

Populating the interactive namespace from numpy and matplotlib

## Homework #6 ¶

10.40

	Average	Outstanding	Poor	Tot
Most desirable	20	21	4	45
Good	25	3	36	64
Adequate	8	14	2	24
Undesirable	7	10	6	23
total	60	48	48	156

Pearson's chi-square test

$$\chi^2 = \sum_{i,j} (n_{ij} - \hat{E}_{ij})^2 / \hat{E}_{ij}$$

where  $n_{ij}$  are the numbers in the table and  $\hat{E}_{ij} = \frac{(\text{row } i \text{ total})(\text{column } j \text{ total})}{\text{grand total}}$

Yields 50.5500113225 on this data set

$$\text{df} = (r - 1)(c - 1) = 3 * 2 = 6$$

Reject  $H_0$  if  $\chi^2 > \chi_\alpha^2$

And here, if  $\alpha = 0.05$  (or do I have that backwards?)  $\chi_\alpha^2$  equals

12.591587243743978

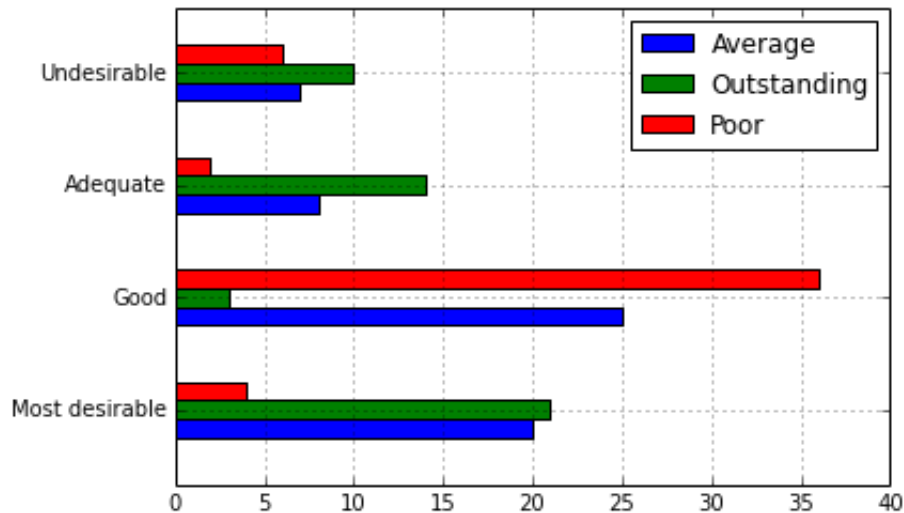
And therefore, because  $\chi^2 = 50.55$  exceeds 12.59,  $H_0$  is rejected. The  $p - \text{value} = \mathbb{P}[\chi_6^2 > 50.55]$  equals

3.6466244468513764e-09

a.) the  $\chi^2$  equals 50.55 b.) the p-value is very small c.) Yes, because we rejected the null hypothesis d.) I have no idea

## 10.41

To me, simply visually looking at the data does not lead me to either accept or reject the research hypothesis



## 10.42

Pearson's Chi-squared test

data: df

X-squared = 13.0252, df = 3, p-value = 0.004582

	0	1	2	3
0	16	22.4	25.6	16
1	34	47.6	54.4	34

- a.) Apparently the last row of every cell is the expected number.
- b.)  $3 * 1 = 3$
- c.) The p-value is small enough for us to reject the null hypothesis.

## 10.43

- a.) Because the p-value is now over 90% we cannot reject the null-hypothesis.
- b.) By combining the data, we now only have one degree of freedom. With only one degree, you must have some pretty big evidence for you to reject the null-hypothesis.

## 10.45

a.) By visual inspection of the data, you can see that there is evidence. Those three states have much higher adoption rates than the other three states... But at this point I feel so thoroughly bombarded with different test statistics, that I would not even know how to test this hypothesis.

b.) It provides justification because there is a higher rate of adoption amongst farmers who were provided information about the effectiveness of IPM.

## 8.6

a.) Visual inspection yields no evidence to indicate any difference

$$F = 4.849086119327985$$

One-way analysis of means

data: df2\$a and df2\$b

$$F = 4.847, \text{ num df} = 3, \text{ denom df} = 20, \text{ p-value} = 0.01077$$

Using two different methods, I come to the conclusion that F is about 4.85.

b.) The critical value of F for  $\alpha = 0.05$  is 3.09839121214. Because the computed value of F exceeds this value, we reject the null hypothesis of equality of the mean. However, since the two values are in the same order of magnitude, we are not surprised that a visual inspection of the data was inconclusive.

c.)  $\text{p-value} = 0.0107735195164$

d.) Each of the populations have a normal distribution, equal variance and are randomly sampled.

e.) There could be a problem where one device randomly received too many of one type of soil sample, thus throwing off the assumptions

## 8.9

$n_1 = n_2 = n_3 = 5$  are the sample sizes.

$t = 3$  is the number of populations.

apparently  $\mu = 11$  and therefore  $\tau_1 = -1.8$   $\tau_2 = -1.0$   $\tau_3 = 2.8$

which only leaves  $\sigma$ ... but I'm not exactly sure how to calculate this. I will simply take the mean of the various variances:  $\sigma = \sqrt{\frac{33.7+29+46.7}{3}} = 6.04$

## 8.12

$$\text{residuals} = \epsilon_{ij} = y_{ij} - \bar{y}_i$$

	1	2	3
count	5.000000	5.000000	5.000000
mean	9.600000	10.000000	13.800000
std	5.319774	5.385165	6.83374
min	4.000000	5.000000	8.000000
25%	5.000000	7.000000	9.000000
50%	10.000000	9.000000	12.000000
75%	12.000000	10.000000	15.000000
max	17.000000	19.000000	25.000000

Before we even begin, we notice that the book has a mistake in its calculations. The first sample mean, should be 9.6, not 9.2 as the book has written:  $\frac{5+17+12+10+4}{5} = 9.6$

With that in mind, we calculate:

	0	1	2	3	4
1	-4.6	7.4	2.4	0.4	-5.6
2	9.0	0.0	-1.0	-3.0	-5.0
3	11.2	1.2	-1.8	-4.8	-5.8

b.) The sample variances are not equal, however they are not wildly different. So I would say that the AOV conditions are not satisfied, but one could probably run the analysis anyways.

## 8.30

Kruskal-Wallis rank sum test

data: df\$a by df\$b  
Kruskal-Wallis chi-squared = 26.6213, df = 3, p-value = 7.068e-06

a) This is a shift. The F value decreased by almost half

a.) This is a shift. The t-value decreased by almost half.

b.) Even though there is a shift, the p-value remains close to zero, thus we reach the same conclusions as before.

## 8.32

Kruskal-Wallis rank sum test

```
data: df$a by df$b  
Kruskal-Wallis chi-squared = 16.5614, df = 3, p-value = 0.0008698
```

One-way analysis of means

```
data: df$a and df$b  
F = 11.0472, num df = 3, denom df = 28, p-value = 5.85e-05
```

a.) I did both an AOV test and a Kruskal-Wallis rank sum test.

b.) Both tests yield a p-value close to zero, thus we reject the null hypothesis and conclude that the different plots of land yield different amounts of corn.

## 8.33

errr... that's what I did. I still make the same conclusions.

## 8.36

No. The AOV conditions appear to be met.

The raw code for this IPython notebook is by default hidden for easier reading.

To toggle on/off the raw code, click [here](#).