarize how to use the method.

- 1 Choose two large primes,  $p$  and  $q$  (typically 1024 bits).
- 2 Compute  $n = p \times q$  and  $z = (p - 1) \times (q - 1)$ .
- 3 Choose a number relatively prime to  $z$  and call it  $d$ .
- 4 Find  $e$  such that  $e \times d = 1 \pmod{z}$ .

- To encrypt a message,  $P$ , compute  $C = P^e \bmod n$ .
- To decrypt  $C$ , compute  $P = C^d \bmod n$ .
- The public key consists of the pair  $(e, n)$  and the private key consists of  $(d, n)$ .